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Practical 2

Plotting a family of characteristic curves of first order PDE

1
$$(y+u)$$
 $u_x + y$ $u_y = x-y$

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eqn1: diff(x(t),t) = y(t) + u(t); /*Characteristic equations*/
       eqn2: diff(y(t),t) = y(t);
       eqn3: diff(u(t),t) = x(t)-y(t);
       sol: desolve([eqn1,eqn2,eqn3],[x(t),y(t),u(t)]);
       psol1: ev(sol, x(0)=1, y(0)=20, u(0)=30);
       psol2: ev(sol, x(0)=5, y(0)=9, u(0)=8);
       psol3: ev(sol, x(0)=0, y(0)=19, u(0)=80);
       wxdraw3d(grid=true, nticks= 500, xlabel="X",ylabel="Y", zlabel="U",
                   line_width=3,
                   color=blue, key="Curve 1",
                   parametric(rhs(psol1[1]),rhs(psol1[2]),rhs(psol1[3]),t,-1,1),
                   color=red, key="Curve 2",
                   parametric(rhs(psol2[1]),rhs(psol2[2]),rhs(psol2[3]),t,-1,1),
                   color=magenta, key="Curve 3",
                   parametric(rhs(psol3[1]),rhs(psol3[2]),rhs(psol3[3]),t,-1,1)
       /*nticks sets the number of points used in plotting, so it controls
       the smmothness of the curve*/
\frac{d}{dt} x(t) = y(t) + u(t)
(%0107) \frac{d}{dt} y(t) = y(t)
($0108) \frac{d}{dt}u(t) = x(t) - y(t)
(%0109) [x(t) = \frac{(y(0) + x(0) + u(0)) \text{ %e}^t}{2}
        \frac{(y(0)-x(0)+u(0)) e^{-t}}{2}, y(t)=y(0) e^{t}, u(t)=
        \frac{(y(0)-x(0)+u(0)) e^{-t}}{2} - \frac{(y(0)-x(0)-u(0)) e^{t}}{2} 
(%0110) [x(t) = \frac{51 \text{ %e}^{t}}{2} - \frac{49 \text{ %e}^{-t}}{2}, y(t) = 20 \text{ %e}^{t}, u(t) = \frac{11 \text{ %e}^{t}}{2}
       + 49 %e ]
(%0111) [x(t)=11 \text{ %e}^{-t}, y(t)=9 \text{ %e}^{-t}, u(t)=2 \text{ %e}^{-t} + 6 \text{ %e}^{-t}]
(%0112) \mathbf{I} \times (t) = \frac{99 \text{ %e}^{t}}{2} - \frac{99 \text{ %e}^{-t}}{2}, y(t) = 19 \text{ %e}^{t}, u(t) = \frac{61 \text{ %e}^{t}}{2}
                                                     Curve 1
                                                     Curve 2
                                                     Curve 3
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$$2 3 u_x + 4 u_y = u$$

$$3 -x u_x + y u_y = 1$$