

https://github.com/t-o-k/Maxima-bezier/rational_bezier_curves_2d.wmxm

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Resources:

"Drawing Circles with Rational Quadratic Bezier Curves"

<https://ctan.uib.no/macros/latex/contrib/lapdf/rcircle.pdf>

"Graphics with MAXIMA"

http://www.austromath.at/daten/maxima/zusatz/Graphics_with_Maxima.pdf

```
(%i1) kill(all)$
```

```
(%i2) load("draw")$
      load("bezier")$
```

```
(%i3) tau: 2*%pi$
```

```
(%i4) no_of_segments: 3$
```

```
(%i5) angle: tau/no_of_segments/2;
```

```
(angle)  $\frac{\pi}{3}$ 
```

```
(%i6) r2: r1/cos(angle);
```

```
(r2) 2 r1
```

```
(%i7) points_evn_x: r1*[ cos(0*angle), cos(2*angle), cos(4*angle) ];
```

```
(points_evn_x)  $\left[ r1, -\frac{r1}{2}, -\frac{r1}{2} \right]$ 
```

```
(%i8) points_evn_y: r1*[ sin(0*angle), sin(2*angle), sin(4*angle) ];
```

```
(points_evn_y)  $\left[ 0, \frac{\sqrt{3} r1}{2}, -\frac{\sqrt{3} r1}{2} \right]$ 
```

```
(%i9) points_odd_x: r2*[ cos(1*angle), cos(3*angle), cos(5*angle) ];
```

```
(points_odd_x)  $\left[ r1, -2 r1, r1 \right]$ 
```

```
(%i10) points_odd_y: r2*[ sin(1*angle), sin(3*angle), sin(5*angle) ];
```

```
(points_odd_y)  $\left[ \sqrt{3} r1, 0, -\sqrt{3} r1 \right]$ 
```

```
(%i12) points1_x: [ points_evn_x[1], points_odd_x[1], points_evn_x[2] ]$
      points1_y: [ points_evn_y[1], points_odd_y[1], points_evn_y[2] ]$
```

```
(%i14) points2_x: [ points_evn_x[2], points_odd_x[2], points_evn_x[3] ]$
      points2_y: [ points_evn_y[2], points_odd_y[2], points_evn_y[3] ]$
```

```
(%i16) points3_x: [ points_evn_x[3], points_odd_x[3], points_evn_x[1] ]$
      points3_y: [ points_evn_y[3], points_odd_y[3], points_evn_y[1] ]$
```

```
(%i17) weights: matrix([ 1, cos(angle), 1 ]);
```

$$(\text{weights}) \begin{pmatrix} 1 & \frac{1}{2} & 1 \end{pmatrix}$$

```
(%i18) define(f1_x(s), rational_bezier_function_1a(matrix(points1_x), weights, s));
```

$$(\%o18) \quad f1_x(s) := \frac{-\frac{r1 s^2}{2} + r1 (1-s) s + r1 (1-s)^2}{s^2 + (1-s) s + (1-s)^2}$$

```
(%i19) define(f1_y(s), rational_bezier_function_1a(matrix(points1_y), weights, s));
```

$$(\%o19) \quad f1_y(s) := \frac{\frac{\sqrt{3} r1 s^2}{2} + \sqrt{3} r1 (1-s) s}{s^2 + (1-s) s + (1-s)^2}$$

```
(%i20) define(f2_x(s), rational_bezier_function_1a(matrix(points2_x), weights, s));
```

$$(\%o20) \quad f2_x(s) := \frac{-\frac{r1 s^2}{2} - 2 r1 (1-s) s - \frac{r1 (1-s)^2}{2}}{s^2 + (1-s) s + (1-s)^2}$$

```
(%i21) define(f2_y(s), rational_bezier_function_1a(matrix(points2_y), weights, s));
```

$$(\%o21) \quad f2_y(s) := \frac{\frac{\sqrt{3} r1 (1-s)^2}{2} - \frac{\sqrt{3} r1 s^2}{2}}{s^2 + (1-s) s + (1-s)^2}$$

```
(%i22) define(f3_x(s), rational_bezier_function_1a(matrix(points3_x), weights, s));
```

$$(\%o22) \quad f3_x(s) := \frac{r1 s^2 + r1 (1-s) s - \frac{r1 (1-s)^2}{2}}{s^2 + (1-s) s + (1-s)^2}$$

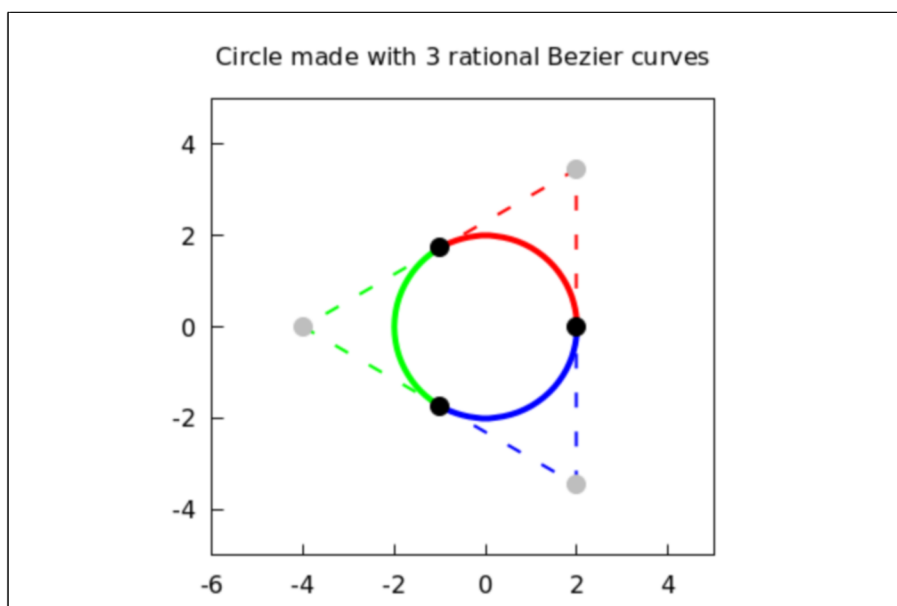
```
(%i23) define(f3_y(s), rational_bezier_function_1a(matrix(points3_y), weights, s));
```

(%o23)
$$f3_y(s) := \frac{-\sqrt{3} r1 (1-s) s - \frac{\sqrt{3} r1 (1-s)^2}{2}}{s^2 + (1-s) s + (1-s)^2}$$

```
(%i24) r1: 2$
```

```
(%i25) wxdraw2d(
    title = "Circle made with 3 rational Bezier curves",
    proportional_axes = xy,
    xrange = [ -6, +5 ],
    yrange = [ -5, +5 ],
    line_width = 4,
    color = red,
    parametric(f1_x(s), f1_y(s), s, 0, 1),
    color = green,
    parametric(f2_x(s), f2_y(s), s, 0, 1),
    color = blue,
    parametric(f3_x(s), f3_y(s), s, 0, 1),
    line_width = 2,
    line_type = dashes,
    point_type = none,
    points_joined = true,
    color = red,
    points("points1_x", "points1_y"),
    color = green,
    points("points2_x", "points2_y"),
    color = blue,
    points("points3_x", "points3_y"),
    point_size = 2,
    point_type = filled_circle,
    points_joined = false,
    color = black,
    points("points_evn_x", "points_evn_y"),
    color = gray,
    points("points_odd_x", "points_odd_y")
);
```

(%t25)



(%o25)