



We are OUDL.

Organization for the Understanding of Dynamic Languages
<http://meetup.com/dynamic/>

What makes Objective C dynamic?

Introduction^{to} Haskell



What makes Objective C dynamic? Kamehameha Bakery donuts

Introduction to Haskell Otto Cake cheesecake



Cake Couture cupcakes



Fendu Bakery croissants & cookies



Saint Germain Bakery palmiers



Mahalo.



Y combinator

Examples in Clojure.

Also includes: blenders and kittens.

Caveat emptor: I make no effort to teach you Clojure.

Kyle Oba
@mudphone
Pas de Chocolat



Not this one.

This one.

```
(defn Y
  [g]
  ((fn [x] (x x)) (fn [x]
                    (g (fn [y] ((x x) y)))))))
```

Let's get started.

Here's a non-recursive
definition of factorial,
using the
Y combinator.


```
(defn Y
  [g]
  ((fn [x] (x x)) (fn [x]
                    (g (fn [y] ((x x) y)))))))
```

```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
        1
        (* n (f (dec n))))))
```

```
(defn factorial
  [n]
  ((Y almost-factorial) n))
```

Questions?

An example: 5!

$$(\text{factorial } 5) = 5 * 4 * 3 * 2 * 1 = 120$$

```
(defn factorial
  [n]
  (if (= n 0)
      1
      (* n (factorial (dec n)))))
```

here to here?



```
(defn factorial
  [n]
  (if (= n 0)
      1
      (* n (factorial (dec n)))))
```

```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
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(defn Y
  [g]
  ((fn [x] (x x)) (fn [x]
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```

```
(defn factorial
  [n]
  ((Y almost-factorial) n))
```

2 Things

1) recursion

2) functions

2 Things

1) recursion

2) functions

“The Y combinator **allows recursion...**
as a set of ***rewrite rules***,
without requiring native recursion
support in the language.”

-- Someone on Wikipedia

replace
“native recursion”
with
manual recursion


```
(defn factorial
  [n]
  (if (= n 0)
      1
      (* n (factorial (dec n)))))
```

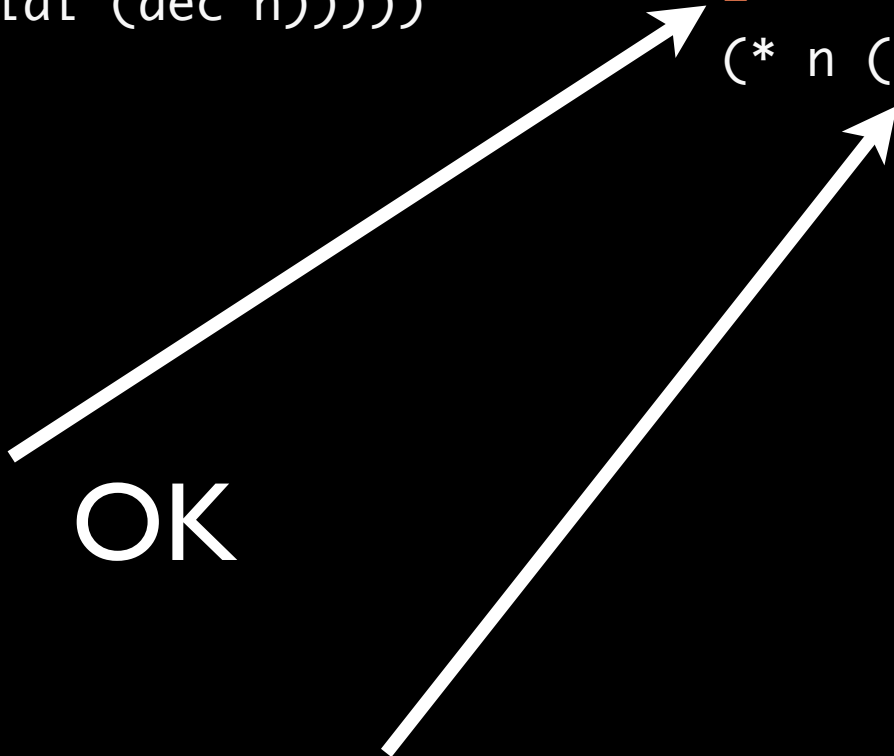
```
(defn fact
  [n]
  (if (= n 0)
      1
      (* n (ERROR (dec n)))))
```

```
(defn factorial
  [n]
  (if (= n 0)
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  [n]
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```

n = 0 OK

n = 1 BOOM!



```
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  [n]
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  (if (= n 0)
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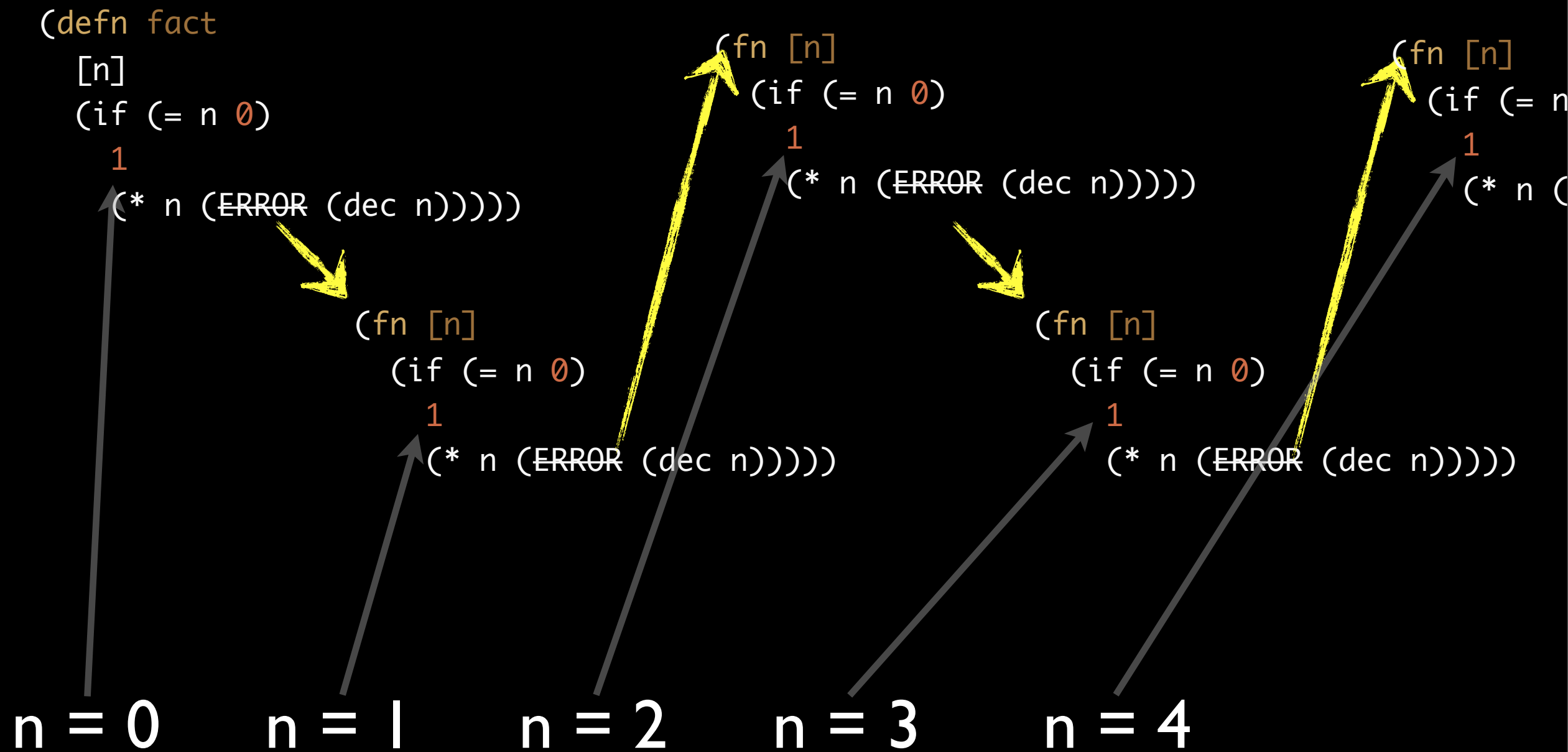


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(fn [n]
  (if (= n 0)
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    (* n (ERROR (dec n)))))
```

```
(fn [n]
  (if (= n 0)
    1
    (* n (
```



```
(fn [n]
  (if (= n 0)
    1
    (* n (
```



replace
“native recursion”
with
~~manual recursion~~
“rewrite rules”

2 Things

1) recursion

2) functions

2 Things

1) recursion

2) functions

Functions are machines.

Functions are relationships,
between inputs and outputs.

A function is a blender.



FIRST ORDER BLENDER

A normal blender that consumes single input
and creates output.



FIRST ORDER BLENDER

A normal blender that consumes single input
and creates output.



HIGHER ORDER BLENDER

A special blender that consumes a blender
and outputs another blender.

FIRST ORDER BLENDER

A normal blender that consumes single input
and creates output.

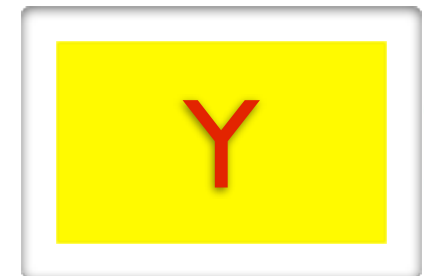


HIGHER ORDER BLENDER

A special blender that consumes a blender
and outputs another blender.

FIXPOINT (BLENDER) COMBINATOR

Consumes a blender and produces a new blender that
can consume any number of inputs.



ONE



ONE



```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
      1
      (* n (f (dec n))))))
```

ONE



```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
      1
      (* n (f (dec n))))))
```

ANY



ONE



ANY



```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
      1
      (* n (f (dec n))))))
```

factorial

if you squint



```
(defn factorial
  [n]
  (if (= n 0)
      1
      (* n (factorial (dec n)))))
```

```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
        1
        (* n (f (dec n))))))
```

```
(defn Y
  [g]
  ((fn [x] (x x)) (fn [x]
                    (g (fn [y] ((x x) y)))))))
```

```
(defn factorial
  [n]
  ((Y almost-factorial) n))
```



I'm so sorry.

No kittens were blended during the creation of this presentation.



No really, done now.

No kittens were blended during the creation of this presentation.

A Clojure Primer

PARENTHESIS

```
(+ 1 2 3)  
;; => 6
```

PREFIX NOTATION

```
(operator arg1 arg2 arg3)
```

FUNCTIONS

```
(defn multby2  
  [n]  
  (* n 2))  
;; (multby2 4) => 8
```

```
(fn [n] (* n 2))
```

```
(defn simple-factorial
  [n]
  (if (= n 0)
      1
      (* n (simple-factorial (dec n)))))
```

```
(defn simple-factorial
  [n]
  (if (= n 0)
      1
      (* n (simple-factorial (dec n)))))
```

```
(defn part
  [self n]
  (if (= n 0)
      1
      (* n (self self (dec n)))))
;; (part part 5) => 120
```

```
(defn simple-factorial
  [n]
  (if (= n 0)
      1
      (* n (simple-factorial (dec n)))))
```

```
(defn part
  [self n]
  (if (= n 0)
      1
      (* n (self self (dec n)))))
;; (part part 5) => 120
```



```
(defn part
  [self n]
  (if (= n 0)
    1
    (* n (self self (dec n)))))
;; (part part 5) => 120
```

```
(defn part2
  [self]
  (fn [n]
    (if (= n 0)
      1
      (* n ((self self) (dec n)))))
;; ((part2 part2) 5) => 120
```

```
(defn part
  [self n]
  (if (= n 0)
    1
    (* n (self self (dec n)))))
;; (part part 5) => 120
```

```
(defn part2
  [self]
  (fn [n]
    (if (= n 0)
      1
      (* n ((self self) (dec n)))))
;; ((part2 part2) 5) => 120
```

```
(defn part2
  [self]
  (fn [n]
    (if (= n 0)
      1
      (* n ((self self) (dec n))))))
;; ((part2 part2) 5) => 120
```

```
(defn part3
  [self]
  (let [f (self self)]
    (fn [n]
      (if (= n 0)
        1
        (* n (f (dec n)))))))
```

```
(defn part2
  [self]
  (fn [n]
    (if (= n 0)
      1
      (* n ((self self) (dec n))))))
;; ((part2 part2) 5) => 120
```

```
(defn part3
  [self]
  (let [f (self self)]
    (fn [n]
      (if (= n 0)
        1
        (* n (f (dec n)))))))
```

```
(defn part3
  [self]
  (let [f (self self)]
    (fn [n]
      (if (= n 0)
        1
        (* n (f (dec n)))))))
```

```
(defn part4
  [self]
  (let [f (fn [y] ((self self) y))]
    (fn [n]
      (if (= n 0)
        1
        (* n (f (dec n)))))))
```

```
(defn part3
  [self]
  (let [f (self self)]
    (fn [n]
      (if (= n 0)
        1
        (* n (f (dec n)))))))
```

```
(defn part4
  [self]
  (let [f (fn [y] ((self self) y))]
    (fn [n]
      (if (= n 0)
        1
        (* n (f (dec n)))))))
```

```
(defn part4
  [self]
  (let [f (fn [y] ((self self) y))]
    (fn [n]
      (if (= n 0)
        1
        (* n (f (dec n)))))))
```

```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
      1
      (* n (f (dec n))))))
```

```
(defn part4
  [self]
  (let [f (fn [y] ((self self) y))]
    (fn [n]
      (if (= n 0)
        1
        (* n (f (dec n)))))))
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```
(defn almost-factorial
  [f]
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    (if (= n 0)
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      (* n (f (dec n))))))
```



```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
        1
        (* n (f (dec n))))))
```

```
(defn part5
  [self]
  (let [f (fn [y] ((self self) y))]
    (almost-factorial f)))
```

```
(defn almost-factorial
  [f]
  (fn [n]
    (if (= n 0)
      1
      (* n (f (dec n)))))))
```

```
(defn part5
  [self]
  (let [f (fn [y] ((self self) y))]
    (almost-factorial f)))
```

```
(defn part5  
  [self]  
  (let [f (fn [y] ((self self) y))]  
    (almost-factorial f)))
```

```
(defn fact5  
  [n]  
  ((part5 part5) n))
```

```
(defn part5  
  [self]  
  (let [f (fn [y] ((self self) y))]  
    (almost-factorial f)))
```

```
(defn fact5  
  [n]  
  ((part5 part5) n))
```

```
(defn fact5
  [n]
  ((part5 part5) n))
```

```
(def fact6
  (let [part (fn [self]
                (let [f (fn [y] ((self self) y))]
                  (almost-factorial f)))]
    (part part)))
```

```
(defn fact5
  [n]
  ((part5 part5) n))
```

```
(def fact6
  (let [part (fn [self]
                (let [f (fn [y] ((self self) y))]
                  (almost-factorial f)))]
    (part part)))
```

```
(def fact6
  (let [part (fn [self]
                (let [f (fn [y] ((self self) y))]
                  (almost-factorial f)))]
    (part part)))
```

```
(def fact7
  (let [x (fn [x]
            (let [f (fn [y] ((x x) y))]
              (almost-factorial f)))]
    (x x)))
```

```
(def fact6
  (let [part (fn [self]
                (let [f (fn [y] ((self self) y))]
                  (almost-factorial f)))]
    (part part)))
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(def fact7
  (let [x (fn [x]
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```
(def fact7
  (let [x (fn [x]
            (let [f (fn [y] ((x x) y))]
              (almost-factorial f)))]
    (x x)))
```

```
(def fact8
  ((fn [x]
     (x x)) (fn [x]
              (let [f (fn [y] ((x x) y))]
                (almost-factorial f)))))
```

```
(def fact7
  (let [x (fn [x]
            (let [f (fn [y] ((x x) y))]
              (almost-factorial f)))]
    (x x)))
```

```
(def fact8
  ((fn [x]
     (x x)) (fn [x]
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                (almost-factorial f)))))
```

```
(defn fact8
  ((fn [x]
    (x x)) (fn [x]
              (let [f (fn [y] ((x x) y))]
                (almost-factorial f))))))
```

```
(defn nearly-Y
  [g]
  ((fn [x] (x x)) (fn [x]
                    (let [f (fn [y] ((x x) y))]
                      (g f))))))
```

```
(defn fact8
  ((fn [x]
    (x x)) (fn [x]
              (let [f (fn [y] ((x x) y))]
                (almost-factorial f))))))
```

```
(defn nearly-Y
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  [g]
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```
(defn factorial
  [n]
  ((Y almost-factorial) n))
```

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(defn Y
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I'm so sorry.

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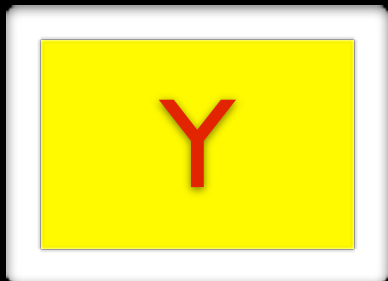
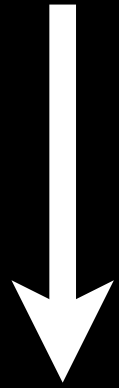

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```
(defn almost-factorial
  [f]
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    (if (= n 0)
        1
        (* n (f (dec n)))))))
```

```
(Y almost-factorial)
;; ((Y almost-factorial) 5) => 120
```

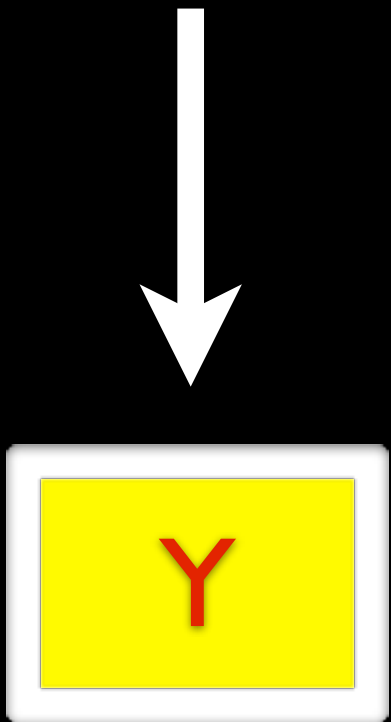
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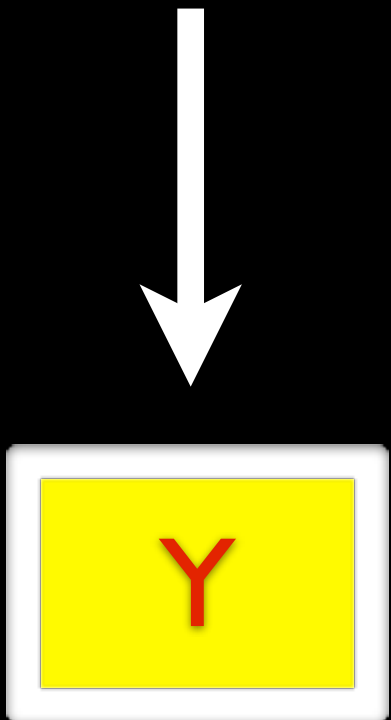
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FACTORIAL

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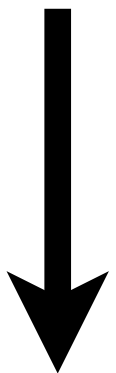
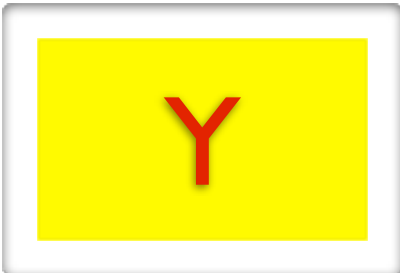
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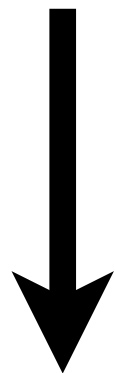
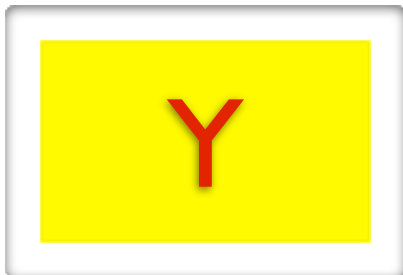
FACTORIAL

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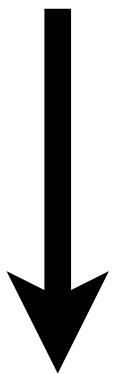
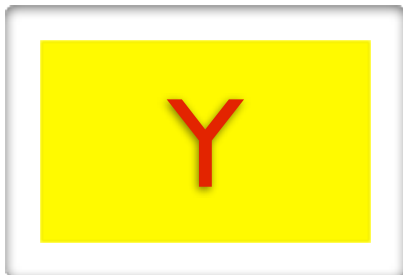
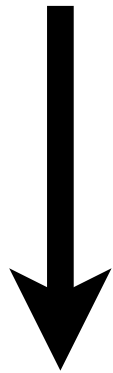
factorial

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factorial

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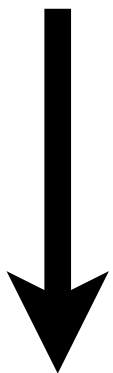
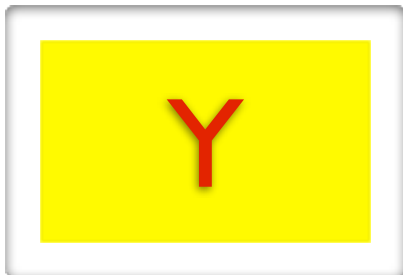
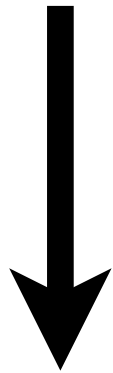
factorial



ONE




```
(defn almost-factorial
  [f]
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    (if (= n 0)
      1
      (* n (f (dec n)))))))
```



factorial



ONE



ANY

