Boolean and Numbers Evaluation Semantics

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E-VAL
$$\frac{}{v \Downarrow v}$$

E-IFTRUE
$$\frac{t_1 \Downarrow true \qquad t_2 \Downarrow v}{\text{if } t_1 \text{ then } t_2 \text{ else } t_3 \Downarrow v}$$

E-IFFALSE
$$\frac{t_1 \Downarrow false \qquad t_3 \Downarrow v}{\text{if } t_1 \text{ then } t_2 \text{ else } t_3 \Downarrow v}$$

E-SUCC
$$\frac{t_1 \Downarrow n}{\text{succ } t_1 \Downarrow \text{succ } n}$$

E-PREDZERO
$$\frac{t_1 \Downarrow 0}{\text{pred } t_1 \Downarrow 0}$$

E-PREDSUCC
$$\frac{t_1 \Downarrow \text{succ } n}{\text{pred } t_1 \Downarrow n}$$

E-ISZEROZERO
$$\frac{t_1 \Downarrow 0}{\text{iszero } t_1 \Downarrow true}$$

E-ISZEROSUCC
$$\frac{t_1 \Downarrow \text{succ } n}{\text{iszero } t_1 \Downarrow false}$$