

FERMAT SIEVE USING COMPLEX NUMBERS

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FERMAT SIEVE USING COMPLEX NUMBERS

If $N = 4k - 1$ then $\{R\}$ is EVEN and $\{i\}$ is ODD

If the real part of the number $\{R\}$ is EVEN:

And $\{R\}$ ends in: 2 And $\{i\}$ ends in:

$p=(R - i) \quad q=(R + i)$	
Resulting Reals (p,q) end in:	Example
1 (1,3)	(22-1)(22+1)
3 (9,5)	(22-3)(22+3)
5 (7,7)	(22-5)(22+5)
7 (5,9)	(22-7)(22+7)
9 (3,1)	(22-9)(22+9)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	△	X	X
X	X	X	X
X	X	X	△
X	X	X	X
X	△	X	X

Notes:

- No $\{R\}$ ending in 2 can generate $\{N\}$ ending in 1 or 7.
- The highest probability is $\{N\}$ ending in 3.

And $\{R\}$ ends in: 4 And $\{i\}$ ends in:

Resulting Reals (p,q) end in:	Example
1 (3,5)	(24-1)(24+1)
3 (1,7)	(24-3)(24+3)
5 (9,9)	(24-5)(24+5)
7 (7,1)	(24-7)(24+7)
9 (5,3)	(24-9)(24+9)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	X	X	X
X	X	△	X
△	X	X	X
X	X	△	X
X	X	X	X

- No $\{R\}$ ending in 4 can generate $\{N\}$ ending in 3 or 9.
- The highest probability is $\{N\}$ ending in 7.

And $\{R\}$ ends in: 6 And $\{i\}$ ends in:

Resulting Reals (p,q) end in:	Example
1 (5,7)	(26-1)(26+1)
3 (3,9)	(26-3)(26+3)
5 (1,1)	(26-5)(26+5)
7 (9,3)	(26-7)(26+7)
9 (7,5)	(26-9)(26+9)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	X	X	X
X	X	△	X
△	X	X	X
X	X	△	X
X	X	X	X

- No $\{R\}$ ending in 6 can generate $\{N\}$ ending in 3 or 9.
- The highest probability is $\{N\}$ ending in 7.

And $\{R\}$ ends in: 8 And $\{i\}$ ends in:

Resulting Reals (p,q) end in:	Example
1 (7,9)	(28-1)(28+1)
3 (5,1)	(28-3)(28+3)
5 (3,3)	(28-5)(28+5)
7 (1,5)	(28-7)(28+7)
9 (9,7)	(28-9)(28+9)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	△	X	X
X	X	X	X
X	X	X	△
X	X	X	X
X	△	X	X

- No $\{R\}$ ending in 8 can generate $\{N\}$ ending in 1 or 7.
- The highest probability is $\{N\}$ ending in 3.

And $\{R\}$ ends in: 0 And $\{i\}$ ends in:

Resulting Reals (p,q) end in:	Example
1 (9,1)	(20-1)(20+1)
3 (7,3)	(20-3)(20+3)
5 (5,5)	(20-5)(20+5)
7 (3,7)	(20-7)(20+7)
9 (1,9)	(20-9)(20+9)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	X	X	△
△	X	X	X
X	X	X	X
△	X	X	X
X	X	X	△

- No $\{R\}$ ending in 0 can generate $\{N\}$ ending in 3 or 7.
- The highest probability is $\{N\}$ ending in 1 or 9.

FERMAT SIEVE USING COMPLEX NUMBERS

If $N = 4k + 1$ then $\{R\}$ is ODD and $\{i\}$ is EVEN

If the real part of the number $\{R\}$ is ODD:

And $\{R\}$ ends in: 1 And $\{i\}$ ends in:

2
4
6
8
0

$p=(R - i) \quad q=(R + i)$

Resulting Reals (p,q) end in:

(9,3)
(7,5)
(5,7)
(3,9)
(1,1)

Example

(21-2)(21+2)
(21-4)(21+4)
(21-6)(21+6)
(21-8)(21+8)
(21-10)(21+10)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	X	△	X
X	X	X	X
X	X	X	X
X	X	△	X
△	X	X	X

Notes:

- No $\{R\}$ ending in 1 can generate $\{N\}$ ending in 3 or 9.
- The highest probability is $\{N\}$ ending in 7.

And $\{R\}$ ends in:

3

And $\{i\}$ ends in:

2
4
6
8
0

Resulting Reals (p,q) end in:

(1,5)
(9,7)
(7,9)
(5,1)
(3,3)

Example

(23-2)(23+2)
(23-4)(23+4)
(23-6)(23+6)
(23-8)(23+8)
(23-10)(23+10)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	X	X	X
X	△	X	X
X	△	X	X
X	X	X	X
X	X	X	△

- No $\{R\}$ ending in 3 can generate $\{N\}$ ending in 1 or 7.
- The highest probability is $\{N\}$ ending in 3.

And $\{R\}$ ends in:

5

And $\{i\}$ ends in:

2
4
6
8
0

Resulting Reals (p,q) end in:

(3,7)
(1,9)
(9,1)
(7,3)
(5,5)

Example

(25-2)(25+2)
(25-4)(25+4)
(25-6)(25+6)
(25-8)(25+8)
(25-10)(25+10)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
△	X	X	X
X	X	X	△
X	X	X	△
△	X	X	X
X	X	X	X

- No $\{R\}$ ending in 5 can generate $\{N\}$ ending in 3 or 7.
- The highest probability is $\{N\}$ ending in 1 or 9.

And $\{R\}$ ends in:

7

And $\{i\}$ ends in:

2
4
6
8
0

Resulting Reals (p,q) end in:

(5,9)
(3,1)
(1,3)
(9,5)
(7,7)

Example

(27-2)(27+2)
(27-4)(27+4)
(27-6)(27+6)
(27-8)(27+8)
(27-10)(27+10)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	X	X	X
X	△	X	X
X	△	X	X
X	X	X	X
X	X	X	△

- No $\{R\}$ ending in 7 can generate $\{N\}$ ending in 1 or 7.
- The highest probability is $\{N\}$ ending in 3.

And $\{R\}$ ends in:

9

And $\{i\}$ ends in:

2
4
6
8
0

Resulting Reals (p,q) end in:

(7,1)
(5,3)
(3,5)
(1,7)
(9,9)

Example

(29-2)(29+2)
(29-4)(29+4)
(29-6)(29+6)
(29-8)(29+8)
(29-10)(29+10)

Semi-Prime $\{N\}$ Ending In:

1	3	7	9
X	X	△	X
X	X	X	X
X	X	X	X
X	X	△	X
△	X	X	X

- No $\{R\}$ ending in 9 can generate $\{N\}$ ending in 3 or 9.
- The highest probability is $\{N\}$ ending in 7.