

# Check Root Finders nx(nz)

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## Open Additional files:

Get dispersion routines by evaluating Disper\_no\_package.nb

Get plotting and printing routines by evaluating PlotPack.nb

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## Data

```
In[1065]:= dataSet = "GDT-Alfven";
```

### RF Parameters

```
In[1066]:= freq = 7.5;  
c = 3. × 108;  
k0 =  $\frac{2 N[\pi] \text{freq } 10^6}{c}$ ;  
nz = 127.324;  
kz = k0 * nz
```

```
Out[1070]= 20.
```

## Plasma Parameters

```

ne0 = 0.22 × 1020;
B0 = 1.2;

etaList = Table[0., {i, 1, 5}];
etaList[[1]] = 0.; etaList[[2]] = 1.; etaList[[3]] = 0.0;
etaList[[4]] = 0.; etaList[[5]] = 0.;

TList = Table[0., {i, 1, 6}];
TList[[1]] = .0001; TList[[2]] = 0.;
TList[[3]] = 0.0001; TList[[4]] = 0.;
TList[[5]] = 0.; TList[[6]] = 0.;

modellist = Table[0, {i, 1, 6}];
modellist[[1]] = 1; modellist[[2]] = 1;
modellist[[3]] = 1; modellist[[4]] = 0;
modellist[[5]] = 0; modellist[[6]] = 0;

nminList = Table[0., {i, 1, 6}];
nminList[[1]] = -1; nminList[[2]] = -2;
nminList[[3]] = -2; nminList[[4]] = -2;
nminList[[5]] = -2; nminList[[6]] = -2;

nmaxList = Table[0., {i, 1, 6}];
nmaxList[[1]] = 1; nmaxList[[2]] = 2;
nmaxList[[3]] = 2; nmaxList[[4]] = 2;
nmaxList[[5]] = 2;
nmaxList[[6]] = 2;

```

---

Low Density,  $n_e = 1. \times 10^{19}$ ,  
All waves cut off

```
In[1071]:= ne0 = 0.1 × 1020;
```

---

Find Roots T = 0.1 ev

```
In[1085]:= TList[[1]] = 0.0001;
          TList[[3]] = 0.0001;
```

## Cold Plasma

```
In[1087]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
           paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1087]= {0. + 54.7545 i, 3838.11}

dataSet=GDT-Alfven
freq=7.5
ne0= $1. \times 10^{19}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1089]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
           paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1089]= {0. + 55.3905 i, 3868.93, 176 202., 0. - 55.3905 i, -3868.93, -176 202.}

dataSet=GDT-Alfven
ne0= $1. \times 10^{19}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1091]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1091]= {0. + 55.3905 i, 3868.93, 176 202., 0. - 55.3905 i, -3868.93, -176 202.}

Out[1093]= {nx -> 0. + 55.3905 i}

Out[1094]= {nx -> 3868.93 - 3.5419 × 10-62 i}

Out[1095]= {nx -> 176 202. + 1.52824 × 10-63 i}

Out[1096]= {nx -> 0. - 55.3905 i}

Out[1097]= {nx -> -3868.93 + 3.5419 × 10-62 i}

Out[1098]= {nx -> -176 202. - 1.52824 × 10-63 i}

dataSet=GDT-Alfven
ne0=1. × 1019
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1100]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1100]= {0. + 55.3905 i, 3868.93, 176 202., 0. - 55.3905 i, -3868.93, -176 202.}

Out[1102]= {nx -> -3.56023 × 10-67 + 55.3905 i}

Out[1103]= {nx -> 3868.93 - 3.54189 × 10-62 i}

Out[1104]= {nx -> 3868.93 - 2.25164 × 10-63 i}

Out[1105]= {nx -> 3.56023 × 10-67 - 55.3905 i}

Out[1106]= {nx -> -3868.93 + 3.54189 × 10-62 i}

Out[1107]= {nx -> -3868.93 + 2.25164 × 10-63 i}

dataSet=GDT-Alfven
ne0=1. × 1019
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

## Find Roots T = 1ev

```
In[1113]:= TList[[1]] = 0.001;
          TList[[3]] = 0.001;
```

### Cold Plasma

```
In[1109]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1109]= {0. + 54.7545 i, 3838.11}

dataSet=GDT-Alfven
freq=7.5
ne0= $1. \times 10^{19}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

### Warm Plasma (6th order system solved with NSolve)

```
In[1111]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1111]= {0. + 55.3905 i, 3868.93, 176 202., 0. - 55.3905 i, -3868.93, -176 202.}

dataSet=GDT-Alfven
ne0= $1. \times 10^{19}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1115]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];

Out[1115]= {4.8776 × 10-7 - 55.3468 i, 4084.82 - 0.0571229 i, 55 450.5 + 0.0081923 i,
  -4.8776 × 10-7 + 55.3468 i, -4084.82 + 0.0571229 i, -55 450.5 - 0.0081923 i}

Out[1117]= {nx → 4.8776 × 10-7 - 55.3468 i}

Out[1118]= {nx → 4084.82 - 0.0571229 i}

Out[1119]= {nx → 55 450.5 + 0.0081923 i}

Out[1120]= {nx → -4.8776 × 10-7 + 55.3468 i}

Out[1121]= {nx → -4084.82 + 0.0571229 i}

Out[1122]= {nx → -55 450.5 - 0.0081923 i}

dataSet=GDT-Alfven
ne0=1. × 1019
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.001, 0., 0.001, 0., 0., 0.}
modelList={0, 0, 2, 0, 0, 0}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1124]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1124]= {4.8776 × 10-7 - 55.3468 i, 4084.82 - 0.0571229 i, 55450.5 + 0.0081923 i,
  -4.8776 × 10-7 + 55.3468 i, -4084.82 + 0.0571229 i, -55450.5 - 0.0081923 i}

Out[1126]= {nx → 4.8776 × 10-7 - 55.3468 i}

Out[1127]= {nx → 4084.74 - 0.0571175 i}

Out[1128]= {nx → 4084.74 - 0.0571175 i}

Out[1129]= {nx → -4.8776 × 10-7 + 55.3468 i}

Out[1130]= {nx → -4084.74 + 0.0571175 i}

Out[1131]= {nx → -4084.74 + 0.0571175 i}

dataSet=GDT-Alfven
ne0=1. × 1019
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.001, 0., 0.001, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```



## Find Roots T = 5ev

```
In[1133]:= TList[[1]] = 0.005;
           TList[[3]] = 0.005;
```

### Cold Plasma

```
In[1135]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
           paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1135]= {0. + 54.7545 i, 3838.11}

dataSet=GDT-Alfven
freq=7.5
ne0= $1. \times 10^{19}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

### Warm Plasma (6th order system solved with NSolve)

```
In[1137]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
           paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1137]= {0.00511244 - 55.1516 i, 5188.77 - 1418.54 i, 23954.2 + 560.118 i,
           -0.00511244 + 55.1516 i, -5188.77 + 1418.54 i, -23954.2 - 560.118 i}

dataSet=GDT-Alfven
ne0= $1. \times 10^{19}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1139]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];

Out[1139]= {0.00511244 - 55.1516 i, 5188.77 - 1418.54 i, 23 954.2 + 560.118 i,
  -0.00511244 + 55.1516 i, -5188.77 + 1418.54 i, -23 954.2 - 560.118 i}

Out[1141]= {nx -> 0.00511244 - 55.1516 i}
Out[1142]= {nx -> 5188.77 - 1418.54 i}
Out[1143]= {nx -> 23 954.2 + 560.118 i}
Out[1144]= {nx -> -0.00511244 + 55.1516 i}
Out[1145]= {nx -> -5188.77 + 1418.54 i}
Out[1146]= {nx -> -23 954.2 - 560.118 i}

dataSet=GDT-Alfven
ne0=1. × 1019
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
modelList={0, 0, 2, 0, 0, 0}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1148]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, modelList}];

Out[1148]= {0.00511244 - 55.1516 i, 5188.77 - 1418.54 i, 23 954.2 + 560.118 i,
  -0.00511244 + 55.1516 i, -5188.77 + 1418.54 i, -23 954.2 - 560.118 i}

Out[1150]= {nx -> 0.00511244 - 55.1516 i}

Out[1151]= {nx -> 5187.15 - 1410.75 i}

Out[1152]= {nx -> 5187.15 - 1410.75 i}

Out[1153]= {nx -> -0.00511244 + 55.1516 i}

Out[1154]= {nx -> -5187.15 + 1410.75 i}

Out[1155]= {nx -> -5187.15 + 1410.75 i}

dataSet=GDT-Alfven
ne0=1. × 1019
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
modelList={0, 0, 2, 0, 0, 0}

```

## Find Roots T = 50ev

```
In[1157]:= TList[[1]] = 0.05;
          TList[[3]] = 0.05;
```

### Cold Plasma

```
In[1159]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1159]= {0. + 54.7545 i, 3838.11}

dataSet=GDT-Alfven
freq=7.5
ne0= $1. \times 10^{19}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

### Warm Plasma (6th order system solved with NSolve)

```
In[1161]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1161]= {1047.61 - 2416.22 i, 0.030746 - 52.8956 i, 8455.93 + 687.452 i,
          -1047.61 + 2416.22 i, -0.030746 + 52.8956 i, -8455.93 - 687.452 i}

dataSet=GDT-Alfven
ne0= $1. \times 10^{19}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1172]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1172]= {1047.61 - 2416.22 i, 0.030746 - 52.8956 i, 8455.93 + 687.452 i,
  -1047.61 + 2416.22 i, -0.030746 + 52.8956 i, -8455.93 - 687.452 i}

Out[1174]= {nx -> 1047.61 - 2416.22 i}

Out[1175]= {nx -> 0.030746 - 52.8956 i}

Out[1176]= {nx -> 8455.93 + 687.452 i}

Out[1177]= {nx -> -1047.61 + 2416.22 i}

Out[1178]= {nx -> -0.030746 + 52.8956 i}

Out[1179]= {nx -> -8455.93 - 687.452 i}

dataSet=GDT-Alfven
ne0=1. × 1019
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1181]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1181]= {1047.61 - 2416.22 i, 0.030746 - 52.8956 i, 8455.93 + 687.452 i,
  -1047.61 + 2416.22 i, -0.030746 + 52.8956 i, -8455.93 - 687.452 i}

Out[1183]= {nx -> 1030.53 - 2423.05 i}
Out[1184]= {nx -> 0.030746 - 52.8956 i}
Out[1185]= {nx -> 0.030746 - 52.8956 i}
Out[1186]= {nx -> -1030.53 + 2423.05 i}
Out[1187]= {nx -> -0.030746 + 52.8956 i}
Out[1188]= {nx -> -0.030746 + 52.8956 i}

dataSet=GDT-Alfven
ne0=1. × 1019
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

---

Higher density,  $n_e = 1.5 \times 10^{19}$ ,

# Alfven wave propagates

```
In[1190]:= ne0 =  $1.5 \times 10^{20}$ ;
```

## Find Roots T = 0.1 ev

```
In[1191]:= TList = Table[0., {i, 1, 6}];
TList[[1]] = .0001; TList[[2]] = 0.;
TList[[3]] = .0001; TList[[4]] = 0.;
TList[[5]] = 0.;
TList[[6]] = 0.;
```

## Cold Plasma

```
In[1195]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1195]= {102.764, 0. + 13 638.3 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $1.5 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1197]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1197]= {0. + 13 707.5 i, 102.7, 176 193., 0. - 13 707.5 i, -102.7, -176 193.}

dataSet=GDT-Alfven
ne0= $1.5 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1208]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1208]= {0. + 13 707.5 i, 102.7, 176 193., 0. - 13 707.5 i, -102.7, -176 193.}

Out[1210]= {nx -> 1.25407 x 10-61 + 13 707.5 i}
Out[1211]= {nx -> 102.7 + 6.29186 x 10-68 i}
Out[1212]= {nx -> 176 193. + 1.50865 x 10-63 i}
Out[1213]= {nx -> -1.25407 x 10-61 - 13 707.5 i}
Out[1214]= {nx -> -102.7 - 6.29186 x 10-68 i}
Out[1215]= {nx -> -176 193. - 1.50865 x 10-63 i}

dataSet=GDT-Alfven
ne0=1.5 x 1020
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```



## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1217]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1217]= {0. + 13 707.5 i, 102.7, 176 193., 0. - 13 707.5 i, -102.7, -176 193.}

Out[1219]= {nx -> 1.25408 x 10-61 + 13 707.5 i}

Out[1220]= {nx -> 102.7 + 6.2919 x 10-68 i}

Out[1221]= {nx -> 102.7 + 6.03048 x 10-63 i}

Out[1222]= {nx -> -1.25408 x 10-61 - 13 707.5 i}

Out[1223]= {nx -> -102.7 - 6.2919 x 10-68 i}

Out[1224]= {nx -> -102.7 - 6.03048 x 10-63 i}

dataSet=GDT-Alfven
ne0=1.5 x 1020
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

## Find Roots T = 1ev

```
In[1226]:= TList = Table[0., {i, 1, 6}];
          TList[[1]] = 0.001; TList[[2]] = 0.;
          TList[[3]] = 0.001; TList[[4]] = 0.;
          TList[[5]] = 0.;
          TList[[6]] = 0.;
```

## Cold Plasma

```
In[1230]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
```

```
Out[1230]:= {102.764, 0. + 13 638.3 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $1.5 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1232]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
```

```
Out[1232]:= {0.20195 + 14 469.6 i, 102.697 + 8.72338  $\times 10^{-8}$  i, 55 470.1 + 0.00710428 i,
          -0.20195 - 14 469.6 i, -102.697 - 8.72338  $\times 10^{-8}$  i, -55 470.1 - 0.00710428 i}

dataSet=GDT-Alfven
ne0= $1.5 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.001, 0., 0.001, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1234]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1234]= {0.20195 + 14 469.6 i, 102.697 + 8.72338 × 10-8 i, 55 470.1 + 0.00710428 i,
  -0.20195 - 14 469.6 i, -102.697 - 8.72338 × 10-8 i, -55 470.1 - 0.00710428 i}

Out[1236]= {nx → 0.20195 + 14 469.6 i}
Out[1237]= {nx → 102.697 + 8.72338 × 10-8 i}
Out[1238]= {nx → 55 470.1 + 0.00710428 i}
Out[1239]= {nx → -0.20195 - 14 469.6 i}
Out[1240]= {nx → -102.697 - 8.72338 × 10-8 i}
Out[1241]= {nx → -55 470.1 - 0.00710428 i}

dataSet=GDT-Alfven
ne0=1.5 × 1020
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.001, 0., 0.001, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1243]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1243]= {0.20195 + 14 469.6 i, 102.697 + 8.72338 × 10-8 i, 55 470.1 + 0.00710428 i,
  -0.20195 - 14 469.6 i, -102.697 - 8.72338 × 10-8 i, -55 470.1 - 0.00710428 i}

Out[1245]= {nx → 0.202155 + 14 472.7 i}
Out[1246]= {nx → 102.697 + 8.72338 × 10-8 i}
Out[1247]= {nx → 102.697 + 8.72338 × 10-8 i}
Out[1248]= {nx → -0.202155 - 14 472.7 i}
Out[1249]= {nx → -102.697 - 8.72338 × 10-8 i}
Out[1250]= {nx → -102.697 - 8.72338 × 10-8 i}

dataSet=GDT-Alfven
ne0=1.5 × 1020
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.001, 0., 0.001, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

## Find Roots T = 5ev

```
In[1256]:= TList = Table[0., {i, 1, 6}];
          TList[[1]] = 0.005; TList[[2]] = 0.;
          TList[[3]] = 0.005; TList[[4]] = 0.;
          TList[[5]] = 0.;
          TList[[6]] = 0.;
```

## Cold Plasma

```
In[1260]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1260]= {102.764, 0. + 13 638.3 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $1.5 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1262]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1262]= {4701.81 + 18 244.7 i, 102.683 + 0.00161781 i, 24 263.2 + 213.085 i,
          -4701.81 - 18 244.7 i, -102.683 - 0.00161781 i, -24 263.2 - 213.085 i}

dataSet=GDT-Alfven
ne0= $1.5 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1264]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1264]= {4701.81 + 18 244.7 i, 102.683 + 0.00161781 i, 24 263.2 + 213.085 i,
  -4701.81 - 18 244.7 i, -102.683 - 0.00161781 i, -24 263.2 - 213.085 i}

Out[1266]= {nx -> 4701.81 + 18 244.7 i}
Out[1267]= {nx -> 102.683 + 0.00161781 i}
Out[1268]= {nx -> 24 263.2 + 213.085 i}
Out[1269]= {nx -> -4701.81 - 18 244.7 i}
Out[1270]= {nx -> -102.683 - 0.00161781 i}
Out[1271]= {nx -> -24 263.2 - 213.085 i}

dataSet=GDT-Alfven
ne0= $1.5 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1273]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1273]= {4701.81 + 18 244.7 i, 102.683 + 0.00161781 i, 24 263.2 + 213.085 i,
  -4701.81 - 18 244.7 i, -102.683 - 0.00161781 i, -24 263.2 - 213.085 i}

Out[1275]= {nx -> 4828.42 + 18 342.3 i}

Out[1276]= {nx -> 102.683 + 0.00161781 i}

Out[1277]= {nx -> 102.683 + 0.00161781 i}

Out[1278]= {nx -> -4828.42 - 18 342.3 i}

Out[1279]= {nx -> -102.683 - 0.00161781 i}

Out[1280]= {nx -> -102.683 - 0.00161781 i}

dataSet=GDT-Alfven
ne0= $1.5 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

## Find Roots T = 50ev

```
In[1282]:= TList = Table[0., {i, 1, 6}];
          TList[[1]] = .05; TList[[2]] = 0.;
          TList[[3]] = 0.05; TList[[4]] = 0.;
          TList[[5]] = 0.;
          TList[[6]] = 0.;
```

## Cold Plasma

```
In[1286]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1286]= {102.764, 0. + 13 638.3 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $1.5 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1288]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1288]= {102.584 + 0.0441028 i, 7289.22 + 305.127 i, 9896.95 + 4768.98 i,
          -102.584 - 0.0441028 i, -7289.22 - 305.127 i, -9896.95 - 4768.98 i}

dataSet=GDT-Alfven
ne0= $1.5 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
```



## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1290]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1290]= {102.584 + 0.0441028 i, 7289.22 + 305.127 i, 9896.95 + 4768.98 i,
  -102.584 - 0.0441028 i, -7289.22 - 305.127 i, -9896.95 - 4768.98 i}

Out[1292]= {nx -> 102.584 + 0.0441028 i}
Out[1293]= {nx -> 7289.22 + 305.127 i}
Out[1294]= {nx -> 9896.95 + 4768.98 i}
Out[1295]= {nx -> -102.584 - 0.0441028 i}
Out[1296]= {nx -> -7289.22 - 305.127 i}
Out[1297]= {nx -> -9896.95 - 4768.98 i}

dataSet=GDT-Alfven
ne0= $1.5 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1299]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1299]= {102.584 + 0.0441028 i, 7289.22 + 305.127 i, 9896.95 + 4768.98 i,
  -102.584 - 0.0441028 i, -7289.22 - 305.127 i, -9896.95 - 4768.98 i}

Out[1301]= {nx -> 102.584 + 0.0441029 i}
Out[1302]= {nx -> 8796.53 + 3132.34 i}
Out[1303]= {nx -> 8796.53 + 3132.34 i}
Out[1304]= {nx -> -102.584 - 0.0441029 i}
Out[1305]= {nx -> -8796.53 - 3132.34 i}
Out[1306]= {nx -> -8796.53 - 3132.34 i}

dataSet=GDT-Alfven
ne0= $1.5 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

---

Higher density,  $n_e = 2.2 \times 10^{19}$ ,

above Alfvén resonance. Is there any sign of kinetic Alfvén wave?

```
In[1308]:= ne0 =  $2.2 \times 10^{20}$ ;
```

## Find Roots $T = 0.1$ eV

```
In[1309]:= TList = Table[0., {i, 1, 6}];
TList[[1]] = .0001; TList[[2]] = 0.;
TList[[3]] = .0001; TList[[4]] = 0.;
TList[[5]] = 0.;
TList[[6]] = 0.;
```

## Cold Plasma

```
In[1313]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1313]:= {171.832, 0. + 16 922.8 i}

dataSet=GDT-Alfvén
freq=7.5
ne0= $2.2 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1315]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1315]:= {0. + 17 010. i, 171.768, 176 193., 0. - 17 010. i, -171.768, -176 193.}

dataSet=GDT-Alfvén
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1317]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1317]= {0. + 17 010. i, 171.768, 176 193., 0. - 17 010. i, -171.768, -176 193.}

Out[1319]= {nx -> 1.55617 x 10-61 + 17 010. i}
Out[1320]= {nx -> 171.768 + 6.50914 x 10-68 i}
Out[1321]= {nx -> 176 193. + 1.49888 x 10-63 i}
Out[1322]= {nx -> -1.55617 x 10-61 - 17 010. i}
Out[1323]= {nx -> -171.768 - 6.50914 x 10-68 i}
Out[1324]= {nx -> -176 193. - 1.49888 x 10-63 i}

dataSet=GDT-Alfven
ne0=2.2 x 1020
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1326]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1326]= {0. + 17 010. i, 171.768, 176 193., 0. - 17 010. i, -171.768, -176 193.}

Out[1328]= {nx -> 1.55619 x 10-61 + 17 010.1 i}
Out[1329]= {nx -> 171.768 + 6.50924 x 10-68 i}
Out[1330]= {nx -> 171.768 + 1.01634 x 10-62 i}
Out[1331]= {nx -> -1.55619 x 10-61 - 17 010.1 i}
Out[1332]= {nx -> -171.768 - 6.50924 x 10-68 i}
Out[1333]= {nx -> -171.768 - 1.01634 x 10-62 i}

dataSet=GDT-Alfven
ne0=2.2 x 1020
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.0001, 0., 0.0001, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

## Find Roots T = 1ev

```
In[1335]:= TList = Table[0., {i, 1, 6}];
          TList[[1]] = 0.001; TList[[2]] = 0.;
          TList[[3]] = 0.001; TList[[4]] = 0.;
          TList[[5]] = 0.;
          TList[[6]] = 0.;
```

## Cold Plasma

```
In[1339]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
```

```
Out[1339]= {171.832, 0. + 16 922.8 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $2.2 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1341]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
```

```
Out[1341]= {0.250414 + 17 953.1 i, 171.761 + 9.17177  $\times 10^{-8}$  i, 55 480.4 + 0.00663982 i,
          -0.250414 - 17 953.1 i, -171.761 - 9.17177  $\times 10^{-8}$  i, -55 480.4 - 0.00663982 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.001, 0., 0.001, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1343]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1343]= {0.250414 + 17 953.1 i, 171.761 + 9.17177 × 10-8 i, 55 480.4 + 0.00663982 i,
  -0.250414 - 17 953.1 i, -171.761 - 9.17177 × 10-8 i, -55 480.4 - 0.00663982 i}

Out[1345]= {nx → 0.250414 + 17 953.1 i}
Out[1346]= {nx → 171.761 + 9.17177 × 10-8 i}
Out[1347]= {nx → 55 480.4 + 0.00663982 i}
Out[1348]= {nx → -0.250414 - 17 953.1 i}
Out[1349]= {nx → -171.761 - 9.17177 × 10-8 i}
Out[1350]= {nx → -55 480.4 - 0.00663982 i}

dataSet=GDT-Alfven
ne0=2.2 × 1020
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.001, 0., 0.001, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1352]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1352]:= {0.250414 + 17 953.1 i, 171.761 + 9.17177 × 10-8 i, 55 480.4 + 0.00663982 i,
  -0.250414 - 17 953.1 i, -171.761 - 9.17177 × 10-8 i, -55 480.4 - 0.00663982 i}

Out[1354]:= {nx → 0.250779 + 17 958.7 i}
Out[1355]:= {nx → 171.761 + 9.17177 × 10-8 i}
Out[1356]:= {nx → 171.761 + 9.17177 × 10-8 i}
Out[1357]:= {nx → -0.250779 - 17 958.7 i}
Out[1358]:= {nx → -171.761 - 9.17177 × 10-8 i}
Out[1359]:= {nx → -171.761 - 9.17177 × 10-8 i}

dataSet=GDT-Alfven
ne0=2.2 × 1020
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.001, 0., 0.001, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```



## Find Roots T = 5ev

```
In[1361]:= TList = Table[0., {i, 1, 6}];
          TList[[1]] = 0.005; TList[[2]] = 0.;
          TList[[3]] = 0.005; TList[[4]] = 0.;
          TList[[5]] = 0.;
          TList[[6]] = 0.;
```

## Cold Plasma

```
In[1365]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1365]= {171.832, 0. + 16 922.8 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $2.2 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1367]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1367]= {5751.96 + 22 565.1 i, 171.728 + 0.00269261 i, 24 365.8 + 149.55 i,
          -5751.96 - 22 565.1 i, -171.728 - 0.00269261 i, -24 365.8 - 149.55 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1369]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1369]= {5751.96 + 22 565.1 i, 171.728 + 0.00269261 i, 24 365.8 + 149.55 i,
  -5751.96 - 22 565.1 i, -171.728 - 0.00269261 i, -24 365.8 - 149.55 i}

Out[1371]= {nx -> 5751.96 + 22 565.1 i}
Out[1372]= {nx -> 171.728 + 0.00269261 i}
Out[1373]= {nx -> 24 365.8 + 149.55 i}
Out[1374]= {nx -> -5751.96 - 22 565.1 i}
Out[1375]= {nx -> -171.728 - 0.00269261 i}
Out[1376]= {nx -> -24 365.8 - 149.55 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1378]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1378]= {5751.96 + 22 565.1 i, 171.728 + 0.00269261 i, 24 365.8 + 149.55 i,
  -5751.96 - 22 565.1 i, -171.728 - 0.00269261 i, -24 365.8 - 149.55 i}

Out[1380]= {nx -> 5904.04 + 22 723.9 i}

Out[1381]= {nx -> 171.728 + 0.00269261 i}

Out[1382]= {nx -> 171.728 + 0.00269261 i}

Out[1383]= {nx -> -5904.04 - 22 723.9 i}

Out[1384]= {nx -> -171.728 - 0.00269261 i}

Out[1385]= {nx -> -171.728 - 0.00269261 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.005, 0., 0.005, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

## Find Roots T = 50ev

```
In[1387]:= TList = Table[0., {i, 1, 6}];
          TList[[1]] = 0.05; TList[[2]] = 0.;
          TList[[3]] = 0.05; TList[[4]] = 0.;
          TList[[5]] = 0.;
          TList[[6]] = 0.;
```

## Cold Plasma

```
In[1391]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];
```

```
Out[1391]:= {171.832, 0. + 16 922.8 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $2.2 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1393]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];
```

```
Out[1393]:= {171.474 + 0.100576 i, 7497.82 + 131.964 i, 11 825.1 + 6056.76 i,
          -171.474 - 0.100576 i, -7497.82 - 131.964 i, -11 825.1 - 6056.76 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1395]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1395]= {171.474 + 0.100576 i, 7497.82 + 131.964 i, 11825.1 + 6056.76 i,
  -171.474 - 0.100576 i, -7497.82 - 131.964 i, -11825.1 - 6056.76 i}

Out[1397]= {nx -> 171.474 + 0.100576 i}
Out[1398]= {nx -> 7497.82 + 131.964 i}
Out[1399]= {nx -> 11825.1 + 6056.76 i}
Out[1400]= {nx -> -171.474 - 0.100576 i}
Out[1401]= {nx -> -7497.82 - 131.964 i}
Out[1402]= {nx -> -11825.1 - 6056.76 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1404]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1404]= {171.474 + 0.100576 i, 7497.82 + 131.964 i, 11825.1 + 6056.76 i,
  -171.474 - 0.100576 i, -7497.82 - 131.964 i, -11825.1 - 6056.76 i}

Out[1406]= {nx -> 171.475 + 0.100577 i}

Out[1407]= {nx -> 10861. + 3573.08 i}

Out[1408]= {nx -> 10861. + 3573.08 i}

Out[1409]= {nx -> -171.475 - 0.100577 i}

Out[1410]= {nx -> -10861. - 3573.08 i}

Out[1411]= {nx -> -10861. - 3573.08 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.05, 0., 0.05, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

## Find Roots T = 500ev

```
In[1413]:= TList = Table[0., {i, 1, 6}];
          TList[[1]] = 0.5; TList[[2]] = 0.;
          TList[[3]] = 0.5; TList[[4]] = 0.;
          TList[[5]] = 0.;
          TList[[6]] = 0.;
```

## Cold Plasma

```
In[1417]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1417]= {171.832, 0. + 16 922.8 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $2.2 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1419]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1419]= {169.609 + 0.464606 i, 2450.31 + 11.7149 i, 4551.73 + 729.11 i,
          -169.609 - 0.464606 i, -2450.31 - 11.7149 i, -4551.73 - 729.11 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.5, 0., 0.5, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1421]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1421]= {169.609 + 0.464606 i, 2450.31 + 11.7149 i, 4551.73 + 729.11 i,
  -169.609 - 0.464606 i, -2450.31 - 11.7149 i, -4551.73 - 729.11 i}

Out[1423]= {nx -> 169.609 + 0.464606 i}
Out[1424]= {nx -> 2450.31 + 11.7149 i}
Out[1425]= {nx -> 4551.73 + 729.11 i}
Out[1426]= {nx -> -169.609 - 0.464606 i}
Out[1427]= {nx -> -2450.31 - 11.7149 i}
Out[1428]= {nx -> -4551.73 - 729.11 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.5, 0., 0.5, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```



## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1430]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1430]= {169.609 + 0.464606 i, 2450.31 + 11.7149 i, 4551.73 + 729.11 i,
  -169.609 - 0.464606 i, -2450.31 - 11.7149 i, -4551.73 - 729.11 i}

Out[1432]= {nx -> 169.648 + 0.465305 i}

Out[1433]= {nx -> 3632.25 + 365.42 i}

Out[1434]= {nx -> 3632.25 + 365.42 i}

Out[1435]= {nx -> -169.648 - 0.465305 i}

Out[1436]= {nx -> -3632.25 - 365.42 i}

Out[1437]= {nx -> -3632.25 - 365.42 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.5, 0., 0.5, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

## Find Roots T = 500ev

```
In[1439]:= TList = Table[0., {i, 1, 6}];
          TList[[1]] = 0.5; TList[[2]] = 0.;
          TList[[3]] = 0.5; TList[[4]] = 0.;
          TList[[5]] = 0.;
          TList[[6]] = 0.;
```

## Cold Plasma

```
In[1443]:= ColdDis2FS[freq, ne0, B0, nz, etaList]
          paramPrint[{dataSet, freq, ne0, B0, nz, etaList}];

Out[1443]= {171.832, 0. + 16 922.8 i}

dataSet=GDT-Alfven
freq=7.5
ne0= $2.2 \times 10^{20}$ 
B0=1.2
nz=127.324
etaList={0., 1., 0., 0., 0.}
```

## Warm Plasma (6th order system solved with NSolve)

```
In[1445]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
          paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList}];

Out[1445]= {169.609 + 0.464606 i, 2450.31 + 11.7149 i, 4551.73 + 729.11 i,
          -169.609 - 0.464606 i, -2450.31 - 11.7149 i, -4551.73 - 729.11 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.5, 0., 0.5, 0., 0., 0.}
```

## Warm Plasma (6th order system solved with FindRoot i.e. all species modelList=1)

```

In[1447]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model1 = Table[1, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model1], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model1], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model1}];

Out[1447]= {169.609 + 0.464606 i, 2450.31 + 11.7149 i, 4551.73 + 729.11 i,
  -169.609 - 0.464606 i, -2450.31 - 11.7149 i, -4551.73 - 729.11 i}

Out[1449]= {nx -> 169.609 + 0.464606 i}

Out[1450]= {nx -> 2450.31 + 11.7149 i}

Out[1451]= {nx -> 4551.73 + 729.11 i}

Out[1452]= {nx -> -169.609 - 0.464606 i}

Out[1453]= {nx -> -2450.31 - 11.7149 i}

Out[1454]= {nx -> -4551.73 - 729.11 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.5, 0., 0.5, 0., 0., 0.}
model1={1, 1, 1, 1, 1, 1}

```

## Hot Plasma (Full Maxwellian system solved with FindRoot i.e. all species modelList=2)

```

In[1456]:= rootsWarm = WarmDis6[freq, ne0, B0, nz, etaList, TList]
model2 = Table[2, {i, 1, 6}];
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList,
  nminList, nmaxList, model2], {nx, rootsWarm[[1]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[2]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[3]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[4]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[5]]}, MaxIterations -> 30]
FindRoot[DisFuncGeneral[freq, ne0, B0, nz, nx, etaList, TList, nminList,
  nmaxList, model2], {nx, rootsWarm[[6]]}, MaxIterations -> 30]
paramPrint[{dataSet, ne0, B0, freq, nz, etaList, TList, model2}];

Out[1456]= {169.609 + 0.464606 i, 2450.31 + 11.7149 i, 4551.73 + 729.11 i,
  -169.609 - 0.464606 i, -2450.31 - 11.7149 i, -4551.73 - 729.11 i}

Out[1458]= {nx -> 169.648 + 0.465305 i}

Out[1459]= {nx -> 3632.25 + 365.42 i}

Out[1460]= {nx -> 3632.25 + 365.42 i}

Out[1461]= {nx -> -169.648 - 0.465305 i}

Out[1462]= {nx -> -3632.25 - 365.42 i}

Out[1463]= {nx -> -3632.25 - 365.42 i}

dataSet=GDT-Alfven
ne0= $2.2 \times 10^{20}$ 
B0=1.2
freq=7.5
nz=127.324
etaList={0., 1., 0., 0., 0.}
TList={0.5, 0., 0.5, 0., 0., 0.}
model2={2, 2, 2, 2, 2, 2}

```

Stix criterion for kinetic Alfven wave  $\beta_i > \frac{8}{3} m_e / m_i \left(1 - \frac{\omega^2}{4\Omega_i^2}\right)$

```
8. / 3. / 3670 * (1 - (7.5 / (4 * 9.15) ^2))
```

```
0.000722544
```

- By my calculation at 500 ev,  $\beta_i = 0.003$  so meets criterion by a lot. But I don ' t see a propagating or weakly damped wave.