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## Homework 6

$$\sum = \begin{pmatrix} 2 & 2 \\ 2 & 4 \\ 2 & 6 \\ 0 & 0 \\ -1 & -4 \\ -2 & -4 \\ -3 & -6 \end{pmatrix}$$

$$\widehat{Y}_{1} = \overrightarrow{u}_{1}^{\mathsf{T}} \cdot \overrightarrow{X} = u_{11} \cdot X_{1} + u_{12} \cdot X_{2}$$

$$\widehat{Y}_{2} = \overrightarrow{u}_{2}^{\mathsf{T}} \cdot \overrightarrow{X} = u_{21} \cdot X_{1} + u_{22} \cdot X_{2}$$

where 
$$Cov(X) = S = V \cdot \Delta \cdot V^T$$
is a spectral decomposition
and  $V = (\vec{u}_1 \cdot \vec{u}_2)$ 

$$\frac{1}{2} = \frac{1}{n} \times \frac{1}{n} \times \frac{1}{n} = \frac{1}{n} \begin{pmatrix} 2 & 2 & 2 & 0 & -1 & -2 & -3 \\ 2 & 6 & 0 & -4 & -4 & -4 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}.$$

$$S = \frac{1}{h-1} \left( X - \frac{1}{2h} \frac{1}{x^{7}} \right) \left( X - \frac{1}{2h} \frac{1}{x^{7}} \right) = \frac{1}{h-1} X^{7} X = \frac{1}{6} \left( \frac{26}{42} \right) = \frac{1}{3} \left( \frac{13}{2h} \frac{24}{52} \right)$$

$$N = 7$$

Final a spectral decomposition:

$$|S-JI| = \frac{3}{3} - 7 = \frac{3}{3} + 7 = 64$$

$$= \frac{1}{2} + \frac{65}{9} + \frac{100}{9} = 0 \text{ And } \lambda = \frac{65}{3} \cdot \frac{1}{3} \cdot \frac{100}{9} = \frac{1}{2} \left( \frac{65}{3} + \left( \frac{4225}{9} - \frac{400}{9} \right)^{1/2} \right) = \frac{1}{2} \left( \frac{65}{3} + \left( \frac{4225}{9} - \frac{400}{9} \right)^{1/2} \right) = \frac{1}{2} \left( \frac{65}{3} + \frac{100}{9} - \frac{100}{9} \right)^{1/2}$$

$$= \frac{3}{7} \left( \frac{3}{62} + \frac{3}{7} \left( 3852 \right)_{1/5} \right) = \frac{5}{7} \left( \frac{3}{62} + \frac{3}{16} \frac{214}{5} \right)$$

Cobtain the eigen-vectors:

(b)  $(S-\lambda_1 I) \vec{u}_1 = 0$ (c)  $(S-\lambda_1 I) \vec{u}_1 = 0$ (c)  $(S-\lambda_1 I) \vec{u}_1 = 0$ (d)  $(S-\lambda_1 I) \vec{u}_1 = 0$ (e)  $(S-\lambda_1 I) \vec{u}_1 = 0$ (e)  $(S-\lambda_1 I) \vec{u}_1 = 0$ (f)  $(S-\lambda_1 I) \vec{u}_1 = 0$ (g)  $(S-\lambda_1 I) \vec{u}_1 = 0$ ( 4>  $\left(\frac{13}{3}-\lambda_{1}\right)u_{11} + 8u_{12} = 0$  21-3  $\left(\frac{13}{3}-\frac{66+15\sqrt{17}}{6}\right)u_{11} = -8u_{12}$  and nivinalize when 40  $u_{12} = \frac{-1}{8} \cdot \left( \frac{26 - 65 + 15 \sqrt{17}}{6} \right) = \frac{39 + 15 \sqrt{17}}{48}$   $u_{1} = \left( \frac{39 + 15 \sqrt{17}}{48} \right) - 2 \sqrt{15} \sqrt{15}$ ui ≈ (0'4298) (V2), compite uz the same way: uz≈ (-0'9029). Then: S= V. A. VT where V= (4, 42)= (01929 -019029) and  $V = \left(\frac{Q}{QP + 1P J I J}\right)$ Finally, the first and second PCs are:  $\widetilde{Y}_1 = \widetilde{u_1} \cdot \widetilde{Z} = 04298 \cdot X_1 + 019029 \cdot X_2$ (B) Détermine the prepartien et total variance due to the first sample PC. That is: Su +62 , where hi = 65 + 18+17, Su = 3, Sz = 3? λi ≈ 21/1411 ≈ 0/9757

Compare the contributions of the two variates to the determination, of the first PC based on loadings:

As seen in Q: \$\frac{1}{2} = \frac{0'4298}{v\_0} \ \text{\$\text{\$X\$}\_1 + \frac{0'9029}{u\_p} \text{\$\text{\$X\$}\_2}}

Where the ansee using the loadings that both variates autibute positively and the antribution of &z is ausiderally greater than the firsts.

a) Compare the contribution of the two variates based to the determination of the first PC based on sample correlations.

Let's compute the sample correlations:

Cor (Y1, X1) = V = U = \ \frac{\lambda\_1}{\S\_{11}} \approx 019493

Corr (Y, X2) = 1,2 = U12 - 1 = 019972

Obtaining the same result: Both maintes contribute positively and Ze contribution is greater than Zis.

@ Repeat @ to @ with standarized data.

Osing that  $Cov(\tilde{Z}) = Covr(\tilde{Z})$ , we can study  $Cvr(\tilde{Z})$  without amputing  $\tilde{Z}$ . Let's obtain the spectral decomposition of  $Cvr(\tilde{Z})$ .

Compute 
$$Corv(\vec{X}) = D^{1/2} \cdot S \cdot D^{1/2}$$
,  $D^{-1/2}(\sqrt{n^{1/3}}) = \sqrt{n^{1/2}}$  of  $\sqrt{n^{1/2}}$  of  $\sqrt{n^{1/$ 

Using leadings we see that both variables contribute the same to the first PC (ui, = uix= to), and both positively. We obtain the same result comparing sample correlations:

Corr ( Is, Z) = U; Jh = U; Th = Corr ( Is, Z2) = 0'9806.

Problem 2 1 Hake first PC of X1, X2 is 1 = 1/2 X, + 1/2 X2, 13 it possible that Cor (X,, X2) 40? We know that Ix = 5, \$ = 5 = 1 (1) the first eigen-vector Covr (X1, X2) = Cov (X1, X2) , Cov (X1, X2) 40 at Cov(X1, X2) 40. Let V. D. VT = I be a spectral de composition of I = Cov (). Then V= (v, v2), A= (1 h2) with lish >2>0. Since 51 152 and 51 = 12 (1) => 52 = 12 (-1) => V=12 (1-1)  $\sum = \begin{pmatrix} O_{11} & O_{12} \\ O_{21} & O_{22} \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \lambda_1 & \lambda_2 \\ \lambda_1 & -\lambda_2 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ \lambda_1 & -\lambda_2 \end{pmatrix}$  $= \frac{1}{2} \left( \frac{\lambda_1 + \lambda_2}{\lambda_1 - \lambda_2} \right) = \sum_{i=1}^{n} O_{i2} = C_{ev} \left( \frac{\lambda_1}{\lambda_2} \right) = \frac{\lambda_1 - \lambda_2}{2}$   $= \frac{1}{2} \left( \frac{\lambda_1 + \lambda_2}{\lambda_1 + \lambda_2} \right) = \sum_{i=1}^{n} O_{i2} = C_{ev} \left( \frac{\lambda_1}{\lambda_2} \right) = \frac{\lambda_1 - \lambda_2}{2}$   $= \frac{1}{2} \left( \frac{\lambda_1 + \lambda_2}{\lambda_1 + \lambda_2} \right) = \sum_{i=1}^{n} O_{i2} = C_{ev} \left( \frac{\lambda_1}{\lambda_2} \right) = \frac{\lambda_1 - \lambda_2}{2}$   $= \frac{1}{2} \left( \frac{\lambda_1 + \lambda_2}{\lambda_1 + \lambda_2} \right) = \sum_{i=1}^{n} O_{i2} = C_{ev} \left( \frac{\lambda_1}{\lambda_2} \right) = \frac{\lambda_1 - \lambda_2}{2}$   $= \frac{\lambda_1 - \lambda_2}{2}$ 

=> Corr (X1, X2) >0

Problem 3 Problem 8.12 on page 474: Using table 1.5.

Summarize the data in fewer than P=7 dimensions. Conduct PCA using both S= Ca (X) and Q= Gvv(X). What have you learned? Does it make any difference which matrix is used for the analysis? Can the data be summarize in 3 or less dim. ? Can you interpret the PC's?

Using the a code attached we conduct PCA. Starting with Cov (\$\overline{\mathbb{Z}}) = S:

Compile S and it's spectral decomposition. What it is really relevant about S is that Sii < 10 Vi Eld. 3, 4, 7 (

Siz = 800'62

Ses = 11'36, Sie = 30'98.

(Szz >>> Sii Vi +2).

the eigenvalues of S are:

 $\lambda_1 = 304'26$ ,  $\lambda_2 = 28'28$ ,  $\lambda_3 = 41'46$ ,  $\lambda_4 = 2'52$  $\lambda_5 = 1'27$ ,  $\lambda_6 = 0'5287$ ,  $\lambda_7 = 0'2096$ .

Again, 1, >> 12>13 >> 14 \_\_

the proportion of total sample variance due to the first 3 PCs is:

This could fell us that indeed we can summarize the data using the first 3 PCs. However, S22 being so high (and so close to Var II = 1 = 304/26) makes us think that the I PC is bosically X2, and due to its huge raviance we are obtaining a unbalanced PC. We can check the loadings to anythin our hypotheris:

where we can see that  $\mathbb{Z}_2$  is unbalancing of analysis. To dodge this Kind of effects we should study  $\mathbb{Q}$  instead of  $\mathbb{S}$ .

We procede to the analysis of Q; It's eigen values are:  $\lambda'_1 = 2'3368$ ,  $\lambda'_2 = 1'386$ ,  $\lambda'_3 = 1'204$ ,  $\lambda'_4 = 0'7271$   $\lambda'_5 = 0'6535$ ,  $\lambda'_6 = 0'5367$ ,  $\lambda'_7 = 0'1869$ .

We can see they are more balanced. The first 3 eigen vectors are:

$$\vec{U}_{1} = \begin{cases}
-0.12368 \\
-0.1266 \\
-0.1266
\end{cases}$$

$$\vec{U}_{2} = \begin{cases}
-0.1245 \\
-0.12245
\end{cases}$$

$$\vec{U}_{3} = \begin{cases}
-0.1245 \\
-0.12245
\end{cases}$$

$$\vec{U}_{3} = \begin{cases}
-0.1368 \\
-0.1364
\end{cases}$$

$$\vec{U}_{3} = \begin{cases}
-0.1368 \\
-0.1368 \\
0.1368
\end{cases}$$

$$\vec{U}_{3} = \begin{cases}
-0.1368 \\
-0.1368 \\
0.1368
\end{cases}$$

$$\vec{U}_{3} = \begin{cases}
-0.1368 \\
-0.1368 \\
0.1368
\end{cases}$$

$$\vec{U}_{3} = \begin{cases}
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\end{cases}$$

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\end{cases}$$

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0.1368 \\
0.1368
\end{cases}$$

$$\vec{U}_{3} = \begin{cases}
-0.1368 \\
0.1368 \\
0.1368
\end{cases}$$

$$\vec{U}_{3} = \begin{cases}
-0.1368 \\
0.1368 \\
0.1368
\end{cases}$$

We can see a huge different with the ui previously calculated for S:

There is a balance between the early betiens of every variate, and  $X_2$ doesn't appear move than the others. This confirms our hypothesis

even move (it could also happen that  $X_2$  was a relevant variate

when the data is standarized, but this teachs us that that doesn't

always happen, so we should always standarized our data for

PCA).
Finally let's compute the proportion of total sample variance due to the first 3 PCs:

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$$\frac{\lambda_{1} + \lambda_{2} + \lambda_{3}}{S_{01} + \dots + S_{77}} = \frac{\lambda_{1} + \lambda_{2} + \lambda_{3}}{7} \approx 0'7038$$

We are sommanizing a let of our data using only 3 PCs. but not quite enough to say that we can just use this 3 PCs instead of X. Again, this is very different from the 0'99 obtained studying S.

Problem 4 Consider two samples of equal sizes hi=n2:

$$\vec{X}_{11}$$
,  $-$ ,  $\vec{X}_{1n_1}$  with summary  $\vec{X}_{10}$  (6),  $\vec{X}_{2}$  = (6),  $\vec{X}_{2}$  = (6),  $\vec{X}_{2}$  = (42),  $\vec{X}_{2}$  (42)  $\vec{X}_{211}$  -,  $\vec{X}_{2n_2}$  statistics

For a new observation  $\vec{x}_0 = \begin{pmatrix} x_{01} \\ x_{02} \end{pmatrix}$ , consider:

1. Classifier 1: Fishers rule if only xo, is observed. 2. Classifier 2: Fisher's rule if only xor is observed. 3. Classifier 3: Fisher's rule based on Zo.

Does there exist a xo, such that Classifiers I and 2 agree while disagreeing with Chasifier 3?

Latts compute the different classifiers using Fisher's role:

(1) 
$$(x_1 - x_{12})^7 \cdot \sigma_{11}^{-1} (x_{c_1} - \frac{1}{2}(x_{11} + x_{12})) = (6 - c) \cdot \frac{1}{4} \cdot (x_{c_1} - \frac{1}{2}(6 + c)) = \frac{6}{4}(x_{c_1} - 3) 7/0$$
  $q_{c_2} \times \sigma_{1} 7/3$ 

(2) 
$$(x_{21}-x_{22})^{7}$$
,  $\sigma_{22}^{-1}(x_{02}-\frac{1}{2}(x_{02}+x_{02}))=\frac{-6}{4}(x_{02}-3)>0$   $4>\frac{x_{02}\leq 3}{x_{02}}$ 

3 Spooled = 
$$\frac{1}{16-4} \left( \frac{1}{2} - \frac{2}{4} \right) = \frac{1}{6} \left( \frac{2}{12} - \frac{1}{2} \right)$$
 $(\overline{x_1} - \overline{x_2})^T \text{Spooled}^T (\overline{x_0} - \frac{1}{2}(\overline{x_1} + \overline{x_2})) = \left( \frac{6}{16} \right)^T \frac{1}{16} \left( \frac{2}{12} - \frac{1}{2} \right) \left( \frac{x_0}{x_0} - \left( \frac{3}{3} \right) \right) =$ 
 $= (1, -1) \left( \frac{2}{12} - \frac{1}{2} \right) \left( \frac{x_{11} - 3}{x_{12} - 3} \right) = (3, -3) \left( \frac{x_{21} - 3}{6} \right) = 3(x_{21} - 3) - 3(x_{22} - 3) =$ 
 $= 3x_{21} - 3x_{22} \ge 0$ 
 $\Rightarrow x_{21} > x_{22} \ge 0$ 
 $\Rightarrow x_{21}$ 

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$$(2) (X_{21} - X_{12})^{T} \cdot \sigma_{22}^{-1} \cdot (X_{02} - \frac{1}{2}(X_{21} + X_{22})) = \begin{cases} X_{21} = X_{11} \\ X_{22} = X_{12} \\ \sigma_{11} = \sigma_{22} \end{cases}$$

$$= (X_{11} - X_{12})^{T} \cdot \sigma_{11}^{-1} \cdot (X_{02} - \frac{1}{2}(X_{11} + X_{12})) = (X_{02} - X_{02})^{T} \cdot \sigma_{11}^{-1} \cdot (X_{02} - X_{02})^{T} \cdot \sigma_{12}^{-1} \cdot (X_{02} - X_{02})^{T} \cdot \sigma_{12}^{T} \cdot \sigma_{12}^{-1} \cdot (X_{02} - X_{02})^{T} \cdot \sigma_$$

3) 
$$\left(\overline{X}_{1} - \overline{X}_{2}\right)^{T} \circ S_{0} \circ \operatorname{d}\left(\overline{X}_{0} - \frac{1}{2}(\overline{X}_{1} + \overline{X}_{2})\right) = \left(66\right) \frac{1}{6} \cdot \left(\frac{2-1}{-12}\right) \cdot \left(\overline{X}_{0} - \left(\frac{3}{3}\right)\right) = \left(11\right) \left(\frac{2-4}{-12}\right) \cdot \left(\overline{X}_{0} - \left(\frac{3}{3}\right)\right) = \left(11\right) \left(\frac{2-4}{-12}\right) \cdot \left(\frac{2-4}{-$$

Suppose both @ and @ assign Class 1, then:

201 > 3 { X01 + X02 7/6 -> (3) assigns class 1.

Suprese both @ and @ assign Ches 2, then 1

X0123 / X01+X02 26 -> (3) assigns class 7.

Solution: no. it doesn't exist to such that @ and @ agree and at the same time disagree with 3.

Problem 6 Considering three independent distribution:

TC1:  $N_{p}(\bar{n}^{2}, \Sigma)$ ,  $N_{1}$ TC2:  $N_{p}(\bar{n}^{2}, \Sigma)$ ,  $N_{2}$ , use  $S_{peoled} = \frac{1}{(n_{1}+n_{2}+n_{3}-3)} \cdot ((n_{1}-1)S_{1}+(n_{2}-1)S_{3})$ . TC3:  $N_{p}(\bar{n}^{2}, \Sigma)$ ,  $N_{3}$  Suppose that, upon electifying to using Fisher's role, between TC, and TC2 xo is allocated to TC2 and between TC2 and TC3. To allocated in TC3. Show that In the companion between TC2 and TC3, Xo is allocated to TC3.

This is simply by transitivity of the Mahalanabis distance:

dm (xo, The) & dm (xo, Thi) |=> dm (xo, Thi) & dm (xo, Thi)

dm (xo, Mi) & dm (xo, Thi)

And Knowing that you comparing This tij (i \( \)), Fisher's rule classifies \( \tilde{\chi} \) in The if and only if  $d_{M}(\vec{x}_{0}, \vec{\mu}_{0}) \leq d_{M}(\vec{x}_{0}, \vec{\mu}_{0})$ .
This is only possible because the matrix spooled is common to the three tisher's rules.

Problem 7 For the dataset on Table 1.6, anstruct Fisher's Alle. Moveover, Calcolate the apparent error rate (AER), as well as the expected actual error rate (EAER) using Lachen branch's holdowl.

Using the code attached we obtained the following Fix her's

$$\vec{w} = \begin{pmatrix} 0 & 0 & 2341 \\ -0 & 0 & 3447 \\ 0 & 2 & 10 & 27 \\ -0 & 10 & 8343 \\ -0 & 125345 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 17494 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 135152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 17494 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 135152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 17494 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 135152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 17494 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 135152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 17494 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 135152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 17494 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 135152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 17494 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 135152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 17494 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 6 & 191909 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 2704 \\ 216 & 267 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 2704 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 2704 \\ 162 & 2704 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 2704 \\ 162 & 2704 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\ 162 & 2704 \\ 162 & 2704 \\ 7 & 185152 \end{pmatrix}, \vec{w}_{0} = \begin{pmatrix} -40 & 0 & 2704 \\$$

Using this classifier we can campute the AER by classifying each element of our population and seeing how many we classify incorrectly. We obtain 10 errors at of nitnz=98 elements:

AEQ= 10/1020408

In order to compute the EAER we use Lachenbruch's holdoid: For each element in our populations, recompute the Fisher's rule without using that element (n,+n2=9.7) and classify it wing the classifier obtained. By following this procedure we obtain a total of 13 errors:

EA EQ = 13 = 01327

As expected, EAEQ > AEQ. This doesn't always happen, but it is the expected result.