Tabla A-1. Parejas de la transformada de Laplace.

	f(t)	F(s)
1	Unidad de impulso $\delta(t)$	1
2	Unidad de paso 1(t)	$\frac{1}{s}$
3	t	$\frac{1}{s^2}$
4	$\frac{t^{n-1}}{(n-1)!} \qquad (n=1, 2, 3,)$	$\frac{1}{s^n}$
5	$t^n$ $(n = 1, 2, 3,)$	$\frac{n!}{s^{n+1}}$
6	$e^{-at}$	$\frac{1}{s+a}$
7	te <sup>- at</sup>	$\frac{1}{(s+a)^2}$
8	$\frac{1}{(n-1)!} t^{n-1} e^{-at}  (n=1,2,3,)$	$\frac{1}{(s+a)^n}$
9	$t^n e^{-at}$ $(n = 1, 2, 3,)$	$\frac{n!}{(s+a)^{n+1}}$
10	$\operatorname{sen}\omega \mathrm{t}$	$\frac{\omega}{s^2 + \omega^2}$
11	$\cos \omega t$	$\frac{s}{s^2 + \omega^2}$
12	$\mathrm{senh}\omega t$	$\frac{\omega}{s^2 - \omega^2}$
13	$\cosh \omega t$	$\frac{s}{s^2 - \omega 2}$
14	$\frac{1}{a}(1-e^{-at})$	$\frac{1}{s(s+a)}$
15	$\frac{1}{b-a}(e^{-at}-e^{-bt})$	$\frac{1}{(s+a)(s+b)}$
16	$\frac{1}{b-a}(be^{-bt}-ae^{-at})$	$\frac{s}{(s+a)(s+b)}$
17	$\frac{1}{ab}\left[1+\frac{1}{a-b}\left(be^{-at}-ae^{-bt}\right)\right]$	$\frac{1}{s(s+a)(s+b)}$

(continúa)

Tabla A-1. (Continuación).

	(			
	f(t)	F(s)		
18	$\frac{1}{a^2}(1 - e^{-at} - ate^{-at})$	$\frac{1}{s(s+a)^2}$		
19	$\frac{1}{a^2}(at-1+e^{-at})$	$\frac{1}{s^2(s+a)}$		
20	$e^{-at}$ sen $\omega t$	$\frac{\omega}{(s+a)^2+\omega^2}$		
21	$e^{-at}\cos\omega t$	$\frac{s+a}{(s+a)^2+\omega^2}$		
22	$\frac{\omega_n}{\sqrt{1-\zeta^2}}e^{-\zeta\omega_n t} \operatorname{sen} \omega_n \sqrt{1-\zeta^2}t  (0<\zeta<1)$	$\frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$		
23	$-\frac{1}{\sqrt{1-\zeta^2}}e^{-\zeta\omega_n t}\operatorname{sen}(\omega_n\sqrt{1-\zeta^2}t-\phi)$ $\phi = \tan^{-1}\frac{\sqrt{1-\zeta^2}}{\zeta}$	$\frac{s}{s^2 + 2\zeta\omega_n s + \omega_n^2}$		
24	$(0 < \zeta < 1, 0 < \phi < \pi/2)$ $-\frac{1}{\sqrt{1-\zeta^2}}e^{-\zeta\omega_n t}\operatorname{sen}(\omega_n\sqrt{1-\zeta^2}t+\phi)$ $\phi = \tan^{-1}\frac{\sqrt{1-\zeta^2}}{\zeta}$ $(0 < \zeta < 1, 0 < \phi < \pi/2)$	$\frac{\omega_n^2}{s(s^2 + 2\zeta\omega_n s + \omega_n^2)}$		
25	$1-\cos\omega t$	$\frac{\omega^2}{s(s^2+\omega^2)}$		
26	$\omega t = \operatorname{sen} \omega t$	$\frac{\omega^3}{s^2(s^2+\omega^2)}$		
27	$\operatorname{sen} \omega t - \omega t \cos \omega t$	$\frac{2\omega^3}{(s^2+\omega^2)^2}$		
28	$\frac{1}{2\omega}t \operatorname{sen} \omega t$	$\frac{s}{(s^2 + \omega^2)^2}$		
29	$t\cos \omega t$	$\frac{s^2 - \omega^2}{(s^2 + \omega^2)^2}$		
30	$\frac{1}{\omega_2^2 - \omega_1^2} (\cos \omega_1 t - \cos \omega_2 t) \qquad (\omega_1^2 \neq \omega_2^2)$	$\frac{s}{(s^2 + \omega_1^2)(s^2 + \omega_2^2)}$		
31	$\frac{1}{2\omega}\left(\operatorname{sen}\omega t + \omega t \cos \omega t\right)$	$\frac{s^2}{(s^2+\omega^2)^2}$		

Tabla A-2. Propiedades de la transformada de Laplace.

1	$\mathcal{L}[Af(t)] = AF(s)$		
2	$\mathcal{L}[f_1(t) \pm f_2(t)] = F_1(s) \pm F_2(s)$		
3	$\mathcal{L}_{\pm}\left[\frac{d}{dt} f(t)\right] = sF(s) - f(0\pm)$		
4	$\mathcal{L}_{\pm}\left[\frac{d^2}{dt^2}f(t)\right] = s^2 F(s) - s f(0\pm) - \dot{f}(0\pm)$		
5	$\mathcal{L}_{\pm} \left[ \frac{d^n}{dt^n} f(t) \right] = s^n F(s) - \sum_{k=1}^n s^{n-k} f^{(k-1)}(0\pm)$		
	donde $f(t) = \frac{d^{k-1}}{dt^{k-1}} f(t)$		
6	$\mathcal{L}_{\pm}\left[\int f(t) dt\right] = \frac{F(s)}{s} + \frac{1}{s} \left[\int f(t) dt\right]_{t=0\pm}$		
7	$\mathcal{L}_{\pm\pm}\left[\int\cdots\int f(t)(dt)^n\right] = \frac{F(s)}{s^n} + \sum_{k=1}^n \frac{1}{s^{n-k+1}}\left[\int\cdots\int f(t)(dt)^k\right]_{t=0\pm}$		
8	$\mathcal{L}\left[\int_0^t f(t) dt\right] = \frac{F(s)}{s}$		
9	$\int_0^\infty f(t) dt = \lim_{s \to 0} F(s)  \text{si } \int_0^\infty f(t) dt \text{ salidas}$		
10	$\mathcal{L}[e^{-\alpha t} f(t)] = F(s+a)$		
11	$\mathcal{L}[f(t-\alpha)1(t-\alpha)] = e^{-\alpha s} F(s) \qquad a \geqslant 0$		
12	$\mathcal{L}[tf(t)] = -\frac{dF(s)}{ds}$		
13	$\mathcal{L}[t^2 f(t)] = \frac{d^2}{ds^2} F(s)$		
14	$\mathcal{L}[t^n f(t)] = (-1)^n \frac{d^n}{ds^n} F(s)  (n = 1, 2, 3,)$		
15	$\mathcal{L}\left[\frac{1}{t} f(t)\right] = \int_{s}^{\infty} F(s) ds  \text{si } \lim_{t \to 0} \frac{1}{t} f(t) \text{ salidas}$		
16	$\mathscr{L}\left[f\left(\frac{1}{a}\right)\right] = aF(as)$		
17	$\mathcal{L}\left[\int_0^t f_1(t-\tau) f_2(\tau) d\tau\right] = F_1(s)F_2(s)$		
18	$\mathcal{L}[f(t)g(t)] = \frac{1}{2\pi j} \int_{c-j\omega}^{c+j\infty} F(p)G(s-p) dp$		

Por último se presentan dos teoremas frecuentemente utilizados junto con las transformadas de Laplace de la función pulso y de la función impulso.

Teorema de valor inicial	$f(0+) = \lim_{t \to 0+} f(t) = \lim_{s \to \infty} sF(s)$
Teorema de valor final	$f(\infty) = \lim_{t \to \infty} f(t) = \lim_{s \to 0} sF(s)$
Función pulso $f(t) = \frac{A}{t_0} 1(t) - \frac{A}{t_0} 1(t - t_0)$	$\mathcal{L}[f(t)] = \frac{A}{t_0 s} - \frac{A}{t_0 s} e^{-st_0}$
Función impulso $g(t) = \lim_{t_0 \to 0} \frac{A}{t_0},  \text{para } 0 < t < t_0$ $= 0, \qquad \text{para } t < 0, t_0 < t$	$\mathcal{L}[g(t)] = \lim_{t_0 \to 0} \left[ \frac{A}{t_0 s} (1 - e^{-st_0}) \right]$ $= \lim_{t_0 \to 0} \frac{\frac{d}{dt_0} \left[ A(1 - e^{-st_0}) \right]}{\frac{d}{dt_0} \left( t_0 s \right)}$ $= \frac{As}{s} = A$