

# NEWTON LAWS OF MOTION

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- Newtonian Mechanics/ Classical Mechanics
- Newton's Laws
- Inertial Reference frames
- Particular Forces (Gravitational Force, Weight, Normal Force, Tension)
- Application of Newton's Laws
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# CLASSICAL MECHANICS(CM)

- The field of study in which we study the causes of motion is called “DYNAMICS”
- The approach to dynamics we consider in this chapter and ahead known as “CLASSICAL MECHANICS”.
- Often referred to as “Newtonian Mechanics”

# CAUSES OF MOTION(SOME EXAMPLES)

<i>Table : Some accelerated Motions and their Causes</i>		
<i>Object</i>	<i>Change in Motion</i>	<i>Major Cause (Environment)</i>
Apple	Falls from tree	Earth's Gravity
Billiard Ball	Bounces off another	Other ball, table, gravity(earth)
Skier	Slides down hill	Earth's gravity, friction(snow), air resistance
Beam of Electrons	Focusing and deflection	EM fields(Magnets & Voltage Differences)
Comet Halley	Round trip through solar system	Sun's Gravity

# NEWTONIAN MECHANICS

- Classical Mechanics ~ Newtonian Mechanics,
- The study of the relationship between a Force and the Acceleration it causes is called Newtonian Mechanics.
- We shall focus on its three primary laws of motion
  1. First Law of Motion: a qualitative analysis
  2. Second Law of Motion: a quantitative analysis
  3. Third Law of Motion

# LIMITATION OF NEWTONIAN MECHANICS.

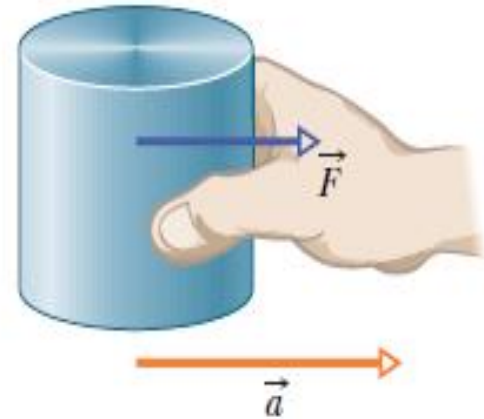
- It does not apply to all situations.
- If the speeds are quite high or very large say the body moves with the speed of light then **we will replace Newtonian mechanics by Einstein's special theory of relativity**, which holds for any speed, including those near the speed of light.
- If the interacting bodies are on the scale of atomic structure(might be electrons in an atom) we must replace **Newtonian mechanics by Quantum mechanics.**

# INTRODUCTION TO FORCE

- Physics is the study of motion
- Physics is also the study of those causes that produces motion in an object.
- That cause is known as FORCE
- A Force is defined generally as a “pull or a push” on the object.
- The force is said to **act** on the object to change its velocity.
- Examples(car slams on a pole, a Force from the pole causes a car to stop)

# INTRODUCTION TO FORCE

- Force is measured by the acceleration it produces.
- However, acceleration is a vector quantity with both magnitude and direction.
- To find force we should have the mass of the object and acceleration produced.

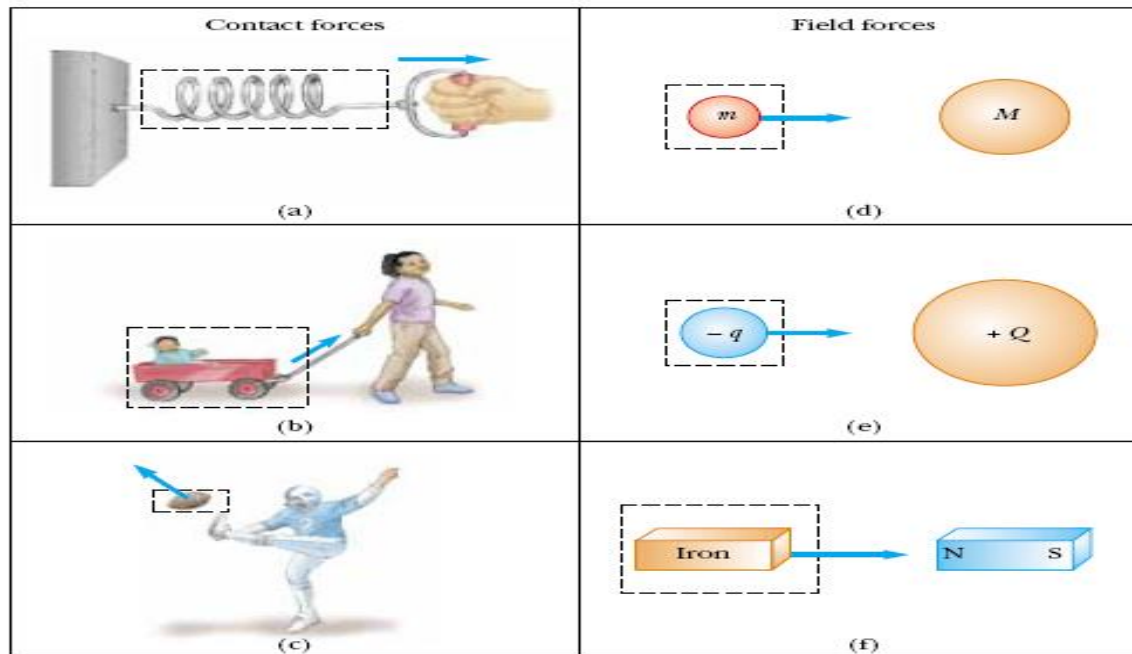


A force  $\vec{F}$  on the standard kilogram gives that body an acceleration  $\vec{a}$ .

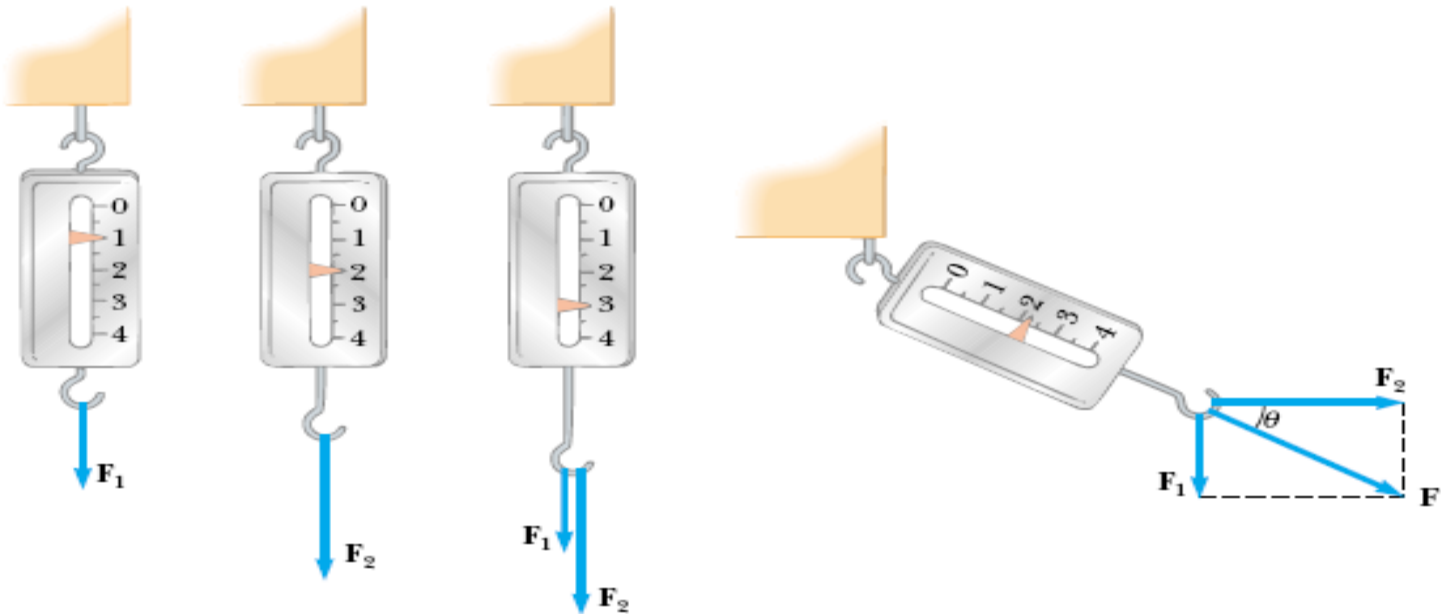


# THE CONCEPT OF FORCE

- The net force acting on an object is defined as the vector sum of all forces acting on the object. (We sometimes refer to the net force as the *total force*, *the resultant force*, or *the unbalanced force*.)
- If the net force exerted on an object is zero, the acceleration of the object is zero and its velocity remains constant.
- When the velocity of an object is constant (including when the object is at rest), the object is said to be in equilibrium.



## Measuring the Strength of a Force



**Because forces are vector quantities, you must use the rules of vector addition to obtain the net force acting on an object.**

# REFERENCE FRAMES

- A “**frame of reference**” is just a set of coordinates: something you use to measure the things that matter in Newtonian problems, that is to say, positions and velocities, so we also need a clock.
- An **inertial frame** is defined as one in which Newton’s law of inertia holds—that is, anybody which isn’t being acted on by an outside force stays at rest if it is initially at rest, horizontal or continues to move at a constant velocity if that’s what it was doing, to begin with.
- In other words, we can say that Newton’s First law is not true in all reference frames.

# Newton's First Law and Inertial Frames

Any reference frame that moves with constant velocity relative to an inertial frame is itself an inertial frame.

## Newton 1<sup>st</sup> Law of Motion

“In the absence of external forces, when viewed from an inertial reference frame, an object at rest remains at rest and an object in motion continues in motion with a constant velocity (that is, with a constant speed in a straight line)”.

## Mass

Mass is that property of an object that specifies how much resistance an object exhibits to changes in its velocity.

Mass is an inherent property of an object and is independent of the object's surroundings and of the method used to measure it. Also, mass is a scalar quantity and thus obeys the rules of ordinary arithmetic.

**Note: Mass and weight are two different quantities**

## Newton's Second Law

“When viewed from an inertial reference frame, the acceleration of an object is directly proportional to the net force acting on it and inversely proportional to its mass” .

$$\sum \mathbf{F} = m\mathbf{a}$$

$$\sum F_x = ma_x \quad \sum F_y = ma_y \quad \sum F_z = ma_z$$

### Unit of Force

The SI unit of force is the **newton**, which is defined as the force that, when acting on an object of mass 1 kg, produces an acceleration of  $1 \text{ m/s}^2$ . From this definition and Newton's second law, we see that the newton can be expressed in terms of the following fundamental units of mass, length, and time:

$$1 \text{ N} \equiv 1 \text{ kg} \cdot \text{m/s}^2$$

## **Question:**

When a bus stops suddenly, the passengers tend to move forward relative to their seats. Why? Give reason(s).

The passengers in a bus tend to fall backward when it starts suddenly due to inertia as the passengers tend to remain in the state of rest while the bus starts to move. When the bus stops suddenly, people fall forward because their inertia as they are in state of motion even when the bus has come to rest.

# Example Problem

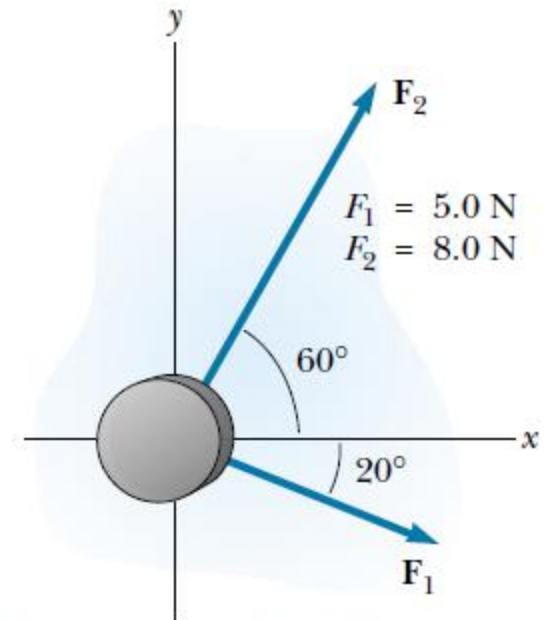
A hockey puck having a mass of 0.30 kg slides on the horizontal, frictionless surface of an ice rink. Two forces act on the puck, as shown in Figure . The force  $\mathbf{F}_1$  has a magnitude of 5.0 N, and the force  $\mathbf{F}_2$  has a magnitude of 8.0 N. Determine both the magnitude and the direction of the puck's acceleration.

**Solution** The resultant force in the  $x$  direction is

$$\begin{aligned}\sum F_x &= F_{1x} + F_{2x} = F_1 \cos(-20^\circ) + F_2 \cos 60^\circ \\ &= (5.0 \text{ N})(0.940) + (8.0 \text{ N})(0.500) = 8.7 \text{ N}\end{aligned}$$

The resultant force in the  $y$  direction is

$$\begin{aligned}\sum F_y &= F_{1y} + F_{2y} = F_1 \sin(-20^\circ) + F_2 \sin 60^\circ \\ &= (5.0 \text{ N})(-0.342) + (8.0 \text{ N})(0.866) = 5.2 \text{ N}\end{aligned}$$



A hockey puck moving on a frictionless surface accelerates in the direction of the resultant force  $\mathbf{F}_1 + \mathbf{F}_2$ .

## Solution cont'd

Now we use Newton's second law in component form to find the  $x$  and  $y$  components of acceleration:

$$a_x = \frac{\Sigma F_x}{m} = \frac{8.7 \text{ N}}{0.30 \text{ kg}} = 29 \text{ m/s}^2$$

$$a_y = \frac{\Sigma F_y}{m} = \frac{5.2 \text{ N}}{0.30 \text{ kg}} = 17 \text{ m/s}^2$$

The acceleration has a magnitude of

$$a = \sqrt{(29)^2 + (17)^2} \text{ m/s}^2 = 34 \text{ m/s}^2$$

and its direction relative to the positive  $x$  axis is

$$\theta = \tan^{-1} \left( \frac{a_y}{a_x} \right) = \tan^{-1} \left( \frac{17}{29} \right) = 30^\circ$$



# The Gravitational Force and Weight

We are well aware that all objects are attracted to the Earth. The attractive force exerted by the Earth on an object is called the gravitational force  $F_g$ . *This force is directed* toward the center of the Earth, and its magnitude is called the weight of the object.

$$\mathbf{F}_g = m\mathbf{g}$$

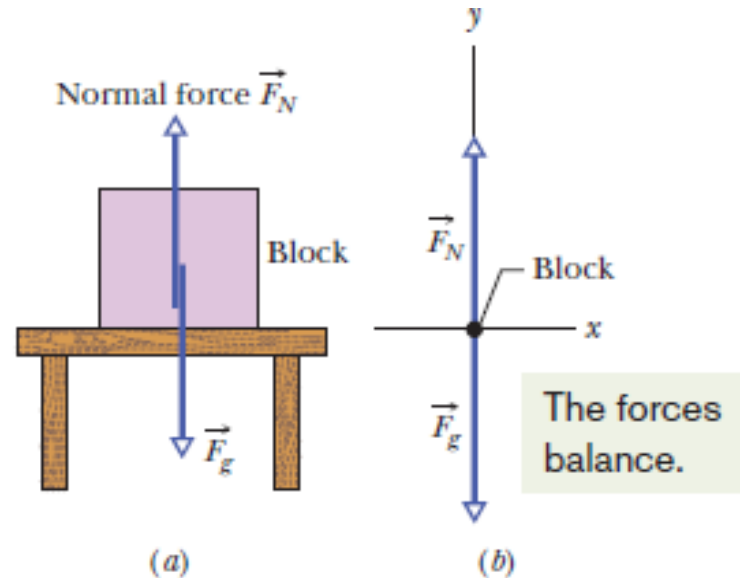
## The Normal Force

When a body presses against a surface, the surface (even a seemingly rigid one) deforms and pushes on the body with a normal force that is perpendicular to the surface.

**Note:** To solve problems with Newton's second law, we often draw a free-body diagram in which the only body shown is the one for which we are summing forces.

The normal force is the force on the block from the supporting table.

The gravitational force on the block is due to Earth's downward pull.



## How Much Do You Weigh in an Elevator?

You have most likely had the experience of standing in an elevator that accelerates upward as it moves toward a higher floor. In this case, you feel heavier. In fact, if you are standing on a bathroom scale at the time, the scale measures a force magnitude that is greater than your weight. Thus, you have tactile and measured evidence that leads you to believe you are heavier in this situation. *Are you heavier?*

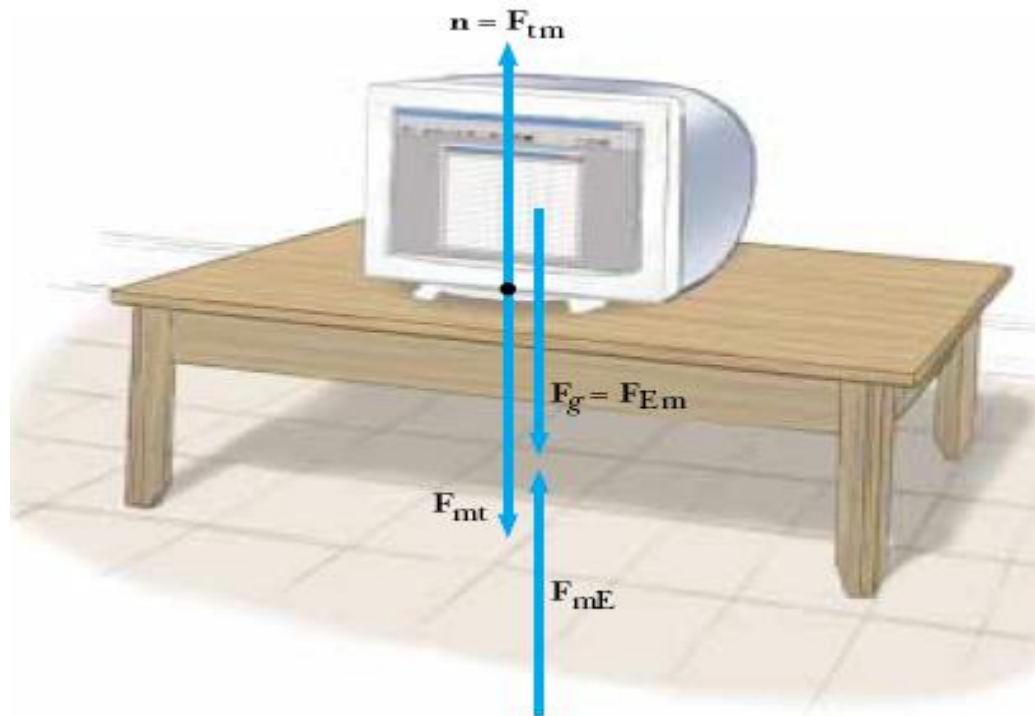
## The Answer is: NO

No, your weight is unchanged. To provide the acceleration upward, the floor or scale must exert on your feet an upward force that is greater in magnitude than your weight. It is this greater force that you feel, which you interpret as feeling heavier. The scale reads this upward force, not your weight, and so its reading increases.

# Newton's Third Law

If two objects interact, the force  $F_{12}$  exerted by object 1 on object 2 is equal in magnitude and opposite in direction to the force  $F_{21}$  exerted by object 2 on object 1:

$$\mathbf{F}_{12} = -\mathbf{F}_{21}$$



This is equivalent to stating that a single isolated force cannot exist.

# APPLICATION OF NEWTON'S LAWS

- In this section we apply Newton's laws to objects that are either in equilibrium ( $a = 0$ ) or accelerating along a straight line under the action of constant external forces
- We assume that the objects behave as particles so that we need not worry about rotational motion.
- We also neglect the effects of friction in those problems involving motion; this is equivalent to stating that the surfaces are *frictionless*.
- Finally, we usually neglect the mass of any ropes involved.

## Tension:

When a rope attached to an object is pulling on the object, the rope exerts a force  $T$  on the object, and the magnitude of that force is called the tension in the rope.

### Objects in Equilibrium

$$\sum F_y = T - F_g = 0 \quad \text{or} \quad T = F_g$$

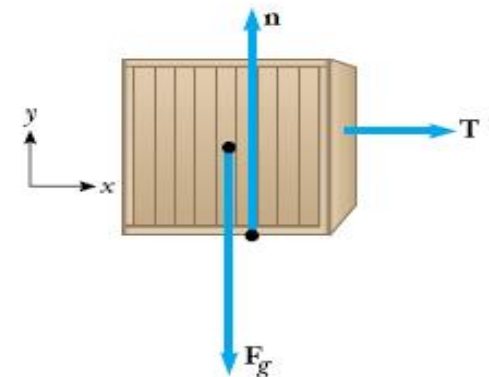
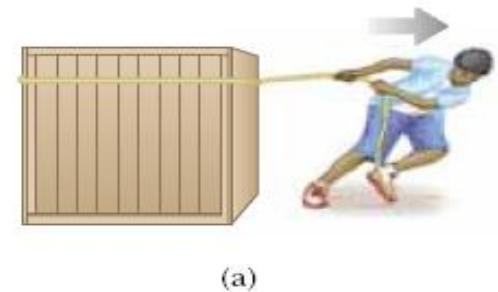
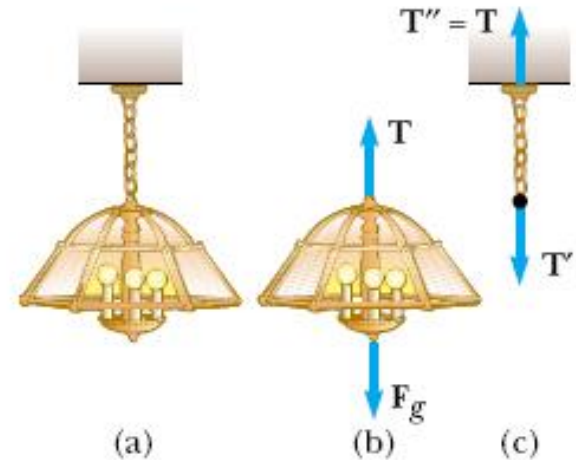
### Objects Experiencing a Net Force

$$\sum F_x = T = ma_x \quad \text{or} \quad a_x = \frac{T}{m}$$

$$n + (-F_g) = 0 \quad \text{or} \quad n = F_g$$

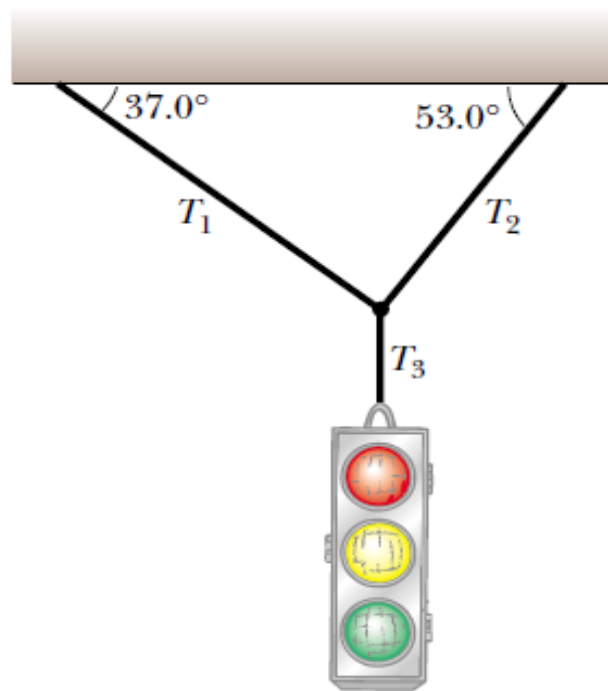
$$v_{xf} = v_{xi} + \left(\frac{T}{m}\right)t$$

$$x_f = x_i + v_{xi}t + \frac{1}{2}\left(\frac{T}{m}\right)t^2$$

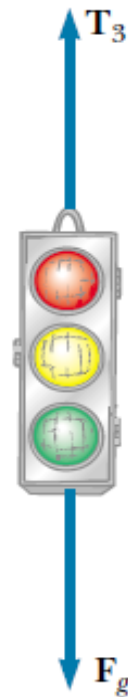


# Example Problem

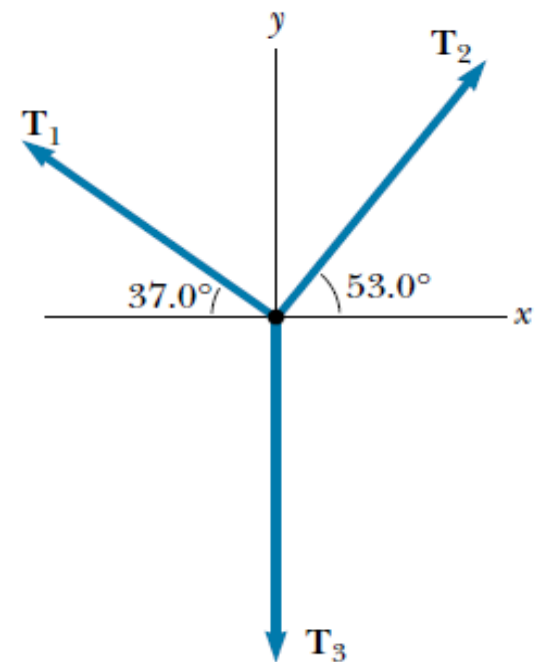
A traffic light weighing 125 N hangs from a cable tied to two other cables fastened to a support. The upper cables make angles of  $37.0^\circ$  and  $53.0^\circ$  with the horizontal. Find the tension in the three cables.



(a)



(b)



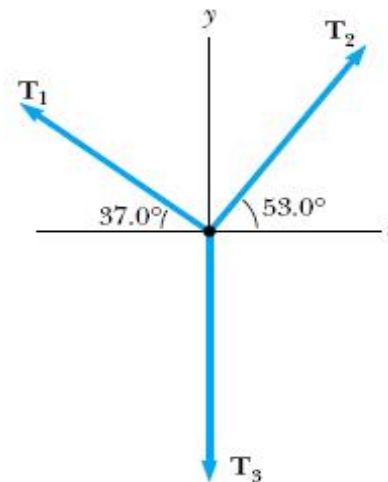
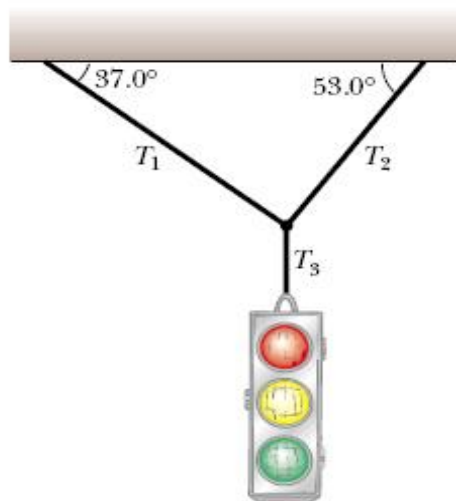
(c)

(a) A traffic light suspended by cables. (b) Free-body diagram for the traffic light. (c) Free-body diagram for the knot where the three cables are joined.

# Solution:

In Figure (b) the force  $\mathbf{T}_3$  exerted by the vertical cable supports the light, and so  $T_3 = F_g = 125 \text{ N}$ . Next, we choose the coordinate axes shown in Figure (c) and resolve the forces acting on the knot into their components:

Force	$x$ Component	$y$ Component
$\mathbf{T}_1$	$-T_1 \cos 37.0^\circ$	$T_1 \sin 37.0^\circ$
$\mathbf{T}_2$	$T_2 \cos 53.0^\circ$	$T_2 \sin 53.0^\circ$
$\mathbf{T}_3$	0	$-125 \text{ N}$





## Solution:

Knowing that the knot is in equilibrium ( $\mathbf{a} = 0$ ) allows us to write

$$(1) \quad \sum F_x = -T_1 \cos 37.0^\circ + T_2 \cos 53.0^\circ = 0$$

$$(2) \quad \sum F_y = T_1 \sin 37.0^\circ + T_2 \sin 53.0^\circ + (-125 \text{ N}) = 0$$

From (1) we see that the horizontal components of  $\mathbf{T}_1$  and  $\mathbf{T}_2$  must be equal in magnitude, and from (2) we see that the sum of the vertical components of  $\mathbf{T}_1$  and  $\mathbf{T}_2$  must balance the weight of the light. We solve (1) for  $T_2$  in terms of  $T_1$  to obtain

$$T_2 = T_1 \left( \frac{\cos 37.0^\circ}{\cos 53.0^\circ} \right) = 1.33 T_1$$

This value for  $T_2$  is substituted into (2) to yield

$$T_1 \sin 37.0^\circ + (1.33 T_1) (\sin 53.0^\circ) - 125 \text{ N} = 0$$

$$T_1 = 75.1 \text{ N}$$

$$T_2 = 1.33 T_1 = 99.9 \text{ N}$$

**What If?** Suppose the two angles in Figure (a) are equal. What would be the relationship between  $T_1$  and  $T_2$ ?

**Answer** We can argue from the symmetry of the problem that the two tensions  $T_1$  and  $T_2$  would be equal to each other. Mathematically, if the equal angles are called  $\theta$ , Equation (3) becomes

$$T_2 = T_1 \left( \frac{\cos \theta}{\cos \theta} \right) = T_1$$

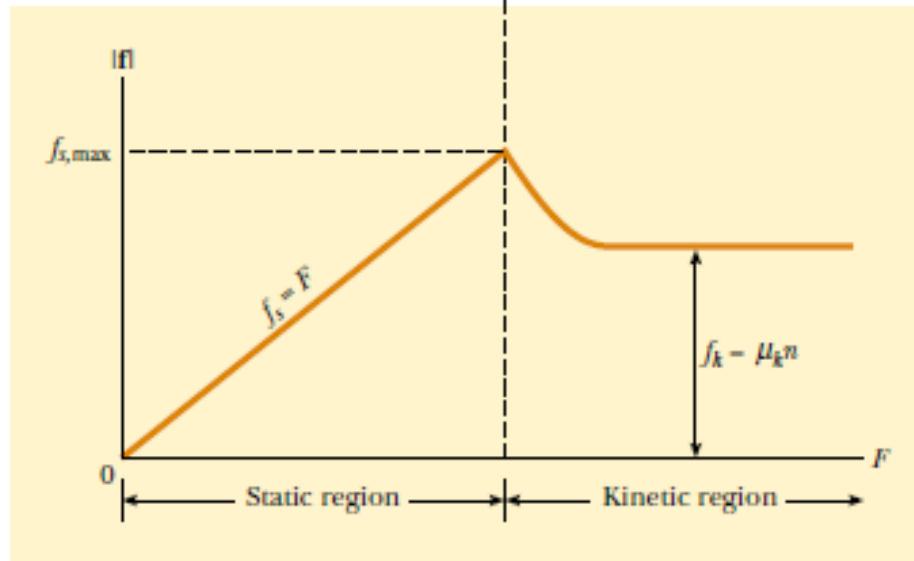
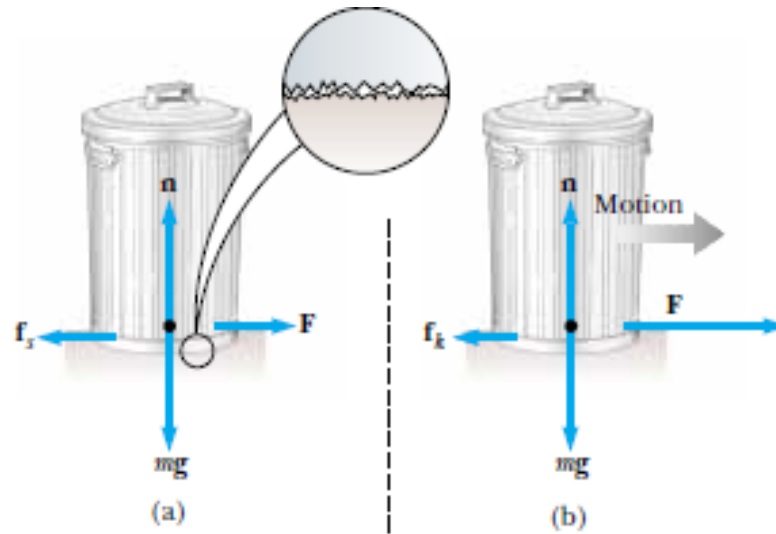
which also tells us that the tensions are equal. Without knowing the specific value of  $\theta$ , we cannot find the values of  $T_1$  and  $T_2$ . However, the tensions will be equal to each other, regardless of the value of  $\theta$ .

# Forces of Friction

When an object is in motion either on a surface or in a viscous medium such as air or water, there is resistance to the motion because the object interacts with its surroundings. We call such resistance a force of friction.

Forces of friction are very important in our everyday lives. They allow us to walk or run and are necessary for the motion of wheeled vehicles.

# Static and Kinetic Friction



- The magnitude of the force of static friction between any two surfaces in contact can have the values.

$$f_s \leq \mu_s n$$

- The magnitude of the force of kinetic friction acting between two surfaces is

$$f_k = \mu_k n$$

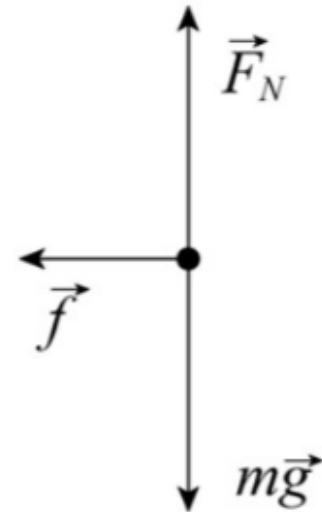
- The values of  $\mu_s$  and  $\mu_k$  depend on the nature of the surfaces, but  $\mu_k$  is generally less than  $\mu_s$ .
- The direction of the friction force on an object is parallel to the surface with which the object is in contact and opposite to the actual motion (kinetic friction) or the impending motion (static friction) of the object relative to the surface.

### Example:

A baseball player with mass 79kg, sliding into a base is slowed by a force of friction of 470N. What is the coefficient of kinetic friction between the player and the ground?

Draw a free body diagram.

$$\mu_k = \frac{f}{F_N} = \frac{470\text{N}}{(79\text{kg})(9.8\text{m/s}^2)} = 0.61$$



## Experimental Determination of $\mu_s$ and $\mu_k$

The following is a simple method of measuring coefficients of friction: Suppose a block is placed on a rough surface inclined relative to the horizontal, as shown in Figure 5.19. The incline angle is increased until the block starts to move. Show that by measuring the critical angle  $\theta_c$  at which this slipping just occurs, we can obtain  $\mu_s$ .

**Solution** Conceptualizing from the free body diagram in Figure 5.19, we see that we can categorize this as a Newton's second law problem. To analyze the problem, note that the only forces acting on the block are the gravitational force  $mg$ , the normal force  $n$ , and the force of static friction  $f_s$ . These forces balance when the block is not moving. When we choose  $x$  to be parallel to the plane and  $y$  perpendicular to it, Newton's second law applied to the block for this balanced situation gives

$$(1) \quad \sum F_x = mg \sin \theta - f_s = ma_x = 0$$

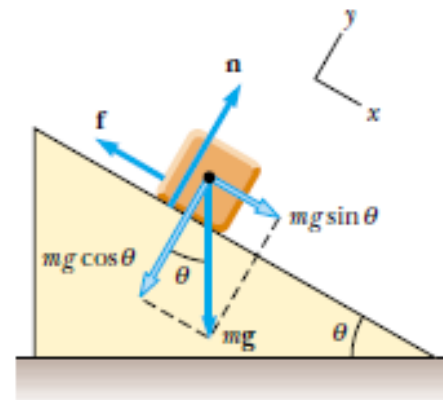
$$(2) \quad \sum F_y = n - mg \cos \theta = ma_y = 0$$

We can eliminate  $mg$  by substituting  $mg = n/\cos \theta$  from (2) into (1) to find

$$(3) \quad f_s = mg \sin \theta = \left( \frac{n}{\cos \theta} \right) \sin \theta = n \tan \theta$$

When the incline angle is increased until the block is on the verge of slipping, the force of static friction has reached its maximum value  $\mu_s n$ . The angle  $\theta$  in this situation is the critical angle  $\theta_c$ , and (3) becomes

$$\mu_s n = n \tan \theta_c$$



**Figure 5.19** (Example 5.12) The external forces exerted on a block lying on a rough incline are the gravitational force  $mg$ , the normal force  $n$ , and the force of friction  $f$ . For convenience, the gravitational force is resolved into a component along the incline  $mg \sin \theta$  and a component perpendicular to the incline  $mg \cos \theta$ .

$$\mu_s = \tan \theta_c$$

For example, if the block just slips at  $\theta_c = 20.0^\circ$ , then we find that  $\mu_s = \tan 20.0^\circ = 0.364$ .

To finalize the problem, note that once the block starts to move at  $\theta \geq \theta_c$ , it accelerates down the incline and the force of friction is  $f_k = \mu_k n$ . However, if  $\theta$  is reduced to a value less than  $\theta_c$ , it may be possible to find an angle  $\theta'_c$  such that the block moves down the incline with constant speed ( $a_x = 0$ ). In this case, using (1) and (2) with  $f_s$  replaced by  $f_k$  gives

$$\mu_k = \tan \theta'_c$$

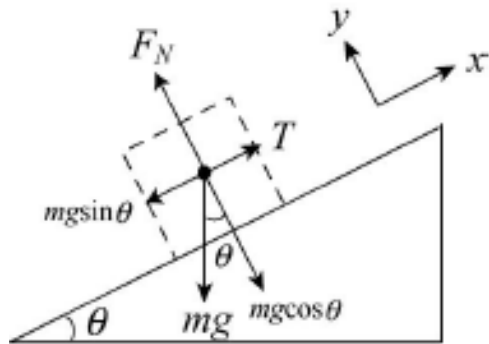
where  $\theta'_c < \theta_c$ .

## Example:

In Figure shown below, let the mass of the block be 6.5 kg and the angle  $\theta$  be  $40^\circ$ .

Find (a) the tension in the cord and

(b) the normal force acting on the block. (c) If the cord is cut, find the magnitude of the resulting acceleration of the block.



$$T - mg \sin \theta = 0$$

$$F_N - mg \cos \theta = 0,$$

$$(a) T = 6.5 \times 9.8 \times \sin(40) = 40.94 \text{ N}$$

$$(b) F_N = 6.5 \times 9.8 \times \cos(40) = 48.79 \text{ N}$$

$$(c) a = -g \sin \theta = -9.8 \sin(40) = -6.299 \text{ m/s}^2$$





# RECAPITULATION

1. An example of an inertial reference frame is:
  - A. any reference frame that is not accelerating
  - B. a frame attached to a particle on which there are no forces
  - C. any reference frame that is at rest
  - D. a reference frame attached to the center of the universe
  - E. a reference frame attached to Earth

ans: B

2. An object moving at constant velocity in an inertial frame must:
- A. have a net force on it
  - B. eventually stop due to gravity
  - C. not have any force of gravity on it
  - D. have zero net force on it
  - E. have no frictional force on it

**ans: D**

A newton is the force:

- A. of gravity on a 1 kg body
- B. of gravity on a 1 g body
- C. that gives a 1 g body an acceleration of  $1 \text{ cm/s}^2$
- D. that gives a 1 kg body an acceleration of  $1 \text{ m/s}^2$
- E. that gives a 1 kg body an acceleration of  $9.8 \text{ m/s}^2$

ans: D

The standard 1-kg mass is attached to a compressed spring and the spring is released. If the mass initially has an acceleration of  $5.6 \text{ m/s}^2$ , the force of the spring has a magnitude of:

- A. 2.8 N
- B. 5.6 N
- C. 11.2 N
- D. 0
- E. an undetermined amount

**ans: B**

Acceleration is always in the direction:

- A. of the displacement
- B. of the initial velocity
- C. of the final velocity
- D. of the net force
- E. opposite to the frictional force

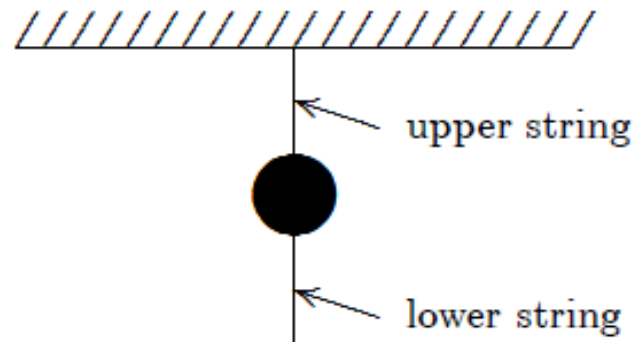
ans: D

The term “mass” refers to the same physical concept as:

- A. weight
- B. inertia
- C. force
- D. acceleration
- C. volume

ans: B

A heavy ball is suspended as shown. A quick jerk on the lower string will break that string but a slow pull on the lower string will break the upper string. The first result occurs because:



- A. the force is too small to move the ball
- B. action and reaction is operating
- C. the ball has inertia
- D. air friction holds the ball back
- E. the ball has too much energy

ans: C