

Assignment 6

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GitHub : https://github.com/ORION-22/RegexSoftware_ASSIGNMENT.git

Q1. Calculate/ derive the gradients used to update the parameters in cost function optimization for simple linear regression.

⇒

Gradient Descent:

Gradient descent is an iterative optimization algorithm to find the minimum of a function.

The equation for simple regression is

$$y = a_1 * x + a_0$$

we know that cost or error(e) = $y^{\wedge} - y$

for n data points:

$$f(a) = \frac{1}{2n} \sum_{i=1}^n (y^{\wedge} - y)^2$$

$$f(a) = \frac{1}{2n} \sum_{i=1}^n (y^{\wedge} - (a_1 * x + a_0))^2$$

α = learning rate or the size of the step we take towards finding the optimal fit line

$$\frac{df(a)}{da_0}$$

partial derivative of $f(a)$ w. r.t a_0 will give the value of parameter a_0

$$a_0 = \frac{2}{n} \sum_{i=1}^n (y^{\wedge} - (a_1 * x + a_0))$$

$\frac{df(a)}{da_1}$ partial derivative of $f(a)$ w. r.t a_1 will give the value of parameter

$$a_1 = \frac{2}{n} \sum_{i=1}^n x(y^{\wedge} - (a_1 * x + a_0))$$

$$\text{New } a_0 = a_0 - \alpha \frac{df(a)}{da_0}$$

$$\text{New } a_1 = a_1 - \alpha \frac{df(a)}{da_1}$$

Q2. What does the sign of gradient say about the relationship between the parameters and cost function?

⇒

The cost function is a function of the parameters and when the sign is positive then the step will decrease as seen below:

$$\text{New } a_0 = a_0 - [\text{+ve gradient}] * \alpha$$

when the sign is negative then the step will increase as seen below:

$$\text{New } a_0 = a_0 - [-\text{ve gradient}] * \alpha$$

$$\text{New } a_0 = a_0 + [\text{gradient}] * \alpha$$

Q3. Why Mean squared error is taken as the cost function for regression problems.

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MSE or Mean Squared Error is used to check how close predictions made by the model are to actual values. It calculates the error as actual - prediction and squares the difference to eliminate the negative values.

The lower the MSE, the closer is prediction to actual. In Regression models, a lower MSE usually indicates a better fit.

Q4. What is the effect of learning rate on optimization, discuss all the cases?

⇒

In an ideal scenario with an optimal learning rate, the cost function value will be minimized rather quickly.

If we take a large learning rate then the cost function value will be minimized very quickly but will settle at a value that is not the lowest.

If we take a lower than optimal learning rate, then even after substantial iterations the cost function will not minimize sufficiently and will take longer time.