Please check the examination deta	ails below	<i>i</i> before ente	ering your candidate information
Candidate surname			Other names
Pearson Edexcel nternational Advanced Level	Centr	e Number	Candidate Number
Wednesday 1	5 J	anu	ary 2020
Morning (Time: 2 hours 30 minu	tes)	Paper Re	eference <b>WMA02/01</b>
Mathematics			
International Advance Core Mathematics C34		rel	
You must have: Mathematical Formulae and Sta	tistical <sup>·</sup>	Tables (Blu	Total Mark ue), calculator

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

## Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 15 questions in this question paper. The total mark for this paper is 125.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

## **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ▶





1. 
$$f(x) = 2x^4 + x^2 - 3x + 8$$

The curve with equation y = f(x) has a single turning point when  $x = \alpha$ 

(a) Show that  $\alpha$  is a solution of the equation

$$x = \sqrt[3]{\frac{3 - 2x}{8}}$$
 (3)

The iterative formula

$$x_{n+1} = \sqrt[3]{\frac{3 - 2x_n}{8}} \qquad x_1 = 0.6$$

is used to find an approximate value for  $\alpha$ .

(b) Calculate the value of  $x_2$  and the value of  $x_3$  giving your answers to 4 decimal places.

(2)

(c) By choosing a suitable interval, show that  $\alpha = 0.607$  to 3 decimal places.



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2. (a) Find the first 4 terms, in ascending powers of x, of the binomial expansion of

$$\left(\frac{1}{4} - 3x\right)^{\frac{1}{2}}$$

giving each coefficient in its simplest form.

**(5)** 

By substituting  $x = \frac{1}{100}$  into the answer for (a),

(b) find an approximation for  $\sqrt{22}$ , giving your answer to 4 decimal places.

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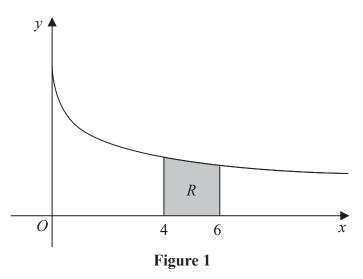


Figure 1 shows a sketch of the curve with equation  $y = \frac{10}{1 + \sqrt{x}}, x \ge 0$ 

The finite region R, shown shaded in Figure 1, is bounded by the curve, the line with equation x = 4, the x-axis and the line with equation x = 6

(a) Use the trapezium rule, with four strips, to find an estimate for the area of R. Show your working and give your answer to 2 decimal places.

**(4)** 

(b) Using your answer to part (a) and making your method clear, estimate the value of

$$(i) \quad \int_2^3 \frac{60}{1 + \sqrt{2x}} \, \mathrm{d}x$$

(ii) 
$$\int_4^6 \frac{13 + 3\sqrt{x}}{1 + \sqrt{x}} \, \mathrm{d}x$$

(Solutions relying entirely on calculator technology are not acceptable.)

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4. (a) Sketch the graph with equation

$$y = |2x - 7| + 1$$

stating the coordinates of the minimum point and the coordinates of the point where the graph cuts the *y*-axis.

**(3)** 

(b) Solve the equation

$$14 - x = |2x - 7| + 1$$

**(4)** 

A straight line *l* has equation  $y = \frac{1}{2}x + k$ , where *k* is a constant.

Given that *l* does not meet or intersect y = |2x - 7| + 1

(c) find the range of possible values of k.

**(2)** 


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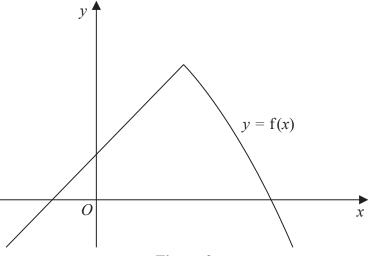


Figure 2

The continuous function f is defined by

$$f(x) = \begin{cases} 9 + 3x & x \le 6 \\ B - Ax^2 & x > 6 \end{cases}$$
 where A and B are positive constants

A sketch of y = f(x) is shown in Figure 2.

(a) Find the range of f.

**(1)** 

Given that one of the solutions of the equation f(x) = 0 is 12

- (b) (i) find the other solution,
  - (ii) find the value of A and the value of B.

**(4)** 

(c) Find the value of ff(0).

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**6.** Given that

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{4x\ln x}{y} \qquad x > 0, \quad y > 0$$

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- 7. Given  $y = 3x(2x 5)^4$ 
  - (a) show that

$$\frac{\mathrm{d}y}{\mathrm{d}x} = 15(2x - 5)^3(Ax + B)$$

where A and B are integers to be found.

**(4)** 

	(b)	Hence find	the range	of values	of $x$ for	which y is	decreasing
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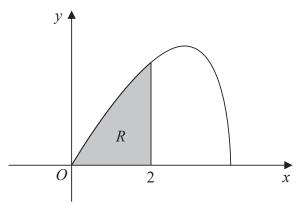


Figure 3

Figure 3 shows a sketch of the curve with parametric equations

$$x = 4\sin t, \quad y = 3\sin 2t, \quad 0 \leqslant t \leqslant \frac{\pi}{2}$$

The region R, shown shaded in Figure 3, is bounded by the curve, the x-axis and the line with equation x = 2

Find the exact area of R.

(Solutions relying entirely on calculator technology are not acceptable.)

**(7)** 

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**(6)** 

**9.** With respect to a fixed origin O, the lines  $l_1$  and  $l_2$  are given by the equations

$$l_1: \quad \mathbf{r} = \begin{pmatrix} 2\\1\\3 \end{pmatrix} + \lambda \begin{pmatrix} -2\\1\\4 \end{pmatrix}$$

$$l_2: \quad \mathbf{r} = \begin{pmatrix} 10 \\ c \\ 3 \end{pmatrix} + \mu \begin{pmatrix} a \\ b \\ -2 \end{pmatrix}$$

where a, b and c are constants and  $\lambda$  and  $\mu$  are scalar parameters.

Given that

- $l_1$  and  $l_2$  meet when  $\lambda = -2$
- $l_1$  and  $l_2$  are perpendicular

find the value of a, the value of b and the value of c.


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10. The curve C has equation

$$y^3 + 4x^2y - 2x = 0$$

(a) Find, in simplest form,  $\frac{dy}{dx}$  in terms of x and y.

**(5)** 

(b) Hence find the coordinates of the points on C where  $\frac{dy}{dx} = 0$ 

**(6)** 

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**11.** (a) Prove

$$\frac{\cos 3\theta}{2\sin \theta} + \frac{\sin 3\theta}{2\cos \theta} \equiv \cot 2\theta \qquad \theta \neq \frac{n\pi}{2} \ n \in \mathbb{Z}$$

**(4)** 

**(4)** 

(b) Hence solve, for  $0 < x < \frac{\pi}{2}$ 

$$\frac{\cos 3x}{2\sin x} + \frac{\sin 3x}{2\cos x} = 5\cos 2x$$

giving your answers to 3 decimal places where appropriate.

(Solutions based entirely on graphical or numerical methods are not acceptable.)



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$\int_{1}^{3} \frac{3x^{2} + 8}{x^{2} - 4x} dx \tag{7}$	$1^{-3}v^2 \perp Q$	
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13. A curve has parametric equations

$$x = t^2 + 3t \qquad y = \frac{2t}{1 - t} \qquad t \neq 1$$

(a) Find  $\frac{dy}{dx}$  in terms of t, giving your answer as a simplified fraction.

**(4)** 

(b) Find an equation for the tangent to the curve at the point P, where t = 2 Write your answer in the form ax + by + c = 0, where a, b and c are integers to be found.

**(4)** 

The tangent to the curve at P cuts the curve at the point Q.

(c) Use algebra to find the coordinates of Q.

**(5)** 

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14. A scientist is studying a population of lizards on an island.

The number of lizards, N, in the population, t years after the start of the study, is modelled by the equation

$$N = \frac{1800}{2 + 3e^{-0.2t}} \qquad t \in \mathbb{R}, t \ge 0$$

Use the model to answer parts (a), (b), (c) and (d).

(a) Find the number of lizards in the population at the start of the study.

**(1)** 

The model predicts an upper limit to the number of lizards on the island.

(b) State the value of this limit.

**(1)** 

(c) Find the value of t when N = 780. Give your answer to one decimal place.

(4)

(d) (i) Show that the rate of growth,  $\frac{dN}{dt}$ , is given by

$$\frac{\mathrm{d}N}{\mathrm{d}t} = \frac{N(900 - N)}{A}$$

where A is a constant to be found.

(ii) Hence state the value of N at which the rate of growth is a maximum.

(5)

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**15.** 

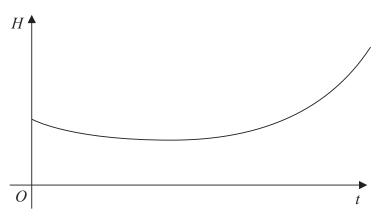


Figure 4

A jet is flying over the sea.

The height above sea level, H metres, of the jet is modelled by the equation

$$H = \frac{8000}{56 + 9\cos t^{\circ} + 40\sin t^{\circ}} \qquad 0 \leqslant t \leqslant 200$$

where t is the time in seconds, measured from when the jet passed over a boat.

Figure 4 is a sketch showing the graph of H against t.

## Use the model to answer parts (a), (c) and (d).

(a) Find the height above sea level of the jet as it passed over the boat.

(1)

(b) Write  $9\cos t^{\circ} + 40\sin t^{\circ}$  in the form  $R\cos(t - \alpha)^{\circ}$  where R > 0 and  $0 < \alpha < 90$ Give the exact value of R and the value of  $\alpha$  to one decimal place.

(3)

- (c) Find (i) the minimum height of the jet above sea level,
  - (ii) the value of t at which this minimum height occurs.

**(3)** 

(d) Find the value of t when the jet is  $150 \,\mathrm{m}$  above sea level.

(4)

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