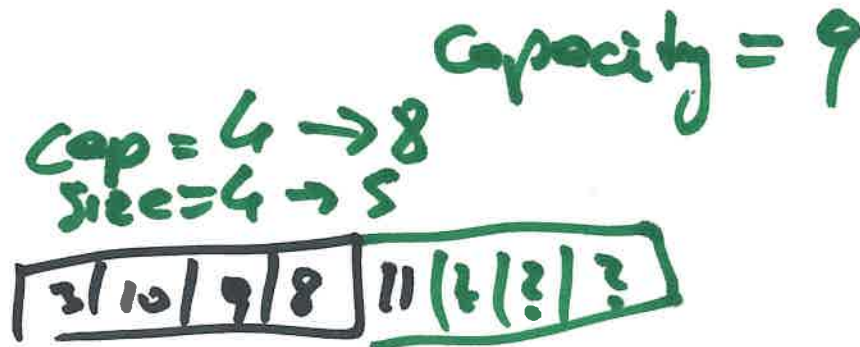
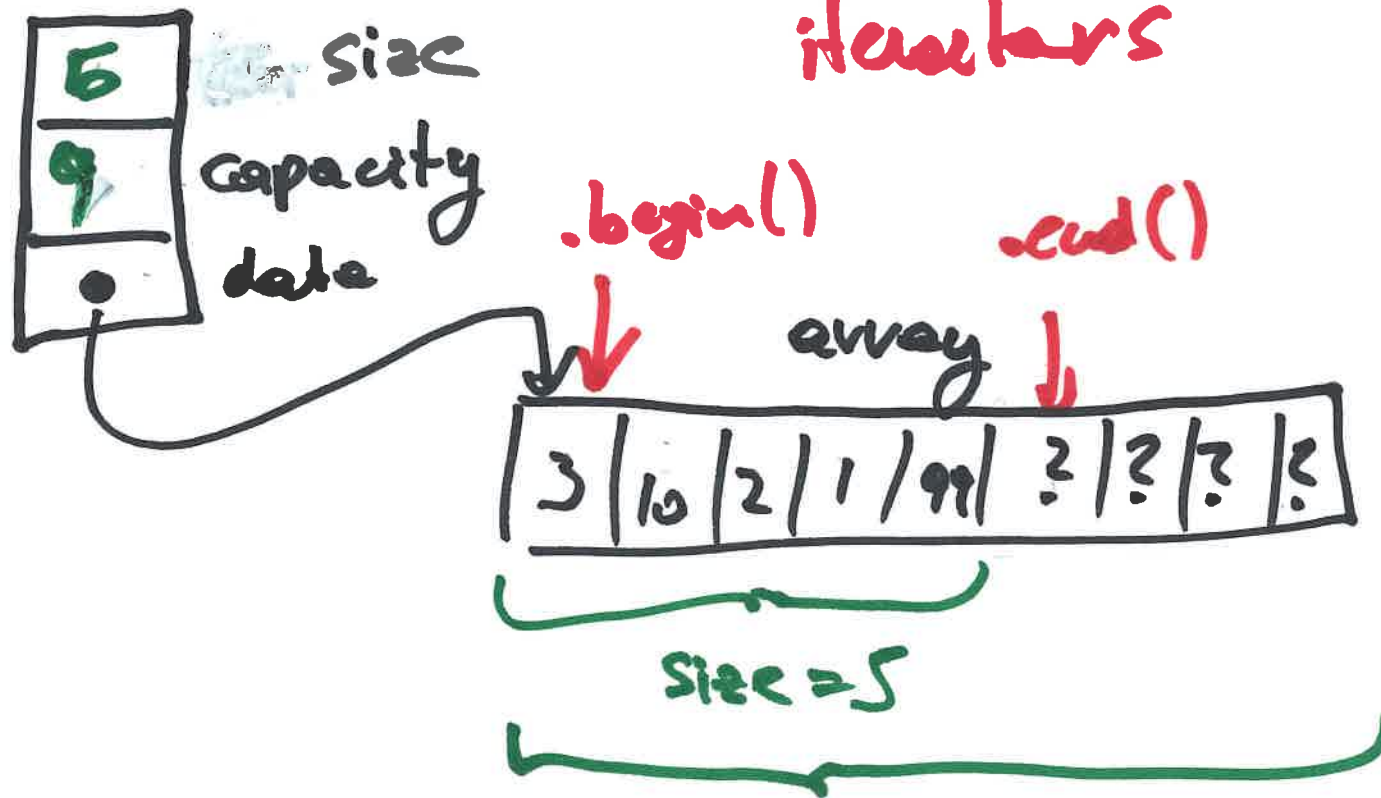


CS 2341

Chapter 3

Lists, Stacks, and Queues

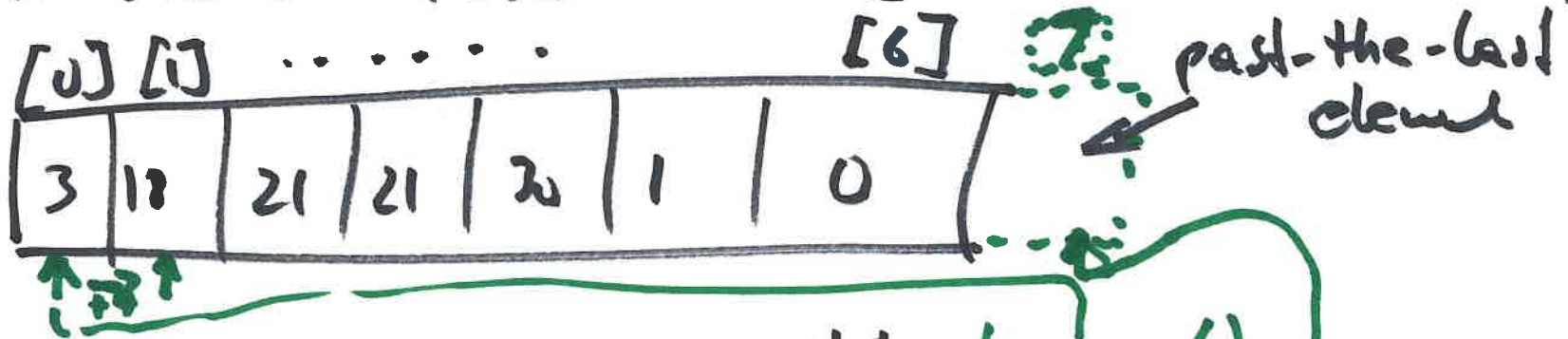
DS Vector (std::vector)



2x size every time we run out of capacity

Iterators for vectors

`std::vector<int> v = { 3, 18, 21, 21, 21, 1, 0 };`



`std::vector<int>::iterator it1 = v.begin()`
`std::vector<int>::iterator it2 = v.end()`

`it1++;` // go to the next element

`std::cout << *it1 << "\n";` \Rightarrow 18

"dereference" the iterator

```

1  #ifndef MATRIX_H
2  #define MATRIX_H
3
4  #include <vector>
5  using namespace std;
6
7  template <typename Object>
8  class matrix
9  {
10     public:
11     matrix( int rows, int cols ) : array( rows )
12     {
13         for( auto & thisRow : array )
14             thisRow.resize( cols );
15     }
16
17     matrix( vector<vector<Object>>> v ) : array( v )
18     { }
19     matrix( vector<vector<Object>>> && v ) : array( std::move( v ) )
20     { }
21
22     const vector<Object> & operator[] ( int row ) const
23     { return array[ row ]; }
24     vector<Object> & operator[] ( int row )
25     { return array[ row ]; }
26
27     int numRows( ) const
28     { return array.size( ); }
29     int numcols( ) const
30     { return numRows( ) ? array[ 0 ].size( ) : 0; }
31     private:
32     vector<vector<Object>>> array;
33 };
34 #endif

```

Figure 1.26 A complete matrix class

1.7.2 operator[]

The idea of operator[] is that if we have a matrix m , then $m[i]$ should return a vector corresponding to row i of matrix m . If this is done, then $m[i][j]$ will give the entry in position j for vector $m[i]$, using the normal vector indexing operator. Thus, the matrix operator[] returns a vector<Object> rather than an Object.

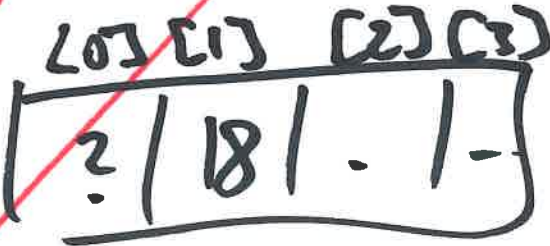
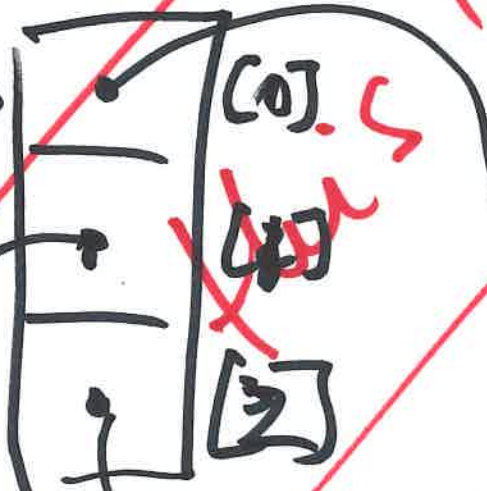
Matrix

array of arrays
rows 3

cols 4

} 12

*x m

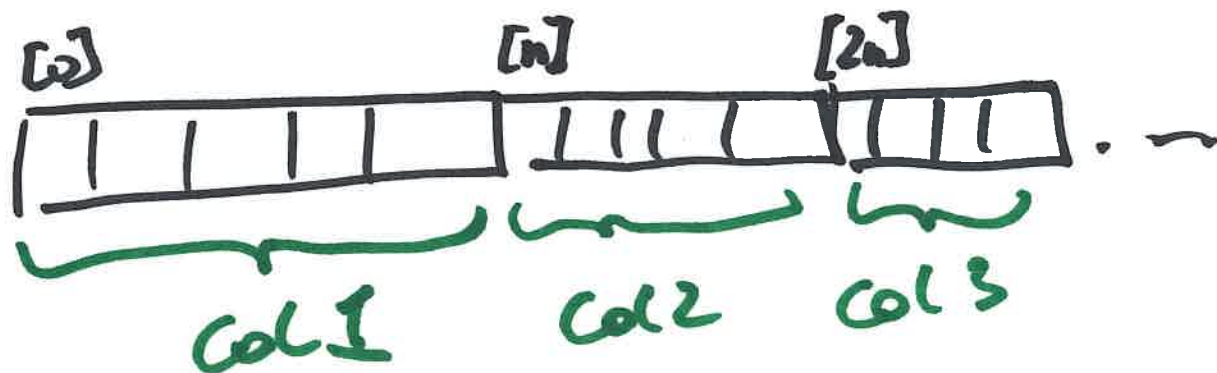
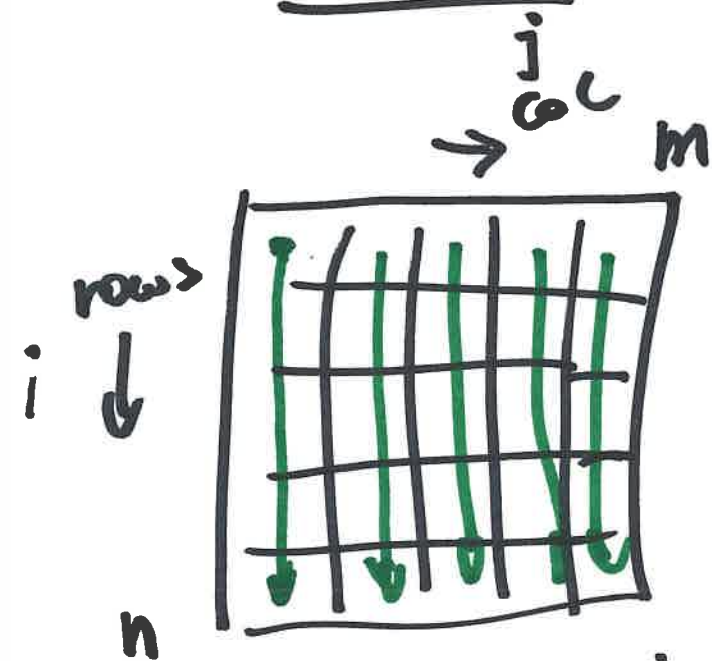


do not

$$m[1][1] = 18;$$

Matrix

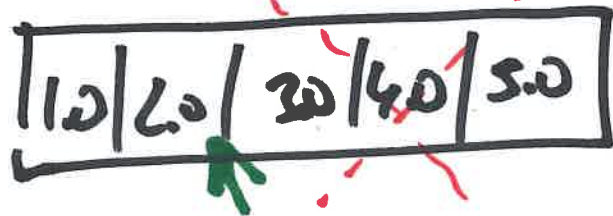
n rows \times m col



column-major orientation

index into array: $i, j \Rightarrow j \times n + i$

Insert into a vector (array)



insert 2.5

2. copy ↓



1. new array

1. allocate memory
 $O(1)$

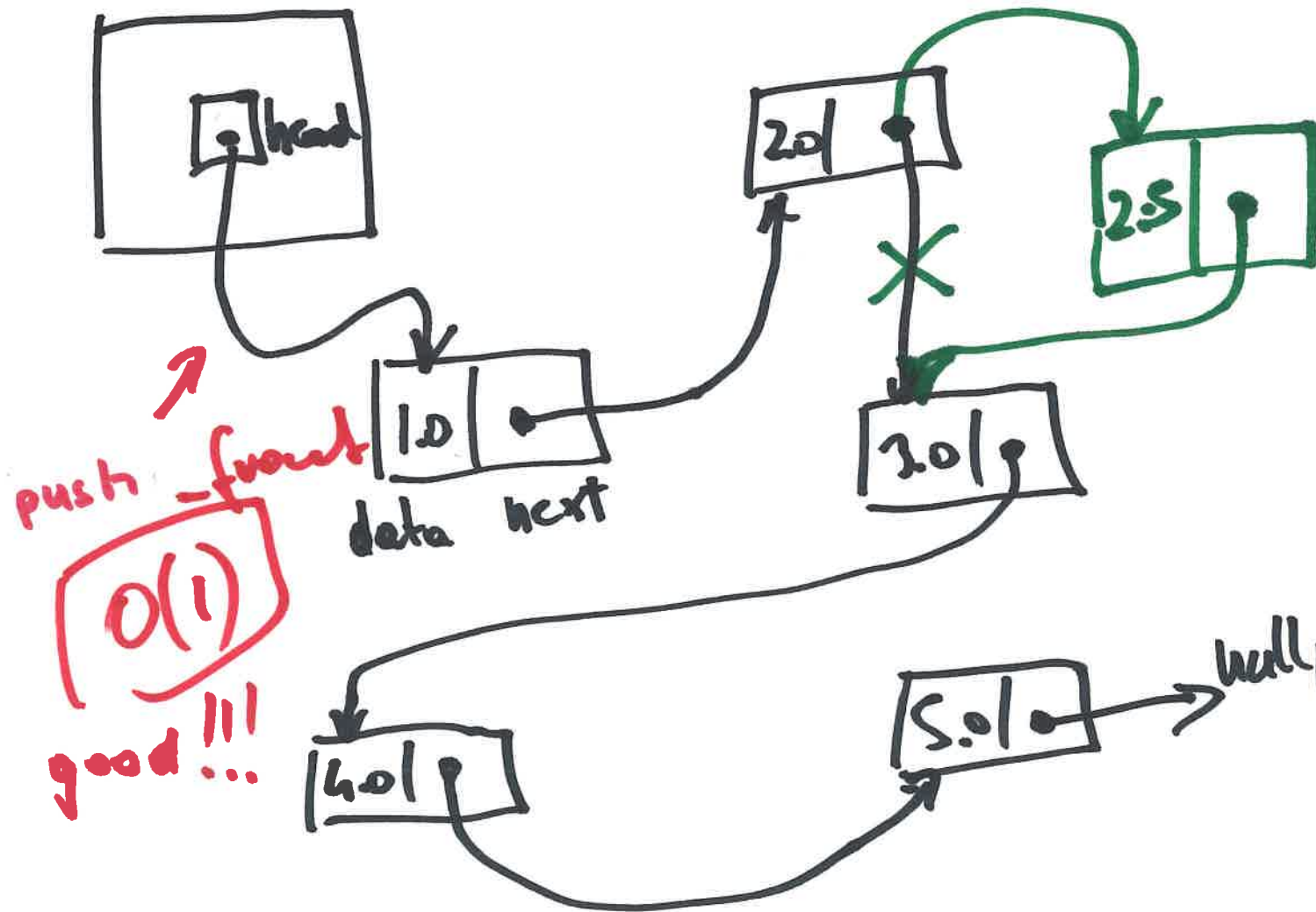
2. copy + insert
 $O(n)$ bad!

3. delete old
array from
memory

$O(1)$

Linked List (singly-linked list)

insert (2.5 after 2)



1. allocate memory
 $O(1)$

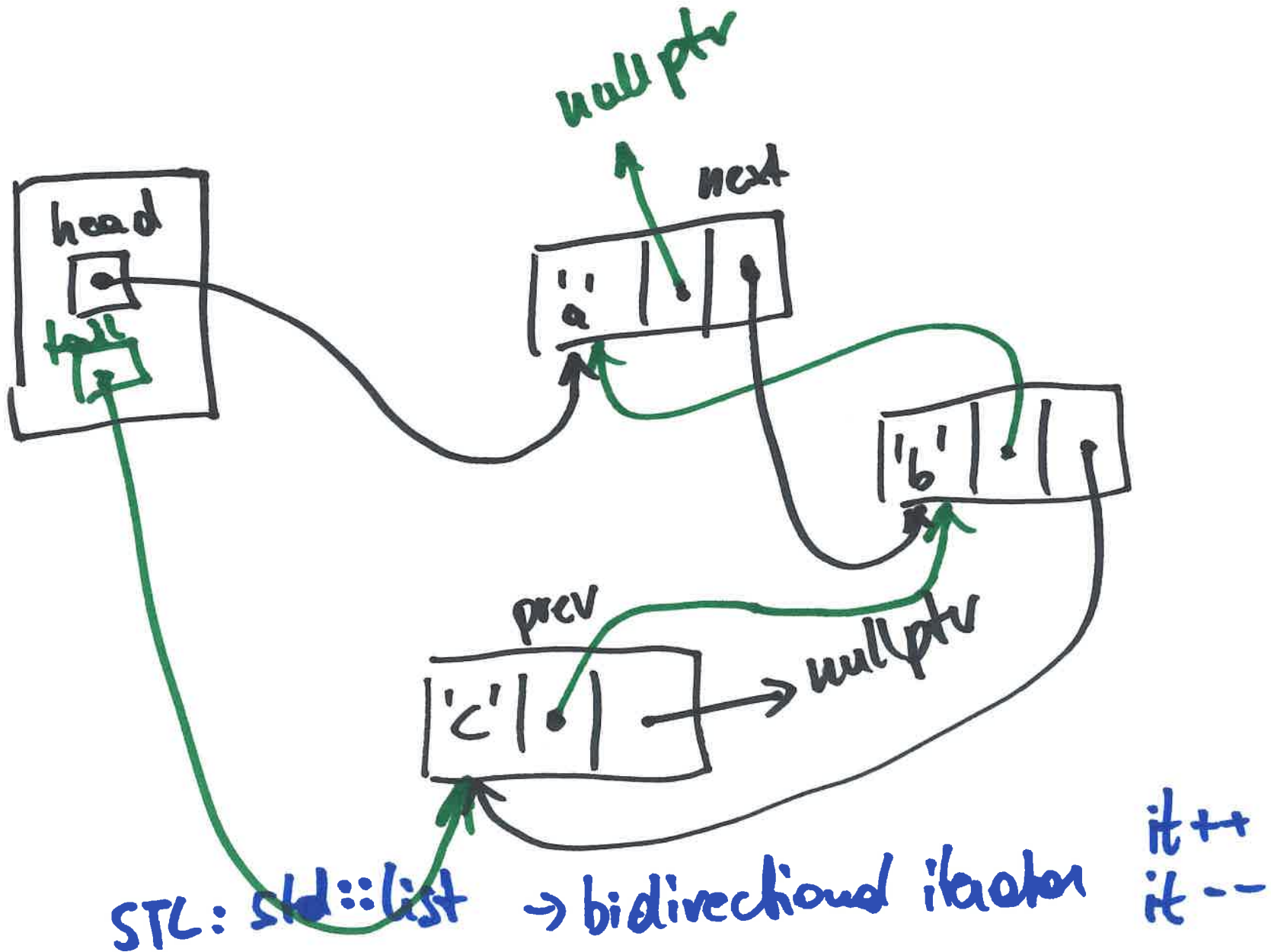
2. Link new element
 $O(1)$

1.5 find insertion point
 $O(n)$

bad!

STL: forward-list with forward iterator (only ++)

Doubly-linked List



Time Complexity

Each element is allocated in a linked list individually, so we do not need contiguous memory and we do not need to copy/move data for insertion and deletion. What is the time complexity for the following operations using lists or arrays (Big-O notation)?

Operation	Array	STL vector	Singly Linked List	Doubly Linked List
insert a new element at a random location	$O(n)$	$O(n)$	$O(n)$	$O(n)$
insert a new element (front)	$O(n)$	$O(n)$	$O(1)$	$O(1)$
insert a new element (back)	$O(n)$	$O(1)$	$O(n)$	$O(1)$
access an element (with index)	$O(1)$	$O(1)$	$O(n)$	$O(n)$
access an element (with iterator)	—	$O(1)$	$O(1)$	$O(1)$
find an element by value	$O(n)$	$O(n)$	$O(n)$	$O(n)$
delete an element	$O(n)$	$O(n)$	$O(n)$	$O(n)$
delete the whole data structure	$O(1)$	$O(1)$	$O(n)$	$O(n)$

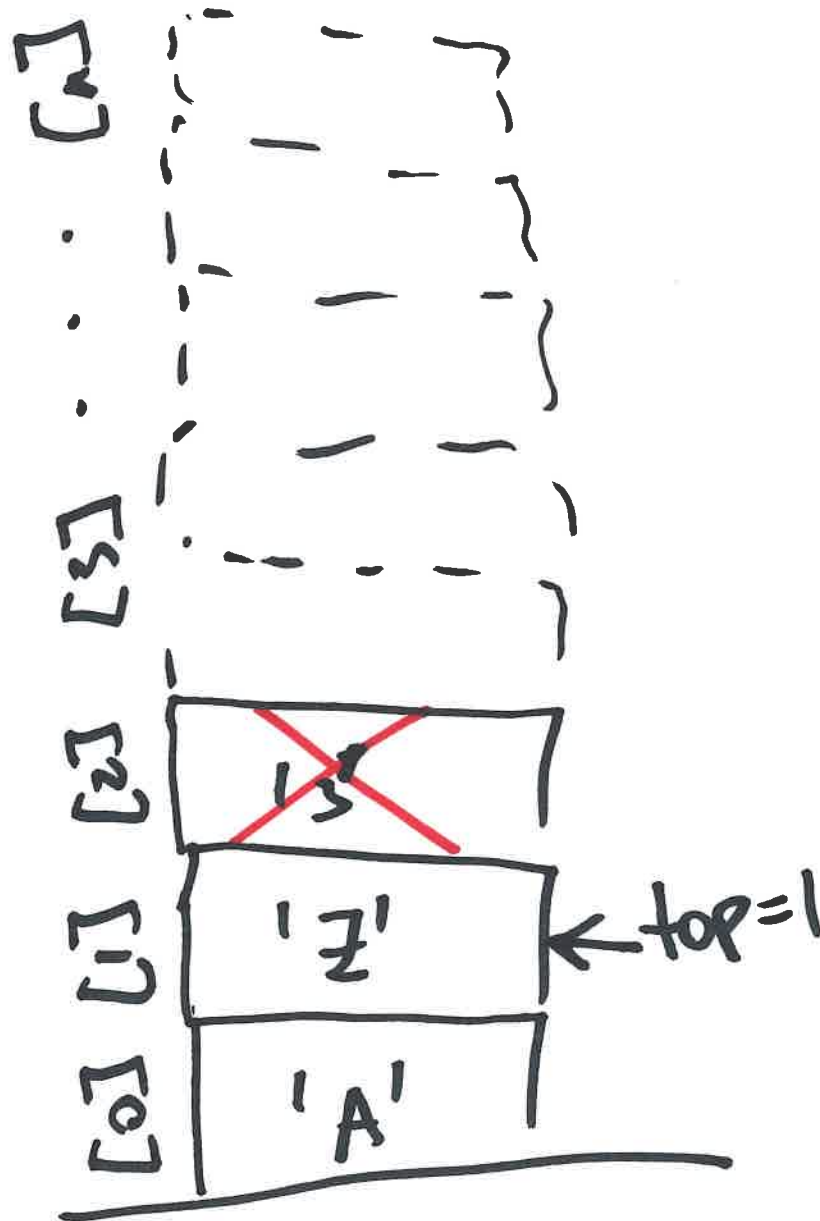
* no Capacity left

** if sorted \rightarrow binary search $\rightarrow O(\log n)$
 *** first element $O(1)$

*** last element $\rightarrow O(1)$

Stack

LIFO (last-in first-out)



push('A')
push('z')
push('3')

$O(1)$

pop() → '3'

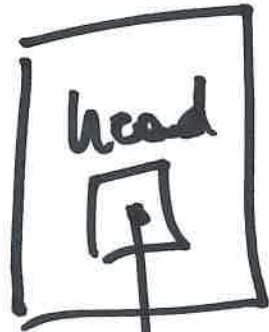
$O(1)$

Implement as array
empty stack top = -1
size = top + 1

Stack

List implementation

using push-back



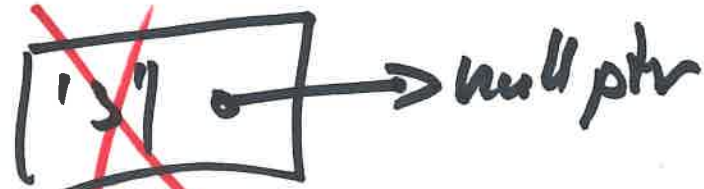
don't do this!!

~~push('A')~~

~~push('2')~~ $O(n)$

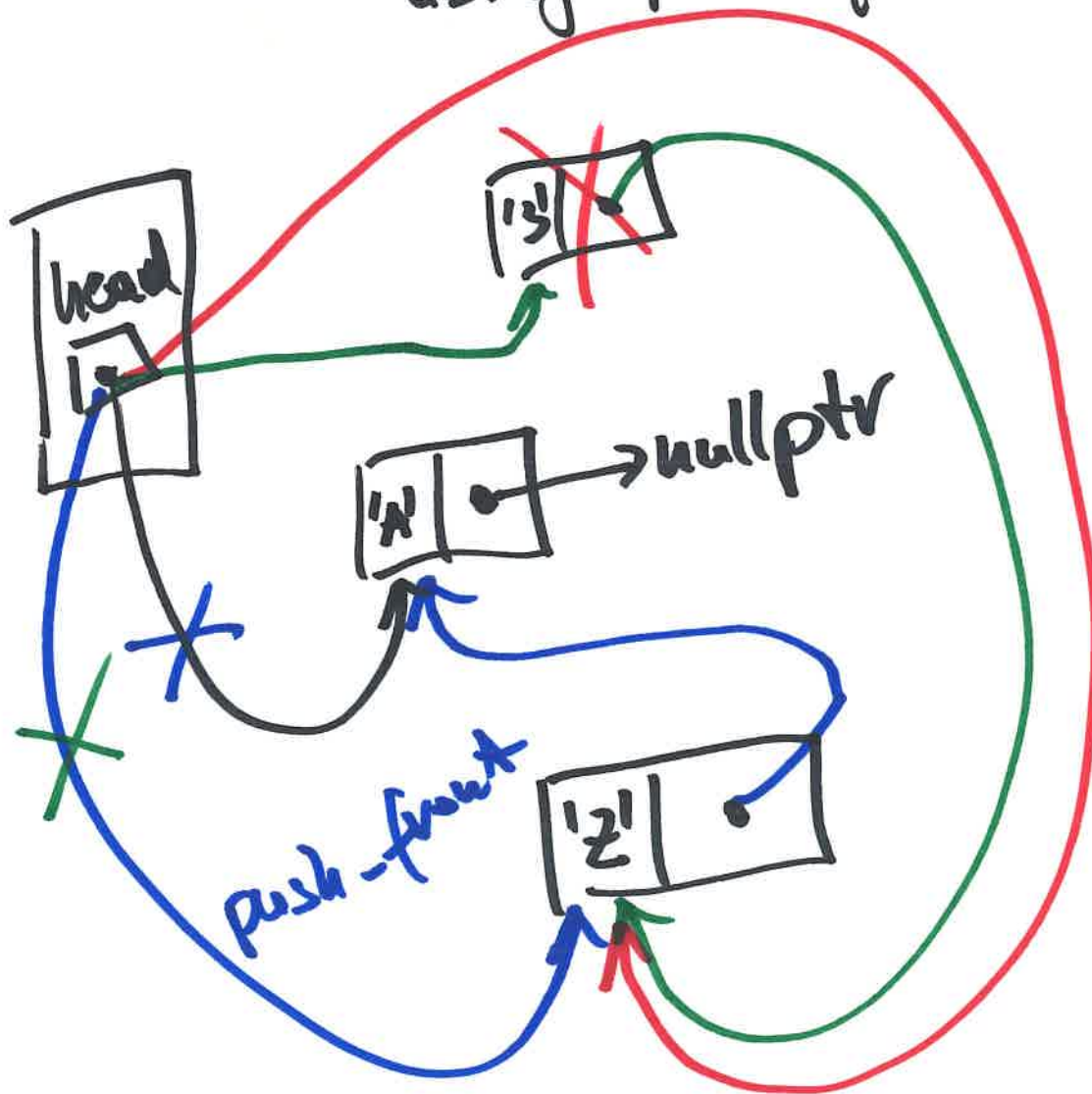
~~push('3')~~

pop(1 → 3) $O(n)$



Stack
using push-front

List



push('A') $O(1)$
push('z')
push('3')

pop() $\rightarrow 3$ $O(1)$

#include <iostream>

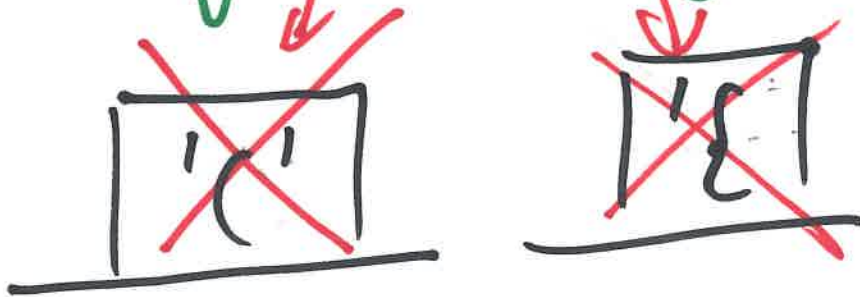
Check for balanced brackets

int main () {

std::cout << "Hello World!" << "\n";

return 0;

}



Empty stack means
brackets are balanced

Post fix notation

arg 1	arg 2	operator	
5	9	+	$\Rightarrow 14$

pre fix notation

operator	arg 1	arg 2	
+	5	9	$\Rightarrow 14$

infix notation

arg 1	operator	arg 2	
5	+	9	$\Rightarrow 14$

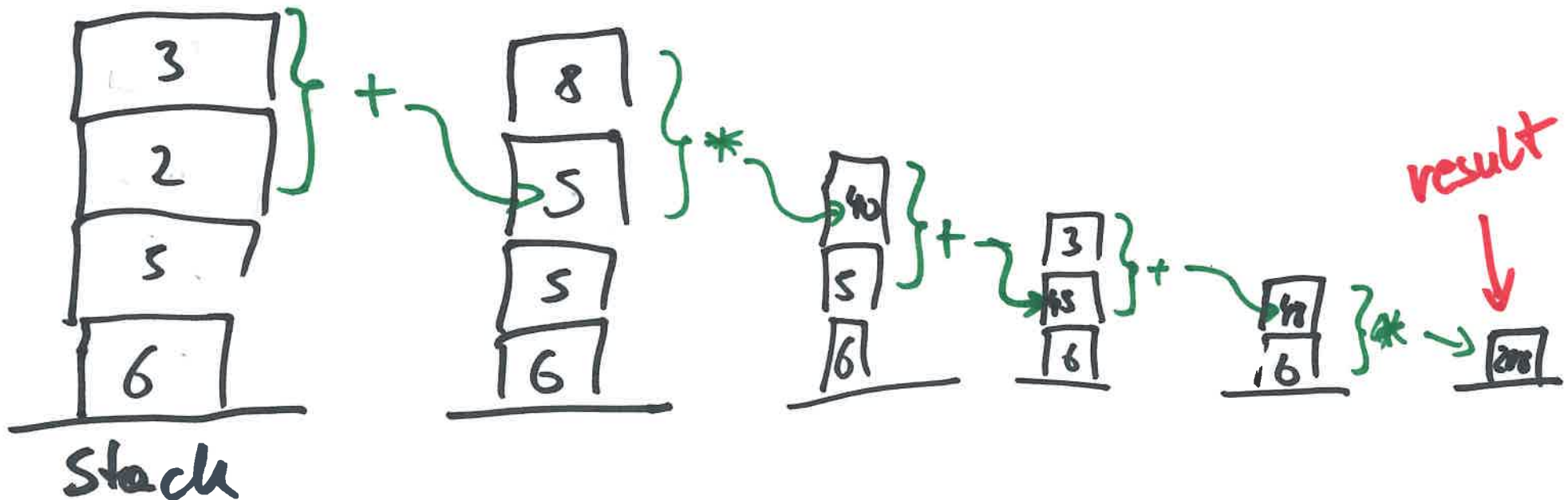
Evaluate a Postfix Expression

$$6\ 5\ 2\ 3 + 8 * + 3 + * = ?$$

- read left-to-right

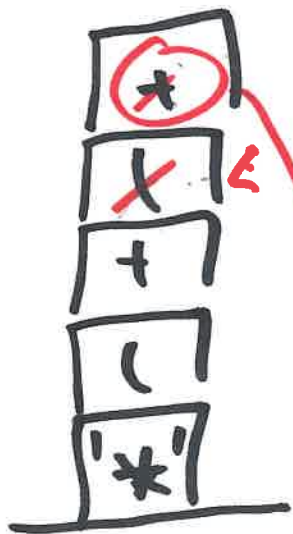
- numbers \rightarrow stack

operators pop the top 2 elements from the stack and push the result back on the stack



Infix to Postfix

Input: $6 * (5 + (2 + 3) * 8 + 3)$

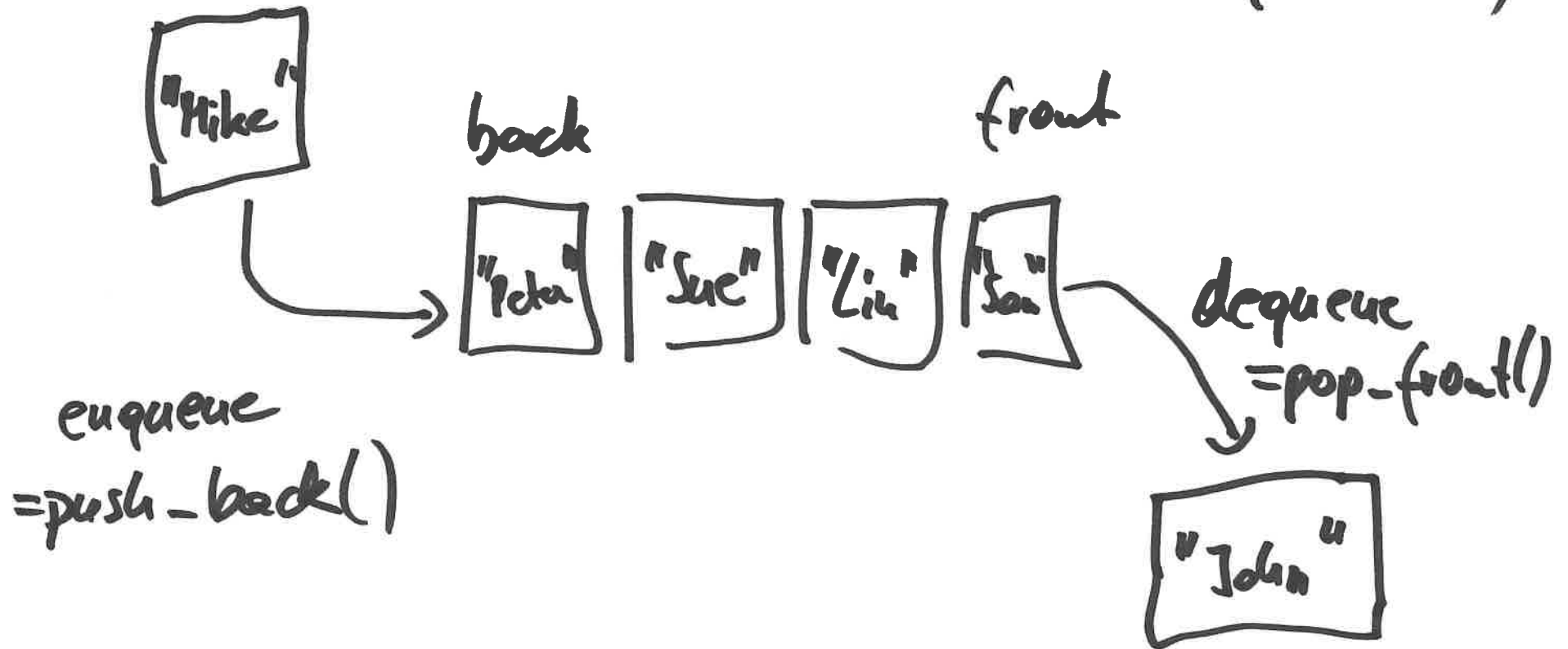


- operands go to output
- operators and parentheses go to stack (be careful with the order of operations)

Output: 6 5 2 3 + 8 * 3 + + *

Queue

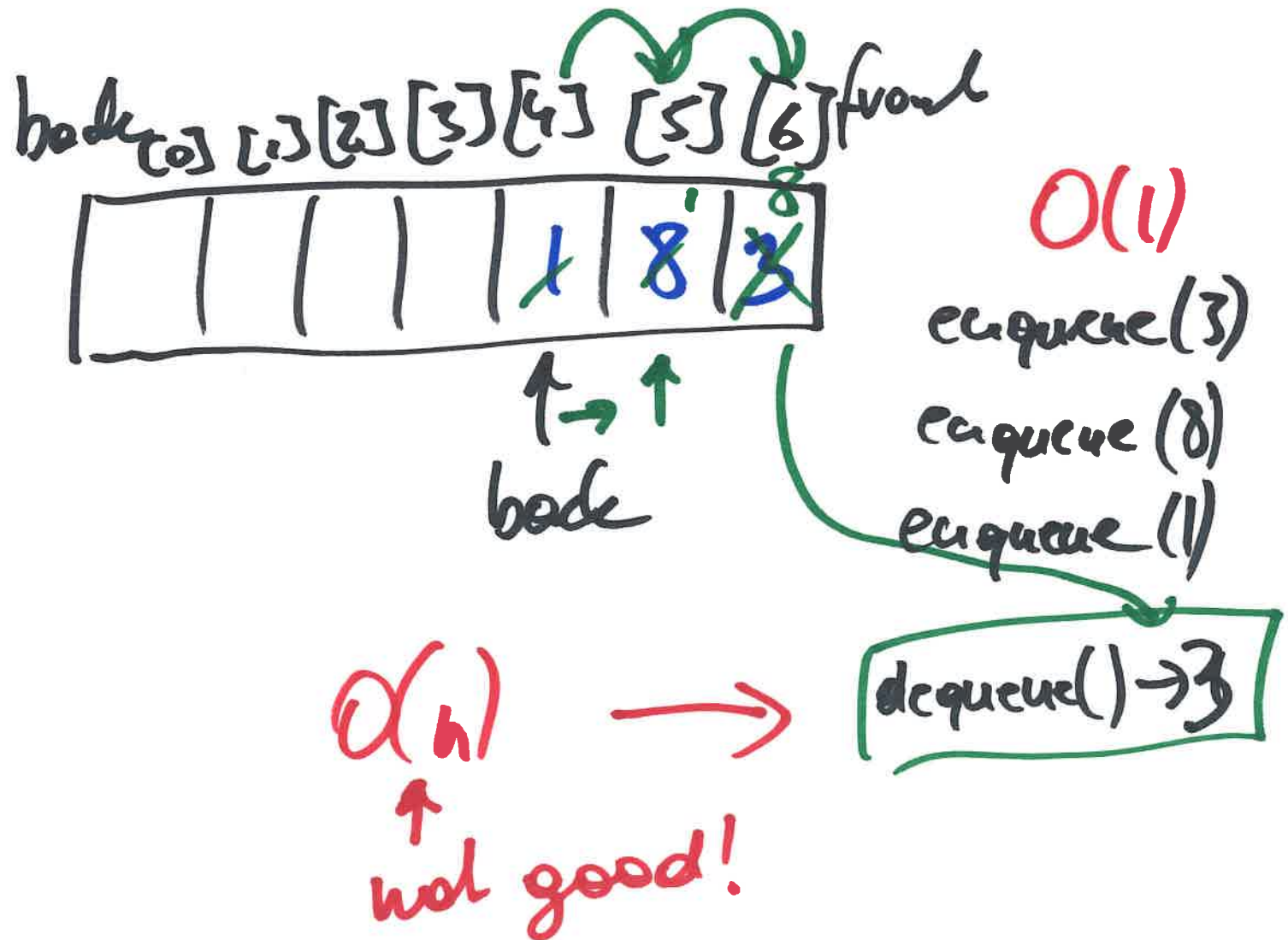
FIFO (first in
first out)



Implementations:

- Vector / array \rightarrow circular buffer
- doubly linked list
- `std::deque`

Queue Array



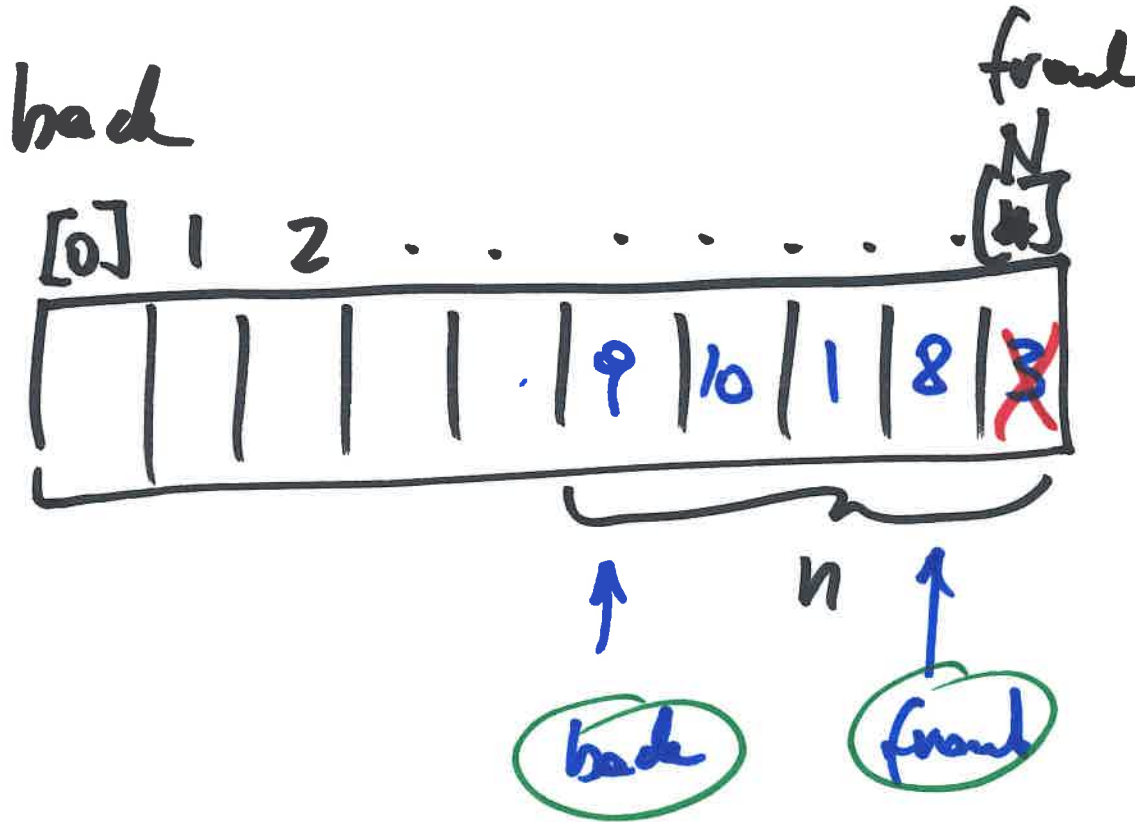
Queue

Array (circular buffer)

$O(1)$

enqueue(3)

enqueue(8)
moves "back"



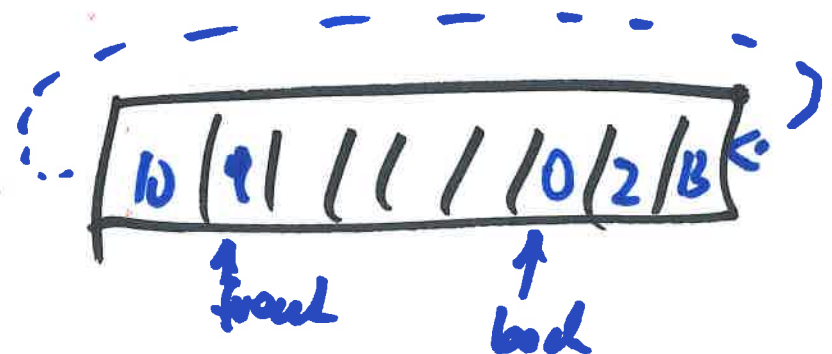
$O(1)$

dequeue()

moves "front"

N

→ circular buffer



Queue doubly-linked list

push-back

$O(1)$

enqueue (3);

enqueue (8);

dequeue (); $\rightarrow 3$ $O(1)$

pop-front

