lp_programming_2

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0.1 Programming Assignment #2, LP, Fall 2022

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```
[18]: import numpy as np
      import pandas as pd
      import random
      from scipy.sparse import rand
      from scipy.linalg import lu_factor, lu_solve, cho_factor, cho_solve
[19]: def A_matrix (U, L, density, m, n):
          #define a matrix of random values between 0 and 1 of specific density and \Box
       \hookrightarrow size
          matrix=rand(m,n,density)
          #interpolate between upper and lower bounds with randomly generated number
          matrix = matrix*(U-L)+L
          #convert array to dataframe
          matrix_df=pd.DataFrame(matrix.toarray())
          #cycle through rows and check if all values in row are zero
          for row in matrix_df.index:
              if (matrix_df.loc[row,:]==0).all():
                  #if all values in row are zero, then recurse
                  return A_matrix(U,L,density,m,n)
          #cycle through columns and check if all values in column are zero
          for col in matrix df.columns:
              if (matrix_df.loc[:,col]==0).all():
                  #if all values in column are zero, then recurse
                  return A_matrix(U,L,density,m,n)
          return matrix.toarray()
      def b_matrix (U, L, density, m, n):
          #define a matrix of random values between 0 and 1 of specific density and \Box
       ⇔size
          matrix=rand(m,n,density)
          #interpolate between upper and lower bounds with randomly generated number
          matrix = matrix*(U-L)+L
          #convert array to dataframe
```

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matrix_df=pd.DataFrame(matrix.toarray())
          #cycle through rows and check if all values in row are zero
          return matrix.toarray()
[20]: A=A_matrix(100,0,0.4,10,10)
      b=b_matrix(50,0,0.8,10,1)
      lu, piv = lu_factor(A)
      x = lu_solve((lu, piv), b)
      print(x)
     [[ 0.108236 ]
      [ 0.24695984]
      [ 0.75035242]
      [-1.92928781]
      [-0.1544934]
      [ 0.02957011]
      [-0.27335293]
      [-0.01142524]
      [ 0.51052497]
      [ 0.38513341]]
[21]: x = np.linalg.solve(A,b)
      print(x)
     [[ 0.108236 ]
      [ 0.24695984]
      [ 0.75035242]
      [-1.92928781]
      [-0.1544934]
      [ 0.02957011]
      [-0.27335293]
      [-0.01142524]
      [ 0.51052497]
      [ 0.38513341]]
[22]: A_inv = np.linalg.inv(A)
      print(A_inv.dot(b))
     [[ 0.108236 ]
      [ 0.24695984]
      [ 0.75035242]
      [-1.92928781]
      [-0.1544934]
      [ 0.02957011]
      [-0.27335293]
      [-0.01142524]
      [ 0.51052497]
```

[0.38513341]]

```
[23]: def is_pos_def(x):
          return np.all(np.linalg.eigvals(x) > 0)
      def cho_fun (B):
          D=(1/2*(B+np.transpose(B)))
          while False == is_pos_def(D):
              np.fill_diagonal(D, D.diagonal() + 20) # we add a large number to_
       \hookrightarrow diagonal
          return cho_solve(cho_factor(D),b)
      cho_fun(A)
[23]: array([[ 1.40466061],
             [ 1.48829233],
             [ 1.97740526],
             [-0.45639418],
             [ 0.34999757],
             [-0.71108676],
             [-1.01265374],
             [ 0.81237752],
             [-0.97552707],
             [-2.12799683]])
[23]:
```