Project03

Isaiah Thompson Ocansey

2022-10-11

(1a) Bring in the training set optdigits.tra, which has sixty-four inputs plus the target variable that indicates the digit. Examine the data briefly. Remove columns that are unary (i.e., containing only one values) or close to being unary (i.e., nearly all values are the same except a few). And check on possible missing values.

```
traindat<- read.table(file=
"https://archive.ics.uci.edu/ml/machine-learning-databases/optdigits/optdigits.tra",
sep=",", header = FALSE, na.strings = c("NA", "", " "),
col.names = c(paste("x", 1:64, sep=""), "digit"))
testdat <- read.table(file=
"https://archive.ics.uci.edu/ml/machine-learning-databases/optdigits/optdigits.tes",
sep=",", header = FALSE, na.strings = c("NA", "", " "),
col.names = c(paste("x", 1:64, sep=""), "digit"))
dim(traindat); dim(testdat)</pre>
```

```
## [1] 3823 65
```

[1] 1797 65

The training data set has 3823 observations and 65 variables whiles the testing data set has 1797 observations and 65 variables.

```
data<-rbind(traindat,testdat)
head(data);dim(data)</pre>
```

```
x21
##
      x1 x2 x3 x4 x5 x6 x7 x8
                                   x9
                                      x10 x11 x12 x13 x14
                                                               x15
                                                                    x16
                                                                         x17 x18
                                                                                   x19
                                                                                        x20
## 1
       0
          1
              6 15 12
                                 0
                                    0
                                         7
                                             16
                                                   6
                                                        6
                                                            10
                                                                  0
                                                                       0
                                                                            0
                                                                                 8
                                                                                    16
                                                                                           2
                                                                                                0
                             0
       0
          0 10 16
                      6
                                 0
                                    0
                                         7
                                             16
                                                   8
                                                       16
                                                             5
                                                                  0
                                                                       0
                                                                            0
                                                                                11
                                                                                    16
                                                                                           0
                                                                                                6
       0
          0
              8 15 16 13
                             0
                                 0
                                    0
                                             11
                                                   9
                                                            16
                                                                       0
                                                                            0
                                                                                 0
                                                                                      0
                                                                                           0
                                                                                                7
                                         1
                                                       11
                                                                  1
                                         0
                                                                  7
                                                                                 3
## 4
       0
           0
              0
                  3
                    11 16
                             0
                                 0
                                    0
                                              5
                                                  16
                                                       11
                                                            13
                                                                       0
                                                                            0
                                                                                    15
                                                                                           8
                                                                                                1
##
   5
       0
           0
              5 14
                      4
                         0
                                 0
                                    0
                                         0
                                             13
                                                   8
                                                        0
                                                             0
                                                                  0
                                                                       0
                                                                            0
                                                                                 3
                                                                                    14
                                                                                           4
                                                                                                0
                             0
           0 11 16
                    10
                         1
                                 0
                                         4
                                             16
                                                  10
                                                       15
                                                             8
                                                                  0
                                                                       0
                                                                            0
                                                                                    16
                                                                                           3
                                                                                               11
                                                       x32
                                   x28 x29
                                             x30
                                                                x34
                                                                     x35
                                                                          x36 x37
                                                                                         x39
##
      x22
          x23 x24
                    x25
                         x26
                              x27
                                                  x31
                                                            x33
                                                                                    x38
                                                                                              x40
## 1
       11
             2
                  0
                       0
                            5
                                16
                                      3
                                           0
                                                5
                                                    7
                                                         0
                                                              0
                                                                   7
                                                                       13
                                                                             3
                                                                                  0
                                                                                       8
                                                                                            7
                                                                                                 0
                           12
                                                                                                 0
## 2
       14
             3
                  0
                       0
                                12
                                      0
                                           0
                                              11
                                                         0
                                                              0
                                                                  12
                                                                       12
                                                                             0
                                                                                  0
                                                                                       8
                                                                                           12
                                                   11
## 3
             0
                  0
                       0
                            0
                                 3
                                         14
                                              12
                                                    2
                                                         0
                                                              0
                                                                       16
                                                                            16
                                                                                 16
                                                                                                 0
       14
                                      4
                                                                   1
                                                                                      16
## 4
       15
             6
                  0
                       0
                           11
                                16
                                    16
                                         16
                                              16
                                                   10
                                                         0
                                                              0
                                                                   1
                                                                        4
                                                                             4
                                                                                 13
                                                                                      10
                                                                                            2
                                                                                                 0
## 5
        0
             0
                  0
                       0
                            6
                                16
                                    14
                                           9
                                                2
                                                    0
                                                         0
                                                              0
                                                                   4
                                                                       16
                                                                             3
                                                                                  4
                                                                                      11
                                                                                                 0
                                                         0
                                                              0
                                                                                 12
                                                                                                 0
##
   6
       13
             0
                  0
                       0
                            1
                                14
                                      6
                                           9
                                              14
                                                    0
                                                                   0
                                                                        0
                                                                             0
                                                                                      10
                                                                                            0
          x42 x43 x44 x45
                              x46 x47 x48 x49 x50 x51 x52 x53 x54 x55 x56 x57 x58 x59
      x41
## 1
        0
             4
                 12
                       0
                               13
                                           0
                                               0
                                                    0
                                                        14
                                                              9
                                                                  15
                                                                        9
                                                                                  0
                            1
                                      5
```

```
## 2
        0
             7
                 15
                       1
                            0
                                13
                                    11
                                           0
                                               0
                                                    0
                                                        16
                                                              8
                                                                  10
                                                                       15
                                                                             3
                                                                                       0
                                                                                            0
                                                                                                10
                           10
## 3
        0
             2
                 12
                      16
                                 0
                                      0
                                           0
                                               0
                                                    0
                                                         2
                                                             16
                                                                   4
                                                                        0
                                                                             0
                                                                                  0
                                                                                       0
                                                                                            0
                                                                                                 9
##
        0
             0
                  0
                       0
                           15
                                 4
                                      0
                                           0
                                                0
                                                    0
                                                         0
                                                              3
                                                                  16
                                                                        0
                                                                             0
                                                                                  0
                                                                                       0
                                                                                            0
                                                                                                 0
             0
                 14
                       3
                            0
                                               0
                                                              8
                                                                   4
                                                                                                 4
## 5
        0
                                 4
                                           0
                                                    0
                                                        10
                                                                            12
                                                                                  0
                                                                                       0
                                                                                            0
                                    11
                                                                       11
##
        0
             0
                  0
                       6
                           16
                                 6
                                      0
                                           0
                                               0
                                                    0
                                                         5
                                                             15
                                                                  15
                                                                        8
                                                                             8
                                                                                  3
                                                                                            0
                                                                                                10
      x60
          x61 x62 x63 x64 digit
##
## 1
             7
                       0
                            0
       14
                  1
                                   0
## 2
                            0
       16
            15
                  3
                       0
                                   0
## 3
       14
             0
                  0
                       0
                            0
                                   7
## 4
                  2
                       0
                            0
                                   4
        1
            15
## 5
       12
            14
                  7
                       0
                            0
                                   6
                                   2
## 6
       16
            16
                 16
                      16
                            6
## [1] 5620
                 65
```

In order to delete unitary variables and check for missing values, we combine both the testing and the training data sets. The combined data set has 5620 observations and 65 variables.

```
#Check Distinct values of the data

for (j in 1:NCOL(data)){
    x <- data[,j]
    print(table(x, useNA="ifany"))
}</pre>
```

```
## x
##
## 5620
## x
                   2
                        3
                                    5
                                                7
                                                      8
##
       0
             1
                               4
                                          6
                                                      4
## 4761
          424
                221
                      112
                             55
                                   23
                                         11
                                                9
##
##
       0
                  2
                        3
                               4
                                    5
                                                7
                                                                 10
                                                                                         14
                                                                                               15
             1
                                          6
                                                      8
                                                            9
                                                                       11
                                                                             12
                                                                                   13
   1266
          358
                381
                      363
                            355
                                  363
                                        368
                                              333
                                                    317
                                                          312
                                                                263
                                                                      206
                                                                            195
                                                                                        110
                                                                                              151
##
     16
##
    105
## x
##
                  2
                        3
                              4
                                    5
                                                      8
                                                            9
                                                                 10
                                                                             12
                                                                                   13
                                                                                         14
                                                                                               15
       0
            1
                                          6
                                                7
                                                                       11
                                                    211
##
          108
                 81
                       72
                             91
                                   82
                                        110
                                              117
                                                          229
                                                                302
                                                                      343
                                                                            637
                                                                                  588
                                                                                        626
                                                                                             706
    162
##
     16
## 1155
## x
       0
                   2
                        3
                                    5
                                          6
                                                7
                                                      8
                                                            9
                                                                 10
                                                                             12
                                                                                         14
##
            1
                               4
                                                                       11
                                                                                   13
                                                                                               15
           97
                                                                                              689
##
    183
                 98
                       94
                            110
                                  108
                                       151
                                             165
                                                    236
                                                          211
                                                                289
                                                                      322
                                                                            555
                                                                                  556
                                                                                        542
##
     16
## 1214
## x
##
       0
             1
                  2
                        3
                               4
                                    5
                                          6
                                                7
                                                      8
                                                            9
                                                                 10
                                                                       11
                                                                             12
                                                                                   13
                                                                                         14
                                                                                               15
                            251
                                  250
                                        220
                                                    217
                                                          154
                                                                189
                                                                            244
                                                                                        156
## 1611
          505
                367
                      282
                                              177
                                                                      145
                                                                                  200
                                                                                              212
##
     16
##
    440
## x
##
       0
             1
                   2
                        3
                               4
                                    5
                                          6
                                                7
                                                      8
                                                                 10
                                                                       11
                                                                             12
                                                                                   13
                                                                                         14
                                                                                               15
```

##	4277	285	178	132	104	90	68	71	59	44	44	48	52	28	44	32
##	16															
##	64 x															
##	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
##	5458	40	28	14	12	13	10	4	12	4	5	4	8	1	3	3
##	16															
##	1															
##	x 0	1	2	5												
	5610	5	4	1												
##	x															
##	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
	3228 16	420	356	307	292	200	177	179	154	79	79	66	36	18	19	9
##	10															
##																
##	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
##	502	131	133	160	150	161	175	177	227	210	228	276	320	368	455	645
##	16 1302															
##																
##	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
##	53	29	63	44	145	172	186	189	370	330		323	440	496	500	598
##	16															
	1358															
##	x 0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
##	217	114	113	111		226		217		277		352	396	368	373	414
##	16															
	1203															
##																
44.44	x	1	0	2	4	F	C	7	0	0	10	11	10	10	1.4	15
## ##	x 0	1 191	2	3 185	4 241	5 176	6 169	7 190	8 288	9 185		11 244	12 336	13 332	14 305	15 393
	x	1 191	2 200	3 185	4 241	5 176	6 169	7 190	8 288	9 185	10 213	11 244	12 336	13 332	14 305	15 393
## ##	x 0 1111															
## ## ## ##	x 0 1111 16 861 x	191	200	185	241	176	169	190	288	185	213	244	336	332	305	393
## ## ## ##	x 0 1111 16 861 x	191	200	185	241	176 5	169	190	288	185	213	244	336	332	305	393 15
## ## ## ## ##	x 0 1111 16 861 x 0 3652	191	200	185	241	176 5	169	190	288	185	213	244	336	332	305	393
## ## ## ##	x 0 1111 16 861 x 0 3652 16	191	200	185	241	176 5	169	190	288	185	213	244	336	332	305	393 15
## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98	191	200	3 210	241 4 204	176 5	169	190	288	185	213	244	336	332	305	393 15
## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x	191 1 290	200 2 295	3 210 3	241 4 204	176 5 134	6 98	7 109 7	288 8 124	9 72	213 10 50	11 62 11	336 12 56	13 57	305 14 56	393 15
## ## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x 0 5429	191 1 290	200 2 295	3 210	241 4 204	176 5 134	6 98	7 109	288 8 124	9 72	213 10 50	244 11 62	336 12 56	13 57	305 14 56	393 15
## ## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x 0 5429	191 1 290	200 2 295	3 210 3 26	241 4 204 4 11	176 5 134	6 98	7 109 7	288 8 124	9 72	213 10 50	11 62 11	336 12 56	13 57	305 14 56	393 15
## ## ## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x 0 5429 x	191 1 290 1 50	2 2 295 2 34	3 210 3	241 4 204	176 5 134	6 98	7 109 7	288 8 124	9 72	213 10 50	11 62 11	336 12 56	13 57	305 14 56	393 15
## ## ## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x 0 5429 x 0 5607 x	191 1 290 1 50 1 7	2 2 2 3 4 2 3 3	3 210 3 26 3 2	241 4 204 4 11 5 1	176 5 134 5 15	6 98 6 12	7 109 7 13	288 8 124 8 8	9 72 9 8	10 50 10 3	11 62 11 6	336 12 56 12 2	13 57 13 2	305 14 56 15 1	393 15 53
## ## ## ## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x 0 5429 x 0 5607 x 0	191 1 290 1 50 1 7	200 2 295 2 34 2 3	3 210 3 26 3 2	241 4 204 4 11 5 1	176 5 134 5 15	6 98 6 12	7 109 7 13	288 8 124 8 8	9 72 9 8	10 50 10 3	11 62 11 6	336 12 56 12 2	13 57 13 2	305 14 56 15 1	393 15 53
## ## ## ## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x 0 5429 x 0 5607 x 0 2745	191 1 290 1 50 1 7	2 2 2 3 4 2 3 3	3 210 3 26 3 2	241 4 204 4 11 5 1	176 5 134 5 15	6 98 6 12	7 109 7 13	288 8 124 8 8	9 72 9 8	10 50 10 3	244 11 62 11 6	336 12 56 12 2	13 57 13 2	305 14 56 15 1	393 15 53
## ## ## ## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x 0 5429 x 0 5607 x 0 2745 16	191 1 290 1 50 1 7	200 2 295 2 34 2 3	3 210 3 26 3 2	241 4 204 4 11 5 1	176 5 134 5 15	6 98 6 12	7 109 7 13	288 8 124 8 8	9 72 9 8	10 50 10 3	11 62 11 6	336 12 56 12 2	13 57 13 2	305 14 56 15 1	393 15 53
## ## ## ## ## ## ## ## ## ##	x 0 11111 16 861 x 0 3652 16 98 x 0 5429 x 0 5607 x 0 2745 16 16	191 1 290 1 50 1 7	200 2 295 2 34 2 3	3 210 3 26 3 2	241 4 204 4 11 5 1	176 5 134 5 15	6 98 6 12	7 109 7 13	288 8 124 8 8	9 72 9 8	10 50 10 3	11 62 11 6	336 12 56 12 2	13 57 13 2	305 14 56 15 1	393 15 53

## ## ## :	792 16 1175 ×	163	162	161	137	157	152	171	200	199	236	264	354	351	445	501
## ## ## ##	0 1225 16 738	1 422	2 304	3 268	4 282	5 257	6 229	7 204	8 244	9 214		11 189	12 196	13 199		15 239
## ##	0 1367 16 926	1 343	2 259	3 235	4 239	5 224	6 194	7 165	8 218	9 150		11 176	12 235	13 220	14 243	15 216
## ##	0 1504 16 847	1 136	2 177	3 114	4 169	5 123	6 158	7 148	8 223	9 191	10 200	11 222	12 313	13 296		15 403
## ##	0 3518 16 49	1 305	2 305	3 241	4 325	5 140	6 176	7 107	8 125	9 54	10 63	11 60	12 57	13 20	14 36	15 39
## :	0 5520	1 32 1	2 21	3 15	4 15	5 8	6 6	7 1	8 2							
## ! ## :	5614 x 0	6	2	3	4	5	6	7	8	9	10	11	12	13	14	15
	2787 16 1	419	333			329		229	251	99	70	49	35	7	5	5
## ## ## ##	0 984 16 1259	1 195	2 182	3 171	4 165	5 161	6 139	7 169	8 200	9 171	10 149	11 215	12 332	13 280	14 378	15 470
## ## ## :	0 819 16 1251				4 237											
## : ## ## :	0 1044 16 1580				4 154											
## : ##	0		2 221		4 214											

```
1
          2 3
                  4 5 6 7 8
                                          10
                                                 12
                                                         14
                                                             15
                                     9
                                             11
                                                     13
## 3359 296 228 188 209 194 226 173 320
                                      92
                                          87
                                              59
                                                 59
                                                     52
                                                         41
                                                             34
## 16
##
## x
## 0
       1
## 5606
       12
## x
## 0
        1
## 5615
## x
                      5 6 7 8
## 0 1
          2
               3
                  4
                                     9
                                         10
                                             11
                                                 12
                                                     13
                                                         14
                                                            15
## 3326 311 252 263 249 260 161 194 265
                                              74
                                      84
                                          76
                                                 52
                                                     28
                                                         23
## 0 1
          2
              3
                  4
                      5 6
                             7
                                 8
                                     9
                                         10
                                             11
                                                 12
                                                     13
                                                         14
## 1422 265 216 170 163 160 140 199 275 172 158 177 328 227 226 310
## 16
## 1012
## x
       1
           2
               3
                   4
                       5
                           6
                              7
                                  8
                                     9
                                         10
                                             11
                                                12
                                                     13
                                                         14
                                                            15
## 1061 129 163 139 212 158 147 148 278 163 189 208 275 217 303 321
## 16
## 1509
## x
      1
          2
              3
                  4
                      5
                         6
                             7
                                 8
                                     9
                                         10
                                             11
                                                12
                                                    13
                                                        14
                                                            15
## 822 120 101 91 146 120 122 141 229 182 210 196 323 314 359 441
  16
## 1703
## x
          2 3 4 5 6 7 8 9 10 11
## 0
      1
                                                12
                                                    13
                                                        14
## 924 167 154 148 208 159 181 198 271 215 248 216 363 307 378 459
## 16
## 1024
## x
## 0
               3
                   4
                       5
                          6
                             7
                                  8
                                     9
                                         10
                                                         14
      1
           2
                                             11
                                                 12
                                                     13
## 2632 341 312 269 307 287 256 254 522 174 147
                                              53
                                                     13
## x
## 0
## 5620
## x
## 0
            2
                3
                   4
                       5
                           6
                               7
       1
## 5572
               7
                   6
                       3
       16
           13
## x
           2
               3
                       5
                               7
                                          10
      1
                   4
                           6
                                   8
                                      9
                                              11
                                                 12
                                                     13
                                                         14
                                                             15
## 3798 370 293 234 255 169
                          99
                              87
                                  88
                                          30
                                              31
                                                 32
                                                     24
                                                         19
                                                             31
                                      34
## 16
## 26
## x
       1
                             7
               3
                  4
                      5
                          6
                                 8
                                     9
                                         10
                                             11
                                                12
                                                    13
## 2087 232 164 163 167 115 118 105 146 119 146 151 244 247 253 334
## 16
## 829
## x
```

## ## ## ##	0 1783 16 958	1 256	2 138	3 138	4 179	5 136	6 126	7 140	8 196	9 185	10 167	11 173	12 220	13 240	14 281	15 304
## ## ##	0 1322 16 1060	1 298	2 204	3 185	4 213	5 161	6 156	7 150	8 214	9 197	10 190	11 183	12 251	13 248	14 247	15 341
##	0 1012 16 749	1 177	2 168	3 135	4 222	5 180	6 166	7 209	8 280	9 268	10 257	11 298	12 354	13 368	14 371	15 406
##	0 2626 16 34	1 336	2 237	3 256	4 242	5 245	6 204	7 251	8 332	9 192	10 116	11 168	12 175	13 88	14 71	15 47
##	0 5550	1 44	2 14	3 2	4 6	5 1	6 3									
## ## ##	0 5584 x	1 22	2 4	3 4	4 1	5 2	7	8	10 1							
## ## ## ##	0 4273 16 5	1 422	2 276	3 204	4 142	5 88	6 48	7 53	8 41	9 23	10 13	11 9	12 8	13 8	14	15 6
## ## ## ##	0 1100 16 557	1 212	2 197	3 193	4 242	5 218	6 221	7 233	8 313	9 253	10 251	11 338	12 336	13 294	14 332	15 330
## ##	0 339 16 1173	1 154	2 176	3 139	4 330	5 262	6 242	7 237	8 354	9 301	10 310	11 305	12 332	13 314	14 339	15 313
## ##	0 366 16 1161					5 286										15 387
## ##	0 1057 16 969					5 132										
## ## ## ##	0 2723					5 199							12 160	13 87		15 139

```
## 161
## x
                                                                      13
##
      0
            1
                 2
                      3
                            4
                                 5
                                       6
                                            7
                                                  8
                                                       9
                                                            10
                                                                 12
## 5300
          94
                78
                     54
                           29
                                32
                                      12
                                            7
                                                  7
                                                       2
                                                            3
                                                                  1
                                                                       1
## x
##
      0
            1
## 5618
## x
##
      0
            1
                 2
                      3
                            4
                                 5
                                       6
                                            7
                                                  8
                                                       9
                                                            10
## 4922
               193
                    101
                           58
                                33
                                      12
                                                  3
                                                             2
         283
## x
                 2
                                 5
                                            7
##
      0
            1
                      3
                            4
                                       6
                                                  8
                                                       9
                                                           10
                                                                      12
                                                                           13
                                                                                 14
                                                                                       15
                                                                 11
                                                               245
              373
                    325
                         324
                               339
                                    314 308
                                               294
                                                          264
                                                                     204
                                                                                     198
## 1288
         339
                                                    254
                                                                          216
                                                                                138
##
     16
##
    197
## x
##
      0
                 2
                      3
                            4
                                 5
                                       6
                                            7
                                                  8
                                                       9
                                                           10
                                                                            13
                                                                                 14
                                                                                       15
            1
                                                                 11
                                                                      12
##
    225
           55
                68
                     83
                           79
                                79 116 122 175 217
                                                          245
                                                               361
                                                                     561
                                                                          578
                                                                                     683
##
     16
## 1397
## x
##
      0
            1
                 2
                      3
                            4
                                 5
                                       6
                                            7
                                                  8
                                                       9
                                                           10
                                                                 11
                                                                      12
                                                                            13
                                                                                       15
                                      85 114 160 181
##
    394
          94
              107
                     79
                           90 104
                                                          213
                                                               266
                                                                    575
                                                                           494
                                                                                494
                                                                                     619
##
     16
## 1551
##
      0
                 2
                      3
                            4
                                 5
                                       6
                                            7
                                                  8
                                                       9
                                                           10
                                                                 11
                                                                      12
                                                                            13
                                                                                 14
                                                                                       15
            1
## 1494
         273 215 253 202
                               215 218 207
                                               273 245
                                                          238
                                                                207
                                                                     316
                                                                           230
                                                                                217
                                                                                      269
##
     16
## 548
## x
##
            1
                 2
                      3
                            4
                                 5
                                       6
                                            7
                                                  8
                                                       9
                                                           10
                                                                 11
                                                                      12
                                                                            13
                                                                                 14
                                                                                       15
         394 204 166 144 120 112
                                                      78
                                                            63
                                                                 71
                                                                      75
                                                                            63
## 3714
                                         118
                                                 88
                                                                                 30
                                                                                       44
##
     16
##
    136
## x
##
      0
           1
                 2
                      3
                            4
                                 5
                                       6
                                            7
                                                  8
                                                       9
                                                            10
                                                                 11
                                                                      12
                                                                            13
                                                                                 14
                                                                                       15
## 5303
          96
                44
                     40
                           15
                                27
                                      21
                                           12
                                                 11
                                                       8
                                                            3
                                                                 10
                                                                       7
                                                                             6
                                                                                  4
                                                                                        7
##
     16
##
      6
## x
              2 3 4
                           5
                               6
                                   7
         1
## 554 571 557 572 568 558 558 566 554 562
missing_percent <- function(df, filename=NULL){</pre>
vnames <- colnames(df); vnames</pre>
n <- nrow(df)
out <- NULL
for (j in 1: ncol(df)){
vname <- colnames(df)[j]</pre>
x <- as.vector(df[,j])</pre>
n1 \leftarrow sum(is.na(x), na.rm=T)
n2 <- sum(x=="NA", na.rm=T)</pre>
n3 <- sum(x=="", na.rm=T)
```

```
nmiss <- n1 + n2 + n3
ncomplete <- n-nmiss
out <- rbind(out, c(col.number=j, vname=vname,
mode=mode(x), n.levels=length(unique(x)),
ncomplete=ncomplete, miss.perc=nmiss/n))
}
out <- as.data.frame(out)
row.names(out) <- NULL
if (!is.null(filename)) write.csv(out, file = filename, row.names=F)
return(out)
}
missing_percent(data)</pre>
```

##		col.number	vname	mode	n.levels	ncomplete	miss.perc
##	1	1	x1	${\tt numeric}$	1	5620	0
##	2	2	x2	numeric	9	5620	0
##	3	3	x3	numeric	17	5620	0
##	4	4	x4	numeric	17	5620	0
##	5	5	x5	${\tt numeric}$	17	5620	0
##	6	6	х6	numeric	17	5620	0
##	7	7	x7	${\tt numeric}$	17	5620	0
##	8	8	x8	numeric	17	5620	0
##	9	9	x9	${\tt numeric}$	4	5620	0
##	10	10	x10	${\tt numeric}$	17	5620	0
##	11	11	x11	${\tt numeric}$	17	5620	0
##	12	12	x12	${\tt numeric}$	17	5620	0
##	13	13	x13	${\tt numeric}$	17	5620	0
##	14	14	x14	${\tt numeric}$	17	5620	0
##	15	15	x15	${\tt numeric}$	17	5620	0
##	16	16	x16	${\tt numeric}$	15	5620	0
##	17	17	x17	${\tt numeric}$	5	5620	0
##	18	18	x18	${\tt numeric}$	17	5620	0
##	19	19	x19	${\tt numeric}$	17	5620	0
##	20	20	x20	${\tt numeric}$	17	5620	0
##	21	21	x21	${\tt numeric}$	17	5620	0
##	22	22	x22	${\tt numeric}$	17	5620	0
##	23	23	x23	${\tt numeric}$	17	5620	0
##	24	24	x24	${\tt numeric}$	9	5620	0
##	25	25		numeric	2	5620	0
##	26	26	x26	${\tt numeric}$	17	5620	0
##	27	27	x27	${\tt numeric}$	17	5620	0
##	28	28	x28	numeric	17	5620	0
##	29	29	x29	${\tt numeric}$	17	5620	0
##	30	30	x30	${\tt numeric}$	17	5620	0
##	31	31	x31	numeric	17	5620	0
##	32	32	x32	numeric	3	5620	0
##	33	33	x33	${\tt numeric}$	2	5620	0
##	34	34	x34	numeric	16	5620	0
##	35	35		${\tt numeric}$	17	5620	0
##	36	36	x36	${\tt numeric}$	17	5620	0
##	37	37	x37	${\tt numeric}$	17	5620	0
##	38	38	x38	${\tt numeric}$	17	5620	0

```
## 39
                39
                      x39 numeric
                                           15
                                                    5620
                                                                   0
##
   40
                40
                      x40 numeric
                                            1
                                                    5620
                                                                   0
##
   41
                41
                      x41 numeric
                                            8
                                                    5620
                                                                   0
                42
                                                                   0
##
   42
                      x42 numeric
                                           17
                                                    5620
##
   43
                43
                      x43 numeric
                                           17
                                                    5620
                                                                   0
                                                                   0
   44
##
                44
                      x44 numeric
                                           17
                                                    5620
## 45
                45
                      x45 numeric
                                           17
                                                    5620
                                                                   0
## 46
                46
                      x46 numeric
                                           17
                                                    5620
                                                                   0
## 47
                47
                      x47 numeric
                                           17
                                                                   0
                                                    5620
##
   48
                48
                      x48 numeric
                                            7
                                                    5620
                                                                   0
##
   49
                49
                      x49 numeric
                                            9
                                                    5620
                                                                   0
                                                                   0
##
   50
                50
                      x50 numeric
                                           17
                                                    5620
                                           17
## 51
                51
                                                                   0
                      x51 numeric
                                                    5620
## 52
                52
                      x52 numeric
                                           17
                                                    5620
                                                                   0
                                                                   0
## 53
                53
                      x53 numeric
                                           17
                                                    5620
## 54
                54
                                           17
                                                                   0
                      x54 numeric
                                                    5620
                                                                   0
## 55
                55
                                           17
                      x55 numeric
                                                    5620
   56
                56
                                                                   0
##
                      x56 numeric
                                           13
                                                    5620
                                                                   0
##
   57
                57
                                            2
                      x57 numeric
                                                    5620
##
   58
                58
                      x58 numeric
                                           11
                                                    5620
                                                                   0
##
   59
                59
                      x59 numeric
                                           17
                                                    5620
                                                                   0
                                                                   0
## 60
                60
                      x60 numeric
                                           17
                                                    5620
## 61
                61
                                           17
                                                                   0
                      x61 numeric
                                                    5620
## 62
                62
                      x62 numeric
                                           17
                                                    5620
                                                                   0
## 63
                63
                      x63 numeric
                                           17
                                                    5620
                                                                   0
## 64
                64
                      x64 numeric
                                           17
                                                    5620
                                                                   0
## 65
                                           10
                                                                   0
                65 digit numeric
                                                    5620
```

From the above output, it can be observed that we have no missing values in the data set

```
# removing target variable
df1 <- data.matrix(traindat[,-c(33,65)]) # Train
df2 <- data.matrix(testdat[,-c(33,65)]) # Test

# Remove the Unary variables
new_traindat <- df1[,apply(df1, 2, var, na.rm=TRUE) != 0] # Train
new_testdat <- df2[,apply(df2, 2, var, na.rm=TRUE) != 0] # Test
dim(new_traindat);dim(new_testdat)

## [1] 3823 61</pre>
```

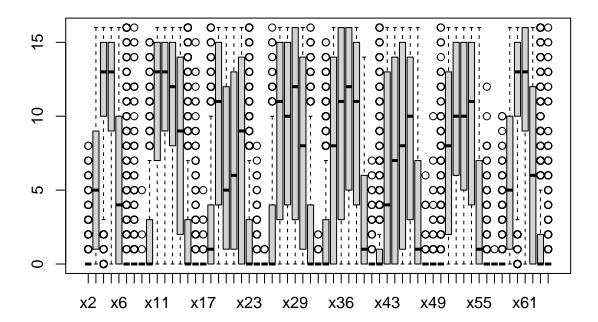
I have removed all the columns with unitary values from both the testing and training data sets. After removing the columns with unitary values, we have 3823 observations 61 variables for the training set. Likewise, We have 1797 observations and 61 variables for the testing set.

(1b) Excluding the target variables, run the ordinary principal components analysis (PCA) with the training set. Output the scree plot of the variances (i.e., eigenvalues) of the principal components. Make a scatter plot of the first two PCs and show the target class variable (i.e., digit number) with different symbols and colors. Recall that this also corresponds to a multidimensional scaling (MDS) analysis of data. Interpret results. • Be careful with the normalization or standardization of the data before performing PCA. Make parallel boxplots of the attributes and inspect for necessity of data normalization.

BOXPLOTS OF TRAINING AND TESTING DATA SETS

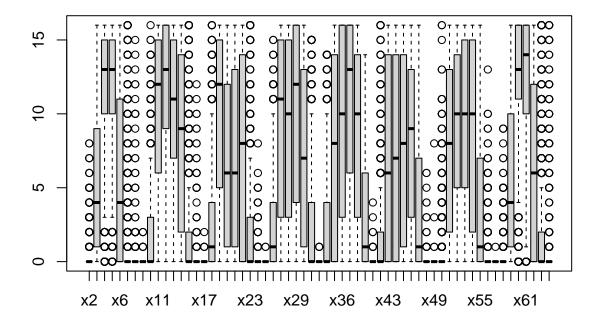
[1] 1797

Boxplot of Training data



boxplot(new_testdat, main="Boxplot of Testing data")

Boxplot of Testing data

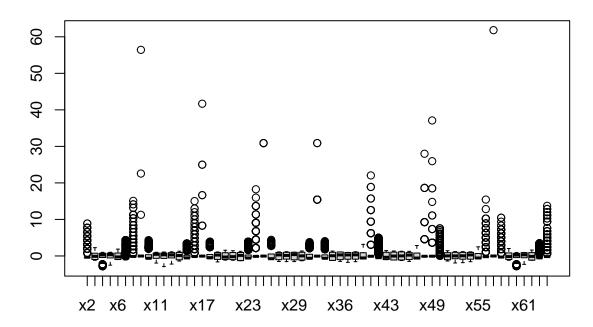


 ${\it Clearly}, from the above box plots, it is necessary that we standardize the data before the principal component analysis$

STANDARDIZE THE TRAINING AND TESTING DATA

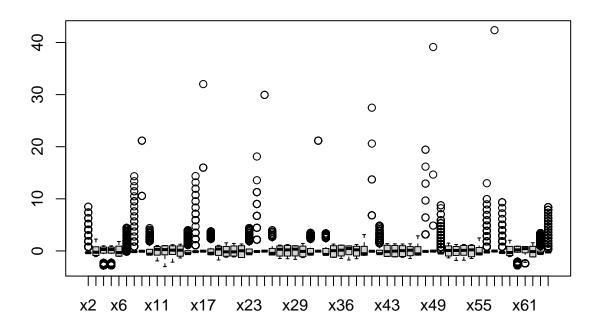
```
scaled_new_traindat <- data.frame(apply(new_traindat, 2, scale, center=T, scale=T))
boxplot(scaled_new_traindat, main="Boxplot of standardized Training data")</pre>
```

Boxplot of standardized Training data



```
scaled_new_testdat <- data.frame(apply(new_testdat, 2, scale, center=T, scale=T))
boxplot(scaled_new_testdat, main="Boxplot of standardized Testing data")</pre>
```

Boxplot of standardized Testing data



From the boxplots above, we can observe that the standardized data sets seem normal for the principal component analysis

ORDINARY PRINCIPAL COMPONENT ANALYSUS ON THE TRAINING DATA SET

```
pca.train <- prcomp(scaled_new_traindat, scale=FALSE, retx=TRUE,center=FALSE);</pre>
```

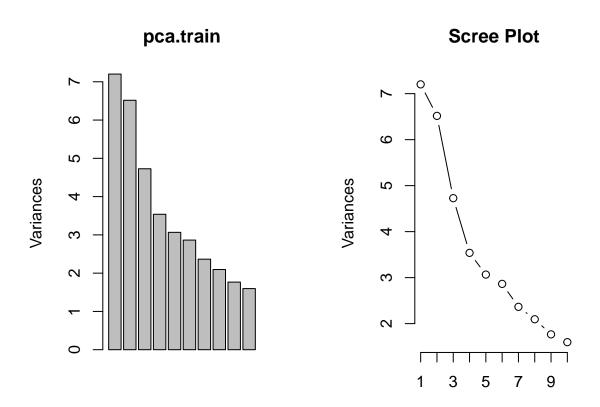
OBTAINING EIGENVALUES

```
eigen(cov(scaled_new_traindat), only.values = T)$values
```

```
## [1] 7.20179133 6.51696036 4.72764717 3.53828965 3.06630997 2.86412950
## [7] 2.36531710 2.09493689 1.76627760 1.59705595 1.49407201 1.48721245
## [13] 1.37760221 1.29374146 1.17282747 1.14859807 1.12561870 1.02565153
## [19] 0.99925276 0.91357286 0.87165403 0.85442179 0.70748871 0.68849032
## [25] 0.64403360 0.61343679 0.57631445 0.56141407 0.53047561 0.49360755
## [31] 0.45218590 0.43610867 0.40015798 0.38867786 0.37555770 0.36762791
## [37] 0.32845474 0.29940488 0.27970539 0.27017947 0.26224683 0.24059564
## [43] 0.21433266 0.20658560 0.19220898 0.19048782 0.17229587 0.16675202
## [49] 0.15946094 0.15080540 0.14628710 0.13536792 0.12890361 0.11961022
## [55] 0.11202967 0.10121850 0.09530269 0.08829583 0.07680299 0.06610966
## [61] 0.05803759
```

PLOTING THE VARIANCES USING SCREE AND BAR CHART

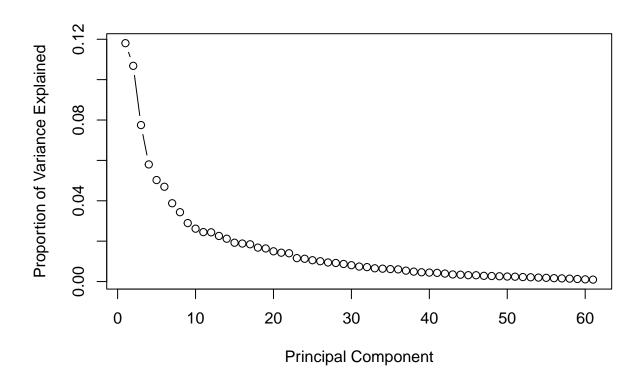
```
par(mfrow=c(1,2), mar=rep(4,4))
plot(pca.train)
screeplot(pca.train, type="lines", main="Scree Plot")
```

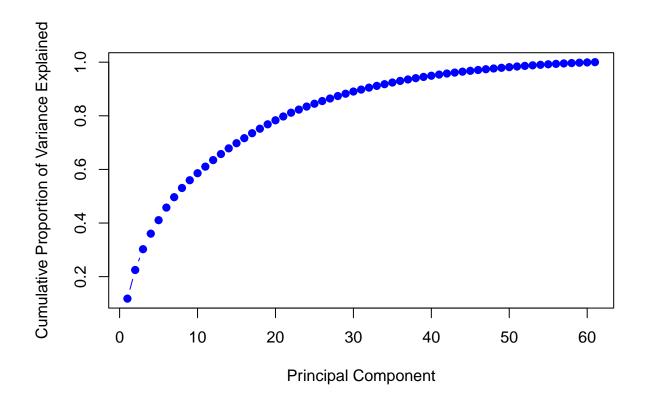


From the above bar charts and scree plot, we can observe that the first two principal components explains the most variations in the training data set

CUMULATIVE PROPORTIONS OF VARIATION EXPLAINED

```
sd.pc <- pca.train$sdev
var.pc <- sd.pc^2
prop.pc <- var.pc/sum(var.pc)
# NONCUMULATIVE
plot(prop.pc, xlab = "Principal Component",
    ylab = "Proportion of Variance Explained", type = "b")</pre>
```

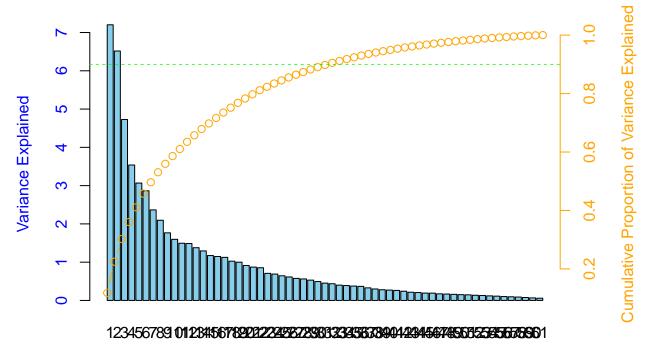




We further illustrate the principal components using the cumulative proportion of the variances explained. We can also observe here that the first two principal components explained the most variations.

THE PARETO PLOT

Pareto Chart from PCA



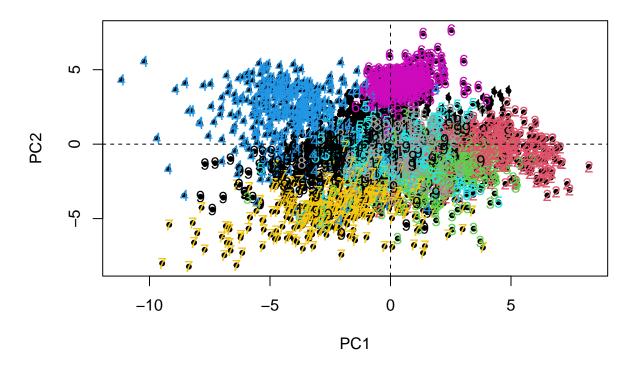
Princippal Components

From the pareto chart, it can be observed that the first two principal components explains over 90% of the total variations in the dataset

PLOT OF THE FIRST TWO PCs

```
plot(pca.train$x[,1:2], pch=20, main="Ordinary PCA")
text(pca.train$x[,1:2],labels=traindat$digit, col=traindat$digit)
abline(v=0, lty=2)
abline(h=0, lty=2)
```

Ordinary PCA



We plot PC1 against PC2 with a scatter plot. From the plot above, digits closer to one another are more similar than those further away. Also, from the plot we can observe that though the two components hold some information it is unable to set the digits apart very well

(1c) Run kernel PCA on the input variables only. Explain your choice of kernel function and the choice of parameters involved. Output the scree plot of the variances (i.e., eigenvalues) of the resultant principal components. Plot the first two PCs with scatted points and show the target class variable with different symbols and colors. Compare the kPCA results with the PCA results and comment with interpretations.

KERNEL PRINCIPAL COMPONENT ANALYSIS USING GAUSSIAN RADIAL BASIS KERNEL FUNCTION

From the above, we perform the kernel principal component analysis using the Gaussian radial basis kernel family (rbfdot) with a chosen sigma of 0.2 and 35 principal components.

OBTAINING THE EIGENVALUES OF THE KERNEL PRINCIPAL COMPONENTS

eig	(kpc)	# returns	the eigenval	ues		
	a	a 0	a 0	G 4	a	
##	Comp.1	Comp.2	Comp.3	Comp.4	Comp.5	Comp.6
##	0.045765453	0.041596708	0.035691196	0.029532836	0.025804486	0.022385444
##	Comp.7	Comp.8	Comp.9	Comp. 10	Comp.11	Comp.12

```
## 0.020061733 0.014998013 0.014650549 0.012660528 0.012487758 0.011212081
##
                   Comp.14
                               Comp.15
                                            Comp.16
                                                        Comp.17
                                                                    Comp.18
       Comp.13
## 0.010560911 0.009314247 0.008510327 0.008035757 0.007693795 0.007335730
                               Comp.21
                                           Comp.22
       Comp.19
                   Comp.20
                                                        Comp.23
## 0.006301117 0.006250427 0.005773536 0.005396386 0.005290807 0.005062650
       Comp.25
                   Comp.26
                                            Comp.28
                                                        Comp.29
                                                                    Comp.30
                               Comp.27
## 0.004917508 0.004713774 0.004617841 0.004528420 0.004277059 0.004047205
       Comp.31
                   Comp.32
                               Comp.33
                                            Comp.34
                                                        Comp.35
## 0.004002562 0.003851532 0.003702313 0.003540216 0.003430265
```

kernelf(kpc) # returns the kernel used when kpca was performed

```
## Gaussian Radial Basis kernel function.
## Hyperparameter : sigma = 0.02
```

OBTATINING THE PRINCIPAL COMPNENT VECTORS

```
PCV <- pcv(kpc)
dim(PCV); head(PCV)</pre>
```

[1] 3823 35

```
[,2]
                                  [,3]
                                             [,4]
                                                       [,5]
            [,1]
                                                                 [,6]
## [1,] -0.15377681 -0.0210302110 0.07401273 -0.002588424 -0.15766563 -0.06129563
## [3,] 0.09570385 0.0153768249 0.13563393 0.010412746 -0.14249052 0.22167158
      ## [4,]
0.02278909 -0.0001427619 -0.03030259 0.144154511 -0.00250532 -0.11269760
## [6,]
##
            [,7]
                      [,8]
                                  [,9]
                                           [,10]
                                                      [,11]
                                                                [,12]
## [1,] -0.07582866 0.10589364 0.0002964134 -0.07128271 0.001667696 -0.1708688
## [2,] 0.03478120 0.05823238 -0.0263797391 0.09782841 0.033592349 -0.2142274
## [3,] 0.23155259 0.03140502 0.1328871845 -0.12546343 0.066143078 -0.3460351
## [4,] -0.14807000 -0.18057407 -0.1187910864 -0.02040819 0.062778032 0.0461844
## [5,] -0.09496439 -0.01077657 0.0230569225 0.03263365 0.115701197 -0.1918324
## [6,] -0.01238641 -0.21437392 -0.0454048480 -0.01066358 -0.007374907 0.1059449
            [,13]
                      [,14]
                                [,15]
                                          [,16]
                                                     [,17]
                                                               [,18]
## [1,] 0.09082621 0.02207833 0.01234199 0.14667457 0.128935031 -0.19379824
      0.17007562 0.06449209 0.30520245 0.19311296 -0.183456267 -0.17530776
## [2,]
## [3,]
      0.08367048 0.06119612 -0.26104564 -0.04627755 0.006140849 0.27486238
## [4,] -0.06084380 -0.12573223 0.17972315 -0.13885907 0.403044453 0.05070018
## [5,] -0.07260800 -0.43175143 0.11189319 0.08399271 -0.009879835 -0.06207247
## [6,]
       0.11808361 0.14382334 -0.15352559 0.44308355 -0.221770091 0.64966223
##
            [,19]
                      [,20]
                                [,21]
                                          [,22]
                                                    [,23]
## [1,] 0.16370786 -0.13281356 0.24009823 -0.37443240 0.11522068 0.28082652
## [2,] -0.02368080 -0.02139025 0.11852891 -0.45571934 0.02396476 0.03683011
## [3,] 0.04094780 0.30592344 0.10573454 0.06947842 0.01431223 -0.06425728
## [5,] 0.03093163 0.20294461 -0.06114783 -0.16355212 0.09237306 0.20416548
## [6,] -0.17000552 -0.26042520 0.34180757 -0.05323068 0.12007913 0.13355167
##
           [,25]
                    [,26]
                              [,27]
                                        [,28]
                                                  [,29]
## [1,] -0.0572758 -0.0692656 0.11813644 0.03638899 -0.16273140 0.11561867
```

```
## [2,] 0.1831370 0.3332759 0.33173143 0.12858770 -0.25328998 0.30744913
## [3,] 0.3795642 -0.4165232 0.40063120 -0.23358437 0.03781283 -0.01387292
## [4,] 0.2970328 0.3275094 -0.17815082 -0.25907118 0.27001007 0.08246498
## [5,] -0.4043934   0.1241914   0.07161319   0.10302336   0.33313514 -0.24960766
## [6,] -0.5174760 -0.2252214 0.25539888 -0.51350174 0.38686158 -0.12769768
##
            [,31]
                       [,32]
                                  [,33]
                                             [,34]
## [1.] -0.00859139 -0.48203301 -0.03962543 0.14485765 0.09159488
## [2,] 0.27877066 0.13679216 -0.13740537 -0.08143077 -0.69873768
## [3.]
       0.28950673 -0.20637243 -0.04433273 0.06595394 0.13778203
       ## [4,]
## [5,] 0.01518385 -0.08581967 0.24618294 -0.07237327 0.39618133
## [6,] 0.05140023 -0.43602192 -0.63593244 -0.50801579 0.25609868
```

THE DATA PROJECTED IN THE KERNEL PCA SPACE

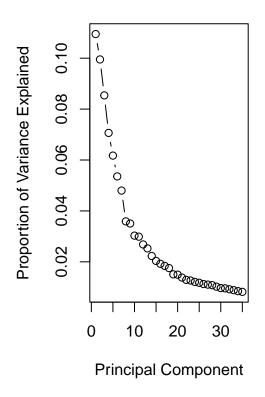
```
PC <- rotated(kpc)
dim(PC); head(PC);</pre>
```

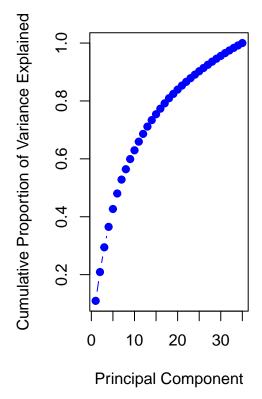
[1] 3823 35

```
[,2]
                            [,3]
                                      [,4]
                                                [,5]
                                                          [,6]
         [,1]
## 1 -26.90499 -3.3443128 10.098847 -0.2922435 -15.5538019 -5.245653 -5.8157552
                       9.341186 9.8525386 -11.0674494 -11.223554
## 2 -23.29866 0.5952701
                                                               2.6675788
## 3 16.74447 2.4452875 18.506903 1.1756410 -14.0567688 18.970554 17.7591582
     3.95525 11.9705593 16.575406 -3.6164142 11.6348153 -8.892275 -11.3563770
3.98721 \ -0.0227026 \ -4.134712 \ 16.2756258 \ -0.2471512 \ -9.644610 \ -0.9499885
## 6
##
                              [,10]
                                        [,11]
          [,8]
                     [,9]
                                                  [,12]
                                                           [,13]
      6.0716663 0.01660183 -3.4501684 0.07961698 -7.324084 3.667050
      3.3388933 -1.47750412 4.7350125 1.60372216 -9.182597 6.866695
     1.8006825 7.44288492 -6.0725805 3.15771670 -14.832373 3.378142
## 4 -10.3536480 -6.65337586 -0.9877809 2.99706702 1.979638 -2.456530
## 5 -0.6179005 1.29139632 1.5795079 5.52365583 -8.222661 -2.931502
## 6 -12.2916437 -2.54308239 -0.5161301 -0.35208323
                                              4.541198 4.767550
         [,14]
                   [,15]
                            [,16]
                                      [,17]
                                              [,18]
                                                        [,19]
## 1
      2.2964580 9.9297556 5.932565 -5.3960685 -4.916418 -0.5704509 -0.5111282
      2.1790937 -8.4931146 -1.421679 0.1806231 7.708377 0.9863984 7.3101574
## 4 -4.4771191 5.8472891 -4.265848 11.8548987 1.421861 -3.7893303 2.9381630
## 5 -15.3739630 3.6404428 2.580315 -0.2905993 -1.740791 0.7451173 4.8494390
      5.1213140 -4.9949519 13.611837 -6.5230075 18.219450 -4.0952920 -6.2229596
                [,22]
                                                      [,26]
        [,21]
                          [,23]
                                    [,24]
                                             [,25]
## 1 5.299502 -7.724683 2.3305407 5.4352595 -1.076764 -1.248219
                                                           2.085582
## 3 2.333797 1.433366 0.2894901 -1.2436681 7.135668 -7.506064 7.072746
## 4 -1.059412 -3.363459 -8.7663978 -2.2265218 5.584107 5.901969 -3.145076
## 5 -1.349669 -3.374143 1.8684073 3.9515226 -7.602448 2.238024 1.264260
## 6 7.544454 -1.098169 2.4288113 2.5848271 -9.728360 -4.058662 4.508814
                                                       [,33]
##
                 [,29]
                           [,30]
                                     [,31]
                                              [,32]
## 1 0.6299717 -2.660853 1.7889057 -0.1314637 -7.097651 -0.5608560 1.9605391
## 2 2.2261297 -4.141594 4.7569957 4.2656917 2.014184 -1.9448277 -1.1021041
## 3 -4.0438479 0.618285 -0.2146483 4.4299728 -3.038712 -0.6274829 0.8926369
## 4 -4.4850794 4.414988 1.2759364 4.1779126 1.601347 -2.4035973 -8.7852856
```

```
## 5 1.7835560 5.447158 -3.8620456 0.2323402 -1.263644 3.4844592 -0.9795176
## 6 -8.8898199 6.325650 -1.9757978 0.7865158 -6.420165 -9.0009514 -6.8756110
## 1 1.201166
## 2 -9.163178
## 3 1.806860
## 4 7.013511
## 5 5.195483
## 6 3.358453
```

COMPUTATION OF THE NONCUMULATIVE CUMULATIVE PROPORTIONS OF VARIATION EXPLAINED

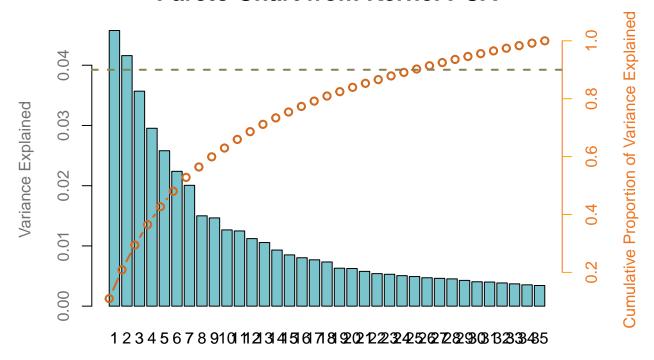




From the above plots, we can also observe that the first two kernel principal component explains a significant variations in the data set

PARETO CHART FROM THE KERNEL PRINCIPAL COMPONENT ANALYSIS

Pareto Chart from Kernel PCA

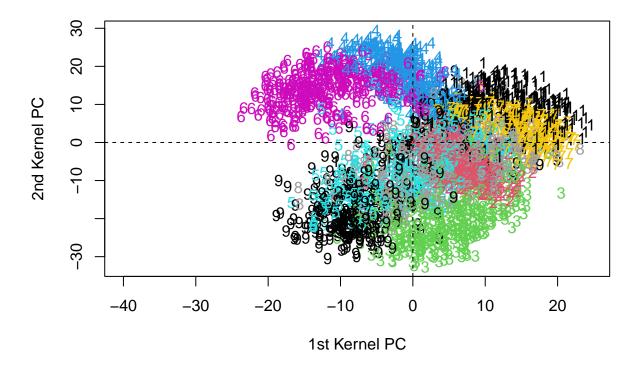


Princippal Components

We can observe from the above pareto chart that the first two principal components explains over 90% of the total variations in the data set.

```
# Plot THE DATA PROJECTION ON THE KERNEL PCS
plot(PC[, 1:2],col=traindat$digit, pch="",
xlab="1st Kernel PC", ylab="2nd Kernel PC")
text(PC[,1:2], labels=traindat$digit, col=traindat$digit)
```

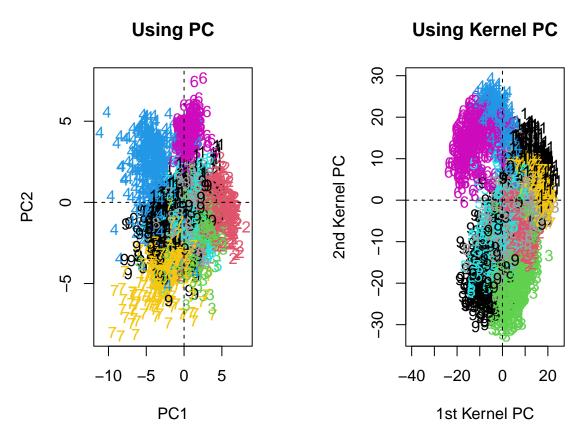
```
abline(v=0, lty=2)
abline(h=0, lty=2)
```



From the above plot, we plot the first kernel principal component against the second kernel principal component and we can also observe from here that though the kernel principal components contain some information it is unable to properly set the hand digits apart

COMPARING ORDINARY PCA AND KPCA ON THE TRAIN DATA

```
par(mfrow=c(1,2), mar=rep(4,4))
#Scatter plot of the first two PCs
plot(pca.train$x[,1:2], pch="", main="Using PC")
text(pca.train$x[,1:2], labels=traindat$digit, col=traindat$digit)
abline(v=0, lty=2)
abline(h=0, lty=2)
# Plot THE DATA PROJECTION ON THE KERNEL PCS
plot(PC[, 1:2], col=traindat$digit, pch="",main="Using Kernel PC",
xlab="1st Kernel PC", ylab="2nd Kernel PC")
text(PC[,1:2], labels=traindat$digit, col=traindat$digit)
abline(v=0, lty=2)
abline(h=0, lty=2)
```



From the above plots, it can be observe that the kernel principal component (kpca) is able to cluster hand-digits better than the ordinary principal component (pc)

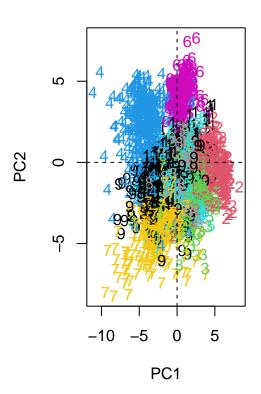
(1d) Apply both the PCA and kPCA results learned from the training data to the test set optdigits.tes, which can be simply done by using the predict() function. Obtain the first two principal components in each case and make similar plots as Part (b) & (c) and compare.

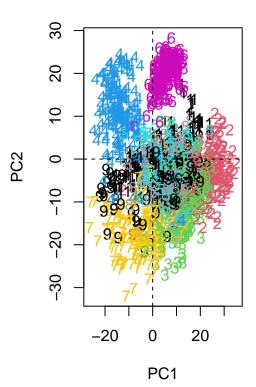
APPLY PCA AND KPCA TO TEST DATA

```
# PCA
pred_pca <- predict(pca.train, new_testdat);
par(mfrow=c(1,2), mar=rep(4,4))
#Scatter plot of the first two PCs
plot(pca.train$x[,1:2], pch="", main="PC1 and PC2 (Train data)")
text(pca.train$x[,1:2], labels=traindat$digit, col=traindat$digit)
abline(v=0, lty=2)
abline(h=0, lty=2)
#Scatter plot of the first two PCs (Predicted)
plot(pred_pca[,1:2], pch="", main="PC1 and PC2 (Test data)")
text(pred_pca[,1:2], labels=testdat$digit, col=testdat$digit)
abline(v=0, lty=2)
abline(h=0, lty=2)</pre>
```

PC1 and PC2 (Train data)

PC1 and PC2 (Test data)





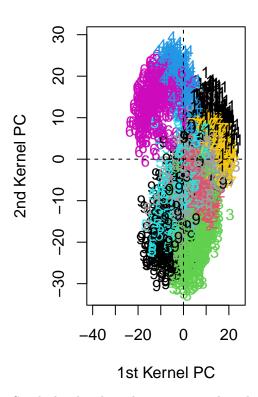
From the two PC plots above, we can observe that the two PCA looks almost similar. Which means PCA predicted the test data somewhat well.

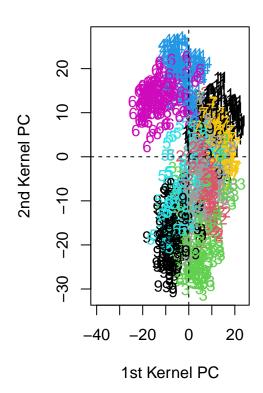
```
# KPCA
pred_kpca <- predict(kpc, scaled_new_testdat );

par(mfrow=c(1,2), mar=rep(4,4))
#Scatter plot of the first two KERNEL PCS
plot(PC[, 1:2],col=traindat$digit, main="k-PC1 and k-PC2 on Train data", pch="",
xlab="1st Kernel PC", ylab="2nd Kernel PC")
text(PC[,1:2], labels=traindat$digit, col=traindat$digit)
abline(v=0, lty=2)
abline(h=0, lty=2)
#Scatter plot of the first two KERNEL PCS Predicted
plot(pred_kpca[, 1:2],col=testdat$digit,main="k-PC1 and k-PC2 on Test data", pch="",
xlab="1st Kernel PC", ylab="2nd Kernel PC")
text(pred_kpca[,1:2], labels=testdat$digit, col=testdat$digit)
abline(v=0, lty=2)
abline(h=0, lty=2)</pre>
```

k-PC1 and k-PC2 on Train data

k-PC1 and k-PC2 on Test data





Similarly, the plots above seem similar which means the kernel pc has been able to predict the test data fairly well though we have some dispersion with the prediction on the test data.

ASSOCIATION RULES

(2a) First read the data into R as transaction data type. This can be done using R function read.transactions() in the arules package:

library(arules)

```
quote="")
                  # DOUBLE/SINGLE QUOTES
dat <- bible;</pre>
dim(dat)
## [1] 31101 12767
inspect(dat[1:5, ])
##
       items
##
   [1] {beginning,
##
         created,
##
         earth,
##
        god,
##
        heaven}
   [2] {darkness,
##
##
        deep,
##
        earth,
##
        face,
##
        form,
##
         god,
##
        moved,
##
         spirit,
##
        upon,
##
         void,
##
         waters,
##
        without}
##
   [3] {god,
##
        let,
##
        light,
        said,
##
        there}
##
##
   [4] {darkness,
##
        divided,
##
        god,
##
         good,
        light,
##
##
        saw}
##
   [5] {called,
##
        darkness,
##
        day,
         evening,
##
##
        first,
##
         god,
##
        light,
##
        morning,
##
        night}
```

(2b) Set up the parameters in R function arules appropriately with your own choices and then perform frequent itemsets and association rule analysis.

THE TOP 10 ITEMS

```
item.freq <- itemFrequency(dat, type = "relative")
item.freq <- sort(item.freq, decreasing = TRUE)
item.freq[1:10]

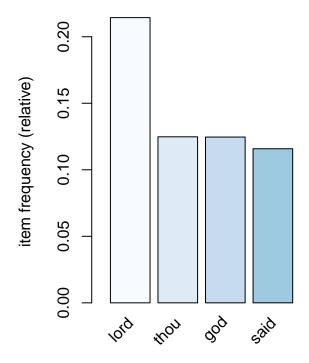
## lord thou god said thy ye thee
## 0.21436610 0.12478698 0.12459406 0.11581621 0.09787467 0.09166908 0.08797145
## out man israel
## 0.07893637 0.07491721 0.07372753</pre>
```

The above output shows the top 10 items

```
#tem.freq0 <- sort(item.freq[1:10], decreasing = TRUE)
#tem.freq0</pre>
```

itemFrequencyPlot(dat,support=0.1, type = c("relative"), cex=1,col=blues9,topN=10, main="Item Frequency

Item Frequency



The above chart shows the top item frequency using a chosen support of 0.1. It can be observed that lord has the highest frequency followed by thou, god and said.

RULES

```
rules <- apriori(dat, parameter = list(support = 0.005, confidence = 0.5,
    target = "rules", maxlen=5))</pre>
```

```
## Apriori
##
## Parameter specification:
    confidence minval smax arem aval original Support maxtime support minlen
##
           0.5
                  0.1
                         1 none FALSE
                                                 TRUE
                                                                0.005
##
   maxlen target ext
         5 rules TRUE
##
##
## Algorithmic control:
   filter tree heap memopt load sort verbose
##
      0.1 TRUE TRUE FALSE TRUE
                                         TRUE
##
## Absolute minimum support count: 155
##
## set item appearances ...[0 item(s)] done [0.00s].
## set transactions ...[12767 item(s), 31101 transaction(s)] done [0.12s].
## sorting and recoding items ... [451 item(s)] done [0.00s].
## creating transaction tree ... done [0.01s].
## checking subsets of size 1 2 3 4 5
## Warning in apriori(dat, parameter = list(support = 0.005, confidence = 0.5, :
## Mining stopped (maxlen reached). Only patterns up to a length of 5 returned!
## done [0.01s].
## writing ... [107 rule(s)] done [0.00s].
## creating S4 object ... done [0.00s].
summary(rules)
## set of 107 rules
## rule length distribution (lhs + rhs):sizes
  2 3 4
## 26 55 26
##
##
     Min. 1st Qu. Median
                              Mean 3rd Qu.
                                              Max.
##
         2
                 3
                         3
                                 3
                                         3
##
##
  summary of quality measures:
##
      support
                         confidence
                                           coverage
                                                                lift
   Min.
           :0.005016
                      Min.
                              :0.5011
                                        Min.
                                               :0.005080
                                                           Min.
                                                                  : 2.343
   1st Qu.:0.006077
                       1st Qu.:0.5475
##
                                        1st Qu.:0.009389
                                                           1st Qu.: 3.524
##
  Median :0.007331
                      Median :0.6176
                                        Median :0.011350
                                                           Median : 5.462
  Mean
          :0.009194
                       Mean
                              :0.6926
                                        Mean
                                              :0.013777
                                                           Mean
                                                                 : 7.915
   3rd Qu.:0.010787
                                                           3rd Qu.: 7.923
##
                       3rd Qu.:0.8370
                                        3rd Qu.:0.015627
##
   Max.
           :0.039002
                       Max.
                              :1.0000
                                        Max.
                                              :0.041478
                                                           Max.
                                                                  :50.943
       count
##
##
  Min.
          : 156.0
  1st Qu.: 189.0
##
## Median: 228.0
         : 285.9
## Mean
## 3rd Qu.: 335.5
## Max.
          :1213.0
```

```
##
## mining info:
## data ntransactions support confidence
##
                        0.005
                31101
##
## apriori(data = dat, parameter = list(support = 0.005, confidence = 0.5, target = "rules", maxlen = 1
inspect(rules[1:10])
##
       lhs
                    rhs
                               support
                                           confidence coverage
                                                                  lift
## [1]
       {wilt}
                 => {thou}
                               0.006687888 1.0000000 0.006687888 8.013656 208
## [2]
       {silver} => {gold}
                               0.005273142 0.5815603 0.009067233 50.102788 164
## [3]
                 => {about}
       {round}
                               0.009260152 0.9729730
                                                     0.009517379 50.943489 288
## [4]
       {hosts}
                 => {lord}
                               0.008777853 0.9545455
                                                     0.009195846 4.452875 273
## [5]
       {right}
                 => {hand}
                               0.005433909 0.5090361 0.010674898 12.225122 169
## [6]
       {cut}
                 => {off}
                               0.006912961 0.6980519 0.009903219 45.418648 215
## [7]
                 => {offering} 0.006109128 0.5792683 0.010546285 35.745681 190
       {burnt}
## [8]
       {pray}
                 => {thee}
                               0.006076975 0.6176471 0.009838912 7.020995 189
## [9] {side}
                 => {on}
                               0.007041574 0.6403509 0.010996431 11.626125 219
## [10] {another} => {one}
                               0.007523874 0.5735294 0.013118549 10.523503 234
summary(rules)
## set of 107 rules
## rule length distribution (lhs + rhs):sizes
## 2 3 4
## 26 55 26
##
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
##
                3
##
## summary of quality measures:
##
      support
                        confidence
                                          coverage
                                                               lift
## Min.
         :0.005016
                      Min.
                             :0.5011
                                       Min. :0.005080
                                                         Min. : 2.343
  1st Qu.:0.006077
                     1st Qu.:0.5475
                                      1st Qu.:0.009389
                                                         1st Qu.: 3.524
## Median :0.007331
                     Median :0.6176
                                       Median :0.011350
                                                         Median : 5.462
## Mean
         :0.009194
                      Mean
                             :0.6926
                                       Mean
                                             :0.013777
                                                          Mean
                                                               : 7.915
## 3rd Qu.:0.010787
                      3rd Qu.:0.8370
                                       3rd Qu.:0.015627
                                                          3rd Qu.: 7.923
## Max.
          :0.039002
                      Max. :1.0000
                                       Max. :0.041478
                                                         Max. :50.943
##
       count
## Min. : 156.0
##
   1st Qu.: 189.0
  Median : 228.0
## Mean
         : 285.9
   3rd Qu.: 335.5
## Max.
          :1213.0
##
## mining info:
## data ntransactions support confidence
##
                31101
                        0.005
##
## apriori(data = dat, parameter = list(support = 0.005, confidence = 0.5, target = "rules", maxlen =
```

```
# LOOK AT ITEMSETS
itemsets <- as(unique(generatingItemsets(rules)), "data.frame")</pre>
frequentItemsets <- itemsets[with(itemsets, order(-support,items)),]</pre>
names(frequentItemsets)[1] <- "itemset"</pre>
write.table(frequentItemsets, file = "", sep = ",", row.names = FALSE)[1:10]
## "itemset", "support"
## "{shalt,thou}",0.039001961351725
## "{lord, saith}", 0.0281984502106042
## "{hast,thou}",0.0268480113179641
## "{ye,your}",0.022861001253979
## "{lord,o}",0.016912639464969
## "{lord, thus}", 0.0162695733256165
## "{lord, thou, thy}", 0.0153049741165879
## "{shalt,thou,thy}",0.0151442075817498
## "{came,pass}",0.0148869811260088
## "{lord, moses}", 0.0148548278190412
## "{saith,thus}",0.0146297546702678
## "{art,thou}",0.0143403749075592
## "{her,she}",0.0140831484518183
## "{thine,thou}",0.0139545352239478
## "{lord, saith, thus}", 0.0138902286100125
## "{god,lord,thy}",0.0134079290054982
## "{thine,thy}",0.0131828558567249
## "{god,lord,thou}",0.0130542426288544
## "{shalt, thee, thou}", 0.0127005562522105
## "{lord, shalt, thou}", 0.0122504099546638
## "{lord, word}", 0.01189672357802
## "{god,thou,thy}",0.0113501173595704
## "{god,lord,saith}",0.0110928909038295
## "{hast,thou,thy}",0.0110285842898942
## "{god,israel,lord}",0.0108999710620237
## "{answered,said}",0.0106748979132504
## "{god,lord,thee}",0.0105462846853799
## "{lord,ye,you}",0.00967814539725411
## "{god, thee, thy}", 0.00964599209028649
## "{god, thee, thou}", 0.00938876563454551
## "{about,round}",0.00926015240667503
## "{lord, ye, your}", 0.0092279990997074
## "{ye,you,your}",0.0092279990997074
## "{god,lord,ye}",0.00890646603003119
## "{hosts,lord}",0.0087778528021607
## "{children,israel,lord}",0.00874569949519308
## "{god,lord,thou,thy}",0.00852062634641973
## "{hast,thee,thou}",0.00807048004887303
## "{god,lord,thus}",0.00784540690009967
## "{hast,lord,thou}",0.00765248705829395
## "{another,one}",0.00752387383042346
## "{thine, thou, thy}", 0.00745956721648822
## "{god,lord,saith,thus}",0.00733095398861773
## "{god,lord,thee,thy}",0.00733095398861773
```

"{god,saith,thus}",0.00733095398861773

```
## "{god,lord,your}",0.00729880068165011
## "{lord, thee, thou, thy}", 0.00726664737468249
## "{on,side}",0.00704157422590913
## "{god,shalt,thou}",0.00697726761197389
## "{commanded,lord}",0.00694511430500627
## "{cut,off}",0.00691296099803865
## "{god,lord,you}",0.00684865438410341
## "{hast,said,thou}",0.00678434777016816
## "{thou, wilt}", 0.0066878878492653
## "{god,ye,your}",0.00662358123533005
## "{lord, shalt, thou, thy}", 0.00659142792836243
## "{lord, shalt, thy}", 0.00659142792836243
## "{god,lord,our}",0.00649496800745957
## "{shalt, thee, thou, thy}", 0.00617343493778335
## "{israel,lord,saith}",0.00614128163081573
## "{burnt,offering}",0.00610912832384811
## "{lord,o,thou}",0.00607697501688049
## "{pray,thee}",0.00607697501688049
## "{lord, o, thy}", 0.00604482170991286
## "{god,lord,thee,thou}",0.00598051509597762
## "{god, thee, thou, thy}", 0.00591620848204238
## "{god,land,lord}",0.00578759525417189
## "{israel,lord,said}",0.00575544194720427
## "{god,lord,shalt,thou}",0.00572328864023665
## "{god,lord,shalt}",0.00572328864023665
## "{hand,right}",0.00543390887752805
## "{lord, saith, ye}", 0.00530529564965757
## "{gold,silver}",0.00527314234268995
## "{thee,thine,thy}",0.00527314234268995
## "{lord,o,thee}",0.00524098903572232
## "{god,hast,thou}",0.0052088357287547
## "{god,lord,therefore}",0.00514452911481946
## "{god,lord,upon}",0.00514452911481946
## "{god,lord,people}",0.00511237580785184
## "{god,lord,out}",0.00508022250088422
## "{god,shalt,thou,thy}",0.00508022250088422
## "{god, shalt, thy}", 0.00508022250088422
## "{before,god,lord}",0.00504806919391659
## "{came,lord,saying}",0.00501591588694897
## NULL
```

(2c) List the top 5 rules in decreasing order of confidence (conf) for item sets of size or length 2 or 3 which satisfy the support threshold that you have specified. Are they interesting rules within the problem context?

```
support confidence
##
                   rules
                                                      coverage
                                                                     lift count
       {wilt} => {thou} 0.006687888 1.0000000 0.006687888 8.013656
                                                                            208
## 2 {silver} => {gold} 0.005273142 0.5815603 0.009067233 50.102788
                                                                            164
## 3 {round} => {about} 0.009260152 0.9729730 0.009517379 50.943489
                                                                            288
      {hosts} => {lord} 0.008777853
                                       0.9545455 0.009195846 4.452875
                                                                            273
      {right} => {hand} 0.005433909 0.5090361 0.010674898 12.225122
## 5
                                                                            169
         {cut} => {off} 0.006912961 0.6980519 0.009903219 45.418648
## 6
                                                                            215
##
           I.HS
                     RHS size
## 1
       {wilt}
                  {thou}
                             2
## 2 {silver}
                  {gold}
                             2
## 3 {round}
                 {about}
                             2
     {hosts}
                  {lord}
                             2
## 4
## 5
      {right}
                  {hand}
                             2
                   {off}
## 6
        {cut}
                             2
# Top 5 rules in decreasing order of confidence
RULES1 <- RULES[RULES$size==c(2,3), ]</pre>
## Warning in RULES\$size == c(2, 3): longer object length is not a multiple of
## shorter object length
RULES1 <- RULES[ order(RULES$confidence, decreasing = TRUE), ]</pre>
head(RULES1, n=5)
##
                             rules
                                        support confidence
                                                               coverage
                                                                              lift count
                 \{wilt\} => \{thou\} 0.006687888
## 1
                                                          1 0.006687888 8.013656
                                                                                     208
          \{\text{shalt}, \text{thee}\} => \{\text{thou}\}\ 0.012700556
## 50
                                                          1 0.012700556 8.013656
                                                                                     395
## 52
           \{\text{shalt,thy}\} => \{\text{thou}\}\ 0.015144208
                                                          1 0.015144208 8.013656
                                                                                     471
## 54
           \{god, shalt\} => \{thou\} 0.006977268
                                                          1 0.006977268 8.013656
                                                                                     217
## 82 {god,saith,thus} => {lord} 0.007330954
                                                          1 0.007330954 4.664917
                                                                                     228
##
                     LHS
                              RHS size
## 1
                 {wilt}
                           {thou}
## 50
           {shalt,thee}
                           {thou}
                                     3
## 52
           {shalt,thy}
                           {thou}
                                     3
            {god,shalt}
                                     3
## 54
                           {thou}
## 82 {god,saith,thus}
                           {lord}
```

The output above shows the top 5 rules in decreasing order of confidence for item sets of size/length 2 or 3

(d) List the top 5 rules in decreasing order of the lift measure for item sets of size 2 or 3. Always interpret the results.

```
# Top 5 rules in decreasing order of lift
RULESa <- RULES[RULES$size==c(2,3), ]

## Warning in RULES$size == c(2, 3): longer object length is not a multiple of
## shorter object length

RULESa <- RULES[ order(RULES$lift,decreasing = TRUE), ]
head(RULESa,n=5)</pre>
```

```
##
                           rules
                                      support confidence
                                                             coverage
                                                                          lift count
              {round} => {about} 0.009260152 0.9729730 0.009517379 50.94349
## 3
                                                                                  288
## 2
              {silver} => {gold} 0.005273142 0.5815603 0.009067233 50.10279
                                                                                 164
## 6
                  {cut} => {off} 0.006912961 0.6980519 0.009903219 45.41865
                                                                                 215
## 7
           {burnt} => {offering} 0.006109128 0.5792683 0.010546285 35.74568
                                                                                 190
## 85 {god,lord,saith} => {thus} 0.007330954 0.6608696 0.011092891 29.07172
                                                                                 228
##
                    LHS
                                 RHS size
## 3
               {round}
                             {about}
## 2
              {silver}
                              {gold}
                                        2
                                        2
## 6
                 {cut}
                               {off}
## 7
               {burnt}
                          {offering}
                                        2
                                        4
## 85 {god,lord,saith}
                              {thus}
```

The above output shows the top 5 rules in decreasing order of the lift measure for item sets of size 2 or 3. We can observe that the top 5 rules have positive lifts which shows a positive relationship

(2e) Find the conviction measures for the top-lift 5 rules in Part (d) and explain how this measure avoids the problems associated with both the confidence and the lift measures.

[1] 5 9

```
inspect(head(rules.pruned)); head(MO)
```

```
##
       lhs
                                        support
                             rhs
                                                    confidence coverage
## [1] {round}
                          => {about}
                                        0.009260152 0.9729730 0.009517379
## [2] {silver}
                                        0.005273142 0.5815603 0.009067233
                          => {gold}
## [3] {cut}
                          => {off}
                                        0.006912961 0.6980519 0.009903219
## [4] {burnt}
                          => {offering} 0.006109128 0.5792683 0.010546285
   [5] {god, lord, saith} => {thus}
                                        0.007330954 0.6608696
                                                               0.011092891
                                        0.007330954 0.5937500 0.012346870
  [6] {god, saith}
                          => {thus}
##
##
       lift
                count
## [1] 50.94349 288
## [2] 50.10279 164
## [3] 45.41865 215
## [4] 35.74568 190
## [5] 29.07172 228
## [6] 26.11912 228
         support chiSquared confidence conviction
##
                                                      cosine
## 1 0.009260152 14514.081 0.9729730 36.293335 0.6868366 0.009517379
## 2 0.005273142
                                        2.362091 0.5140030 0.009067233
                   8057.876 0.5815603
```

```
## 3 0.006912961
                  9580.406 0.6980519
                                         3.260928 0.5603368 0.009903219
## 4 0.006109128
                  6592.220 0.5792683
                                        2.338295 0.4673061 0.010546285
## 5 0.007330954
                   6394.891 0.6608696
                                         2.881687 0.4616529 0.011092891
##
        leverage
                    lift oddsRatio
## 1 0.009078379 50.94349 3588.1176
## 2 0.005167896 50.10279 216.0375
## 3 0.006760756 45.41865
                          268.3654
## 4 0.005938223 35.74568 133.5551
## 5 0.007078786 29.07172 123.1761
```

```
#MO <- interestMeasure(rules, c( "conviction"), transactions=dat)
#dim(MO)</pre>
```

The Conviction measures the implication strength of the rule from statistical independence. Conviction produces an association rule with better predictive ability, unlike lift, Conviction takes into account the strength of the directed association, unlike Confidence, the support of both antecedent and consequent are considered in conviction.