

Python installing alternatives

Python:

<https://www.python.org/downloads/>

Pycharm IDE:

<https://www.jetbrains.com/pycharm/>

Anaconda:

<https://www.anaconda.com/distribution/#download-section>

Google Colab:

<https://colab.research.google.com/>

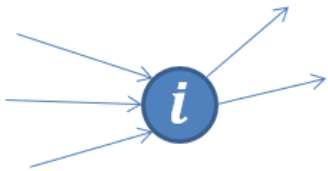
Libraries:

- Numpy
- Scipy
- Matplotlib

Basic utils

#EX0: Understanding model needs

$$\min \sum_{ij \in A} c_{ij} x_{ij}$$



$$\sum_{j \atop ij \in A} x_{ij} - \sum_{j \atop ji \in A} x_{ji} = b_i \quad \forall i \in N$$

$$l_{ij} \leq x_{ij} \leq u_{ij} \quad \forall ij \in A$$

C: cost vector, **dimension: arcs**

b: linear equality constraint, **dimension: nodes**

lb: lower bound, dimension: **arcs**

ub: upper bound, dimension: **arcs**

NA: node arc matrix, **dimension: nodes x arcs**

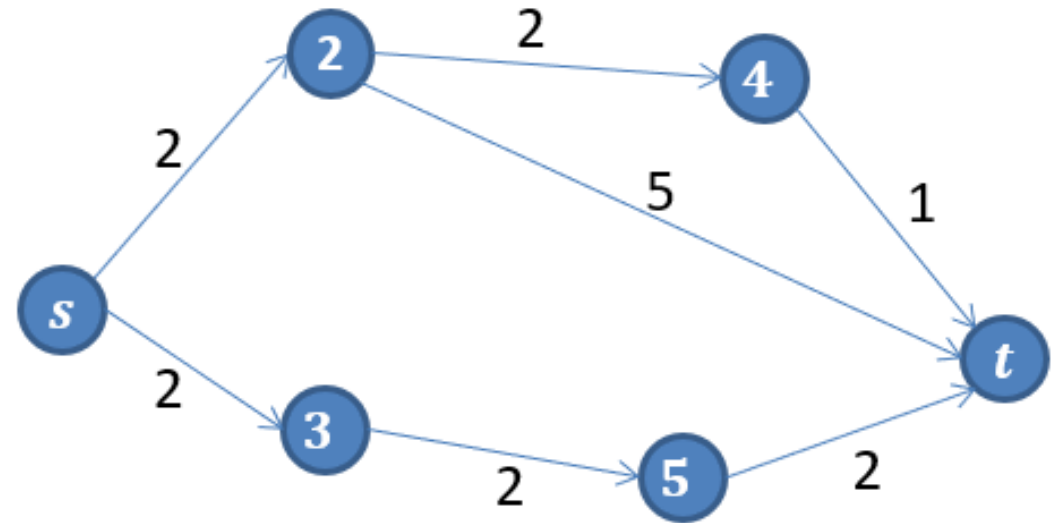
#EX0: Build a function that transforms Node-Node matrix (incidence matrix) to Node-Arc matrix

* Need help? get the solution from repository: https://github.com/rmaranzana/oss11_basic_examples

Shortest Path

#EX1: Basic example SP

- 1) Understand the MCF model formulation.
- 2) Try to translate the math to the python code:
 - 1) Numpy library for matrix operations
 - 2) Scipy library for LP optimization
- 3) Learn to use `scipy.linprog`
- 4) Understand the outputs
- 5) What's the shortest path?

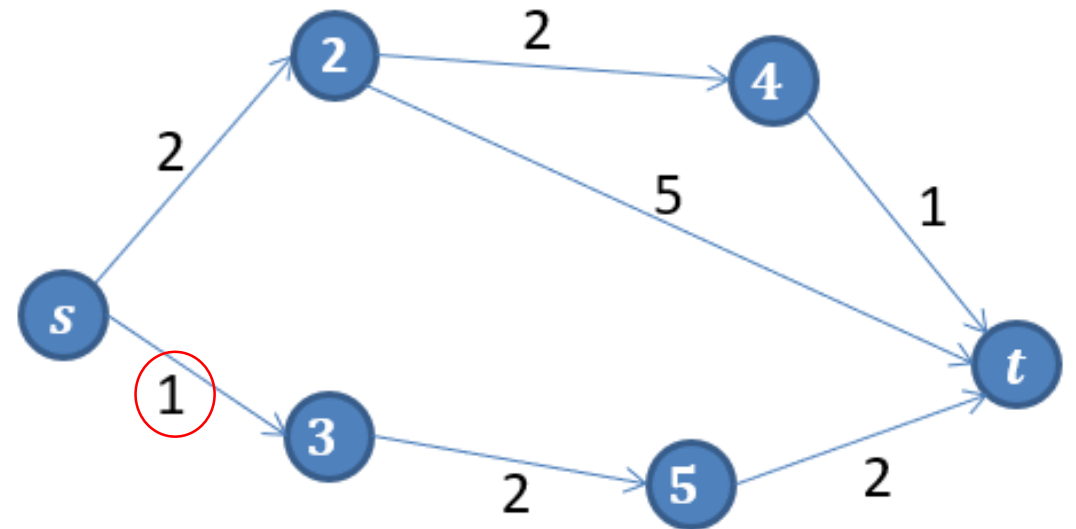


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Shortest Path

#EX2: Basic example SP

- 1) Try the same procedure with this example
- 2) Check the solution
- 3) Try changing the method to SIMPLEX
- 4) Get the shortest path

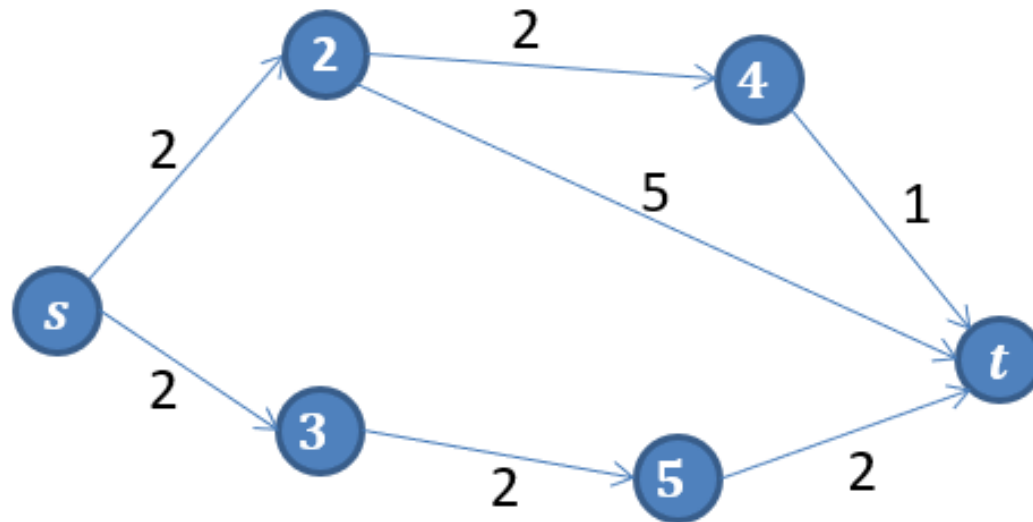


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Shortest Path

#EX3 Basic example SP with Dijkstra algorithm

1) Implement the Dijkstra algorithm and check the #EX1 solution



Dijkstra algorithm

Pseudocode:

Initialize the weights:

for each node_i in graph:

weight(node_i) = inf

 prec[node_i] = 0

weight(initial_node) = 0

Iterate:

while **unexplored_nodes** not empty:

 head = node with minimum weight in **unexplored_nodes**

 pop head node from **unexplored_nodes**

for each neighbor_i of head:

 potential_weight = **weight**[head] + dist[head, neighbor_i]

if potential_weight < **weight**[neighbor]:

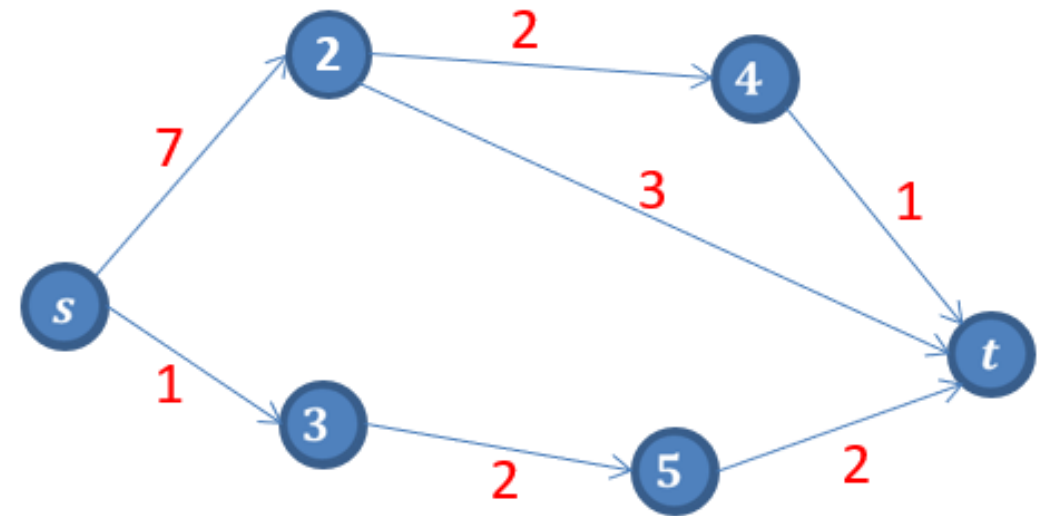
weight[neighbor] = potential weight

 prec[neighbor] = head

Maximum Flow

#EX3: Basic example SP

- 1) Understand the MCF model formulation.
- 2) Translate the math to python code. (*Pay attention to model boundaries, LB / UB*)
- 3) Understand the outputs
- 4) What's the maximum flow?
- 5) What's the minimum cut?

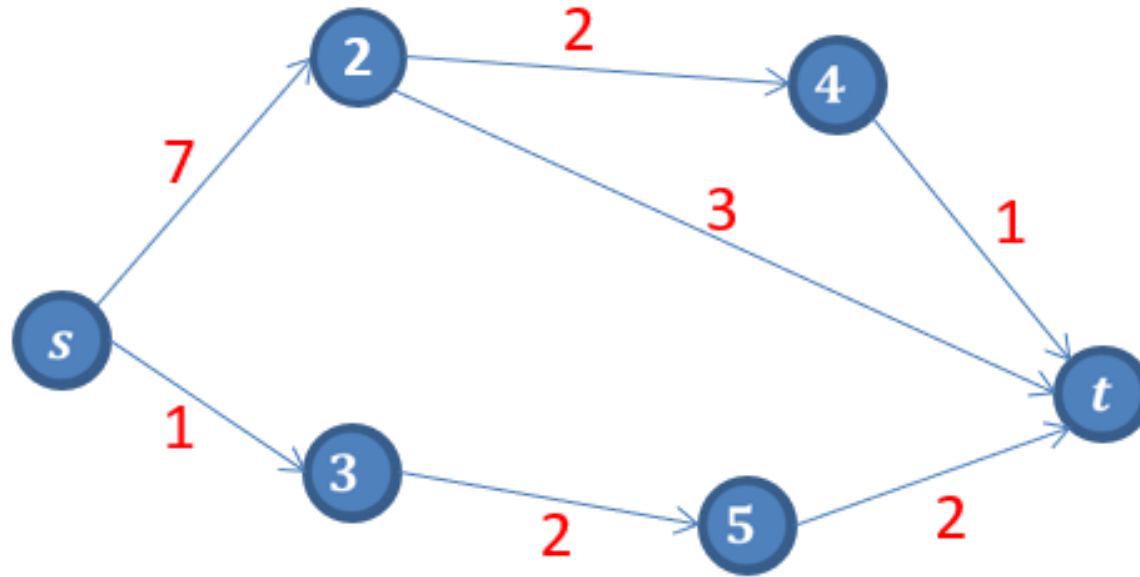


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Maximum Flow

#EX4: Basic example SP with Ford-Fulkerson algorithm

1) Implement the Ford-Fulkerson algorithm and check the #EX3 solution



* Need help? get the solution from repository: https://github.com/rmaranzana/oss11_basic_examples

Ford-Fulkerson algorithm

Pseudocode:

$\text{residual_G} = G$ for all edges (u, v) and 0 for all edges (v, u)

path = perform DFS(source, sink) to find an augmenting path

while **path** exists:

 for each edge in **path**:

$\text{residual_G}(u, v) = \text{flow}(u, v) - \text{path max_capacity}$

$\text{residual_G}(v, u) = \text{flow}(v, u) + \text{path max_capacity}$

path = perform DFS(source, sink)

Transport

#EX5: Transport model example

- 1) Understand the MCF model formulation
- 2) Get the optimum number of units to be carried from factories to warehouses for each arc.

