# Check Root Finders nx(nz)

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## Data

Out[754]= 20.

```
In[749]:= dataSet = "GDT-Alfven"; 

RF Parameters

In[750]:= freq = 7.5; 
        c = 3. \times 10^8; 
        k0 = \frac{2 \, \text{N} \, [\pi]}{\text{c}} freq 10^6; 
        nz = 127.324; 
        kz = k0 * \text{nz}
```

#### Plasma Parameters

```
In[755]:=
     ne0 = 0.1 \times 10^{20};
     B0 = 1.2;
     etaList = Table[0., {i, 1, 5}];
     etaList[1] = 0.; etaList[2] = 1.; etaList[3] = 0.0;
     etaList[[4]] = 0.; etaList[[5]] = 0.;
     TList = Table[0., {i, 1, 6}];
     TList[[1]] = .000; TList[[2]] = 0.;
     TList[3] = 0.0001; TList[4] = 0.;
     TList[5] = 0.; TList[6] = 0.;
     modelList = Table[0, {i, 1, 6}];
     modelList[[1]] = 0; modelList[[2]] = 0;
     modelList[[3]] = 1; modelList[[4]] = 0;
     modelList[[5]] = 0; modelList[[6]] = 0;
     nminList = Table[0., {i, 1, 6}];
     nminList[1] = -1; nminList[2] = -2;
     nminList[3] = -2; nminList[4] = -2;
     nminList[[5]] = -2; nminList[[6]] = -2;
     nmaxList = Table[0., {i, 1, 6}];
     nmaxList[1] = 1; nmaxList[2] = 2;
     nmaxList[3] = 2; nmaxList[4] = 2;
     nmaxList[5] = 2;
     nmaxList[6] = 2;
```

# Low Density, $n_e = 1. \times 10^{19}$ , All waves cut off

```
ln[776] = ne0 = 0.1 \times 10^{20};
```

## Find Roots T = 0.1 ev

B0 = 1.2

nz=127.324

etaList={0., 1., 0., 0., 0.}

```
In[7777]:= TList = Table[0., {i, 1, 6}];
      TList[[1]] = .00; TList[[2]] = 0.;
      TList[3] = 0.001; TList[4] = 0.;
      TList[5] = 0.;
      TList[6] = 0.;
   Cold Plasma
In[781]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[781]= \{0. + 54.7545 i, 3838.11\}
      dataSet=GDT-Alfven
      freq=7.5
      ne0=1. \times 10^{19}
```

```
In[783]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[783]= \{0. + 55.3492 \, \dot{1}, 3866.3, 55481., 0. - 55.3492 \, \dot{1}, -3866.3, -55481.\}
       dataSet=GDT-Alfven
       \text{ne0=1.}\times \text{10}^{\text{19}}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.001, 0., 0., 0.}
```

```
In[785]:= modelList[[3]] = 1;
      rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[786] = \{0. + 55.3492 i, 3866.3, 55481., 0. - 55.3492 i, -3866.3, -55481.\}
Out[787]= \{ nx \rightarrow 0. + 55.3492 \ i \}
Out[788]= \{ nx \rightarrow 3866.3 + 0.1 \}
Out[789]= \{nx \rightarrow 55481. + 0.1\}
Out[790]= \{nx \rightarrow 0. -55.3492 \text{ i}\}
Out[791]= \{ nx \rightarrow -3866.3 + 0.1 \}
Out[792]= \{ nx \rightarrow -55481. + 0. i \}
      dataSet=GDT-Alfven
      ne0=1.\times10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.001, 0., 0., 0.}
      modelList={0, 0, 1, 0, 0, 0}
```

```
In[794]:= modelList[[3]] = 2;
      rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[794] = \{0. + 55.3492 i, 3866.3, 55481., 0. - 55.3492 i, -3866.3, -55481.\}
Out[795]= \{ nx \rightarrow 0. + 55.3492 \ i \}
Out[796]= \{ nx \rightarrow 3866.25 + 0.1 \}
Out[797]= \{nx \rightarrow 3866.25 + 0.1\}
Out[798]= \{nx \rightarrow 0. -55.3492 \text{ i}\}
Out[799]= \{ nx \rightarrow -3866.25 + 0.1 \}
Out[800]= \{ nx \rightarrow -3866.25 + 0.1 \}
      dataSet=GDT-Alfven
      ne0=1.\times10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.001, 0., 0., 0.}
      modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 1ev

```
In[802]:= TList[[1]] = .0;
      TList[3] = 0.001;
   Cold Plasma
In[804]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[804]= \{0. + 54.7545 i, 3838.11\}
      dataSet=GDT-Alfven
      freq=7.5
      ne0=1. \times 10^{19}
      B0 = 1.2
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
```

#### Warm Plasma (6th order system solved with NSolve)

```
In[806]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[806]= \{0.+55.3492 \pm, 3866.3, 55481., 0.-55.3492 \pm, -3866.3, -55481.\}
      dataSet=GDT-Alfven
      ne0=1. \times 10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.001, 0., 0., 0.}
```

```
In[808]:= modelList[[3]] = 1;
```

```
In[809]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[809] = \{0. + 55.3492 i, 3866.3, 55481., 0. -55.3492 i, -3866.3, -55481.\}
Out[810]= \{nx \rightarrow 0. + 55.3492 i\}
Out[811]= \{nx \rightarrow 3866.3 + 0.1\}
Out[812]= \{ nx \rightarrow 55481. + 0.1 \}
Out[813]= \{ nx \rightarrow 0. -55.3492 \ i \}
Out[814]= \{ nx \rightarrow -3866.3 + 0.1 \}
Out[815]= \{ nx \rightarrow -55481. + 0.1 \}
      dataSet=GDT-Alfven
      ne0=1. \times 10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.001, 0., 0., 0.}
      modelList={0, 0, 1, 0, 0, 0}
```

```
In[817]:= modelList[[3]] = 2;
```

```
In[818]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[818] = \{0. + 55.3492 i, 3866.3, 55481., 0. -55.3492 i, -3866.3, -55481.\}
Out[819]= \{ nx \rightarrow 0. + 55.3492 i \}
Out[820]= \{nx \rightarrow 3866.25 + 0.1\}
Out[821]= \{ nx \rightarrow 3866.25 + 0.1 \}
Out[822]= \{ nx \rightarrow 0. -55.3492 \ i \}
Out[823]= \{ nx \rightarrow -3866.25 + 0.1 \}
Out[824]= \{ nx \rightarrow -3866.25 + 0.1 \}
      dataSet=GDT-Alfven
      ne0=1. \times 10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.001, 0., 0., 0.}
      modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 5ev

```
In[826]:= TList[1] = .0;
     TList[3] = 0.005;
```

#### Cold Plasma

```
In[828]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[828]= \{0. + 54.7545 i, 3838.11\}
      dataSet=GDT-Alfven
      freq=7.5
      ne0=1. \times 10^{19}
      B0 = 1.2
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
```

### Warm Plasma (6th order system solved with NSolve)

```
In[830]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[830]= \{0. + 55.1636 i, 3941.69, 24318.9, 0. - 55.1636 i, -3941.69, -24318.9\}
      dataSet=GDT-Alfven
      ne0=1.\times10^{19}
      B0=1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.005, 0., 0., 0.}
```

```
In[832]:= modelList[[3]] = 1;
```

```
In[833]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[833] = \{0. + 55.1636 \pm, 3941.69, 24318.9, 0. - 55.1636 \pm, -3941.69, -24318.9\}
Out[834]= \left\{ nx \rightarrow 6.71064 \times 10^{-242} + 55.1636 \text{ i} \right\}
Out[835]= \{nx \rightarrow 3941.69 - 9.35903 \times 10^{-241} \text{ i} \}
Out[836]= \left\{ nx \rightarrow 24\,318.9 - 1.46382 \times 10^{-240} \,\,\dot{\mathbb{1}} \, \right\}
Out[837]= \{nx \rightarrow -6.71064 \times 10^{-242} - 55.1636 \text{ i}\}
Out[838]= \left\{ nx \rightarrow -3941.69 + 9.35903 \times 10^{-241} \text{ i} \right\}
Out[839]= \{ nx \rightarrow -24318.9 + 1.46382 \times 10^{-240} \text{ i} \}
      dataSet=GDT-Alfven
       ne0=1. \times 10^{19}
       B0 = 1.2
       freq=7.5
       nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.005, 0., 0., 0.}
      modelList={0, 0, 1, 0, 0, 0}
```

```
In[841]:= modelList[[3]] = 2;
       rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[841] = \{0. + 55.1636 i, 3941.69, 24318.9, 0. - 55.1636 i, -3941.69, -24318.9\}
Out[842]= \{ nx \rightarrow 6.71064 \times 10^{-242} + 55.1636 \text{ i} \}
Out[843]= \{nx \rightarrow 3940.03 - 9.39459 \times 10^{-241} \text{ i}\}
Out[844]= \{ nx \rightarrow 3940.03 - 1.84497 \times 10^{-240} \text{ i} \}
Out[845]= \{nx \rightarrow -6.71064 \times 10^{-242} - 55.1636 \text{ i}\}
Out[846]= \{ nx \rightarrow -3940.03 + 9.39459 \times 10^{-241} \text{ i} \}
Out[847]= \{nx \rightarrow -3940.03 + 1.84497 \times 10^{-240} \text{ i} \}
      dataSet=GDT-Alfven
      ne0=1. \times 10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.005, 0., 0., 0.}
      modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 50ev

```
In[849]:= TList[[1]] = .0;
      TList[3] = 0.05;
```

#### Cold Plasma

```
In[851]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[851]= \{0. + 54.7545 i, 3838.11\}
      dataSet=GDT-Alfven
      freq=7.5
      ne0=1. \times 10^{19}
      B0 = 1.2
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
```

```
In[853]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[853]= \{0. + 52.9527 \,\dot{\mathbb{1}}, 5187.91 - 1770.52 \,\dot{\mathbb{1}}, 5187.91 + 1770.52 \,\dot{\mathbb{1}}, 
        0. - 52.9527 \pm , -5187.91 + 1770.52 \pm , -5187.91 - 1770.52 \pm \}
       dataSet=GDT-Alfven
       ne0=1. \times 10^{19}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.05, 0., 0., 0.}
```

```
In[855]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
         nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[855]= \{0. + 52.9527 i, 5187.91 - 1770.52 i, 5187.91 + 1770.52 i, \}
        0. - 52.9527 i, -5187.91 + 1770.52 i, -5187.91 - 1770.52 i}
Out[856]= \left\{ nx \rightarrow 1.09815 \times 10^{-21} + 52.9527 \text{ i} \right\}
Out[857]= \{ nx \rightarrow 5187.91 - 1770.52 \ i \}
Out[858]= \{nx \rightarrow 5187.91 + 1770.52 \text{ i}\}
Out[859]= \left\{ nx \rightarrow -1.09815 \times 10^{-21} - 52.9527 \text{ i} \right\}
Out[860]= \{ nx \rightarrow -5187.91 + 1770.52 i \}
Out[861]= \{ nx \rightarrow -5187.91 - 1770.52 \ i \}
      dataSet=GDT-Alfven
      ne0=1. \times 10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.05, 0., 0., 0.}
      modelList={0, 0, 2, 0, 0, 0}
```

```
In[863]:= modelList[[3]] = 2;
       rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[863]= \{0. + 52.9527 i, 5187.91 - 1770.52 i, 5187.91 + 1770.52 i, \}
        0. - 52.9527 i, -5187.91 + 1770.52 i, -5187.91 - 1770.52 i
Out[864]= \left\{ nx \rightarrow 1.09815 \times 10^{-21} + 52.9527 \text{ i} \right\}
Out[865]= \{ nx \rightarrow 5725.97 - 3.81297 \times 10^{-20} \text{ i} \}
Out[866]= \{nx \rightarrow 5725.97 - 3.61825 \times 10^{-20} \text{ i}\}
Out[867]= \{ nx \rightarrow -1.09815 \times 10^{-21} - 52.9527 \text{ i} \}
Out[868]= \{ nx \rightarrow -5725.97 + 3.81297 \times 10^{-20} \text{ i} \}
Out[869]= \left\{ nx \rightarrow -5725.97 + 3.61825 \times 10^{-20} \text{ i} \right\}
       dataSet=GDT-Alfven
      ne0=1. \times 10^{19}
      B0 = 1.2
       freq=7.5
      nz=127.324
       etaList={0., 1., 0., 0., 0.}
      TList=\{0., 0., 0.05, 0., 0., 0.\}
      modelList={0, 0, 2, 0, 0, 0}
```

# Alfven wave propagates

```
ln[871] = ne0 = 0.15 \times 10^{20};
```

## Find Roots T = 0.1 ev

```
In[872]:= TList = Table[0., {i, 1, 6}];
     TList[1] = .0001; TList[2] = 0.;
     TList[3] = .0001; TList[4] = 0.;
     TList[[5]] = 0.;
     TList[6] = 0.;
```

#### Cold Plasma

```
In[876]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[876]= \{136.848, 2746.25\}
      dataSet=GDT-Alfven
      freq=7.5
      ne0=1.5 \times 10^{19}
      B0 = 1.2
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
```

```
In[878]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[878]= \{135.515, 2775.54, 176198., -135.515, -2775.54, -176198.\}
      dataSet=GDT-Alfven
      ne0=1.5 \times 10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0.0001, 0., 0.0001, 0., 0., 0.}
```

```
In[880]:= modelList[[3]] = 1;
In[881]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
         nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[881]= \{135.515, 2775.54, 176198., -135.515, -2775.54, -176198.\}
Out[882]= \{ nx \rightarrow 135.515 + 4.94259 \times 10^{-66} \text{ i} \}
Out[883]= \left\{ nx \to 2775.54 - 2.54927 \times 10^{-62} \text{ i} \right\}
Out[884]= \{ nx \rightarrow 176\ 198. + 1.52762 \times 10^{-63} \ i \}
Out[885]= \left\{ nx \rightarrow -135.515 - 4.94259 \times 10^{-66} \ \dot{\mathbb{1}} \right\}
Out[886]= \{ nx \rightarrow -2775.54 + 2.54927 \times 10^{-62} \text{ i} \}
Out[887]= \{ nx \rightarrow -176198. -1.52762 \times 10^{-63} \text{ i} \}
      dataSet=GDT-Alfven
      ne0=1.5\times10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0.0001, 0., 0.0001, 0., 0., 0.}
      modelList={0, 0, 1, 0, 0, 0}
```

```
In[889]:= modelList[[3]] = 1;
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[890]= \{ nx \rightarrow 135.517 + 0. i \}
Out[891]= \{ nx \rightarrow 2762.18 + 0.1 \}
Out[892]= \{ nx \rightarrow 176 \ 199. + 0. \ i \}
Out[893]= \{ nx \rightarrow -135.517 + 0. i \}
Out[894]= \{ nx \rightarrow -2762.18 + 0.1 \}
Out[895]= \{ nx \rightarrow -176199. + 0. i \}
      dataSet=GDT-Alfven
      ne0=1.5\times10^{19}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0.0001, 0., 0.0001, 0., 0., 0.}
      modelList={0, 0, 1, 0, 0, 0}
```

## Find Roots T = 1ev

 $ne0=1.5 \times 10^{19}$ 

nz=127.324

etaList={0., 1., 0., 0., 0.}

B0 = 1.2

```
In[897]:= TList = Table[0., {i, 1, 6}];
      TList[1] = 0.001; TList[2] = 0.;
      TList[3] = 0.001; TList[4] = 0.;
      TList[[5]] = 0.;
      TList[6] = 0.;
   Cold Plasma
In[901]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[901]= \{136.848, 2746.25\}
      dataSet=GDT-Alfven
      freq=7.5
```

```
In[903]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
     paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
-135.568 - 6.77704 \times 10^{-6} i, -2930.46 + 0.0410985 i, -55450.2 - 0.0081497 i}
     dataSet=GDT-Alfven
     ne0\!=\!1.5\times10^{19}
     B0 = 1.2
     freq=7.5
     nz=127.324
     etaList={0., 1., 0., 0., 0.}
     TList={0.001, 0., 0.001, 0., 0., 0.}
```

```
In[905]:= modelList[[3]] = 1;
       rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Outgool= \{135.568 + 6.77704 \times 10^{-6} \text{ i}, 2930.46 - 0.0410985 \text{ i}, 55450.2 + 0.0081497 \text{ i}, 
        -135.568 - 6.77704 \times 10^{-6} i, -2930.46 + 0.0410985 i, -55450.2 - 0.0081497 i
Out[906]= \{ nx \rightarrow 135.598 - 2.46519 \times 10^{-32} \text{ i} \}
Out[907]= \{nx \rightarrow 2773.2 - 3.06078 \times 10^{-28} \text{ i}\}
Out[908]= \{ nx \rightarrow 55480.5 + 1.60366 \times 10^{-50} \text{ i} \}
Out[909]= \{ nx \rightarrow -135.598 + 2.46519 \times 10^{-32} \text{ i} \}
Out[910]= \left\{ nx \rightarrow -2773.2 + 3.06078 \times 10^{-28} \text{ i} \right\}
Out[911]= \{nx \rightarrow -55480.5 - 1.60366 \times 10^{-50} \text{ i}\}
      dataSet=GDT-Alfven
       ne0=1.5\times10^{19}
      B0 = 1.2
       freq=7.5
       nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0.001, 0., 0.001, 0., 0., 0.}
      modelList={0, 0, 1, 0, 0, 0}
```

```
In[913]:= modelList[[3]] = 2;
       rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[913]= \left\{135.568 + 6.77704 \times 10^{-6} \, \text{i}, 2930.46 - 0.0410985 \, \text{i}, 55450.2 + 0.0081497 \, \text{i}, \right\}
        -135.568 - 6.77704 \times 10^{-6} i, -2930.46 + 0.0410985 i, -55450.2 - 0.0081497 i
Out[914]= \{nx \rightarrow 135.598 + 0.1\}
Out[915]= \{ nx \rightarrow 2773.18 - 4.00741 \times 10^{-28} \text{ i} \}
Out[916]= \left\{ nx \rightarrow 2773.18 + 2.76402 \times 10^{-24} \text{ i} \right\}
Out[917]= \{nx \rightarrow -135.598 + 0.1\}
Out[918]= \{ nx \rightarrow -2773.18 + 4.00741 \times 10^{-28} \text{ i} \}
Out[919]= \left\{ nx \rightarrow -2773.18 - 2.76402 \times 10^{-24} \text{ i} \right\}
       dataSet=GDT-Alfven
       ne0=1.5\times10^{19}
       B0=1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0.001, 0., 0.001, 0., 0., 0.}
       modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 5ev

 $ne0=1.5 \times 10^{19}$ 

nz=127.324

etaList={0., 1., 0., 0., 0.}

B0 = 1.2

```
In[921]:= TList = Table[0., {i, 1, 6}];
      TList[[1]] = .005; TList[[2]] = 0.;
      TList[3] = 0.005; TList[4] = 0.;
      TList[[5]] = 0.;
      TList[6] = 0.;
   Cold Plasma
In[925]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[925]= \{136.848, 2746.25\}
      dataSet=GDT-Alfven
      freq=7.5
```

```
In[927]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
                                                        paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[927]= \{135.806 + 0.0710588 \,\dot{\mathbb{1}}, \, 3721.61 - 1015.23 \,\dot{\mathbb{1}}, \, 23\,966.3 + 536.81 \,\dot{\mathbb{1}}, \, 3721.61 - 1015.23 \,\dot{\mathbb{1}}, \, 3721.61 - 3721.61 \,\dot{\mathbb{1}}, \, 3
                                                                  -135.806 - 0.0710588 i, -3721.61 + 1015.23 i, -23966.3 - 536.81 i
                                                      dataSet=GDT-Alfven
                                                        ne0=1.5 \times 10^{19}
                                                      B0 = 1.2
                                                      freq=7.5
                                                        nz=127.324
                                                      etaList={0., 1., 0., 0., 0.}
                                                      TList={0.005, 0., 0.005, 0., 0., 0.}
```

```
In[929]:= modelList[[3]] = 1;
       rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[929]= \{135.806 + 0.0710588 \, \dot{\text{1}}, 3721.61 - 1015.23 \, \dot{\text{1}}, 23966.3 + 536.81 \, \dot{\text{1}}, 
        -135.806 - 0.0710588 \pm, -3721.61 + 1015.23 \pm, -23966.3 - 536.81 \pm
Out[930]= \{ nx \rightarrow 135.959 + 1.84823 \times 10^{-24} \text{ i} \}
Out[931]= \{ nx \rightarrow 2824.67 - 1.95776 \times 10^{-18} \text{ i} \}
Out[932]= \{ nx \rightarrow 24326.2 - 6.46235 \times 10^{-26} \text{ i} \}
Out[933]= \{ nx \rightarrow -135.959 - 1.84823 \times 10^{-24} \text{ i} \}
Out[934]= \{ nx \rightarrow -2824.67 + 1.95776 \times 10^{-18} \text{ i} \}
Out[935]= \{ nx \rightarrow -24326.2 + 6.46235 \times 10^{-26} \text{ i} \}
       dataSet=GDT-Alfven
       ne0=1.5 \times 10^{19}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0.005, 0., 0.005, 0., 0., 0.}
       modelList={0, 0, 1, 0, 0, 0}
```

```
In[937]:= modelList[[3]] = 2;
               rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                    nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                     nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                    nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
               FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                    nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                    nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                    nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
              paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[937] = \{135.806 + 0.0710588 i, 3721.61 - 1015.23 i, 23966.3 + 536.81 i, 3721.61 - 1015.23 i, 23966.3 + 536.81 i, 3721.61 - 1015.23 i, 3721.61 - 1015.2
                  -135.806 - 0.0710588 i, -3721.61 + 1015.23 i, -23966.3 - 536.81 i}
Out[938]= \{nx \rightarrow 135.959 + 1.85469 \times 10^{-24} \text{ i}\}
Out[939]= \{ nx \rightarrow 2824.07 - 2.40559 \times 10^{-18} \text{ i} \}
Out[940]= \left\{ nx \rightarrow 2824.07 + 3.83176 \times 10^{-18} \text{ i} \right\}
Out[941]= \{ nx \rightarrow -135.959 - 1.85469 \times 10^{-24} \text{ i} \}
Out[942]= \{ nx \rightarrow -2824.07 + 2.40559 \times 10^{-18} \text{ i} \}
Out[943]= \{nx \rightarrow -2824.07 - 3.83176 \times 10^{-18} \text{ i}\}
              dataSet=GDT-Alfven
              ne0=1.5\times10^{19}
              B0 = 1.2
              freq=7.5
              nz=127.324
              etaList={0., 1., 0., 0., 0.}
              TList={0.005, 0., 0.005, 0., 0., 0.}
              modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 50ev

#### Find Roots T = 1ev

```
In[945]:= TList = Table[0., {i, 1, 6}];
      TList[1] = 0.05; TList[2] = 0.;
      TList[3] = 0.05; TList[4] = 0.;
      TList[5] = 0.;
      TList[6] = 0.;
   Cold Plasma
In[949]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[949]= \{136.848, 2746.25\}
      dataSet=GDT-Alfven
      freq=7.5
      ne0=1.5 \times 10^{19}
      B0=1.2
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
```

```
In[951]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
                                        paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[951]= \{734.654 - 1732.23 \, \dot{1}, 139.433 + 0.449897 \, \dot{1}, 8454.02 + 733. \, \dot{1}, 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02
                                               -734.654 + 1732.23 i, -139.433 - 0.449897 i, -8454.02 - 733. i
                                      dataSet=GDT-Alfven
                                      ne0=1.5 \times 10^{19}
                                      B0 = 1.2
                                      freq=7.5
                                      nz=127.324
                                      etaList={0., 1., 0., 0., 0.}
                                      TList={0.05, 0., 0.05, 0., 0., 0.}
```

```
In[953]:= modelList[[3]] = 1;
               rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
               FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                     nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                     nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
               FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                     nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                     nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                     nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
              FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                     nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
               paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[953]= \{734.654 - 1732.23 \, \dot{1}, 139.433 + 0.449897 \, \dot{1}, 8454.02 + 733. \, \dot{1}, 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02 + 6454.02
                  -734.654 + 1732.23 i, -139.433 - 0.449897 i, -8454.02 - 733. i
Out[954]= \{ nx \rightarrow 140.165 + 2.19837 \times 10^{-21} \text{ i} \}
Out[955]= \{ nx \rightarrow 140.165 + 2.04675 \times 10^{-18} \text{ i} \}
Out[956]= \{ nx \rightarrow 4559.13 + 774.33 \, \dot{\mathbb{1}} \}
Out[957]= \{ nx \rightarrow -140.165 - 2.19837 \times 10^{-21} \text{ i} \}
Out[958]= \left\{ nx \rightarrow -140.165 - 2.04675 \times 10^{-18} \text{ i} \right\}
Out[959]= \{ nx \rightarrow -4559.13 - 774.33 \ i \}
              dataSet=GDT-Alfven
              ne0=1.5\times10^{19}
              B0 = 1.2
              freq=7.5
              nz=127.324
               etaList={0., 1., 0., 0., 0.}
              TList={0.05, 0., 0.05, 0., 0., 0.}
              modelList={0, 0, 1, 0, 0, 0}
```

```
In[961]:= modelList[[3]] = 2;
                  rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
                  FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
                  FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
                  FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
                 FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
                 FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
                 FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
                         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
                   paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[961]= \{734.654 - 1732.23 \, \dot{\mathbb{1}}, 139.433 + 0.449897 \, \dot{\mathbb{1}}, 8454.02 + 733. \, \dot{\mathbb{1}}, 9454.02 + 733. \, \dot{\mathbb{1}}
                      -734.654 + 1732.23 i, -139.433 - 0.449897 i, -8454.02 - 733. i
Out[962]= \{ nx \rightarrow 140.166 + 2.19838 \times 10^{-21} \text{ i} \}
Out[963]= \{nx \rightarrow 140.166 + 2.04791 \times 10^{-18} \text{ i}\}
Out[964]= \{ nx \rightarrow 3868.69 - 4.68199 \times 10^{-15} \text{ i} \}
Out[965]= \{ nx \rightarrow -140.166 - 2.19838 \times 10^{-21} \text{ i} \}
Out[966]= \{ nx \rightarrow -140.166 - 2.04791 \times 10^{-18} \text{ i} \}
Out[967]= \{ nx \rightarrow -3868.69 + 4.68199 \times 10^{-15} \text{ i} \}
                  dataSet=GDT-Alfven
                 ne0=1.5 \times 10^{19}
                  B0 = 1.2
                  freq=7.5
                 nz=127.324
                  etaList={0., 1., 0., 0., 0.}
                 TList={0.05, 0., 0.05, 0., 0., 0.}
                 modelList={0, 0, 2, 0, 0, 0}
```

# above Alfven resonance. Is there any sign of kinetic Alfven wave?

```
ln[969] = ne0 = 2.2 \times 10^{20};
```

## Find Roots T = 0.1 ev

```
In[970]:= TList = Table[0., {i, 1, 6}];
     TList[1] = .00; TList[2] = 0.;
     TList[3] = 0.001; TList[4] = 0.;
     TList[5] = 0.;
     TList[6] = 0.;
```

#### Cold Plasma

```
In[974]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[974]= \{171.832, 0. + 16922.8 i\}
      dataSet=GDT-Alfven
      freq=7.5
      ne0=2.2 \times 10^{20}
      B0 = 1.2
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
```

```
In[976]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
\mathsf{Out}_{[976]} = \{0. + 16994.9 \, \text{i}, \, 171.765, \, 55505.3, \, 0. \, -16994.9 \, \text{i}, \, -171.765, \, -55505.3\}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.001, 0., 0., 0.}
```

```
In[978]:= modelList[[3]] = 1;
      rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[979] = \{0. + 16994.9 i, 171.765, 55505.3, 0. - 16994.9 i, -171.765, -55505.3\}
Out[980]= \{ nx \rightarrow 0. + 16994.9 \, i \}
Out[981]= \{ nx \rightarrow 171.765 + 0.1 \}
Out[982]= \{ nx \rightarrow 55505.3 + 0.1 \}
Out[983]= \{ nx \rightarrow 0. - 16994.9 i \}
Out[984]= \{ nx \rightarrow -171.765 + 0. i \}
Out[985]= \{ nx \rightarrow -55505.3 + 0.1 \}
      dataSet=GDT-Alfven
      ne0=2.2 \times 10^{20}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.001, 0., 0., 0.}
      modelList={0, 0, 1, 0, 0, 0}
```

```
In[987]:= modelList[[3]] = 2;
      rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
      FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[987] = \{0. + 16994.9 i, 171.765, 55505.3, 0. - 16994.9 i, -171.765, -55505.3\}
Out[988]= \{ nx \rightarrow 0. + 16999.2 \ i \}
Out[989]= \{ nx \rightarrow 171.765 + 0.1 \}
Out[990]= \{ nx \rightarrow 171.765 + 0.1 \}
Out[991]= \{ nx \rightarrow 0. - 16999.2 i \}
Out[992]= \{ nx \rightarrow -171.765 + 0. i \}
Out[993]= \{ nx \rightarrow -171.765 + 0. i \}
      dataSet=GDT-Alfven
      ne0=2.2 \times 10^{20}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.001, 0., 0., 0.}
      modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 1ev

```
In[995]:= TList[1] = .0;
      TList[3] = 0.001;
   Cold Plasma
In[997]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
      paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[997]= \{171.832, 0. + 16922.8 i\}
      dataSet=GDT-Alfven
      freq=7.5
      ne0=2.2 \times 10^{20}
      B0 = 1.2
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
```

#### Warm Plasma (6th order system solved with NSolve)

```
In[999]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
      paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[999] = \{0. + 16994.9 i, 171.765, 55505.3, 0. - 16994.9 i, -171.765, -55505.3\}
      dataSet=GDT-Alfven
      ne0=2.2 \times 10^{20}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.001, 0., 0., 0.}
```

```
In[1001]:= modelList[[3]] = 1;
```

```
In[1002]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[1002] = \{0. + 16994.9 \, \dot{1}, 171.765, 55505.3, 0. - 16994.9 \, \dot{1}, -171.765, -55505.3\}
Out[1003]= \{ nx \rightarrow 0. + 16994.9 \, i \}
Out[1004]= \{nx \rightarrow 171.765 + 0.1\}
Out[1005]= \{nx \rightarrow 55505.3 + 0.1\}
Out[1006]= \{ nx \rightarrow 0. - 16994.9 \ i \}
Out[1007]= \{ nx \rightarrow -171.765 + 0.1 \}
Out[1008]= \{ nx \rightarrow -55505.3 + 0.1 \}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.001, 0., 0., 0.}
       modelList={0, 0, 1, 0, 0, 0}
```

```
In[1010]:= modelList[[3]] = 2;
```

```
In[1011]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
         nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[1011]= \{0. + 16994.9 \, \dot{1}, 171.765, 55505.3, 0. - 16994.9 \, \dot{1}, -171.765, -55505.3\}
Out[1012]= \{nx \rightarrow 0. + 16999.2 \text{ i}\}
Out[1013]= \{nx \rightarrow 171.765 + 0.1\}
Out[1014]= \{ nx \rightarrow 171.765 + 0. i \}
Out[1015]= \{ nx \rightarrow 0. - 16999.2 \ i \}
Out[1016]= \{nx \rightarrow -171.765 + 0.i\}
Out[1017]= \{ nx \rightarrow -171.765 + 0.1 \}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.001, 0., 0., 0.}
       modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 5ev

```
In[1019]:= TList[1] = .0;
      TList[3] = 0.005;
```

#### Cold Plasma

```
In[1021]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
       paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[1021]= \{171.832, 0. + 16922.8 i\}
       dataSet=GDT-Alfven
       freq=7.5
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
```

### Warm Plasma (6th order system solved with NSolve)

```
In[1023]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
Out[1023]= \{0. + 17202.1 \pm, 171.754, 24534.9, 0. -17202.1 \pm, -171.754, -24534.9\}
      dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
      B0 = 1.2
      freq=7.5
      nz=127.324
      etaList={0., 1., 0., 0., 0.}
      TList={0., 0., 0.005, 0., 0., 0.}
```

```
In[1025]:= modelList[[3]] = 1;
```

```
In[1026]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
Out[1026]= \{0. + 17202.1 \pm, 171.754, 24534.9, 0. -17202.1 \pm, -171.754, -24534.9\}
Out[1027]= \left\{ nx \rightarrow -1.63568 \times 10^{-240} + 17202.1 \text{ i} \right\}
Out[1028]= \{ nx \rightarrow 171.754 + 1.39641 \times 10^{-243} \text{ i} \}
Out[1029]= \left\{ nx \to 24\,534.9 - 1.10806 \times 10^{-240} \,\,\dot{\mathbb{1}} \, \right\}
Out[1030]= \left\{ nx \rightarrow 1.63568 \times 10^{-240} - 17202.1 \text{ i} \right\}
Out[1031]= \left\{ nx \rightarrow -171.754 - 1.39641 \times 10^{-243} \text{ i} \right\}
Out[1032]= \{ nx \rightarrow -24534.9 + 1.10806 \times 10^{-240} \text{ i} \}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.005, 0., 0., 0.}
       modelList={0, 0, 1, 0, 0, 0}
```

```
In[1034]:= modelList[[3]] = 2;
       rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
        FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
        paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
\text{Out}[1034] = \{0. + 17202.1 \pm, 171.754, 24534.9, 0. -17202.1 \pm, -171.754, -24534.9\}
Out[1035]= \left\{ nx \rightarrow -2.65689 \times 10^{-240} + 17272.8 \text{ i} \right\}
Out[1036]= \{ nx \rightarrow 171.754 + 1.39641 \times 10^{-243} \text{ i} \}
Out[1037]= \{ nx \rightarrow 171.754 - 2.52907 \times 10^{-240} \text{ i} \}
Out[1038]= \left\{ nx \rightarrow 2.65689 \times 10^{-240} - 17272.8 \text{ i} \right\}
Out[1039]= \left\{ nx \rightarrow -171.754 - 1.39641 \times 10^{-243} \, \dot{\mathbb{1}} \right\}
Out[1040]= \left\{ nx \rightarrow -171.754 + 2.52907 \times 10^{-240} \text{ i} \right\}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.005, 0., 0., 0.}
       modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 20ev

```
In[1487]:= TList[1] = .0;
      TList[3] = 0.02;
```

#### Cold Plasma

```
In[1489]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
       paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[1489]= \{171.832, 0. + 16922.8 i\}
       dataSet=GDT-Alfven
       freq=7.5
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
```

```
In[1491]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
\texttt{Out[1491]= \{0.+17502.9 i, 171.711, 12077.2, 0.-17502.9 i, -171.711, -12077.2\}}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.02, 0., 0., 0.}
```

```
In[1493]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
          nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
\text{Out} [1493] = \{0. + 17502.9 \pm, 171.711, 12077.2, 0. - 17502.9 \pm, -171.711, -12077.2\}
Out[1494]= \{nx \rightarrow -5.18738 \times 10^{-57} + 17502.9 \text{ i}\}
Out[1495]= \{ nx \rightarrow 171.711 + 5.60906 \times 10^{-60} \text{ i} \}
Out[1496]= \{ nx \rightarrow 12077.2 \}
Out[1497]= \left\{ nx \rightarrow 5.18738 \times 10^{-57} - 17502.9 \text{ i} \right\}
Out[1498]= \left\{ nx \rightarrow -171.711 - 5.60906 \times 10^{-60} \text{ i} \right\}
Out[1499]= \{ nx \rightarrow -12077.2 \}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.02, 0., 0., 0.}
       modelList={0, 0, 2, 0, 0, 0}
```

```
In[1501]:= modelList[[3]] = 2;
       rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
        paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
\text{Out}[1501] = \{0. + 17502.9 \pm, 171.711, 12077.2, 0. - 17502.9 \pm, -171.711, -12077.2\}
Out[1502]= \left\{ nx \rightarrow -8.44149 \times 10^{-56} + 17976.7 \text{ i} \right\}
Out[1503]= \{nx \rightarrow 171.711 + 5.60919 \times 10^{-60} \text{ i}\}
Out[1504]= \{ nx \rightarrow 171.711 - 1.13966 \times 10^{-56} \text{ i} \}
Out[1505]= \left\{ nx \rightarrow 8.44149 \times 10^{-56} - 17976.7 \text{ i} \right\}
Out[1506]= \{ nx \rightarrow -171.711 - 5.60919 \times 10^{-60} \text{ i} \}
Out[1507]= \left\{ nx \rightarrow -171.711 + 1.13966 \times 10^{-56} \text{ i} \right\}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList=\{0., 0., 0.02, 0., 0., 0.\}
       modelList={0, 0, 2, 0, 0, 0}
```

## Find Roots T = 50ev

```
In[1042]:= TList[1] = .0;
      TList[3] = 0.05;
```

#### Cold Plasma

```
In[1044]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
       paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
Out[1044]= \{171.832, 0. + 16922.8 i\}
       dataSet=GDT-Alfven
       freq=7.5
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
```

```
In[1046]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
        paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
\texttt{Out[1046]=} \quad \{0.\ +\ 17\ 671.\ \dot{\texttt{1}}\ ,\ 171.626\ ,\ 7591.79\ ,\ 0.\ -\ 17\ 671.\ \dot{\texttt{1}}\ ,\ -\ 171.626\ ,\ -\ 7591.79\}
        dataSet=GDT-Alfven
        ne0=2.2 \times 10^{20}
        B0 = 1.2
        freq=7.5
        nz=127.324
        etaList={0., 1., 0., 0., 0.}
        TList={0., 0., 0.05, 0., 0., 0.}
```

```
In[1048]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
          nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
\text{Out}[1048] = \{0. + 17671.\,\dot{1}, 171.626, 7591.79, 0. - 17671.\,\dot{1}, -171.626, -7591.79\}
Out[1049]= \{ nx \rightarrow -1.69521 \times 10^{-20} + 17671. i \}
Out[1050]= \{nx \rightarrow 171.626 + 2.12067 \times 10^{-23} \text{ i}\}
Out[1051]= \{ nx \rightarrow 7591.79 - 1.36718 \times 10^{-21} \text{ i} \}
Out[1052]= \{ nx \rightarrow 1.69521 \times 10^{-20} - 17671. i \}
Out[1053]= \{ nx \rightarrow -171.626 - 2.12067 \times 10^{-23} \text{ i} \}
Out[1054]= \{ nx \rightarrow -7591.79 + 1.36718 \times 10^{-21} \text{ i} \}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList=\{0., 0., 0.05, 0., 0., 0.\}
       modelList={0, 0, 2, 0, 0, 0}
```

```
In[1056]:= modelList[[3]] = 2;
       rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
       FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
          nmaxList, modelList], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
       paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];
\text{Out}[1056] = \{0. + 17671. \pm, 171.626, 7591.79, 0. - 17671. \pm, -171.626, -7591.79\}
Out[1057]= \{nx \rightarrow -3.51919 \times 10^{-19} - 0.0772452 \text{ i}\}
Out[1058]= \{nx \rightarrow 171.626 + 4.24175 \times 10^{-23} \text{ i}\}
Out[1059]= \{ nx \rightarrow -171.626 - 4.92385 \times 10^{-20} \text{ i} \}
Out[1060]= \left\{ nx \to 3.51919 \times 10^{-19} + 0.0772452 \text{ i} \right\}
Out[1061]= \{ nx \rightarrow -171.626 - 4.24175 \times 10^{-23} \text{ i} \}
Out[1062]= \{nx \rightarrow 171.626 + 4.92385 \times 10^{-20} \text{ i}\}
       dataSet=GDT-Alfven
       ne0=2.2 \times 10^{20}
       B0 = 1.2
       freq=7.5
       nz=127.324
       etaList={0., 1., 0., 0., 0.}
       TList={0., 0., 0.05, 0., 0., 0.}
       modelList={0, 0, 2, 0, 0, 0}
```

# Stix criterion for kinetic Alfven wave $\beta_i > \frac{8}{3} m_e / m_i \left(1 - \frac{\omega^2}{4 \Omega_i^2}\right)$

 $ln[1064]:= 8. / 3. / 3670 * (1 - (7.5 / (4 * 9.15) ^2))$ Out[1064]= 0.000722544

> ■ By my calculation at 500 ev,  $\beta_i = 0.003$  so meets criterion by a lot. But I don't see a propagating or weakly damped wave.