Bistable motif: parameter sampling

Finding the condition of multistationarity

We consider the following reactions:

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\begin{split} &K+S\leftrightharpoons KS\to K+S_p\\ &K^{\color{red} *}+S\leftrightharpoons K^{\color{red} *}S\to K^{\color{red} *}+S_p\\ &S_p\to S\\ &K\leftrightharpoons K^{\color{red} *}\\ &KS\leftrightharpoons K^{\color{red} *}S \end{split}
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The species of the system are:

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\{S, S_p, K, K^*, KS, K^*S\}
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In total, there are 11 reations and 6 species.

We firstly construct the ordinary differential equations based on mass-action kinetics. Then compute the determinant of Jacobian, using the solution at critical point (steady state) to calculate the determinant. The (necessary) condition for multistationarity is to make determinant equal to zero (non-zero determinant implys injectivity).

```
A = Table[0, {11}, {6}];
A[[1]][[1]] = -1;
A[[1]][[3]] = -1;
A[[1]][[5]] = 1;
A[[2]] = -A[[1]];
A[[3]][[3]] = 1; A[[3]][[2]] = 1; A[[3]][[5]] = -1;
A[[4]][[1]] = -1;
A[[4]][[4]] = -1;
A[[4]][[6]] = 1;
A[[5]] = -A[[4]];
A[[6]][[4]] = 1;
A[[6]][[2]] = 1;
A[[6]][[6]] = -1;
A[[7]][[2]] = -1;
A[[7]][[1]] = 1;
A[[8]][[3]] = -1; A[[8]][[4]] = 1; A[[9]] = -A[[8]];
A[[10]][[5]] = -1; A[[10]][[6]] = 1; A[[11]] = -A[[10]];
stoiM = Transpose[A];
 (* Now we construct the rate vector *)
ks = \{k_1 \times x_3 \times x_1, k_2 \times x_5, k_3 \times x_5, k_4 \times x_4 \times x_1, k_5 \times x_5, k_5 \times x_5 \times x_5, k_5 \times x_5 \times x_5, k_5 \times x_5 \times x_5
             k_5 \times x_6, k_6 \times x_6, k_7 \times x_2, k_8 \times x_3, k_9 \times x_4, k_{10} \times x_5, k_{11} \times x_6};
ssEqns = stoiM.ks;
mC = RowReduce[NullSpace[A]];
 subsEqns = {ssEqns[[2]], ssEqns[[4]],
             ssEqns[[5]], ssEqns[[6]], x_1 + x_2 + x_5 + x_6 - T_1, x_3 + x_4 + x_5 + x_6 - T_2;
jacobian = D[subsEqns, \{\{x_1, x_2, x_3, x_4, x_5, x_6\}\}\}];
\texttt{detJ} = \texttt{Collect[Distribute[Det[jacobian]], \{x_1, x_2, x_3, x_4, x_5, x_6\}];}
 solution =
         Solve[{subsEqns[[1]], subsEqns[[2]], subsEqns[[3]], subsEqns[[4]]} == 0},
             \{x_2, x_4, x_5, x_6\}];
detSubs = Replace[detJ, solution[[1]], {0, Infinity}];
 (* Equivilant to detSubs=detJ/.solution[[1]]; *)
polSubs = Numerator[Together[detSubs]];
 finalSubs = Collect[Distribute[polSubs], x , FactorTerms]
```

 $-\,k_{2}^{2}\,\,k_{5}^{2}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,2\,\,k_{2}\,\,k_{3}\,\,k_{5}^{2}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,k_{3}^{2}\,\,k_{5}^{2}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,2\,\,k_{2}^{2}\,\,k_{5}\,\,k_{6}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,4\,\,k_{2}\,\,k_{3}\,\,k_{5}\,\,k_{6}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,k_{3}^{2}\,\,k_{5}^{2}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,2\,\,k_{2}^{2}\,\,k_{5}^{2}\,\,k_{5}\,\,k_{6}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,4\,\,k_{2}\,\,k_{3}\,\,k_{5}\,\,k_{6}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,k_{3}^{2}\,\,k_{5}^{2}\,\,k_{7}\,\,k_{8}\,\,k_{9}\,-\,k_{3}^{2}\,\,k_{7}^{2}\,\,k_{9$ $2 k_3^2 k_5 k_6 k_7 k_8 k_9 - k_2^2 k_6^2 k_7 k_8 k_9 - 2 k_2 k_3 k_6^2 k_7 k_8 k_9 - k_3^2 k_6^2 k_7 k_8 k_9 - k_2^2 k_5^2 k_7 k_9^2 - k_1^2 k_1^2$ $2\;k_2\;k_3\;k_5^2\;k_7\;k_9^2-k_3^2\;k_5^2\;k_7\;k_9^2-2\;k_2^2\;k_5\;k_6\;k_7\;k_9^2-4\;k_2\;k_3\;k_5\;k_6\;k_7\;k_9^2-2\;k_3^2\;k_5\;k_6\;k_7\;k_9^2-2\;k_3^2\;k_5\;k_6\;k_7\;k_9^2-2\;k_3^2\;k_5^$ $k_2^2 \ k_6^2 \ k_7 \ k_9^2 - 2 \ k_2 \ k_3 \ k_6^2 \ k_7 \ k_9^2 - k_3^2 \ k_6^2 \ k_7 \ k_9^2 - 2 \ k_2 \ k_5^2 \ k_7 \ k_8 \ k_9 \ k_{10} - 2 \ k_3 \ k_5^2 \ k_7 \ k_8 \ k_9 \ k_{10} - 2 \ k_9 \ k_{10} - 2 \ k_9 \ k_9 \ k_9 \ k_{10} - 2 \ k_$ $4\;k_2\;k_5\;k_6\;k_7\;k_8\;k_9\;k_{10}\;-\;4\;k_3\;k_5\;k_6\;k_7\;k_8\;k_9\;k_{10}\;-\;2\;k_2\;k_6^2\;k_7\;k_8\;k_9\;k_{10}\;-\;2\;k_3\;k_6^2\;k_7\;k_8\;k_9\;k_{10}\;-\;2\;k_2\;k_6^2\;k_7\;k_8^2\;k_9\;k_{10}\;-\;2\;k_2\;k_6^2\;k_7\;k_8^2\;k_9\;k_{10}\;-\;2\;k_2\;k_6^2\;k_7\;k_8^2\;k_9\;k_{10}\;-\;2\;k_2\;k_6^2\;k_7\;k_8^2\;k_9\;k_{10}\;-\;2\;k_2\;k_6^2\;k_7\;k_8^2\;k_9^2\;$ $2 k_2 k_5^2 k_7 k_9^2 k_{10} - 2 k_3 k_5^2 k_7 k_9^2 k_{10} - 4 k_2 k_5 k_6 k_7 k_9^2 k_{10} - 4 k_3 k_5 k_6 k_7 k_9^2 k_{10} - 2 k_2 k_6^2 k_7 k_9^2 k_{10}
2\;k_3\;k_6^2\;k_7\;k_9^2\;k_{10}\;-\;k_5^2\;k_7\;k_8\;k_9\;k_{10}^2\;-\;2\;k_5\;k_6\;k_7\;k_8\;k_9\;k_{10}^2\;-\;k_6^2\;k_7\;k_8\;k_9\;k_{10}^2\;-\;k_5^2\;k_7\;k_9^2\;k_{10}^2\;-\;k_9^2\;k_{10}^2\;k_{10}^2\;-\;k_9^2\;k_{10}^2\; 2\ k_5\ k_6\ k_7\ k_9^2\ k_{10}^2\ -\ k_6^2\ k_7\ k_9^2\ k_{10}^2\ -\ 2\ k_2^2\ k_5\ k_7\ k_8\ k_9\ k_{11}\ -\ 4\ k_2\ k_3\ k_5\ k_7\ k_8\ k_9\ k_{11}\ -\ 2\ k_3^2\ k_5\ k_7\ k_8\ k_9\ k_{11}\ -\ 2\ k_3\ k_9\ k_{11}\ -\ 2\ k_9\ k_{11}\ -\$ $2\ k_2^2\ k_6\ k_7\ k_8\ k_9\ k_{11}-4\ k_2\ k_3\ k_6\ k_7\ k_8\ k_9\ k_{11}-2\ k_3^2\ k_6\ k_7\ k_8\ k_9\ k_{11}-2\ k_2^2\ k_5\ k_7\ k_9^2\ k_{11} 4 k_2 k_3 k_5 k_7 k_9^2 k_{11} - 2 k_3^2 k_5 k_7 k_9^2 k_{11} - 2 k_2^2 k_6 k_7 k_9^2 k_{11} - 4 k_2 k_3 k_6 k_7 k_9^2 k_{11} - 2 k_3^2 k_6 k_7 k_9^2 k_{11} 2\;k_2\;k_5\;k_7\;k_8\;k_9\;k_{10}\;k_{11}-2\;k_3\;k_5\;k_7\;k_8\;k_9\;k_{10}\;k_{11}-2\;k_2\;k_6\;k_7\;k_8\;k_9\;k_{10}\;k_{11}-2\;k_3\;k_6\;k_7\;k_8\;k_9\;k_{10}\;k_{11}-2\;k_8\;k_9\;k_{10}-2\;k_9\;k_{11}-2\;k_9\;k_{11}-2\;k_9\;k_9\;k_{10}-2\;k_9\;k_{10}-2\;k$ $2\;k_2\;k_5\;k_7\;k_9^2\;k_{10}\;k_{11}-2\;k_3\;k_5\;k_7\;k_9^2\;k_{10}\;k_{11}-2\;k_2\;k_6\;k_7\;k_9^2\;k_{10}\;k_{11}-2\;k_3\;k_6\;k_7\;k_9^2\;k_{10}\;k_{11}-2\;k_2\;k_6\;k_7\;k_9^2\;k_{10}-2\;k_2\;k_6\;k_7\;k_9^2\;k_{10}-2\;k_2\;k_9\;k_9^2\;k_{10}-2\;k_2\;k_9^2\;k_9^2\;k_{10}-2\;k_2\;k_9^2\;k_9^2\;k_{10}-2\;k_9^2\;k_9^2\;k_{10}-2\;k_9^2\;k_9^2\;k_9^2\;k_{10}-2\;k_9^2$ $k_2^2 \; k_7 \; k_8 \; k_9 \; k_{11}^2 \; - \; 2 \; k_2 \; k_3 \; k_7 \; k_8 \; k_9 \; k_{11}^2 \; - \; k_3^2 \; k_7 \; k_8 \; k_9 \; k_{11}^2 \; - \; k_2^2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; 2 \; k_2 \; k_3 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; 2 \; k_1 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_3 \; k_1 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_3 \; k_1 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_2 \; k_2$ $k_{3}^{2}\ k_{7}\ k_{9}^{2}\ k_{11}^{2}\ +\ \left(-\ k_{1}\ k_{2}\ k_{4}^{2}\ k_{7}\ k_{10}\ k_{11}\ -\ k_{1}\ k_{3}\ k_{4}^{2}\ k_{7}\ k_{10}\ k_{11}\ -\ k_{1}\ k_{2}\ k_{4}^{2}\ k_{7}\ k_{11}^{2}\ -\ k_{1}\ k_{3}\ k_{4}^{2}\ k_{7}\ k_{11}^{2}\right)\ x_{1}^{3}\ +\ k_{1}^{2}\ k_{1$
$\left(-\,k_{2}^{2}\,\,k_{4}\,\,k_{5}\,\,k_{6}\,\,k_{8}^{2}\,-\,2\,\,k_{2}\,\,k_{3}\,\,k_{4}\,\,k_{5}\,\,k_{6}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{5}\,\,k_{6}\,\,k_{8}^{2}\,-\,k_{2}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,2\,\,k_{2}\,\,k_{3}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,2\,\,k_{2}\,\,k_{3}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{4}^{2}\,\,k_{6}^{2}\,\,k_{8}^{2}\,-\,k_{3}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6}^{2}\,\,k_{6$ k_{2}^{2} k_{4} k_{5} k_{7} k_{8}^{2} - 2 k_{2} k_{3} k_{4} k_{5} k_{7} k_{8}^{2} - k_{3}^{2} k_{4} k_{5} k_{7} k_{8}^{2} - k_{2}^{2} k_{4} k_{6} k_{7} k_{8}^{2} - 2 k_{2} k_{3} k_{4} k_{5} k_{7} k_{8}^{2} - 2 k_{7} k_{8} - 2 k_{8} k_{8} - 2 k_{8} - 2 k_{8} k_{8} - 2 k_{8} - 2 k_{8} k_{8} - 2 $k_$ $k_3^2 \ k_4 \ k_6 \ k_7 \ k_8^2 - k_1 \ k_2 \ k_3 \ k_5^2 \ k_8 \ k_9 - k_1 \ k_3^2 \ k_5^2 \ k_8 \ k_9 - 2 \ k_1 \ k_2 \ k_3 \ k_5 \ k_6 \ k_8 \ k_9 - 2 \ k_1 \ k_3^2 \ k_5 \ k_6 \ k_8 \ k_9 - 2 \ k_1 \ k_2 \ k_3 \ k_5 \ k_6 \ k_8 \ k_9 - 2 \ k_1 \ k_2 \ k_3 \ k_5 \ k_6 \ k_8 \ k_9 - 2 \ k_1 \ k_2 \ k_3 \ k_5 \ k_6 \ k_8 \ k_9 - 2 \ k_1 \ k_2 \ k_3 \ k_5 \ k_6 \ k_8 \ k_9 - 2 \ k_1 \ k_2 \ k_3 \ k_5 \ k_6 \ k_8 \ k_9 - 2 \ k_1 \ k_2 \ k_9 \$ k_2^2 k_4 k_6 k_7 k_8 k_9 - 2 k_2 k_3 k_4 k_6 k_7 k_8 k_9 - k_3^2 k_4 k_6 k_7 k_8 k_9 - 2 k_1 k_2 k_5 k_6 k_7 k_8 k_9 - $2 k_1 k_3 k_5 k_6 k_7 k_8 k_9 - k_1 k_2 k_6^2 k_7 k_8 k_9 - k_1 k_3 k_6^2 k_7 k_8 k_9 - k_1 k_2 k_3 k_5^2 k_9^2 - k_1 k_3^2 k_5^2 k_9^2 - k_1 k_3^2 k_5^2 k_9^2 - k_1 k_2^2 k_3 k_9^2 k_9^2 - k_1 k_2^2 k_3 k_9^2 k_9^2 - k_1 k_2^2 k_3 k_9^2 k_9^2 - k_1 k_2^2 k_3^2 k_9^2 k_9^2 - k_1 k_2^2 k_3^2 k_9^2 k_9^2 - k_1 k_2^2 k_3^2 k_9^2 k_9^2$ $k_1 k_3 k_5^2 k_7 k_9^2 - 2 k_1 k_2 k_5 k_6 k_7 k_9^2 - 2 k_1 k_3 k_5 k_6 k_7 k_9^2 - k_1 k_2 k_6^2 k_7 k_9^2 - k_1 k_3 k_6^2 k_7 k_9^2 - k_1 k_7 k_$ $2\;k_2\;k_4\;k_5\;k_6\;k_8^2\;k_{10}\;-\;2\;k_3\;k_4\;k_5\;k_6\;k_8^2\;k_{10}\;-\;2\;k_2\;k_4\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_4^2\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_3\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_6^2\;k_8^2\;k_{10}\;-\;2\;k_6^2\;k_6$ $2\;k_2\;k_4\;k_5\;k_7\;k_8^2\;k_{10}\;-\;2\;k_3\;k_4\;k_5\;k_7\;k_8^2\;k_{10}\;-\;2\;k_2\;k_4\;k_6\;k_7\;k_8^2\;k_{10}\;-\;2\;k_3\;k_4\;k_6\;k_7\;k_8^2\;k_{10}\;-\;2\;k_2\;k_4\;k_6\;k_7\;k_8^2\;k_{10}\;-\;2\;k_3\;k_4\;k_6\;k_7\;k_8^2\;k_{10}\;-\;2\;k_2\;k_4\;k_6\;k_7\;k_8^2\;k_{10}\;-\;2\;k_3\;k_4\;k_6\;k_7\;k_8^2\;k_{10}\;-\;2\;k_2\;k_4\;k_6\;k_7\;k_8^2\;k_{10}\;-\;2\;k_3\;k_8^2\;k_{10}\;-\;2\;k_3\;k_8^2\;k_{10}\;-\;2\;k_3\;k_8^2\;k_{10}\;-\;2\;k_3\;k_1^2\;k_{10}\;-\;2\;k_3\;k_1^2\;k_{10}\;-\;2\;k_3\;k_1^2\;k_{10}\;-\;2\;k_1^2\;k_{10}\;-\;2\;k_1^2\;k_{10}\;-\;2\;k_1^2\;k_{10}$ $k_1 \; k_3 \;
k_5^2 \; k_8 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_5 \; k_6 \; k_8 \; k_9 \; k_{10} \; - \; 3 \; k_1 \; k_3 \; k_5 \; k_6 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_5 \; k_6 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k$ $2\;k_3\;k_4\;k_5\;k_6\;k_8\;k_9\;k_{10}-k_1\;k_2\;k_6^2\;k_8\;k_9\;k_{10}-2\;k_1\;k_3\;k_6^2\;k_8\;k_9\;k_{10}-2\;k_2\;k_4\;k_6^2\;k_8\;k_9\;k_{10}-2\;k_2^2\;k_3^$ $2\;k_2\;k_4\;k_6\;k_7\;k_8\;k_9\;k_{10}\;-\;2\;k_3\;k_4\;k_6\;k_7\;k_8\;k_9\;k_{10}\;-\;2\;k_1\;k_5\;k_6\;k_7\;k_8\;k_9\;k_{10}\;-\;k_1\;k_6^2\;k_7\;k_8^2\;k_9\;k_{10}\;-\;k_1\;k_6^2\;k_7\;k_8^2\;k_9$ $k_1 \; k_3 \; k_5^2 \; k_9^2 \; k_{10} \; - \; k_1 \; k_2 \; k_5 \; k_6 \; k_9^2 \; k_{10} \; - \; 3 \; k_1 \; k_3 \; k_5 \; k_6 \; k_9^2 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_9^2 \; k_{10} \; - \; 2 \; k_1 \; k_3 \; k_9^2 \; k_{10} \; - \; 2 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2$ $2\ k_{1}\ k_{5}\ k_{6}\ k_{7}\ k_{9}^{2}\ k_{10}\ -\ k_{1}\ k_{6}^{2}\ k_{7}\ k_{9}^{2}\ k_{10}\ -\ k_{4}\ k_{5}\ k_{6}\ k_{8}^{2}\ k_{10}^{2}\ -\ k_{4}\ k_{6}^{2}\ k_{8}^{2}\ k_{10}^{2}\ -\ k_{4}\ k_{5}\ k_{7}\ k_{8}^{2}\ k_{10}^{2}\ -\ k_{8}\ k_{10}^{2}\ -\ k_{10}\ k_{10}\ -\ k_{10}\ -\ k_{10}\ k_{10}\ -\ k_{10}\ k_{10}\ -\ k_{10}\ -\ k_{10}\ -\ k_{10}\ -\ k_{10}\ k_{10}\ -\ k_{10}\ k_{10}\ -\ k_{10}\ k_{10}\ -\ k_{1$ $k_4 \; k_6 \; k_7 \; k_8^2 \; k_{10}^2 \; - \; k_1 \; k_5 \; k_6 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_4 \; k_5 \; k_6 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_4 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \;
k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_6^2 \; k_8 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_9^2 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_9 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_9 \; k_9 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_9 \; k_9$ $k_1 k_5 k_7 k_8 k_9 k_{10}^2 - k_4 k_5 k_7 k_8 k_9 k_{10}^2 - k_1 k_6 k_7 k_8 k_9 k_{10}^2 - k_4 k_6 k_7 k_8 k_9 k_{10}^2$ $k_1 k_5 k_6 k_9^2 k_{10}^2 - k_1 k_6^2 k_9^2 k_{10}^2 - k_1 k_5 k_7 k_9^2 k_{10}^2 - k_1 k_6 k_7 k_9^2 k_{10}^2 - k_2 k_3 k_4 k_5 k_8^2 k_{11}$ $k_{3}^{2} \; k_{4} \; k_{5} \; k_{8}^{2} \; k_{11} \; - \; k_{2}^{2} \; k_{4} \; k_{6} \; k_{8}^{2} \; k_{11} \; - \; 3 \; k_{2} \; k_{3} \; k_{4} \; k_{6} \; k_{8}^{2} \; k_{11} \; - \; 2 \; k_{3}^{2} \; k_{4} \; k_{6} \; k_{8}^{2} \; k_{11} \; - \; k_{2}^{2} \; k_{4} \; k_{7} \; k_{8}^{2} \; k_{11} \; - \; k_{1}^{2} \; k_{1} \; k_{2}^{2} \; k_{3} \; k_{3} \; k_{4} \; k_{5} \; k_{7} \; k_{8}^{2} \; k_{11} \; - \; k_{1}^{2} \; k_{1}^{2} \; k_{2}^{2} \; k_{3} \; k_{4} \; k_{5} \; k_{7} \; k_{8}^{2} \; k_{11} \; - \; k_{1}^{2} \; k_{1}^{2} \; k_{2}^{2} \; k_{3} \; k_{4} \; k_{5} \; k_{7} \; k_{8}^{2} \; k_{11} \; - \; k_{1}^{2} \; k_{1}^{2} \; k_{2}^{2} \; k_{3} \; k_{4} \; k_{5} \; k_{7} \; k_{8}^{2} \; k_{11} \; - \; k_{1}^{2} \;$ $2\;k_2\;k_3\;k_4\;k_7\;k_8^2\;k_{11}\;-\;k_3^2\;k_4\;k_7\;k_8^2\;k_{11}\;-\;k_2\;k_4\;k_5\;k_7\;k_8^2\;k_{11}\;-\;k_3\;k_4\;k_5\;k_7\;k_8^2\;k_{11}\;-\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_1^2\;k_2^2\;k_1^2\;$ k_2 k_4 k_6 k_7 k_8^2 k_{11} - k_3 k_4 k_6 k_7 k_8^2 k_{11} - 2 k_1 k_2 k_3 k_5 k_8 k_9 k_{11} - 2 k_1 k_3^2 k_5 k_8 k_9 k_{11} k_2 k_3 k_4 k_5 k_8 k_9 k_{11} - k_3^2 k_4 k_5 k_8 k_9 k_{11} - 2 k_1 k_2 k_3 k_6 k_8 k_9 k_{11} - 2 k_1 k_3^2 k_6 k_8 k_9 k_{11} $k_2^2 \; k_4 \; k_6 \; k_8 \; k_9 \; k_{11} \; - \; 3 \; k_2 \; k_3 \; k_4 \; k_6 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_3^2 \; k_4 \; k_6 \; k_8 \; k_9 \; k_{11} \; - \; k_2^2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_1^2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_1^2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_1^2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_1^2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_1^2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_1^2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_1^2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_1^2 \; k_1 \; k_1 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_3 \; k_1 \; k_2 \; k_2 \; k_3 \; k_4 \; k_1 \; k_2 \; k_2 \; k_3 \; k_2 \; k_3 \; k_4 \; k_1 \; k_2 \; k_2 \; k_3 \; k_2 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_2 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_2 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_3 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \;$ $k_2 \; k_4 \; k_5 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; k_3 \; k_4 \; k_5 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_2 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_3 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{11} \; - \; 2 \; k_1 \; k_9 \; k_{$ k_2 k_4 k_6 k_7 k_8 k_9 k_{11} - k_3 k_4 k_6 k_7 k_8 k_9 k_{11} - 2 k_1 k_2 k_3 k_5 k_9^2 k_{11} - 2 k_1 k_3^2 k_5 k_9^2 k_{11} - $2 k_1 k_2 k_3 k_6 k_9^2 k_{11} - 2 k_1 k_3^2 k_6 k_9^2 k_{11} - 2 k_1 k_2 k_5 k_7 k_9^2 k_{11} - 2 k_1 k_3 k_5 k_7 k_9^2 k_{11} 2 k_1 k_2 k_6 k_7 k_9^2 k_{11} - 2 k_1 k_3 k_6 k_7 k_9^2 k_{11} - k_3 k_4 k_5 k_8^2 k_{10} k_{11} - k_2 k_4 k_6 k_8^2 k_{10} k_{11}
2\;k_3\;k_4\;k_6\;k_8^2\;k_{10}\;k_{11}-k_2\;k_4\;k_7\;k_8^2\;k_{10}\;k_{11}-k_3\;k_4\;k_7\;k_8^2\;k_{10}\;k_{11}-k_4\;k_5\;k_7\;k_8^2\;k_{10}\;k_{11}-k_8^2\;k_8^2\;k_{10}^2\;k_{11}-k_8^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_8^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}^2\;k_{11}-k_8^2\;k_{11}^2\;$ $k_4 \; k_6 \; k_7 \; k_8^2 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_3 \; k_4 \; k_5 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_6 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{10} \; k_{11} \; - \; k_1 \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_8 \; k_9 \; k_{10} \; k$ $2\ k_1\ k_3\ k_6\ k_8\ k_9\ k_{10}\ k_{11}\ -\ k_2\ k_4\ k_6\ k_8\ k_9\ k_{10}\ k_{11}\ -\ 2\ k_3\ k_4\ k_6\ k_8\ k_9\ k_{10}\ k_{11}\ -\ 2\ k_8\ k_{10}\ k_{11}\ -\ 2\ k_{11}\ k_{11}\$ $k_1 \; k_2 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_3 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_3 \; k_1 \; k_2 \; k_2 \; k_3 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \;$ $k_1 \; k_5 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_4 \; k_5 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_8 \; k_9 \; k_{10} \; k_{11} \; - \; k_8 \; k_9 \; k_{10} \; k_{10} \; k_{11} \; - \; k_8 \; k_9 \; k_{10} \; k_{10} \; k_{10} \; k_{11} \; - \; k_8 \; k_9 \; k_{10} \;$ $k_1 k_3 k_7 k_9^2 k_{10} k_{11} - k_1 k_5 k_7 k_9^2 k_{10} k_{11} - k_1 k_6 k_7 k_9^2 k_{10} k_{11} - k_2 k_3 k_4 k_8^2 k_{11}^2 k_2 \ k_3 \ k_4 \ k_8 \ k_9 \ k_{11}^2 - k_3^2 \ k_4 \ k_8 \ k_9 \ k_{11}^2 - k_1 \ k_2 \ k_7 \ k_8 \ k_9 \ k_{11}^2 - k_1 \ k_3 \ k_7 \ k_8 \ k_9 \ k_{11}^2 - k_2 \ k_4 \ k_7 \ k_8 \ k_9 \ k_{11}^2 - k_1 \ k_2 \ k_7 \ k_8 \ k_9 \ k_{11}^2 - k_1 \ k_1 \ k_2 \ k_7 \ k_8 \ k_9 \ k_{11}^2 - k_1 \ k_1 \ k_2 \ k_7 \ k_8 \ k_9 \ k_{11}^2 - k_2 \ k_4 \ k_7 \ k_8 \ k_9 \ k_{11}^2 - k_1 \ k_2 \ k_1 \ k_2 \ k_1 \ k_2 \ k_1 \ k_1 \ k_2 \ k_2 \ k_2 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 \ k_2 \ k_2 \ k_2 \ k_1 \ k_2 \ k_2 \ k_2 \ k_2 \ k_2 \ k_2 \ k_3 \ k_2 \ k_2 \ k_2 \ k_3 \ k_3 \ k_3 \ k_4 \ k_3 \ k_4 \ k_2 \ k_3 \ k_3 \ k_3 \ k_3 \ k_3 \ k_4 \ k_3 \ k_3 \ k_3 \ k_3 \ k_3 \ k_4 \ k_3 \ k_3 \ k_3 \ k_3 \ k_3 \ k_4 \ k_3 \$ $k_3 \; k_4 \; k_7 \; k_8 \; k_9 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_3 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_3^2 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_3 \; k_7 \; k_9^2 \; k_{11}^2 \, \right) \; x_3 \; + \; x_4 \; k_5 \; k_9 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_3 \; k_7 \; k_9^2 \; k_{11}^2 \, \right) \; x_3 \; + \; x_4 \; k_7 \; k_8 \; k_9 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_3 \; k_7 \; k_9^2 \; k_{11}^2 \, - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_3 \; k_7 \; k_9^2 \; k_{11}^2 \, \right) \; x_3 \; + \; x_4 \; k_7 \; k_8 \; k_9 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_1 \; k_2 \; k_7 \; k_9^2 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_1 \; k_1 \; k_1 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2$ x_1^2 (- k_1 k_2 k_4 k_5 k_7 k_9 k_{10} - k_1 k_3 k_4 k_5 k_7 k_9 k_{10} - k_1 k_2 k_4 k_6 k_7 k_9 k_{10} - k_1 k_3 k_4 k_6 k_7 k_9 k_{10} -

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k_1 \ k_4 \ k_5 \ k_7 \ k_9 \ k_{10}^2 - k_1 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{10}^2 - k_2^2 \ k_4^2 \ k_7 \ k_8 \ k_{11} - 2 \ k_2 \ k_3 \ k_4^2 \ k_7 \ k_8 \ k_{11} -
                                                       k_3^2 \ k_4^2 \ k_7 \ k_8 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_5 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{11} \ - \ 2 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 \ k_2 \ k_3 \ k_1 \ k_2 \ k_1 \ k_2 \ k_1 \ k_2 \ k_3 \ k_2 \ k_3 \ k_2 \ k_3 \ k_4 \ k_5 \ k_7 \ k_9 \ k_1 \ k_2 \ k_3 \ 
                                                       k_1 \; k_2 \; k_4 \; k_6 \; k_7 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_{10} \; k_{11} \; - \; k_2 \; k_4^2 \; k_7 \; k_8 \; k_{10} \; k_{11} \; - \; k_3 \; k_4^2 \; k_7 \; k_8 \; k_{10} \; k_{11} \; - \; k_1 \; k_2^2 \; k_1^2 \; k_1^2 \; k_2^2 \; k_1^2 
                                                       2\;k_1\;k_2\;k_4\;k_7\;k_9\;k_{10}\;k_{11}\;-\;2\;k_1\;k_3\;k_4\;k_7\;k_9\;k_{10}\;k_{11}\;-\;k_1\;k_4\;k_5\;k_7\;k_9\;k_{10}\;k_{11}\;-\;
                                                       k_1 k_4 k_6 k_7 k_9 k_{10} k_{11} - k_2^2 k_4^2 k_7 k_{11}^2 - 2 k_2 k_3 k_4^2 k_7 k_{11}^2 - k_3^2 k_4^2 k_7 k_{11}^2 -
                                                       k_2 k_4^2 k_7 k_8 k_{11}^2 - k_3 k_4^2 k_7 k_8 k_{11}^2 - 2 k_1 k_2 k_4 k_7 k_9 k_{11}^2 - 2 k_1 k_3 k_4 k_7 k_9 k_{11}^2 +
                                                           \left(k_{1}^{2} \; k_{3} \; k_{4} \; k_{5} \; k_{9} \; k_{10} \; + \; k_{1}^{2} \; k_{3} \; k_{4} \; k_{6} \; k_{9} \; k_{10} \; - \; k_{1}^{2} \; k_{4} \; k_{5} \; k_{6} \; k_{9} \; k_{10} \; - \; k_{1}^{2} \; k_{4} \; k_{6}^{2} \; k_{9} \; k_{10} \; - \; k_{1}^{2} \; k_{4} \; k_{5} \; k_{6} \; k_{10}^{2} \; - \; k_{10}^{2} \; k_{10} \; -
                                                                                                              k_1^2 \ k_4 \ k_6^2 \ k_{10}^2 \ - \ k_1^2 \ k_4 \ k_5 \ k_7 \ k_{10}^2 \ - \ k_1^2 \ k_4 \ k_6 \ k_7 \ k_{10}^2 \ - \ k_1 \ k_2 \ k_3 \ k_4^2 \ k_8 \ k_{11} \ - \ k_1 \ k_3^2 \ k_4^2 \ k_8 \ k_{11} \ + \ k_1 \ k_2
                                                                                                                                   k_4^2 \ k_6 \ k_8 \ k_{11} + k_1 \ k_3 \ k_4^2 \ k_6 \ k_8 \ k_{11} - k_1^2 \ k_3 \ k_4 \ k_5 \ k_{10} \ k_{11} - k_1^2 \ k_3 \ k_4 \ k_6 \ k_{10} \ k_{11} - k_1 \ k_2 \ k_4^2 \ k_6 \ k_{10}
                                                                                                                                k_{11}-k_1\ k_3\ k_4^2\ k_6\ k_{10}\ k_{11}-k_1\ k_2\ k_4^2\ k_7\ k_{10}\ k_{11}-k_1\ k_3\ k_4^2\ k_7\ k_{10}\ k_{11}-k_1^2\ k_4\ k_5\ k_7\ k_{10}\ k_{11}-k_1^2\ k_1^2\ 
                                                                                                              \left.k_{1}^{2}\;k_{4}\;k_{6}\;k_{7}\;k_{10}\;k_{11}-k_{1}\;k_{2}\;k_{3}\;k_{4}^{2}\;k_{11}^{2}-k_{1}\;k_{3}^{2}\;k_{4}^{2}\;k_{11}^{2}-k_{1}\;k_{2}\;k_{4}^{2}\;k_{7}\;k_{11}^{2}-k_{1}\;k_{3}\;k_{4}^{2}\;k_{7}\;k_{11}^{2}\right)\;x_{3}\right)\;+\\
2 k_2 k_3 k_4 k_6 k_7 k_8 k_9 - k_3^2 k_4 k_6 k_7 k_8 k_9 - k_1 k_2 k_5^2 k_7 k_9^2 - k_1 k_3 k_5^2 k_7 k_9^2 -
                                                       2\;k_1\;k_2\;k_5\;k_6\;k_7\;k_9^2\;-\;2\;k_1\;k_3\;k_5\;k_6\;k_7\;k_9^2\;-\;k_1\;k_2\;k_6^2\;k_7\;k_9^2\;-\;k_1\;k_3\;k_6^2\;k_7\;k_9^2\;-\;k_1\;k_2\;k_5^2\;k_7\;k_9\;k_{10}\;-\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2
                                                       k_1 \; k_3 \; k_5^2 \; k_7 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_2 \; k_5 \; k_6 \; k_7 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_3 \; k_5 \; k_6 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_8^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_8^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_8^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_2 \; k_8^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_1 \; k_1 \; k_2 \; k_8^2 \; k_7 \; k_9 \; k_{10} \; - \; k_1 \; k_1 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_2 \; k_2 \; k_3 \; k_3
                                                       k_1 \; k_3 \; k_6^2 \; k_7 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_5 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_3 \; k_4 \; k_5 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_8 \; k_9 \; k_{10} \; - \; 2 \; k_2 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; k_1 \; k_9 \; k_9 \; k_{10} \; - \; 2 \; 
                                                         2 k_3 k_4 k_6 k_7 k_8 k_9 k_{10} - k_1 k_2 k_5 k_7 k_9^2 k_{10} - k_1 k_3 k_5 k_7 k_9^2 k_{10} - k_1 k_5^2 k_7 k_9^2 k_{10} -
                                                       k_1 \; k_2 \; k_6 \; k_7 \; k_9^2 \; k_{10} \; - \; k_1 \; k_3 \; k_6 \; k_7 \; k_9^2 \; k_{10} \; - \; 2 \; k_1 \; k_5 \; k_6 \; k_7 \; k_9^2 \; k_{10} \; - \; k_1 \; k_6^2 \; k_7 \; k_9^2 \; k_{10} \; - \; k_1 \; k_5^2 \; k_7 \; k_9 \; k_{10}^2 \; - \; k_1 \; k_1^2 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2
                                                       2\;k_1\;k_5\;k_6\;k_7\;k_9\;k_{10}^2\;-\;k_1\;k_6^2\;k_7\;k_9\;k_{10}^2\;-\;k_4\;k_5\;k_7\;k_8\;k_9\;k_{10}^2\;-\;k_4\;k_6\;k_7\;k_8\;k_9\;k_{10}^2\;-\;k_1^2\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^
                                                       k_1 \ k_5 \ k_7 \ k_9^2 \ k_{10}^2 - k_1 \ k_6 \ k_7 \ k_9^2 \ k_{10}^2 - k_2^2 \ k_4 \ k_5 \ k_7 \ k_8 \ k_{11} - 2 \ k_2 \ k_3 \ k_4 \ k_5 \ k_7 \ k_8 \ k_{11} -
                                                       k_3^2 \; k_4 \; k_5 \; k_7 \; k_8 \; k_{11} \; - \; k_2^2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; 2 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_3^2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; - \; k_1^2 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_4 \; k_4 \; k_5 \; k_1 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_3 \; k_4 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_2 \; 
                                                       k_{3}^{2}\;k_{4}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;-\;k_{2}\;k_{4}\;k_{5}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;-\;k_{3}\;k_{4}\;k_{5}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;-\;k_{2}\;k_{4}\;k_{6}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;-\;k_{2}\;k_{4}\;k_{6}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;-\;k_{2}\;k_{4}\;k_{6}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;-\;k_{2}\;k_{4}\;k_{6}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;-\;k_{2}\;k_{4}\;k_{6}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;-\;k_{2}\;k_{4}\;k_{6}\;k_{7}\;k_{8}\;k_{9}\;k_{11}\;k_{11}\;k_{11}\;k_{12}\;k_{11}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{11}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{11}\;k_{12}\;k_{11}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{11}\;k_{12}\;k_{12}\;k_{11}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12}\;k_{12
                                                       k_3 k_4 k_6 k_7 k_8 k_9 k_{11} - 2 k_1 k_2 k_5 k_7 k_9^2 k_{11} - 2 k_1 k_3 k_5 k_7 k_9^2 k_{11} - 2 k_1 k_2 k_6 k_7 k_9^2 k_{11} -
                                                       k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; 2 \; k_2 \; k_4 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_3 \; k_5 \; k_7 \; k_9 \; k_{10} \; k_{11} \; - \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_1 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_3 \; k_
                                                       k_3 k_4 k_7 k_8 k_9 k_{10} k_{11} - k_4 k_5 k_7 k_8 k_9 k_{10} k_{11} - k_4 k_6 k_7 k_8 k_9 k_{10} k_{11} - k_1 k_2 k_7 k_9^2 k_{10} k_{11} -
                                                       k_1 \; k_3 \; k_7 \; k_9^2 \; k_{10} \; k_{11} \; - \; k_1 \; k_5 \; k_7 \; k_9^2 \; k_{10} \; k_{11} \; - \; k_1 \; k_6 \; k_7 \; k_9^2 \; k_{10} \; k_{11} \; - \; k_2^2 \; k_4 \; k_7 \; k_8 \; k_{11}^2 \; - \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_3 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \;
                                                         2\;k_2\;k_3\;k_4\;k_7\;k_8\;k_{11}^2\;-\;k_3^2\;k_4\;k_7\;k_8\;k_{11}^2\;-\;2\;k_2^2\;k_4\;k_7\;k_9\;k_{11}^2\;-\;4\;k_2\;k_3\;k_4\;k_7\;k_9\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;-\;4\;k_2^2\;k_3^2\;k_4^2\;k_7^2\;k_9^2\;k_{11}^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_9^2\;k_
                                                       2\;k_3^2\;k_4\;k_7\;k_9\;k_{11}^2\;-\;k_2\;k_4\;k_7\;k_8\;k_9\;k_{11}^2\;-\;k_3\;k_4\;k_7\;k_8\;k_9\;k_{11}^2\;-\;k_1\;k_2\;k_7\;k_9^2\;k_{11}^2\;-\;k_1\;k_3\;k_7\;k_9^2\;k_{11}^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;k_2^2\;k_1^2\;-\;k_1^2\;k_2^2\;k_1^2\;k_1^2\;k_2^2\;k_1^2\;k_1^2\;k_2^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k_1^2\;k
                                                         2 \, \left( \, k_{1} \, k_{2} \, k_{4} \, k_{5} \, k_{6} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{5} \, k_{6} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{2} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{3} \, k_{4} \, k_{6}^{2} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{2} \, k_{3} \, k_{3} \, k_{4} \, k_{5}^{2} \, k_{3} \, k_{4} \, k_{5}^{2} \, k_{6} \, k_{8} \, k_{10} \, + \, k_{1} \, k_{2} \, k_{3} \, k_{3}^{2} \, k_{3}^{
                                                                                                              k_1 \; k_2 \; k_4 \; k_5 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_5 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{10} \; + \; k_1 \; k
                                                                                                              k_1 \ k_2 \ k_4 \ k_5 \ k_6 \ k_9 \ k_{10} + k_1 \ k_3 \ k_4 \ k_5 \ k_6 \ k_9 \ k_{10} + k_1 \ k_2 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_3 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_2 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_3 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_1 \ k_2 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_1 \ k_2 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_1 \ k_2 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_1 \ k_2 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_1 \ k_2 \ k_4 \ k_6^2 \ k_9 \ k_{10} + k_1 \ k_1 \ k_1 \ k_2 \ k_1 \ k_1 \ k_2 \ k_1 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 \ k_1 \ k_2 \ k_1 \ k_2 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 \ k_1 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 \ k_1 \ k_2 \ k_2 \ k_2 \ k_1 \ k_2 \ k
                                                                                                              k_1 \; k_2 \; k_4 \; k_5 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_5 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_2 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_9 \; k_{10} \; + \; k_1 \; k_3 \; k_9 \; k_{10} \; + \; k_1 \;
                                                                                                              k_1 \ k_4 \ k_5 \ k_6 \ k_8 \ k_{10}^2 + k_1 \ k_4 \ k_6^2 \ k_8 \ k_{10}^2 + k_1 \ k_4 \ k_5 \ k_7 \ k_8 \ k_{10}^2 + k_1 \ k_4 \ k_6 \ k_7 \ k_8 \ k_{10}^2 +
                                                                                                              k_1 k_4 k_5 k_6 k_9 k_{10}^2 + k_1 k_4 k_6^2 k_9 k_{10}^2 + k_1 k_4 k_5 k_7 k_9 k_{10}^2 + k_1 k_4 k_6 k_7 k_9 k_{10}^2 +
                                                                                                              k_1 k_2 k_3 k_4 k_5 k_8 k_{11} + k_1 k_2 k_3 k_4 k_6 k_8 k_1
                                                                                                              k_1 \; k_2 \; k_4 \; k_5 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_5 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_2 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_8 \; k_{11} \; + \; k_1 \; k_3 \; k_8 \; k_{11} \; + \; k_1 \; k_1 \; k_1 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_1 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_2 \; k_2 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 \; k_2 \; k_1 \; k_1 \; k_2 \; k_1 \; k_1 \; k_1 \; k_1 \; k_2 \; k_1 
                                                                                                              k_1 k_2 k_3 k_4 k_5 k_9 k_{11} + k_1 k_3^2 k_4 k_5 k_9 k_{11} + k_1 k_2 k_3 k_4 k_6 k_9 k_{11} + k_1 k_3^2 k_4 k_6 k_9 k_{11} +
                                                                                                              k_1 \; k_2 \; k_4 \; k_5 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_5 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_2 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; k_3 \; k_4 \; k_6 \; k_7 \; k_9 \; k_{11} \; + \; k_1 \; 
                                                                                                              k_1 \; k_3 \; k_4 \; k_5 \; k_8 \; k_{10} \; k_{11} + k_1 \; k_2 \; k_4 \; k_6 \; k_8 \; k_{10} \; k_{11} + 2 \; k_1 \; k_3 \; k_4 \; k_6 \; k_8 \; k_{10} \; k_{11} + k_1 \; k_2 \; k_4 \; k_7
                                                                                                                                   k_{8}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{3}\ k_{4}\ k_{7}\ k_{8}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{4}\ k_{5}\ k_{7}\ k_{8}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{4}\ k_{6}\ k_{7}\ k_{8}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{2}\ k_{5}\ k_{7}\ k_{8}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{4}\ k_{6}\ k_{7}\ k_{8}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{2}\ k_{5}\ k_{7}\ k_{8}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{2}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{2}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{2}\ k_{2}\ k_{10}\ k_{11}\ +\ k_{1}\ k_{2}\ k_{2}
                                                                                                                k_1 \; k_3 \; k_4 \; k_5 \; k_9 \; k_{10} \; k_{11} + k_1 \; k_2 \; k_4 \; k_6 \; k_9 \; k_{10} \; k_{11} + 2 \; k_1 \; k_3 \; k_4 \; k_6 \; k_9 \; k_{10} \; k_{11} + k_1 \; k_2 \; k_4
                                                                                                                                   k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_3 \ k_4 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_4 \ k_5 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_4 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_2 \ k_6 \ k_7 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_2 \ k_8 \ k_8 \ k_9 \ k_{10} \ k_{11} + k_1 \ k_1 \ k_1 \ k_1 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 \ k_2 \ k_1 \ k_2 
                                                                                                              k_1 \ k_2 \ k_3 \ k_4 \ k_8 \ k_{11}^2 + k_1 \ k_3^2 \ k_4 \ k_8 \ k_{11}^2 + k_1 \ k_2 \ k_4 \ k_7 \ k_8 \ k_{11}^2 + k_1 \ k_3 \ k_4 \ k_7 \ k_8 \ k_{11}^2 +
                                                                                                              k_1 k_2 k_3 k_4 k_9 k_{11}^2 + k_1 k_3^2 k_4 k_9 k_{11}^2 + k_1 k_2 k_4 k_7 k_9 k_{11}^2 + k_1 k_3 k_4 k_7 k_9 k_{11}^2  ) x_3
```

 $factor = k_1^2 k_3 k_4 k_5 k_9 k_{10} + k_1^2 k_3 k_4 k_6 k_9 k_{10} - k_1^2 k_4 k_5 k_6 k_9 k_{10} \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_3 \; \mathbf{k}_4^2 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3^2 \; \mathbf{k}_4^2 \; \mathbf{k}_8 \; \mathbf{k}_{11} + \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_4^2 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} + \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4^2 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_6 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} + \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} - \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} + \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} + \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} + \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} + \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_3 \; \mathbf{k}_4 \; \mathbf{k}_8 \; \mathbf{k}_{11} + \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_1 \; \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_1 \; \mathbf{k}_2 \; \mathbf{k}_1 \; \mathbf{k}_2$ $\mathbf{k}_{1}^{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1}^{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{6} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{4}^{2} \ \mathbf{k}_{6} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{3} \ \mathbf{k}_{4}^{2} \ \mathbf{k}_{6} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{4}^{2} \ \mathbf{k}_{6} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{4}^{2} \ \mathbf{k}_{6} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{4}^{2} \ \mathbf{k}_{6} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{4}^{2} \ \mathbf{k}_{6} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{11} - \mathbf{k}_{1} \ \mathbf{k}_{2} \ \mathbf{k}_{3} \ \mathbf{k}_{4} \ \mathbf{k}_{5} \ \mathbf{k}_{10} \ \mathbf{k}_{$ k_1 k_2 k_3 k_4^2 k_{11}^2 - k_1 k_3^2 k_4^2 k_{11}^2 - k_1 k_2 k_4^2 k_7 k_{11}^2 - k_1 k_3 k_4^2 k_7 k_{11}^2 ;

Factor[factor]

$$k_1 \ k_4 \ \left(k_1 \ k_3 \ k_5 \ k_9 \ k_{10} + k_1 \ k_3 \ k_6 \ k_9 \ k_{10} - k_1 \ k_5 \ k_6 \ k_9 \ k_{10} - k_1 \ k_6^2 \ k_9 \ k_{10} - k_1 \ k_6^2 \ k_9^2 \ k_{10} - k_1 \ k_6^2 \ k_1^2 - k_1 \ k_5 \ k_7 \ k_{10}^2 - k_1 \ k_6 \ k_7 \ k_{10}^2 - k_2 \ k_3 \ k_4 \ k_8 \ k_{11} - k_3^2 \ k_4 \ k_8 \ k_{11} + k_2 \ k_4 \ k_6 \ k_8 \ k_{11} + k_1 \ k_3 \ k_4 \ k_6 \ k_8 \ k_{11} - k_1 \ k_3 \ k_5 \ k_{10} \ k_{11} - k_1 \ k_3 \ k_6 \ k_{10} \ k_{11} - k_2 \ k_4 \ k_6 \ k_{10} \ k_{11} - k_2 \ k_4 \ k_7 \ k_{10} \ k_{11} - k_3 \ k_4 \ k_7 \ k_{10} \ k_{11} - k_1 \ k_5 \ k_7 \ k_{10} \ k_{11} - k_2 \ k_4 \ k_6 \ k_{10} \ k_{11} - k_2 \ k_4 \ k_7 \ k_{10} \ k_{11} - k_2 \ k_4 \ k_7 \ k_{10}^2 - k_1 \ k_6 \ k_7 \ k_{10}^2 - k_2 \ k_4 \ k_7 \ k_{10}^2 - k_1 \ k_6 \ k_7 \ k_{10}^2 - k_2 \ k_4 \ k_7 \ k_{11}^2 - k_3 \ k_4 \ k_7 \ k_{11}^2 \right)$$

$$\text{term} = k_1 \ k_3 \ k_5 \ k_9 \ k_{10} + k_1 \ k_3 \ k_6 \ k_9 \ k_{10} - k_1 \ k_6^2 \ k_9 \ k_{10} - k_1 \ k_6 \ k_7 \ k_{10}^2 - k_1 \ k_6 \ k_7 \ k_{10}^2 - k_2 \ k_3 \ k_4 \ k_8 \ k_{11} - k_3^2 \ k_4 \ k_8 \ k_{11} - k_3^2 \ k_4 \ k_8 \ k_{11} - k_3^2 \ k_4 \ k_8 \ k_{11} - k_2 \ k_4 \ k_6 \ k_{10} \ k_{11} - k_2 \ k_4 \ k_6 \ k_{10} \ k_{11} - k_2 \ k_4 \ k_6 \ k_{10} \ k_{11} - k_2 \ k_4 \ k_6 \ k_{10} \ k_{11} - k_3 \ k_4 \ k_7 \ k_{10} \ k_{11} - k_1 \ k_5 \ k_7 \ k_{10} \ k_{11} - k_1 \ k_5 \ k_7 \ k_{10}^2 + k_{11}^2 \right)$$

$$simpTerm = FullSimplify[term] - (k_2 + k_3) \ k_4 \ k_{11} \ (k_6 \ (-k_8 + k_{10}) + k_3 \ (-k_9 + k_{11}) + k_7 \ (k_{10} + k_{11}) \right)$$

$$simplerTerm = Distribute[simpTerm / (k_1 * k_4)] \ / \cdot \{ (k_2 + k_3) \ / \ k_1 \rightarrow M_1, \ (k_5 + k_6) \ / \ k_4 \rightarrow M_2 \}$$

 $k_{10} \ \left(k_6 \ \left(k_9 + k_{10} \right) \ + k_3 \ \left(- k_9 + k_{11} \right) \ + k_7 \ \left(k_{10} + k_{11} \right) \ \right) \ M_2$

This above term larger than 0 should be the necessary condition.

condition = simplerTerm > 0

$$\begin{array}{l} -\;k_{11}\;\left(k_{6}\;\left(-\,k_{8}\,+\,k_{10}\,\right)\,+\,k_{3}\;\left(k_{8}\,+\,k_{11}\right)\,+\,k_{7}\;\left(k_{10}\,+\,k_{11}\right)\,\right)\;M_{1}\;-\\ k_{10}\;\left(k_{6}\;\left(k_{9}\,+\,k_{10}\,\right)\,+\,k_{3}\;\left(-\,k_{9}\,+\,k_{11}\right)\,+\,k_{7}\;\left(k_{10}\,+\,k_{11}\right)\,\right)\;M_{2}\;>\;0 \end{array}$$

 $-\;k_{11}\;\left(\,k_{6}\;\left(\,-\,k_{8}\,+\,k_{10}\,\right)\;+\,k_{3}\;\left(\,k_{8}\,+\,k_{11}\,\right)\;+\,k_{7}\;\left(\,k_{10}\,+\,k_{11}\,\right)\;\right)\;M_{1}\;-$

By mannual simplying the term, we can have:

$$\begin{aligned} & \text{simpleCond} = (k_3 - k_6) * (M_2 * k_9 * k_{10} - M_1 * k_8 * k_{11}) > \\ & (k_{11} * M_1 + k_{10} * M_2) * ((k_6 * k_{10} + k_3 * k_{11}) + k_7 * (k_{10} + k_{11})) \\ & (k_3 - k_6) (-k_8 k_{11} M_1 + k_9 k_{10} M_2) > (k_6 k_{10} + k_3 k_{11} + k_7 (k_{10} + k_{11})) (k_{11} M_1 + k_{10} M_2) \end{aligned}$$

$$\begin{aligned} & \text{left} = (k_3 - k_6) * (M_2 * k_9 * k_{10} - M_1 * k_8 * k_{11}) / . & \{M_1 \rightarrow (k_2 + k_3) / k_1, M_2 \rightarrow (k_5 + k_6) / k_4\} \end{aligned}$$

$$& (k_3 - k_6) \left(\frac{(k_5 + k_6) k_9 k_{10}}{k_4} - \frac{(k_2 + k_3) k_8 k_{11}}{k_1} \right) \end{aligned}$$

$$& \text{right} = (k_{11} * M_1 + k_{10} * M_2) * ((k_6 * k_{10} + k_3 * k_{11}) + k_7 * (k_{10} + k_{11})) / . \end{aligned}$$

$$& \{M_1 \rightarrow (k_2 + k_3) / k_1, M_2 \rightarrow (k_5 + k_6) / k_4\}$$

$$& \left(\frac{(k_5 + k_6) k_{10}}{k_4} + \frac{(k_2 + k_3) k_{11}}{k_1} \right) (k_6 k_{10} + k_3 k_{11} + k_7 (k_{10} + k_{11})) \end{aligned}$$

To fullfile the assumption of thermodynamic conditions for the reversible reactions, we have the the constraint:

$$\frac{k_1 \, k_{10}}{k_2 \, k_{11}} = \frac{k_4 \, k_8}{k_5 \, k_9}$$

This will give us a even simple condition. Then we will example how will this condition result in the parameter space for multistationarity.

$$\begin{split} & \text{oriCond = simpleCond /. } \{ \text{M}_1 \rightarrow \text{ } (\text{k}_2 + \text{k}_3) \text{ } / \text{k}_1 \text{, } \text{M}_2 \rightarrow \text{ } (\text{k}_5 + \text{k}_6) \text{ } / \text{k}_4 \} \\ & (\text{k}_3 - \text{k}_6) \text{ } \left(\frac{(\text{k}_5 + \text{k}_6) \text{ } \text{k}_9 \text{ } \text{k}_{10}}{\text{k}_4} - \frac{(\text{k}_2 + \text{k}_3) \text{ } \text{k}_8 \text{ } \text{k}_{11}}{\text{k}_1} \right) > \\ & \left(\frac{(\text{k}_5 + \text{k}_6) \text{ } \text{k}_{10}}{\text{k}_4} + \frac{(\text{k}_2 + \text{k}_3) \text{ } \text{k}_{11}}{\text{k}_1} \right) \left(\text{k}_6 \text{ k}_{10} + \text{k}_3 \text{ k}_{11} + \text{k}_7 \text{ } (\text{k}_{10} + \text{k}_{11}) \text{ } \right) \end{split}$$

$$\begin{split} & \textbf{Simplify} \Big[\textbf{oriCond, Assumptions} \rightarrow \frac{k_1 \ k_{10}}{k_2 \ k_{11}} == \ \frac{k_4 \ k_8}{k_5 \ k_9} \Big] \\ & \frac{(k_3 - k_6) \ (k_1 \ k_6 \ k_9 \ k_{10} - k_3 \ k_4 \ k_8 \ k_{11})}{k_1 \ k_4} > \\ & \left(\frac{(k_5 + k_6) \ k_{10}}{k_4} + \frac{(k_2 + k_3) \ k_{11}}{k_1} \right) \ ((k_6 + k_7) \ k_{10} + (k_3 + k_7) \ k_{11}) \end{split}$$

Better to do it manually, then we have the condition with thermodynamic constraint:

thermoCond =

$$\begin{array}{l} \textbf{(k_3-k_6)} \ \ \textbf{(k_6 k_2-k_3 k_5)} \ \ > \ \left(\frac{k_2}{k_9} \times \frac{k_5^2 2 + k_6}{k_5} + \frac{k_5}{k_8} \times \frac{k_2^2 2 + k_3}{k_2}\right) \ \textbf{((k_6+k_7)} \ k_{10} + \textbf{(k_3+k_7)} \ k_{11}\textbf{)} \\ \textbf{(k_3-k_6)} \ \ (-k_3 \ k_5 + k_2 \ k_6) \ \ > \ \left(\frac{\left(k_2^2 + k_3\right) \ k_5}{k_2 \ k_8} + \frac{k_2 \ \left(k_5^2 + k_6\right)}{k_5 \ k_9}\right) \ \textbf{((k_6+k_7)} \ k_{10} + \textbf{(k_3+k_7)} \ k_{11}) \\ \end{array}$$

Fromt the above condition, we can get some general idea that in order to satisfy the thermodynamic condition we should have:

```
Necessarily:
k_3 > k_6 and k_2 > k_5
k_3 < k_6 and k_5 > k_2
With additional (sufficiently):
k_8, k_9 \gg k_{10}, k_{11} and k_7, k_{10}, k_{11} \approx 0
```

Sampling the parameters

Here we try to sampling the parameters by enforcing the thermodynamc constraint. The parameters are sampled in biologically meaningful ranges.

```
(NewKern) In[176]:=
```

```
ClearAll["Global`*"];
A = Table[0, {11}, {6}];
A[[1]][[1]] = -1;
A[[1]][[3]] = -1;
A[[1]][[5]] = 1;
A[[2]] = -A[[1]];
A[[3]][[3]] = 1; A[[3]][[2]] = 1; A[[3]][[5]] = -1;
A[[4]][[1]] = -1;
A[[4]][[4]] = -1;
A[[4]][[6]] = 1;
A[[5]] = -A[[4]];
A[[6]][[4]] = 1;
A[[6]][[2]] = 1;
A[[6]][[6]] = -1;
A[[7]][[2]] = -1;
 A[[7]][[1]] = 1;
 A[[8]][[3]] = -1; A[[8]][[4]] = 1; A[[9]] = -A[[8]];
A[[10]][[5]] = -1; A[[10]][[6]] = 1; A[[11]] = -A[[10]];
 stoiM = Transpose[A];
  (* Now we construct the rate vector *)
 ks = \{k_1 \times x_3 \times x_1, k_2 \times x_5, k_3 \times x_5, k_4 \times x_4 \times x_1, k_5 \times x_5, k_5 \times x_5 \times x_5, k_5 \times x_5 \times x_5, k_5 \times x_5 \times x_
                 k_5 \times x_6, k_6 \times x_6, k_7 \times x_2, k_8 \times x_3, k_9 \times x_4, k_{10} \times x_5, k_{11} \times x_6};
 ssEqns = stoiM.ks;
mC = RowReduce[NullSpace[A]];
 subsEqns = {ssEqns[[2]], ssEqns[[4]],
                 ssEqns[[5]], ssEqns[[6]], x_1 + x_2 + x_5 + x_6 - T_1, x_3 + x_4 + x_5 + x_6 - T_2;
 jacobian = D[subsEqns, \{\{x_1, x_2, x_3, x_4, x_5, x_6\}\}];
 detJ = Collect[Distribute[Det[jacobian]], {x1, x2, x3, x4, x5, x6}];
```

```
solution =
   Solve[{subsEqns[[1]], subsEqns[[2]], subsEqns[[3]], subsEqns[[4]]} == 0,
    \{x_2, x_4, x_5, x_6\}\};
detSubs = Replace[detJ, solution[[1]], {0, Infinity}];
(* Equivilant to detSubs=detJ/.solution[[1]]; *)
polSubs = Numerator[Together[detSubs]];
finalSubs = Collect[Distribute[polSubs], x_, FactorTerms];
(*The above code is the same as first section*)
reactionRates = N[Array[10^(-3) * (10^6)^(\frac{\# - 1}{1023}) &, 1024]];
(* association rates are set as 10^{-3} \sim 10^3 \mu M^{-1} s^{-1},
disassociation and catalytic rates are set as 10^{-3} \sim 10^{3} \, \mathrm{s}^{-1} *)
switchingRates = N[Array[10^{(-3)} * (10^{9})^{(\frac{\#-1}{1535})} &, 1536]];
(* The switching rate between
   different conformations are set as 10^{-3} \sim 10^6 \, s^{-1} *)
concentrations = N[Array[10^{(-3)} * (10^4)^{(\frac{\pi-1}{9})} &, 10]];
(* The concentration values are set as 10^{-3}
 10\mu M (1 molecule in a cell is approximately 2nM) *)
bistableKs = {};
bistableParSets = {};
SeedRandom[];
Timing
 Do[{
      k1 = reactionRates[[RandomInteger[1023]]];
     k2 = reactionRates[[RandomInteger[1023]]];
     k3 = reactionRates[[RandomInteger[1023]]];
     k4 = reactionRates[[RandomInteger[1023]]];
     k5 = reactionRates[[RandomInteger[1023]]];
     k6 = reactionRates[[RandomInteger[1023]]];
     k7 = reactionRates[[RandomInteger[1023]]];
      (*k8=switchingRates[[RandomInteger[1023]]];*)
     k9 = switchingRates[[RandomInteger[1535]]];
      k10 = switchingRates[[RandomInteger[1535]]];
      k11 = switchingRates[[RandomInteger[1535]]];
           k1 \times k10 \times k5 \times k9
              k11 \times k4 \times k2
      If [10^{(-3)} \le k8 \le 10^{3}, [
        left = (k3 - k6) \left(\frac{(k5 + k6) k9 k10}{k4} - \frac{(k2 + k3) k8 k11}{k1}\right);

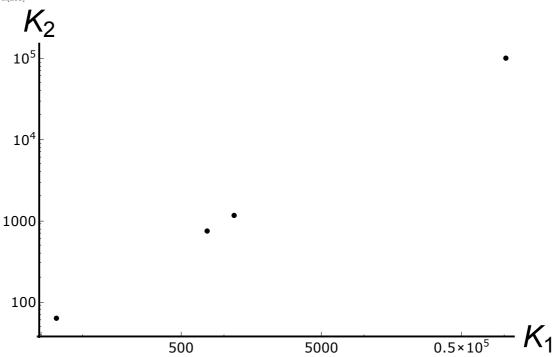
right = \left(\frac{(k5 + k6) k10}{k4} + \frac{(k2 + k3) k11}{k1}\right) (k6 k10 + k3 k11 + k7 (k10 + k11));
        If[left > right, {
           AppendTo[bistableKs,
             {k1, k2, k3, k4, k5, k6, k7, k8, k9, k10, k11, left, right}];
           counter = 1; hitQ = 0;
           randCons = RandomSample[Range[10]] - 1;
           numIterations = Length[randCons];
           While[hitQ == 0 && counter ≤ numIterations, {
              x1 = concentrations[[randCons[[counter]]]];
              finalSol = NSolve[
                  finalSubs = 0 /. \{k_1 \rightarrow k1, k_2 \rightarrow k2, k_3 \rightarrow k3, k_4 \rightarrow k4, k_5 \rightarrow k5, k_6 \rightarrow k6,
                    k_7 \rightarrow k7, k_8 \rightarrow k8, k_9 \rightarrow k9, k_{10} \rightarrow k10, k_{11} \rightarrow k11, x_1 \rightarrow x1}, \{x_3\}];
              x3 = x_3 /. finalSol[[1]];
              realSol = solution /. \{k_1 \rightarrow k1, k_2 \rightarrow k2, k_3 \rightarrow k3, k_4 \rightarrow k4, k_5 \rightarrow k5, k_6 \rightarrow k6,
                   k_7 \rightarrow k7, k_8 \rightarrow k8, k_9 \rightarrow k9, k_{10} \rightarrow k10, k_{11} \rightarrow k11, x_1 \rightarrow x1, x_3 \rightarrow x3};
```

```
T1 = (x_1 + x_2 + x_5 + x_6) /. Flatten[Append[\{x_1 \rightarrow x_1, x_3 \rightarrow x_3\},
                       realSol[[1]]];
                  T2 = (x_3 + x_4 + x_5 + x_6) /. Flatten[Append[\{x_1 \rightarrow x_1, x_3 \rightarrow x_3\},
                       realSol[[1]]];
                  If [10^{(-3)} \le T1 \le 10 \&\& 10^{(-3)} \le T2 \le 10, 
                     AppendTo[bistableParSets,
                      {k1, k2, k3, k4, k5, k6, k7, k8, k9, k10, k11, T1, T2, left, right}];
                     hitQ = 1;
                    }];
                  counter++;
                 }1;
               }];
            }];
          }, {i, 100 000}];
(NewKern) Out[200]=
      {72.412297, Null}
(NewKern) In[201]:=
      Length[bistableParSets]
(NewKern) Out[201]=
      4
(NewKern) In[212]:=
      InputForm[bistableParSets]
(NewKern) Out[212]//InputForms
      {{805.6721616936468, 723.1652294935797, 325.9841474641885, 18.61207189258695, 0.0044173
        0.5945570708544392, 2.1336726036431073, 7.610851088488717, 22.111866678674108, 0.0208
1.584496179647185, 204.38291283628442, 2.523254300495873}, {90.36738814396949, 0.0102
143.02936809965504, 59.45570708544391, 7.329977462151208, 0.42419542706920305, 8.6171
         0.06097279124533667, 0.00029695043338743134, 0.00004462888860375256}, \{753.065660813388143184, 0.00004462888860375256\}
         495.4669185977836, 146.94520707580176, 0.024548746742478266, 0.44774051345422433, 0.3
         1.8946300882401192, 0.41208206515902046, 0.006801008065722134, 5.995672162002269, 0.1
         0.045240897699078575}}
(NewKern) In[202]:=
      transposedBiKs = Transpose[bistableParSets];
                 transposedBiKs[[1]] * transposedBiKs[[10]]
      biParK1 =
                 transposedBiKs[[2]] * transposedBiKs[[11]]
                 transposedBiKs[[4]] * transposedBiKs[[8]]
      biParK2 =
                 transposedBiKs[[5]] * transposedBiKs[[9]]
```

```
(NewKern) In[203]:=
```

```
\label{eq:biPlot} biPlot = ListLogLogPlot[Transpose[\{biParK1, biParK2\}], ImageSize \rightarrow Large, \\
    {\tt PlotRange} \rightarrow {\tt All, \ PlotLabel} \rightarrow {\tt None, \ LabelStyle} \rightarrow \{\tt 32, \ GrayLevel[0]\},
     \textbf{AxesLabel} \rightarrow \{\texttt{"K}_1\texttt{", "K}_2\texttt{"}\} \texttt{, Ticks} \rightarrow \textbf{Automatic, TicksStyle} \rightarrow \textbf{Directive}[\texttt{"Label", 14}] \texttt{,} 
    AxesStyle → Thick, PlotTheme → "Monochrome"]
```

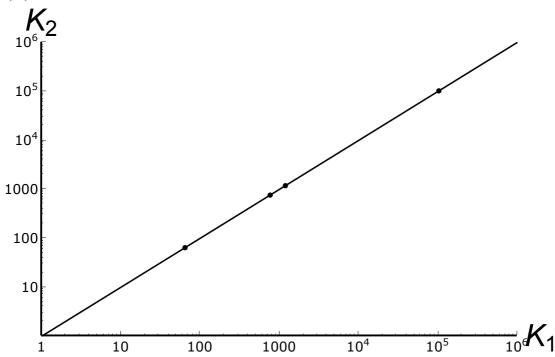
(NewKern) Out[203]=



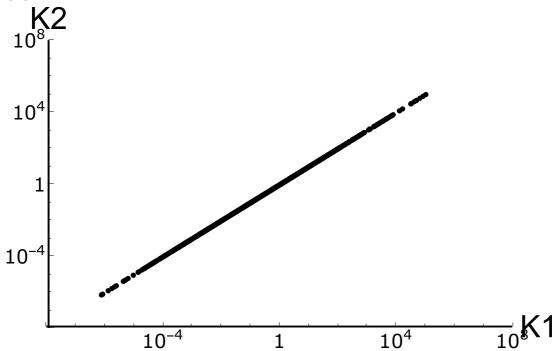
(NewKern) In[204]:=

Show[LogLogPlot[x, $\{x, 10^{\circ}(0), 10^{\circ}6\}$, PlotRange $\rightarrow \{\{10^{\circ}(0), 10^{\circ}6\}, \{10^{\circ}(0), 10^{\circ}6\}\},\$ ${\tt ImageSize} \rightarrow {\tt Large,\ PlotTheme} \rightarrow {\tt "Monochrome"},\ {\tt PlotLabel} \rightarrow {\tt None},$ $\texttt{LabelStyle} \rightarrow \{\texttt{32, GrayLevel}\, [\texttt{0}]\, \}\,,\, \texttt{AxesLabel} \rightarrow \{\texttt{"K}_1\texttt{", "K}_2\texttt{"}\}\,,\, \texttt{Ticks} \rightarrow \texttt{Automatic,}$ ${\tt TicksStyle \rightarrow Directive["Label", 14], AxesStyle \rightarrow Thick], biPlot]}$

(NewKern) Out[204]=



```
(NewKern) In[205]:=
                                Length[bistableKs]
(NewKern) Out[205]=
                                 1054
(NewKern) In[206]:=
                                 transposedKs = Transpose[bistableKs];
                                                                         transposedKs[[1]] * transposedKs[[10]]
                                parK1 =
                                                                          transposedKs[[2]] * transposedKs[[11]]
                                                                         transposedKs[[4]] * transposedKs[[8]]
                                                                          transposedKs[[5]] * transposedKs[[9]]
(NewKern) In[207]:=
                                \verb|plot = ListLogLogPlot[Transpose[{parK1, parK2}], AxesLabel \rightarrow {"K1", "K2"}, \\
                                             ImageSize \rightarrow Large, \ PlotRange \rightarrow \{\{10^{(-8)}, \ 10^{8}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{8}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{10^{(-8)}, \ 10^{(-8)}\}\}, \ \{1
                                             LabelStyle \rightarrow {32, GrayLevel[0]}, AxesStyle \rightarrow Thick, Ticks \rightarrow Automatic,
                                             TicksStyle → Directive["Label", 20], PlotTheme → "Monochrome"]
(NewKern) Out[207]=
```



These above results show that the parameter set within biological meaningful ranges can be reached by increasing the sampling size even when enforcing the thermodynamic constraint. Comparing to results from the other document (without enforcing thermodynamic constraint), the paramter space is largely reduced.

	with thermo	with thermo	without ther
Sampling size	only check bistability	bistability & concentrations	only check bista
10 ⁵	1054	4	11 985
10 ⁶	10 506	52	120 345