https://github.com/t-o-k/Maxima-bezier/bezier\_surface\_with\_control\_grid\_3d.wxmx

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```
(%i1) kill(all)$
(%i2) load("draw")$
       load("bezier")$
(%i3) combine_xyz(xx, yy, zz) := map(lambda([ x, y, z ], [ x, y, z ]), xx, yy, zz)$
(%i4)
       points2a x:
         Γ
            [0.0, 1.0, 2.0, 3.0],
            [0.0, 1.0, 2.0, 4.0],
            [0.0, 1.0, 2.0, 2.5],
            [ 0.0, 1.0, 2.0, 3.0 ]
         ]
       $
(%i5) points2a y:
         [
            [0.0, 0.0, 1.0, 0.0],
            [ 1.0, 1.0, 2.0, 1.0 ],
            [ 2.0, 2.0, 3.0, 2.0 ],
            [ 3.0, 3.0, 5.0, 3.0 ]
         ]
       $
(%i6) points2a z:
         ſ
            [2.0, 0.0, 0.0, -3.0],
            [-2.0, -3.0, -2.0, 3.0],
            [0.0, -4.0, 0.0, 2.0],
            [ 2.0, 0.0, 0.0, -3.0 ]
         ]
       $
(%i9) p x: apply(matrix, points2a x)$
       p y: apply(matrix, points2a y)$
       p_z: apply(matrix, points2a_z)$
```

```
(%i12) define(s x(u, v), bezier function 2a(p x, u, v))$
       define(s y(u, v), bezier function 2a(p y, u, v))$
       define(s z(u, v), bezier function 2a(p z, u, v))$
(\%i13) expand(s x(u, v));
(%o13) 4.5 u^3 v^3 - 7.5 u^3 v^2 + 3.0 u^3 v + 3.0 u
(\%i14) expand(s y(u, v));
(\%014) -3.0 u^3 v^3 + 3.0 u^2 v^3 + 3.0 v - 3.0 u^3 + 3.0 u^2
(\%i15) expand(s z(u, v));
(%o15) 36.0 u^3 v^3 - 54.0 u^2 v^3 + 27.0 u v^3 - 6.0 v^3 - 57.0 u^3 v^2 +
       54.0 u^{2} v^{2} - 36.0 u v^{2} + 18.0 v^{2} + 21.0 u^{3} v + 9.0 u v - 12.0 v - 5.0 u^{3}
        +6.0 u -6.0 u +2.0
(%i16) surface:
          parametric surface(
             s x(u, v)
             s y(u, v),
             s z(u, v)
             u, 0, 1,
             v, 0, 1
          )
       $
(%i18) points2a xyz:
          map(
             combine xyz,
             points2a x,
             points2a y,
             points2a z
          )
       control_grid: apply(mesh, points2a xyz)$
(%i20) points1a_xyz:
          combine xyz(
             flatten(points2a x),
             flatten(points2a y),
             flatten(points2a z)
          )
       control points: points(points1a xyz)$
```

color = red,

**)**;

 $point_size = 1$ , control\_points

```
(%i21) wxdraw3d(
         title = "Bezier surface with control grid",
         proportional axes = xyz,
         xu grid = 20,
         yv_grid = 20,
         view = [6, 331],
         color = black,
         line width = 1,
         wired surface = true,
         surface,
         color = blue,
         line width = 2,
         control_grid,
```

point type = filled circle,

Bezier surface with control grid (%t21)  $0_0^{0.51}^{1.52}^{2.53}^{3.54}$