

GrumpyIR Dynamic Semantics

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The GrumpyIR dynamic (big-step operational) semantics is given as a six-place relation between a function environment δ , a variable environment ρ , heap stores μ and μ' , an expression e , and value v , written $\delta \mid \rho \vdash e \mid \mu \Downarrow v \mid \mu'$, pronounced “under δ and ρ , in memory state μ , e evaluates to v resulting in new state μ' ”. Formally, the dynamic semantics is taken to be the smallest relation satisfying the following transition rules:

Values and variables

$$\begin{array}{c} \text{E-VAL} \\ \hline \delta \mid \rho \vdash v \mid \mu \Downarrow v \mid \mu \end{array} \qquad \begin{array}{c} \text{E-VAR} \\ \hline \rho(x) = v \\ \hline \delta \mid \rho \vdash x \mid \mu \Downarrow v \mid \mu \end{array}$$

A value evaluates to itself and a variable x steps to a value v whenever ρ maps x to v .

Unary and binary operators

$$\begin{array}{c} \text{E-NEG} \\ \hline \delta \mid \rho \vdash e \mid \mu \Downarrow b \mid \mu' \quad b \in \{\text{true}, \text{false}\} \\ \hline \delta \mid \rho \vdash (\text{neg } e) \mid \mu \Downarrow \neg b \mid \mu' \end{array}$$
$$\begin{array}{c} \text{E-BINOP} \\ \hline \delta \mid \rho \vdash e_1 \mid \mu' \Downarrow n_1 \mid \mu'' \quad \delta \mid \rho \vdash e_2 \mid \mu \Downarrow n_2 \mid \mu' \quad n_1 \text{ } b \text{ } n_2 = n \quad b \in \{+, *, -, /\} \\ \hline \delta \mid \rho \vdash (b \text{ } e_1 \text{ } e_2) \mid \mu \Downarrow n \mid \mu'' \end{array}$$

Let-expressions and sequencing

$$\begin{array}{c} \text{E-LET} \\ \hline \delta \mid \rho \vdash e_1 \mid \mu \Downarrow v_1 \mid \mu' \quad \delta \mid [x \mapsto v_1]\rho \vdash e_2 \mid \mu' \Downarrow v_2 \mid \mu'' \\ \hline \delta \mid \rho \vdash (\text{let } x \text{ } e_1 \text{ } e_2) \mid \mu \Downarrow v_2 \mid \mu'' \end{array}$$
$$\begin{array}{c} \text{E-SEQ} \\ \hline \delta \mid \rho \vdash e_1 \mid \mu \Downarrow v_1 \mid \mu' \quad \delta \mid \rho \vdash e_2 \mid \mu' \Downarrow v_2 \mid \mu'' \\ \hline \delta \mid \rho \vdash (\text{seq } e_1 \text{ } e_2) \mid \mu \Downarrow v_2 \mid \mu'' \end{array}$$

Arrays

$$\begin{array}{c}
\text{E-ALLOC} \\
\frac{\delta \mid \rho \vdash e_{size} \mid \mu \Downarrow n \mid \mu' \quad \delta \mid \rho \vdash e_{init} \mid \mu' \Downarrow v_{init} \mid \mu'' \quad l \text{ is a freshly allocated store location} \quad 0 \leq n \quad \forall i, v_i = v_{init}}{\delta \mid \rho \vdash (\text{alloc } e_{size} e_{init}) \mid \mu \Downarrow l \mid [l \mapsto (v_1, v_2, \dots, v_n)]\mu''} \\
\\
\text{E-SET} \\
\frac{\delta \mid \rho \vdash e_{arr} \mid \mu \Downarrow l \mid \mu' \quad \delta \mid \rho \vdash e_{ix} \mid \mu' \Downarrow i \mid \mu'' \quad \delta \mid \rho \vdash e \mid \mu'' \Downarrow v \mid \mu''' \quad 0 \leq i \quad \forall j \neq i, v_j = \mu'''(l)_j}{\delta \mid \rho \vdash (\text{set } e_{arr} e_{ix} e) \mid \mu \Downarrow \text{tt} \mid [l \mapsto (v_1, \dots, v_{i-1}, v, v_{i+1}, \dots, v_n)]\mu'''} \\
\\
\text{E-GET} \\
\frac{\delta \mid \rho \vdash e_{arr} \mid \mu \Downarrow l \mid \mu' \quad \delta \mid \rho \vdash e_{ix} \mid \mu' \Downarrow i \mid \mu'' \quad 0 \leq i \quad \mu''(l)_i = v}{\delta \mid \rho \vdash (\text{get } e_{arr} e_{ix}) \mid \mu \Downarrow v \mid \mu''}
\end{array}$$

Conditionals and function calls

$$\begin{array}{c}
\text{E-COND-TRUE} \\
\frac{\delta \mid \rho \vdash e_{cond} \mid \mu \Downarrow \text{true} \mid \mu' \quad \delta \mid \rho \vdash e_1 \mid \mu' \Downarrow v_1 \mid \mu''}{\delta \mid \rho \vdash (\text{cond } e_{cond} e_1 e_2) \mid \mu \Downarrow v_1 \mid \mu''} \\
\\
\text{E-COND-FALSE} \\
\frac{\delta \mid \rho \vdash e_{cond} \mid \mu \Downarrow \text{false} \mid \mu' \quad \delta \mid \rho \vdash e_2 \mid \mu' \Downarrow v_2 \mid \mu''}{\delta \mid \rho \vdash (\text{cond } e_{cond} e_1 e_2) \mid \mu \Downarrow v_2 \mid \mu''} \\
\\
\text{E-CALL} \\
\frac{\mu_0 = \mu \quad \delta \mid \rho \vdash e_i \mid \mu_{i-1} \Downarrow v_i \mid \mu_i \quad \delta \mid \rho \vdash e_{fun} \mid \mu_n \Downarrow p \mid \mu' \quad \delta(p) = ((x_1, x_2, \dots, x_n), e_{body}) \quad \delta \mid [x_i \mapsto v_i]\rho_0 \vdash e_{body} \mid \mu' \Downarrow v \mid \mu''}{\delta \mid \rho \vdash (\text{call } e_{fun} e_1 e_2 \dots e_n) \mid \mu \Downarrow v \mid \mu''}
\end{array}$$

where ρ_0 is the empty variable environment.