Naive Lie Theory 3.2 Exercises

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September 2025

Notes

Nothing much to say here.

3.2.1

Say we have a path P(x), where $x \in [0,1]$. P(0) = 1 and P(1) = B, and P is continuous. We simply define Q(x) = AP(x). As matrix multiplication is continuous, Q(0) = A and Q(1) = AB, so we have a continuous path from A to AB thus from 1 to AB, as we have one from 1 to A.

3.2.2

Similarly, we have P(x) where P(0) = 1 and P(1) = A. We define $Q(x) = (P(x))^{-1}$, which is a continuous path from 1 to A^{-1} .

3.2.3

3.2.1 and 3.2.2 showed that the set of identity components are closed under group operation and inverse, thus it's a subgroup. Note that simply being closed under group operation is not sufficient, as that only works for finite groups.