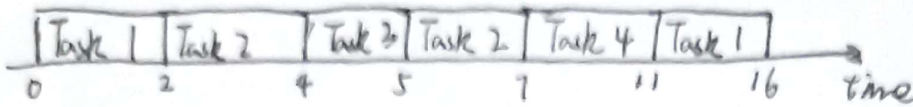


Q1.

(i) $M = LLM(P_i) = LLM(20, 100, 230) = 500$

(ii)



sequence: Task 3, Task 2, Task 4, Task 1.

(iii) Task 3: waiting time: 0

Task 2: waiting time: 2

(iv) Parallel: ~~$R(t) = R^{xt} = e^{0.8t}$~~

overall: $R(t) = 1 - [(1-0.8) \cdot (1-0.8) \cdot (1-0.8)] = 0.992$

Assume there are n devices, each reliability is: $r(t) = 0.8^3$

~~$R(t) = 0.8^3$~~ $R(t) = 1 - (1-r(t))^n \geq R(t)$

$\Rightarrow n \geq 6.73$

So, at least 7 devices

(v)

| Task ID. | response time | waiting time |
|----------|---------------|--------------|
| 1 | 3 | 0 |
| 2 | 5 | 2 |
| 3 | 6 | 3 |
| 4 | 7 | 4 |
| 5 | 8 | 5 |

ave W = ~~$\frac{3+6+9+12+15}{5} = 9$~~ average waiting time = $\frac{0+2+3+4+5}{5} = 2.8$

Q.1

(Vi) 3 tasks, LL bound: $3 \times (2^{\frac{1}{3}} - 1) = 0.7798$

$$\sum_{i=1}^3 u_i = \frac{20}{100} + \frac{20}{150} + \frac{90}{200} = 0.85 > \text{LL bound.}$$

Not schedulable.

(Vii) No, in some algorithm, thread cannot modify context directly.

~~For~~ For kernel, Yes.

(Viii) ① Mutual exclusion ② Hold & wait ③ No preemption.

Bankers : Hold & wait.

there's no ~~chance~~ circular wait.

(ix) P(0) and P(1) may set "flag = True" at the same time,

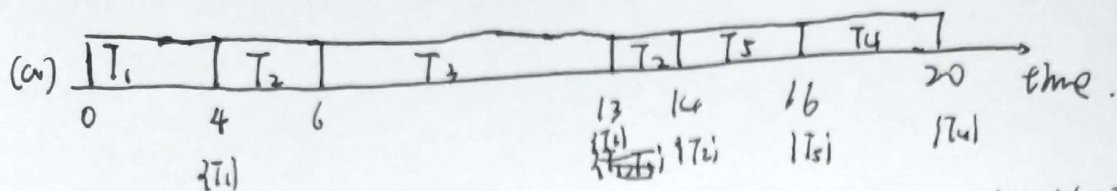
the code will ~~stop~~ at "while(flag[i]);"
block

(x) It's an off-line algorithm

Bratley's algorithm.

Q.2

(i)



$$\text{average waiting time} = \frac{\sum \text{waiting time}}{5} = \frac{0 + 1 + 0 + 5 + 2 + 2}{5} = 2.0$$

$$\text{average waiting time} = \frac{0 + 1 + 0 + 5 + 2}{5} = 2.6s$$

(b)



$$\text{average waiting time} = \frac{0 + 14 + 5 + 8}{5} = 5.4s$$

although we only add e_i from 4 \rightarrow 7, the average waiting time is not increase $\frac{7-4}{5} = 0.6s$ rather than $5.4 - 2.6 = 2.8s$

(ii) EDF.

$$T_i = 2LM(P_i)$$

Q.3

(i) $T_1 = (10, 20)$, $T_2 = (20, 60)$, $T_3 = (30, 180)$

(execution time, period).

$$U = \sum_{i=1}^3 \frac{e_i}{p_i} = \frac{10}{20} + \frac{20}{60} + \frac{30}{180} = 1.$$

(ii) Bound: $\sum_{i=1}^3 u_i = \frac{5}{10} + \frac{12}{60} + \frac{20}{180} = 0.9 < 1 \quad \checkmark$

LLT bound: $3 \times (2^{\frac{1}{3}} - 1) = 0.7798 > \sum_{i=1}^3 u_i \quad \times.$

So RM/D and DMS no feasible.

~~for DMS: we use $pt \leq 1$.~~

(iii) select period of the T_3 .

assign $p_3 = 300$, the DMS is schedulable.

$$\sum_{i=1}^3 u_i = \frac{5}{20} + \frac{12}{60} + \frac{20}{300} = 0.767 < 0.7798.$$

Q. 5

$$(i) \text{Success} = \Pr(5 \text{ success}) + \Pr(4 \text{ success, 1 fail})$$

~~$$= \binom{5}{1} 0.995^1 (1-0.995)^{5-1}$$~~

$$= 0.995^5 + \binom{5}{4} \cdot 0.995^4 (1-0.995)$$

$$= 0.99975$$

$$(ii) \lambda = 0.002$$

$$f(t) = \lambda \cdot e^{-\lambda t}$$

~~$$R(t) = 1 - F(t) =$$~~

$$R(t) = \int_0^\infty f(t) = e^{-\lambda t} = e^{-0.002t} \quad \text{because there are 2 CPUs.}$$

$$R(t) = 1 - (1-R_1(t)) \cdot (1-R_2(t)) = 2e^{-\lambda t} - e^{-2\lambda t}$$

$$\text{where, } t = 200, \lambda = 0.002 \Rightarrow \text{ ~~R(t) = 0.67~~ }$$

$$R(t) = 0.8913.$$

$$(iii) R(t) = \int_0^\infty f(t) = \int_0^\infty 0.2 e^{-0.2t} = e^{-0.2t}$$

$$\lambda(t) = - \frac{dR(t)}{dt} \cdot \frac{1}{R(t)} = 0.2 e^{-0.2t} \cdot \frac{1}{e^{-0.2t}} = 0.2$$