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Surname	Other na	mes
Pearson Edexcel International Advanced Level	Centre Number	Candidate Number
Further Pu Mathemated/Advance	tics F1	
Wednesday 13 January 201 Time: 1 hour 30 minutes	16 – Afternoon	Paper Reference WFM01/01

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

## **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

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1. z = 3 + 2i, w = 1 - i

Find in the form a + bi, where a and b are real constants,

(a) zw

**(2)** 

(b)  $\frac{z}{w^*}$ , showing clearly how you obtained your answer.

(3)

Given that

$$|z + k| = \sqrt{53}$$
, where k is a real constant

(c) find the possible values of k.

**(4)** 

Question 1 continued		blank
		Q1
	(Total 9 marks)	



- 2.  $f(x) = x^2 \frac{3}{\sqrt{x}} \frac{4}{3x^2}, \quad x > 0$ 
  - (a) Show that the equation f(x) = 0 has a root  $\alpha$  in the interval [1.6, 1.7]

**(2)** 

(b) Taking 1.6 as a first approximation to  $\alpha$ , apply the Newton-Raphson process once to f(x) to find a second approximation to  $\alpha$ . Give your answer to 3 decimal places.

(5)

Question 2 continued	L b	Leav blan
	Q	2
	(Total 7 marks)	



**3.** The quadratic equation

$$x^2 - 2x + 3 = 0$$

has roots  $\alpha$  and  $\beta$ .

Without solving the equation,

- (a) (i) write down the value of  $(\alpha + \beta)$  and the value of  $\alpha\beta$ 
  - (ii) show that  $\alpha^2 + \beta^2 = -2$
  - (iii) find the value of  $\alpha^3 + \beta^3$

**(5)** 

- (b) (i) show that  $\alpha^4 + \beta^4 = (\alpha^2 + \beta^2)^2 2(\alpha\beta)^2$ 
  - (ii) find a quadratic equation which has roots

$$(\alpha^3 - \beta)$$
 and  $(\beta^3 - \alpha)$ 

giving your answer in the form  $px^2 + qx + r = 0$  where p, q and r are integers.





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Question 3 continued	



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Question 3 continued	
	Q3
(Total 11 marks)	



- $\mathbf{A} = \begin{pmatrix} -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix}$
- (a) Describe fully the single geometrical transformation represented by the matrix **A**. (3)
- (b) Hence find the smallest positive integer value of n for which

$$\mathbf{A}^n = \mathbf{I}$$

where I is the  $2 \times 2$  identity matrix.

**(1)** 

The transformation represented by the matrix A followed by the transformation represented by the matrix B is equivalent to the transformation represented by the matrix C.

Given that  $C = \begin{pmatrix} 2 & 4 \\ -3 & -5 \end{pmatrix}$ ,

(c) find the matrix **B**.

**(4)** 

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Question 4 continued

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5. (a) Use the standard results for  $\sum_{r=1}^{n} r$  and  $\sum_{r=1}^{n} r^3$  to show that, for all positive integers n,

$$\sum_{r=1}^{n} (8r^3 - 3r) = \frac{1}{2} n(n+1)(2n+3)(an+b)$$

where a and b are integers to be found.

**(4)** 

Given that

$$\sum_{r=5}^{10} (8r^3 - 3r + kr^2) = 22768$$

(b) find the exact value of the constant	k
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**6.** The rectangular hyperbola H has equation  $xy = c^2$ , where c is a non-zero constant.

The point  $P\left(cp, \frac{c}{p}\right)$ , where  $p \neq 0$ , lies on H.

(a) Show that the normal to H at P has equation

$$yp - p^3x = c(1 - p^4)$$

(5)

The normal to H at P meets H again at the point Q.

(b) Find, in terms of c and p, the coordinates of Q.

**(4)** 

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	(Total 9 marks)	



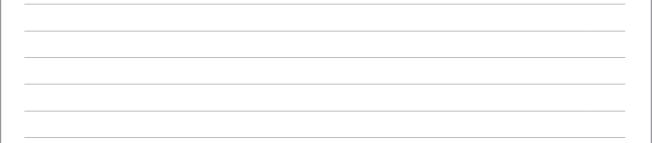
7.	
	$f(x) = x^4 - 3x^3 - 15x^2 + 99x - 130$

(a) Given that x = 3 + 2i is a root of the equation f(x) = 0, use algebra to find the three other roots of the equation f(x) = 0

**(7)** 

(b) Show the four roots of f(x) = 0 on a single Argand diagram.

**(2)** 



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Question 7 continued	01



Question 7 continued	

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8. The parabola P has equation  $y^2 = 4ax$ , where a is a positive constant. The point S is the focus of P.

The point B, which does not lie on the parabola, has coordinates (q, r) where q and r are positive constants and q > a. The line l passes through B and S.

(a) Show that an equation of the line l is

$$(q-a) y = r(x-a)$$
(3)

The line l intersects the directrix of P at the point C.

Given that the area of triangle OCS is three times the area of triangle OBS, where O is the origin,

(b)	show that the area	of triangle	OBC is	$\frac{6}{5}qr$
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(5)

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Question 8 continued

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	<b>Q8</b>
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$f(n) = 4^{n+1} + 5^{2n-1}$	
is divisible by 21	
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	(Total 6 marks)	
	TOTAL FOR PAPER: 75 MARKS	
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