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<b>Time taken</b>	2 days 17 hours
<b>Marks</b>	5.00/5.00
<b>Grade</b>	<b>1.00</b> out of 1.00 ( <b>100%</b> )

## Information

## Representation of belief networks in Python

A belief (or Bayesian) network is represented by a dictionary. The keys are the names of variables. The values are dictionaries themselves. The second level dictionaries have two keys: 'Parents' whose value is a list of the names of the variables that are the parents of the current variable, and 'CPT' whose value is a dictionary again. The keys of the third level dictionaries are tuples of Booleans which correspond to possible assignments of values to the parents of the current node (in the order they are listed) and the values are real numbers representing the probability of the current node being true given the specified assignment to the parents.

### Notes

- Variable names are case sensitive.
- If a node does not have any parents, the value of 'Parents' must be an empty list and the only key of the third level dictionary is the empty tuple.
- For simplicity, we assume that all the variables are Boolean.

### Example

The following is the representation of the *alarm network* presented in the lecture notes.

```
network = {
    'Burglary': {
        'Parents': [],
        'CPT': {
            (): 0.001,
        }
    },

    'Earthquake': {
        'Parents': [],
        'CPT': {
            (): 0.002,
        }
    },

    'Alarm': {
        'Parents': ['Burglary', 'Earthquake'],
        'CPT': {
            (True, True): 0.95,
            (True, False): 0.94,
            (False, True): 0.29,
            (False, False): 0.001,
        }
    },

    'John': {
        'Parents': ['Alarm'],
        'CPT': {
            (True,): 0.9,
            (False,): 0.05,
        }
    },

    'Mary': {
        'Parents': ['Alarm'],
        'CPT': {
            (True,): 0.7,
            (False,): 0.01,
        }
    },
}
```

**Question 1**

Correct

Mark 1.00 out of 1.00

Suppose we want to predict the value of variable  $Y$  based on the values of variables  $x_1$ ,  $x_2$ , and  $x_3$ . Assuming that we want to use a Naive Bayes model for this purpose, create a belief net for the model called `network`. The probabilities must be learnt by using the dataset given below. Use Laplacian smoothing with a pseudocount of 2.

$x_1$	$x_2$	$x_3$	$Y$
T	T	F	F
T	F	F	F
T	T	F	F
T	F	F	T
F	F	F	T
F	T	F	T
F	F	F	T

**Notes**

- Node names are case sensitive.
- Since we are using Python syntax, you can use fraction expressions if you wish. For example you can use  $3/4$  or even  $(2+1)/(2+1+0+1)$  which will be evaluated at runtime.

**For example:**

Test	Result
<pre>from student_answer import network from numbers import Number  # Checking the overall type-correctness of the network # without checking anything question-specific  assert type(network) is dict for node_name, node_info in network.items():     assert type(node_name) is str     assert type(node_info) is dict     assert set(node_info.keys()) == {'Parents', 'CPT'}     assert type(node_info['Parents']) is list     assert all(type(s) is str for s in node_info['Parents'])     for assignment, prob in node_info['CPT'].items():         assert type(assignment) is tuple         assert isinstance(prob, Number)  print("OK")</pre>	OK

**Answer:** (penalty regime: 0, 10, ... %)

1	<code>network = {</code>
2	<code>    'x1': {</code>
3	<code>        'Parents': ['Y'],</code>
4	<code>        'CPT': {</code>
5	<code>            (True,): 3/8,</code>
6	<code>            (False,): 5/7</code>
7	<code>        }</code>
8	<code>    },</code>
9	
10	<code>    'x2': {</code>
11	<code>        'Parents': ['Y'],</code>
12	<code>        'CPT': {</code>
13	<code>            (True,): 3/8,</code>
14	<code>            (False,): 4/7</code>
15	<code>        }</code>
16	<code>    },</code>
17	
18	<code>    'x3': {</code>
19	<code>        'Parents': ['Y'],</code>
20	<code>        'CPT': {</code>

```
21         (True,): 2/8,
22         (False,): 2/7
23     }
24 },
25
26 'Y': {
27     'Parents': [],
28     'CPT': {
29         (): 6/11,
30     }
31 },
32 }
```

	Test	Expected	Got	
✓	<pre>from student_answer import network from numbers import Number  # Checking the overall type-correctness of the network # without checking anything question-specific  assert type(network) is dict for node_name, node_info in network.items():     assert type(node_name) is str     assert type(node_info) is dict     assert set(node_info.keys()) == {'Parents', 'CPT'}     assert type(node_info['Parents']) is list     assert all(type(s) is str for s in node_info['Parents'])     for assignment, prob in node_info['CPT'].items():         assert type(assignment) is tuple         assert isinstance(prob, Number)  print("OK")</pre>	OK	OK	✓

Passed all tests! ✓

Correct

Marks for this submission: 1.00/1.00.

Information

Representation of naïve Bayes models

Naïve Bayes models can be represented with belief networks. However, since they all have a very simple topology (a directed tree of depth one where the root is the class variable and the leaves are the input features), we can use a more compact representation that is only concerned with the values of CPTs.

We assume that all the variables in a naïve Bayes network are binary. For a network with  $n$  binary input features  $X[1]$  to  $X[n]$ , we represent the conditional probability tables (CPTs) that are required in the network, with the following two objects:

- prior: a real number representing  $p(Class=true)$ . The probability  $p(Class=false)$  can be obtained by  $1 - \text{prior}$ .
- likelihood: a tuple of length  $n$  where each element is a pair of real numbers such that  $\text{likelihood}[i][False]$  is  $p(X[i]=true|C=false)$  and  $\text{likelihood}[i][True]$  is  $p(X[i]=true|C=true)$ . That is, likelihood contains the  $2^n$  CPTs that are required at leaf nodes.

Note: in general, indexing sequences with booleans is not ideal, however, here we are using False (for 0) and True (for 1) so that the appearance of the code is closer to the corresponding mathematical notation.

**Question 2**

Correct

Mark 1.00 out of 1.00

Write a function `posterior(prior, likelihood, observation)` that returns the posterior probability of the class variable being true, given the observation; that is, it returns  $p(\text{Class}=\text{true}|\text{observation})$ . The argument `observation` is a tuple of  $n$  Booleans such that `observation[i]` is the observed value (True or False) for the input feature  $X[i]$ . The arguments `prior` and `likelihood` are as described above.

**Notes**

1. [Example 9.36](#) in the textbook is relevant.
2. The model used in the test cases is according to [this network](#). You can download and explore the model in the belief network applet.

**For example:**

Test	Result
<pre>from student_answer import posterior  prior = 0.05 likelihood = ((0.001, 0.3),(0.05,0.9),(0.7,0.99))  observation = (True, True, True)  class_posterior_true = posterior(prior, likelihood, observation) print("P(C=False observation) is approximately {:.5f}"       .format(1 - class_posterior_true)) print("P(C=True  observation) is approximately {:.5f}"       .format(class_posterior_true))</pre>	<p>P(C=False observation) is approximately 0.00248 P(C=True  observation) is approximately 0.99752</p>
<pre>from student_answer import posterior  prior = 0.05 likelihood = ((0.001, 0.3),(0.05,0.9),(0.7,0.99))  observation = (True, False, True)  class_posterior_true = posterior(prior, likelihood, observation) print("P(C=False observation) is approximately {:.5f}"       .format(1 - class_posterior_true)) print("P(C=True  observation) is approximately {:.5f}"       .format(class_posterior_true))</pre>	<p>P(C=False observation) is approximately 0.29845 P(C=True  observation) is approximately 0.70155</p>
<pre>from student_answer import posterior  prior = 0.05 likelihood = ((0.001, 0.3),(0.05,0.9),(0.7,0.99))  observation = (False, False, True)  class_posterior_true = posterior(prior, likelihood, observation) print("P(C=False observation) is approximately {:.5f}"       .format(1 - class_posterior_true)) print("P(C=True  observation) is approximately {:.5f}"       .format(class_posterior_true))</pre>	<p>P(C=False observation) is approximately 0.99454 P(C=True  observation) is approximately 0.00546</p>
<pre>from student_answer import posterior  prior = 0.05 likelihood = ((0.001, 0.3),(0.05,0.9),(0.7,0.99))  observation = (False, False, False)  class_posterior_true = posterior(prior, likelihood, observation) print("P(C=False observation) is approximately {:.5f}"       .format(1 - class_posterior_true)) print("P(C=True  observation) is approximately {:.5f}"       .format(class_posterior_true))</pre>	<p>P(C=False observation) is approximately 0.99987 P(C=True  observation) is approximately 0.00013</p>

**Answer:** (penalty regime: 0, 15, ... %)

```
1 def posterior(prior, likelihood, observation):
2     """returns the posterior probability of the class variable being true,
```

```

3 |     given the observation; that is, it returns p(Class=true|observation).
4 |     The argument observation is a tuple of n Booleans such that observation[i]
5 |     is the observed value (True or False) for the input feature X[i].
6 |     The arguments prior and likelihood are as described above.
7 |     """
8 |     correct = prior
9 |     wrong = 1 - prior
10 |     for i in range(len(likelihood)):
11 |         if observation[i]:
12 |             correct *= likelihood[i][True]
13 |             wrong *= likelihood[i][False]
14 |         else:
15 |             correct *= 1 - likelihood[i][True]
16 |             wrong *= 1 - likelihood[i][False]
17 |     return correct / (correct + wrong)

```

	Test	Expected	Got	
✓	<pre> from student_answer import posterior  prior = 0.05 likelihood = ((0.001, 0.3),(0.05,0.9), (0.7,0.99))  observation = (True, True, True)  class_posterior_true = posterior(prior, likelihood, observation) print("P(C=False observation) is approximately {:.5f}"       .format(1 - class_posterior_true)) print("P(C=True  observation) is approximately {:.5f}"       .format(class_posterior_true)) </pre>	<p>P(C=False observation) is approximately 0.00248</p> <p>P(C=True  observation) is approximately 0.99752</p>	<p>P(C=False observation) is approximately 0.00248</p> <p>P(C=True  observation) is approximately 0.99752</p>	✓
✓	<pre> from student_answer import posterior  prior = 0.05 likelihood = ((0.001, 0.3),(0.05,0.9), (0.7,0.99))  observation = (True, False, True)  class_posterior_true = posterior(prior, likelihood, observation) print("P(C=False observation) is approximately {:.5f}"       .format(1 - class_posterior_true)) print("P(C=True  observation) is approximately {:.5f}"       .format(class_posterior_true)) </pre>	<p>P(C=False observation) is approximately 0.29845</p> <p>P(C=True  observation) is approximately 0.70155</p>	<p>P(C=False observation) is approximately 0.29845</p> <p>P(C=True  observation) is approximately 0.70155</p>	✓
✓	<pre> from student_answer import posterior  prior = 0.05 likelihood = ((0.001, 0.3),(0.05,0.9), (0.7,0.99))  observation = (False, False, True)  class_posterior_true = posterior(prior, likelihood, observation) print("P(C=False observation) is approximately {:.5f}"       .format(1 - class_posterior_true)) print("P(C=True  observation) is approximately {:.5f}"       .format(class_posterior_true)) </pre>	<p>P(C=False observation) is approximately 0.99454</p> <p>P(C=True  observation) is approximately 0.00546</p>	<p>P(C=False observation) is approximately 0.99454</p> <p>P(C=True  observation) is approximately 0.00546</p>	✓

	Test	Expected	Got	
✓	<pre> from student_answer import posterior  prior = 0.05 likelihood = ((0.001, 0.3),(0.05,0.9), (0.7,0.99))  observation = (False, False, False)  class_posterior_true = posterior(prior, likelihood, observation) print("P(C=False observation) is approximately {:.5f}"       .format(1 - class_posterior_true)) print("P(C=True  observation) is approximately {:.5f}"       .format(class_posterior_true)) </pre>	<pre> P(C=False observation) is approximately 0.99987 P(C=True  observation) is approximately 0.00013 </pre>	<pre> P(C=False observation) is approximately 0.99987 P(C=True  observation) is approximately 0.00013 </pre>	✓

Passed all tests! ✓

Correct

Marks for this submission: 1.00/1.00.

#### Information

## Bayesian Spam Filter

In the next three questions, you are asked to develop the learning and classification components of a naive Bayes classifier (a spam filter).

The file [spam-labelled.csv](#) describes 200 emails, labelled as spam or non-spam by human users. Each email is specified by 12 binary attributes, indicating the presence of features such as "Lottery", "MILLION DOLLARS", significant amounts of text in CAPS, an invalid reply-to address, and so on.

The layout of the data is that each row is an example (one email), and columns correspond to attributes (features), which are binary. There are 12 input features (X1 to X12). The last (right-most) column is the class label where 1 means the example is spam (positive) and 0 means non-spam (negative).

Note that there are  $2^{12} = 4096$  possible input patterns; in other words, the data set only contains a small proportion of all possible input patterns. This is a common scenario in machine learning.

The file has Unix-like line breaks. Windows users need to open the file in a proper text editor that supports different line endings. You do not need a spreadsheet to open the file.

In Python, the csv module may come in handy. You can load the content of the file as a list of tuples using the following:

```

with open(file_name) as in_file:
    training_examples = [tuple(row) for row in csv.reader(in_file)]

```

In the next three questions, the above file is available on the server (in the current directory). Therefore a statement like the one above, would read the file. Your function will be tested on the same file format and header but the content (the examples) may vary. Make sure your solution works with the original copy of the file, not your own format.

**Question 3**

Correct

Mark 1.00 out of 1.00

Write a function `learn_prior(file_name, pseudo_count=0)` that takes the file name of the training set and an optional pseudo-count parameter and returns a real number that is the prior probability of spam being true. The parameter `pseudo_count` is a non-negative integer and it will be the same for all the attributes and all the values.

**Notes**

- Pseudo-counts are described in the lecture notes and section 7.2.3 of the textbook.
- Although you see high values of pseudo-count in some test cases, in practice small values are mostly used.

**For example:**

Test	Result
<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv") print("Prior probability of spam is {:.5f}.".format(prior))</pre>	Prior probability of spam is 0.25500.
<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv") print("Prior probability of not spam is {:.5f}.".format(1 - prior))</pre>	Prior probability of not spam is 0.74500.
<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 1) print(format(prior, ".5f"))</pre>	0.25743
<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 2) print(format(prior, ".5f"))</pre>	0.25980
<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 10) print(format(prior, ".5f"))</pre>	0.27727
<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 100) print(format(prior, ".5f"))</pre>	0.37750
<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 1000) print(format(prior, ".5f"))</pre>	0.47773

**Answer:** (penalty regime: 0, 10, ... %)

```
1 import csv
2 def learn_prior(file_name, pseudo_count=0):
3     """takes the file name of the training set and an optional pseudo-count
4     parameter and returns a real number that is the prior probability of spam
5     being true. The parameter pseudo_count is a non-negative integer and
6     it will be the same for all the attributes and all the values.
7     """
8     true_case = 0
9     with open(file_name) as in_file:
10         training_examples = [tuple(row) for row in csv.reader(in_file)]
11         for num_tuple in training_examples[1:]:
12             true_case += int(num_tuple[-1])
13     return (true_case + pseudo_count) / (len(training_examples) - 1 + 2 * pseudo_
```



	Test	Expected	Got	
✓	<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv") print("Prior probability of spam is {:.5f}".format(prior))</pre>	Prior probability of spam is 0.25500.	Prior probability of spam is 0.25500.	✓
✓	<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv") print("Prior probability of not spam is {:.5f}".format(1 - prior))</pre>	Prior probability of not spam is 0.74500.	Prior probability of not spam is 0.74500.	✓
✓	<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 1) print(format(prior, ".5f"))</pre>	0.25743	0.25743	✓
✓	<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 10) print(format(prior, ".5f"))</pre>	0.27727	0.27727	✓
✓	<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 100) print(format(prior, ".5f"))</pre>	0.37750	0.37750	✓
✓	<pre>from student_answer import learn_prior  prior = learn_prior("spam-labelled.csv", pseudo_count = 1000) print(format(prior, ".5f"))</pre>	0.47773	0.47773	✓

Passed all tests! ✓

Correct

Marks for this submission: 1.00/1.00.

**Question 4**

Correct

Mark 1.00 out of 1.00

Write a function `learn_likelihood(file_name, pseudo_count=0)` that takes the file name of a training set (for the spam detection problem) and an optional pseudo-count parameter and returns a sequence of pairs of likelihood probabilities. As described in the representation of likelihood, the length of the returned sequence (list or tuple) must be 12. Each element in the sequence is a pair (tuple) of real numbers such that `likelihood[i][False]` is  $P(X[i]=true|Spam=false)$  and `likelihood[i][True]` is  $P(X[i]=true|Spam=true)$ .

For example:

Test	Result
<pre>from student_answer import learn_likelihood  likelihood = learn_likelihood("spam-labelled.csv") print(len(likelihood)) print([len(item) for item in likelihood])</pre>	<pre>12 [2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2]</pre>
<pre>from student_answer import learn_likelihood  likelihood = learn_likelihood("spam-labelled.csv")  print("P(X1=True   Spam=False) = {:.5f}".format(likelihood[0][False])) print("P(X1=False  Spam=False) = {:.5f}".format(1 - likelihood[0][False])) print("P(X1=True   Spam=True ) = {:.5f}".format(likelihood[0][True])) print("P(X1=False  Spam=True ) = {:.5f}".format(1 - likelihood[0][True]))</pre>	<pre>P(X1=True   Spam=False) = 0.35570 P(X1=False  Spam=False) = 0.64430 P(X1=True   Spam=True ) = 0.66667 P(X1=False  Spam=True ) = 0.33333</pre>
<pre>from student_answer import learn_likelihood  likelihood = learn_likelihood("spam-labelled.csv", pseudo_count=1)  print("With Laplacian smoothing:") print("P(X1=True   Spam=False) = {:.5f}".format(likelihood[0][False])) print("P(X1=False  Spam=False) = {:.5f}".format(1 - likelihood[0][False])) print("P(X1=True   Spam=True ) = {:.5f}".format(likelihood[0][True])) print("P(X1=False  Spam=True ) = {:.5f}".format(1 - likelihood[0][True]))</pre>	<pre>With Laplacian smoothing: P(X1=True   Spam=False) = 0.35762 P(X1=False  Spam=False) = 0.64238 P(X1=True   Spam=True ) = 0.66038 P(X1=False  Spam=True ) = 0.33962</pre>

Answer: (penalty regime: 0, 15, ... %)

```
1 import csv
2 def learn_likelihood(file_name, pseudo_count=0):
3     """takes the file name of a training set (for the spam detection problem)
4     and an optional pseudo-count parameter and returns a sequence of pairs of
5     likelihood probabilities. As described in the representation of likelihood,
6     the length of the returned sequence (list or tuple) must be 12. Each element
7     in the sequence is a pair (tuple) of real numbers such that
8     likelihood[i][False] is P(X[i]=true|Spam=false) and likelihood[i][True]
9     is P(X[i]=true|Spam=true ).
10    """
11    with open(file_name) as in_file:
12        training_examples = [tuple(row) for row in csv.reader(in_file)]
13    likelihood = []
14
15    for i in range(len(training_examples[0]) - 1):
16        xi_true_given_class_false_count = 0 + pseudo_count
17        false_total = 0 + 2 * pseudo_count
18        xi_true_given_class_true_count = 0 + pseudo_count
19        true_total = 0 + 2 * pseudo_count
20        for num_tuple in training_examples[1: ]:
21            if int(num_tuple[-1]): #class true
22                true_total += 1
23                if int(num_tuple[i]): #xi true
24                    xi_true_given_class_true_count += 1
25            else: #class false
26                false_total += 1
27                if int(num_tuple[i]): #xi true
28                    xi_true_given_class_false_count += 1
29        likelihood += [(xi_true_given_class_false_count/false_total, xi_true_g:
30    return likelihood
```

	Test	Expected	Got	
✓	<pre> from student_answer import learn_likelihood  likelihood = learn_likelihood("spam-labelled.csv") print(len(likelihood)) print([len(item) for item in likelihood]) </pre>	12 [2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2]	12 [2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2]	✓
✓	<pre> from student_answer import learn_likelihood  likelihood = learn_likelihood("spam-labelled.csv")  print("P(X1=True   Spam=False) = {:.5f}".format(likelihood[0][False])) print("P(X1=False  Spam=False) = {:.5f}".format(1 - likelihood[0][False])) print("P(X1=True   Spam=True ) = {:.5f}".format(likelihood[0][True])) print("P(X1=False  Spam=True ) = {:.5f}".format(1 - likelihood[0][True])) </pre>	P(X1=True   Spam=False) = 0.35570 P(X1=False  Spam=False) = 0.64430 P(X1=True   Spam=True ) = 0.66667 P(X1=False  Spam=True ) = 0.33333	P(X1=True   Spam=False) = 0.35570 P(X1=False  Spam=False) = 0.64430 P(X1=True   Spam=True ) = 0.66667 P(X1=False  Spam=True ) = 0.33333	✓
✓	<pre> from student_answer import learn_likelihood  likelihood = learn_likelihood("spam-labelled.csv", pseudo_count=1)  print("With Laplacian smoothing:") print("P(X1=True   Spam=False) = {:.5f}".format(likelihood[0][False])) print("P(X1=False  Spam=False) = {:.5f}".format(1 - likelihood[0][False])) print("P(X1=True   Spam=True ) = {:.5f}".format(likelihood[0][True])) print("P(X1=False  Spam=True ) = {:.5f}".format(1 - likelihood[0][True])) </pre>	With Laplacian smoothing: P(X1=True   Spam=False) = 0.35762 P(X1=False  Spam=False) = 0.64238 P(X1=True   Spam=True ) = 0.66038 P(X1=False  Spam=True ) = 0.33962	With Laplacian smoothing: P(X1=True   Spam=False) = 0.35762 P(X1=False  Spam=False) = 0.64238 P(X1=True   Spam=True ) = 0.66038 P(X1=False  Spam=True ) = 0.33962	✓

Passed all tests! ✓

Correct

Marks for this submission: 1.00/1.00.

**Question 5**

Correct

Mark 1.00 out of 1.00

Write a function `nb_classify(prior, likelihood, input_vector)` that takes the learnt prior and likelihood probabilities and classifies an (unseen) input vector. The input vector will be a tuple of 12 integers (each 0 or 1) corresponding to attributes X1 to X12. The function should return a pair (tuple) where the first element is either "Spam" or "Not Spam" and the second element is the certainty. The certainty is the (posterior) probability of spam when the instance is classified as spam, or the probability of 'not-spam' otherwise. If spam and 'not spam' are equally likely (i.e.  $p=0.5$ ) then choose 'not spam'.

This is a very simple function to implement as it only wraps the posterior function developed earlier.

Supply the following functions you developed earlier: `learn_prior` and `learn_likelihood`. Also include import statements and any other function that you may be using (e.g. `posterior`).

**For example:**

Test	Result
<pre>from student_answer import learn_prior, learn_likelihood, nb_classify  prior = learn_prior("spam-labelled.csv") likelihood = learn_likelihood("spam-labelled.csv")  input_vectors = [     (1,1,0,0,1,1,0,0,0,0,0,0),     (0,0,1,1,0,0,1,1,1,0,0,1),     (1,1,1,1,1,0,1,0,0,0,1,1),     (1,1,1,1,1,0,1,0,0,1,0,1),     (0,1,0,0,0,0,1,0,1,0,0,0), ]  predictions = [nb_classify(prior, likelihood, vector)                 for vector in input_vectors]  for label, certainty in predictions:     print("Prediction: {}, Certainty: {:.5f}"           .format(label, certainty))</pre>	<pre>Prediction: Not Spam, Certainty: 0.99351 Prediction: Spam, Certainty: 0.57441 Prediction: Spam, Certainty: 0.59337 Prediction: Spam, Certainty: 0.83465 Prediction: Not Spam, Certainty: 0.99140</pre>
<pre>from student_answer import learn_prior, learn_likelihood, nb_classify  prior = learn_prior("spam-labelled.csv", pseudo_count=1) likelihood = learn_likelihood("spam-labelled.csv", pseudo_count=1)  input_vectors = [     (1,1,0,0,1,1,0,0,0,0,0,0),     (0,0,1,1,0,0,1,1,1,0,0,1),     (1,1,1,1,1,0,1,0,0,0,1,1),     (1,1,1,1,1,0,1,0,0,1,0,1),     (0,1,0,0,0,0,1,0,1,0,0,0), ]  predictions = [nb_classify(prior, likelihood, vector)                 for vector in input_vectors]  for label, certainty in predictions:     print("Prediction: {}, Certainty: {:.5f}"           .format(label, certainty))</pre>	<pre>Prediction: Not Spam, Certainty: 0.99213 Prediction: Spam, Certainty: 0.57759 Prediction: Spam, Certainty: 0.59073 Prediction: Spam, Certainty: 0.83059 Prediction: Not Spam, Certainty: 0.98989</pre>

**Answer:** (penalty regime: 0, 15, ... %)

```
1 import csv
2 def learn_prior(file_name, pseudo_count=0):
3     """takes the file name of the training set and an optional pseudo-count
4     parameter and returns a real number that is the prior probability of spam
5     being true. The parameter pseudo_count is a non-negative integer and
6     it will be the same for all the attributes and all the values.
7     """
8     true_case = 0
9     with open(file_name) as in_file:
10         training_examples = [tuple(row) for row in csv.reader(in_file)]
11         for num_tuple in training_examples[1:]:
12             true_case += int(num_tuple[-1])
```

```

13     return (true_case + pseudo_count) / (len(training_examples) - 1 + 2 * pseudo_count)
14
15 def learn_likelihood(file_name, pseudo_count=0):
16     """takes the file name of a training set (for the spam detection problem)
17     and an optional pseudo-count parameter and returns a sequence of pairs of
18     likelihood probabilities. As described in the representation of likelihood,
19     the length of the returned sequence (list or tuple) must be 12. Each element
20     in the sequence is a pair (tuple) of real numbers such that
21     likelihood[i][False] is P(X[i]=true|Spam=false) and likelihood[i][True]
22     is P(X[i]=true|Spam=true).
23     """
24     with open(file_name) as in_file:
25         training_examples = [tuple(row) for row in csv.reader(in_file)]
26         likelihood = []
27
28     for i in range(len(training_examples[0]) - 1):
29         xi_true_given_class_false_count = 0 + pseudo_count
30         false_total = 0 + 2 * pseudo_count
31         xi_true_given_class_true_count = 0 + pseudo_count
32         true_total = 0 + 2 * pseudo_count
33         for num_tuple in training_examples[1:]:
34             if int(num_tuple[-1]): #class true
35                 true_total += 1
36                 if int(num_tuple[i]): #xi true
37                     xi_true_given_class_true_count += 1
38             else: #class false
39                 false_total += 1
40                 if int(num_tuple[i]): #xi true
41                     xi_true_given_class_false_count += 1
42         likelihood += [(xi_true_given_class_false_count/false_total, xi_true_given_class_true_count/true_total)]
43     return likelihood
44
45 def posterior(prior, likelihood, observation):
46     """returns the posterior probability of the class variable being true,
47     given the observation; that is, it returns p(Class=true|observation).
48     The argument observation is a tuple of n Booleans such that observation[i]
49     is the observed value (True or False) for the input feature X[i].
50     The arguments prior and likelihood are as described above.
51     """
52

```

	Test	Expected	Got	
✓	<pre> from student_answer import learn_prior, learn_likelihood, nb_classify  prior = learn_prior("spam-labelled.csv") likelihood = learn_likelihood("spam-labelled.csv")  input_vectors = [     (1,1,0,0,1,1,0,0,0,0,0,0),     (0,0,1,1,0,0,1,1,1,0,0,1),     (1,1,1,1,1,0,1,0,0,0,1,1),     (1,1,1,1,1,0,1,0,0,1,0,1),     (0,1,0,0,0,0,1,0,1,0,0,0), ]  predictions = [nb_classify(prior, likelihood, vector)                for vector in input_vectors]  for label, certainty in predictions:     print("Prediction: {}, Certainty: {:.5f}"           .format(label, certainty)) </pre>	<pre> Prediction: Not Spam, Certainty: 0.99351 Prediction: Spam, Certainty: 0.57441 Prediction: Spam, Certainty: 0.59337 Prediction: Spam, Certainty: 0.83465 Prediction: Not Spam, Certainty: 0.99140 </pre>	<pre> Prediction: Not Spam, Certainty: 0.99351 Prediction: Spam, Certainty: 0.57441 Prediction: Spam, Certainty: 0.59337 Prediction: Spam, Certainty: 0.83465 Prediction: Not Spam, Certainty: 0.99140 </pre>	✓

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Passed all tests! ✓

Correct

Marks for this submission: 1.00/1.00.