The kinshipsymbols package*

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Abstract

This package defines consistent mathematical symbols for statistical genetics, particularly relating to the kinship model and $F_{\rm ST}$. In addition to providing a long list of symbols, the package has two options that alter the behavior of some of the most common symbols. Option color highlights genotypes (blue), kinship coefficients (dark green), and the standard ancestral allele frequency estimator (red), which is useful for Beamer presentations. Option noT removes the ancestral population T superscript from all symbols that contain it (for simpler presentations).

Contents

1	Intr	oduction	2			
2	Imp	Implementation				
	2.1	Dependencies	7			
	2.2	Initializing variables, modify depending on options	7			
	2.3	Commands for math operators	8			
	2.4	Genotypes	9			
	2.5	Ancestral allele frequencies	9			
	2.6	Wright's $F_{ m ST}$	10			
	2.7	Inbreeding coefficients	11			
	2.8	Kinship coefficients	11			
	2.9	Review of previous work	13			
	2.10	Convergence arrows	13			
		$F_{\rm ST}$ estimators for independent subpopulations	14			
		Estimators based on the standard kinship	14			
		New kinship and $F_{\rm ST}$ estimators	16			
		Estimates from Beagle	17			
		Measures of association and related problems	18			
		Cartoon genotype matrix	18			
3	Ack	nowledgments	19			

^{*}This document corresponds to kinshipsymbols v1.05, dated 2024/11/20.

Command	Symbol	Description
\xij	x_{ij}	Genotype
\x	\mathbf{x}_i	Genotype vector
\X	${f X}$	Genotype matrix
\pit	p_i^T	Ancestral allele frequency
\neq	\hat{p}_i^T	Sample p_i^T estimator
\kt	$oldsymbol{arphi}_{jk}^{T} \ oldsymbol{\Phi}^{T}$	Kinship coefficient
\kinMat	$\boldsymbol{\Phi}^T$	Kinship matrix
\ft	f_j^T	Inbreeding coefficient
\Fst	$F_{ m ST}^{'}$	(Wright's) Fixation index

Table 1: Commands for the most common statistical genetics quantities.

Command	Symbol	Description
\f{A}{B}	f_B^A	Inbreeding of pop. B relative to pop. A
\fl	$f_i^{L_j}$	Local inbreeding coefficient
\fs	$\widetilde{f}_{L_i}^T$	Structural inbreeding coefficient
\kl	$\varphi_{ik}^{L_{jk}}$	Local kinship coefficient
\ks	$f_{L_{jk}}^{T}$	Structural kinship coefficient
\fpw	$f_{L_j}^{L_{jk}}$	Individual pairwise $F_{\rm ST}$ component
\mav	$\overline{p(1-p)}^T$	Mean ancestral variance

Table 2: Commands for more rare statistical genetics quantities.

1 Introduction

This package provides macros for many common symbols involving the genotypes, kinship coefficients, and F_{ST} . Each of Tables 1 to 5 and 8 pairs a command to its symbol and its common description in the field. Note that these symbols work even when not in math mode, so it is not necessary to write Γ inline, Γ works! This is achieved through use of Γ use of Γ ...

Some of these symbols accept arguments for limited flexibility. For example, ξj produces x_{ij} , but ξj [k] produces x_{ik} . Similarly, \times produces φ_{jk}^T , but \times below for details for each command.

Additionally, Tables 6 and 7 lists some math operators and convergence arrows defined by this package (absent in amsmath). These commands do require math mode to work.

Lastly, the package provides \sampleGenMat, which generates the cartoon genotype table shown in Fig. 1. Note that this technically generates a "tabular" table. It is meant to be used in Beamer presentations, but works in standard documents too.

The effects of the package options color and noT are visualized in Figs. 2 to 5. Each of those figures generated the symbols with a particular combination of options:

Command	Symbol	Description
\ktHat	\hat{arphi}_{jk}^T	Unnamed kinship estimator
\ftHat	\hat{f}_i^T	Unnamed inbreeding estimator
\ktHatNamed{example}	$\hat{\varphi}_{jk}^{T, \text{example}}$	Named kinship estimator
\ftHatNamed{example}	$\hat{f}_j^{T, ext{example}}$	Named inbreeding estimator
\ktHatStd	$\hat{\varphi}_{jk}^{T,\mathrm{std}}$	Standard kinship estimator
\ftHatStd	$\hat{f}_{j}^{T,\mathrm{std}}$	Standard inbreeding estimator (I)
\ftHatStdII	$\hat{f}_i^{T,\mathrm{stdII}}$	Alternate inbreeding estimator (II)
\ftHatStdIII	$\hat{f}_i^{T, \mathrm{stdIII}}$	Alternate inbreeding estimator (III)
\ktHatNew	$\hat{\varphi}_{ik}^{T,\mathrm{new}}$	New kinship estimator
\ktHatNewMin	$\hat{arphi}_{\min}^{T,\mathrm{new}}$	Estimator of the asymptotic minimum $\hat{\varphi}_{jk}^{T,\text{new}}$
\ftHatNew	$\hat{f}^{T,\text{new}}$	New inbreeding estimator
\klHatBeagle	$\hat{\varphi}_{jk}^{L_{jk}, \text{beagle}}$	Beagle-based kinship estimator
\flHatBeagle	$\hat{f}_i^{L_j, \text{beagle}}$	Beagle-based inbreeding estimator
\Ajk	A_{jk}	New kinship-related statistic
\AMinHat	\hat{A}_{\min}	Estimator of the asymptotic minimum A_{jk}

Table 3: Commands for miscelaneous kinship and inbreeding estimators.

Command	Symbol	v -	
\FstHatSample	$\hat{F}_{\mathrm{ST},i}^{\mathrm{sample}}$	Sample F_{ST} estimator (one locus)	
\FstHat	$\hat{F}_{ ext{ST}}$	Unnamed F_{ST} estimator	
\FstHatNamed{example}	$\hat{F}_{ ext{ST}}^{ ext{example}}$	Named F_{ST} estimator	
\FstHatWc	$\hat{F}_{ ext{ST}}^{ ext{WC}}$	Weir-Cockerham $F_{\rm ST}$ estimator	
\FstHatHudson	$\hat{F}_{ ext{ST}}^{ ext{Hudson}}$	Hudson Pairwise $F_{\rm ST}$ estimator	
\FstHatHudsonK	$\hat{F}_{\mathrm{ST}}^{\mathrm{HudsonK}}$	Generalized Hudson F_{ST} estimator	
\FstHatIs	$\hat{F}_{\mathrm{ST}}^{\mathrm{indep}}$	Asymptotic $F_{\rm ST}$ estimator for indep. subpops.	
\FstHatStd	$\hat{\hat{F}}_{ ext{ST}}^{ ext{std}}$	Standard $F_{\rm ST}$ estimator (based on $\hat{\varphi}_{jk}^{T,{\rm std}}$)	
\P	$\hat{F}'_{ ext{ST}}$	Standard F_{ST} estimator adjusted 1	
\P	$\hat{F}_{ ext{ST}}^{\prime\prime}$	Standard F_{ST} estimator adjusted 2	
\FstHatNew	$\hat{F}_{ ext{ST}}^{ ext{new}}$	New $F_{\rm ST}$ estimator	

Table 4: Commands for miscelaneous $F_{\rm ST}$ estimators.

Command	Symbol	Description
\Fit	F_{IT}	Wright's total inbreeding
\Fis	$F_{ m IS}$	Wright's local inbreeding
\Gst	$G_{ m ST}$	Nei's genetic diversity measure
\GstPrime	$G'_{ m ST}$	Normalized $G_{\rm ST}$
\Rst	$R_{ m ST}$	$F_{\rm ST}$ estimator for microsatellites
\PhiSt	$\phi_{ m ST}$	AMOVA-based differentiation measure

Table 5: Commands for historical quantities in statistical genetics.

Command	Symbol	Description
\E	E	Expectation
\Var	Var	Variance
\Cov	Cov	Covariance
\round	round	Rounding function
\sgn	sgn	Sign function
\logit	logit	Logit function

Table 6: Commands for math operators.

Command	Symbol	Description
\toas	$\xrightarrow{\text{a.s.}} \xrightarrow{m \to \infty}$	Almost sure convergence as m goes to ∞
\toN	\longrightarrow	Limit as n goes to ∞
\toasNM	$\xrightarrow[n,m\to\infty]{n\to\infty}$	Almost sure convergence as both m and n go to ∞

Table 7: Commands for math convergence arrows.

Command	Symbol	Description
\srmsdp	$SRMSD_p$	Signed root mean square deviation for null p-values
\aucpr	$\mathrm{AUC}_{\mathrm{PR}}$	Area under the precision-recall curve

Table 8: Commands for miscelaneous measures.

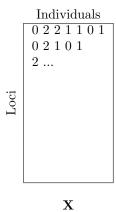


Figure 1: The cartoon genotype matrix generated by $\scalebox{sampleGenMat}$

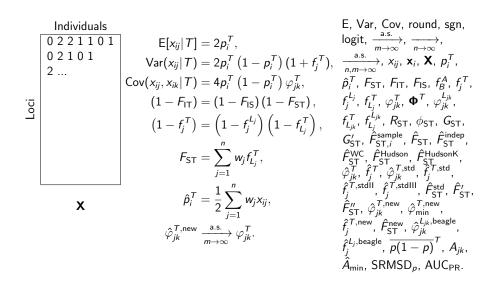


Figure 2: The vanilla version of the symbols (no colors and no omission of ancestral population T in superscripts

- Fig. 2: $\space{kinshipsymbols}$ "vanilla" version (no options). This version shows symbols completely (without omitting the ancestral population T from superscripts) and without color.
- Fig. 3: \usepackage[color]{kinshipsymbols} version. Same as the vanilla version except a few common symbols gain colors:
 - The genotypes $(x_{ij}, \mathbf{x}_i, \mathbf{X})$ become blue (and also the cartoon genotype matrix drawn by \sampleGenMat). Highlighted since this is the observed data from which inferences are drawn.
 - The kinship coefficients (φ_{jk}^T, Φ^T) become dark green. Highlighted since these are the main unknown parameters we wish to estimate.
 - The standard ancestral allele frequency estimator (\hat{p}_i^T) becomes red. Highlighted since this is a particularly problematic estimator that leads to biases in common approaches.
- Fig. 4: \usepackage[noT] {kinshipsymbols} version. Same as the vanilla version except the ancestral population T is omitted in the superscript of several symbols $(p_i^T, \, \hat{p}_i^T, \, f_j^T, \, f_{L_j}^T, \, \varphi_{jk}^T, \, \Phi^T, \, f_{L_{jk}}^T, \, \hat{\varphi}_{jk}^T, \, \hat{f}_j^T, \, \hat{\varphi}_{jk}^{T,\mathrm{std}}, \, \hat{f}_j^{T,\mathrm{std}}, \, \hat{f}_j^{T,\mathrm{std}}, \, \hat{f}_j^{T,\mathrm{new}}, \, \hat{\varphi}_{\min}^{T,\mathrm{new}}, \, \hat{f}_j^{T,\mathrm{new}}, \, \text{and} \, \overline{p(1-p)}^T)$. This option is provided to simplify the heavy notation in a context where T is implicit or fixed.
- Fig. 5: \usepackage[color,noT]{kinshipsymbols} version. A straightforward combination of the color and noT options described above.

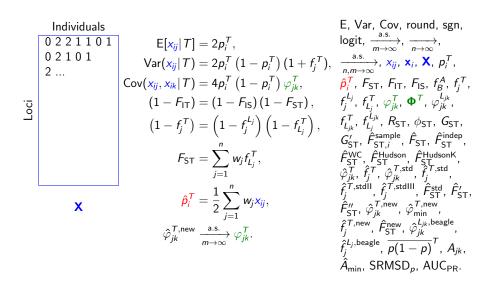


Figure 3: The $\operatorname{\mathtt{color}}$ version of the symbols (with no omission of ancestral population T in superscripts

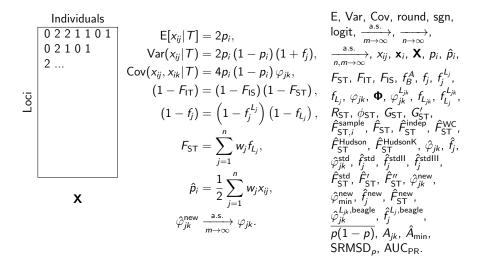


Figure 4: The ${\tt noT}$ version of the symbols (no color, with omission of ancestral population T in superscripts as appropriate

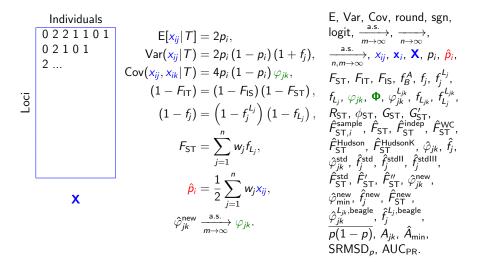


Figure 5: The color,noT version of the symbols (with color and omission of ancestral population T in superscripts as appropriate

2 Implementation

2.1 Dependencies

This package requires amsmath to define the various math symbols and operators, xspace to allow inline math symbols to have appropriate spacings when used outside math mode, xcolor for color management and tricks, and colortbl and multirow for the cartoon genotype matrix.

- 1 \RequirePackage{amsmath}
- 2 \RequirePackage{xspace}
- 3 \RequirePackage{xcolor}
- 4 \RequirePackage{colortbl}
- 5 \RequirePackage{multirow}

2.2 Initializing variables, modify depending on options

Then we define the special colors we want to use (in a way that is easy to tweak later if needed).

\ifcolor LaTeX boolean for whether color option is on or off.

- 6 \newif\ifcolor%
- 7 \colorfalse% default is false

genColor The hardcoded "genotype color" is blue, applied if the color package option is

8 \colorlet{genColor}{blue}

kinColor The hardcoded "kinship color" is a dark green, applied if the color package option is set.

```
9 \colorlet{kinColor}{green!50!black}
```

We also define two tricky commands to handle the ancestra population T superscript that we want to optionally omit. Note that these are internal commands not meant to be used directly outside the package.

 $\$ This is a basic superscript T that becomes blank if the noT package option is set.

11 \newcommand{\kinshipsymbols@T}{^T}

\kinshipsymbols@Ts This is a second superscript T which takes a mandatory argument that is shown next to it as text. Only the T becomes blank if the noT package option is set (the argument is shown alone as a text superscript in that case).

12 \newcommand{\kinshipsymbols@Ts}[1]{^{T,\text{#1}}}

This turns on colors if the color package option is set.

- 14 \colortrue
- 15 }

Similarly, this updates the commands to omit the T superscript if the noT package option is set. Note that the second command still emits the additional text passed as argument in the superscript.

- 16 \DeclareOption{noT}{
- 17 \renewcommand{\kinshipsymbols@T}{}
- 18 \renewcommand{\kinshipsymbols@Ts}[1]{^{\text{#1}}}

19 }

This creates a warning if any additional options are passed, then processes the options.

- 20 \DeclareOption*{\PackageWarning{examplepackage}{Unknown '\CurrentOption'}}
- 21 \ProcessOptions\relax

2.3 Commands for math operators

Here we define some trivial widely-used operators, which are not specific to statistical genetics but which are absent from the standard amsmath package.

\E Expectation of a random variable.

 $22 \DeclareMathOperator{\E}{E}$

\Var Variance of a random variable.

23 \DeclareMathOperator{\Var}{Var}

\Cov Covariance of a random variable.

 $24 \label{locale} \ensuremath{\texttt{Operator}} \ensuremath{\texttt{Cov}} \ensuremath{\texttt{Cov}} \ensuremath{\texttt{Cov}} \ensuremath{\texttt{Acov}} \ensuremath{\texttt{Cov}} \ensuremath{\texttt{Acov}} \ensuremath{\texttt{Cov}} \ensuremath{\texttt{Cov}} \ensuremath{\texttt{Acov}} \ensuremath{\texttt{Cov}} \ensuremath{\texttt{Acov}} \ensuremath{\texttt$

\round The rounding function.

25 \DeclareMathOperator{\round}{round}

```
\sgn The sign function.

26 \DeclareMathOperator{\sgn}{sgn}

\logit The logit function.

27 \DeclareMathOperator{\logit}{logit}
```

2.4 Genotypes

\xij x_{ij} : Genotype variable at locus i of individual j (default). The optional argument allows setting other individuals (\xij[k] gives x_{ik} for individual k). If the package option color is passed, then this symbol turns the color genColor (default blue).

```
28 \newcommand{\xij}[1][j]{%
29 \ensuremath{%
30 \ifcolor \textcolor{genColor}{ \fi%
31    x_{i#1}%
32 \ifcolor } \fi%
33 }%
34 \xspace%
35 }%
```

 \mathbf{x}_i : Genotype vector at locus i (default). The optional argument allows setting other loci ($\mathbf{x}[i']$ gives $\mathbf{x}_{i'}$ for locus i'). If the package option color is passed, then this symbol turns the color genColor (default blue).

```
36 \newcommand{\x}[1][i]{%
37 \ensuremath{%
38 \ifcolor \textcolor{genColor}{ \fi%
39 \mathbf{x}_{#1}%
40 \ifcolor } \fi%
41 }%
42 \xspace%
43 }%
```

XX: Genotype matrix. If the package option color is passed, then this symbol turns the color genColor (default blue).

```
44 \newcommand{\X}{%
45 \ensuremath{%
46 \ifcolor \textcolor{genColor}{ \fi%
47 \mathbf{X}}%
48 \ifcolor } \fi%
49 }%
50 \xspace%
51}%
```

2.5 Ancestral allele frequencies

\pit p_i^T : The ancestral allele frequency at locus i (default). The optional argument allows setting other loci (\pit[i'] gives $p_{i'}^T$ for locus i'). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
52 \newcommand{\pit}[1][i]{%

53 \ensuremath{%

54 p_{#1}\kinshipsymbols@T%
```

```
55 }%
56 \xspace%
57 }%
```

\pith \hat{p}_i^T : The sample estimator of the ancestral allele frequency at locus i (default). The optional argument allows setting other loci (\pith[i'] gives $\hat{p}_{i'}^T$ for locus i'). The parameter being estimated has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed. If the package option color is passed, then this symbol turns the color pithColor (default red).

```
58 \newcommand{\pith}[1][i]{%
59 \ensuremath{%
60 \ifcolor \textcolor{pithColor}{ \fi%
61 \hat{p}_{#1}\kinshipsymbols@T%
62 \ifcolor } \fi%
63 }%
64 \xspace%
65}%
```

2.6 Wright's F_{ST}

\Fst F_{ST} : Wright's Fixation index. Although the T in the subscript technically refers to the ancestral population T, in this case it is never omitted (even if the package option noT is passed) to always match the more traditional and highly recognizable notation.

```
66 \newcommand{\Fst}{%
67 \ensuremath{%
68     F_{\text{ST}}}%
69    }%
70 \xspace%
71 }%
```

\Fit F_{IT} : Wright's total inbreeding coefficient. Although the T in the subscript technically refers to the ancestral population T, in this case it is never omitted (even if the package option noT is passed) to always match the more traditional and highly recognizable notation.

```
72 \newcommand{\Fit}{%
73 \ensuremath{%
74 F_{\text{IT}}}%
75 }%
76 \xspace%
77 }%
```

\Fis $F_{\rm IS}$: Wright's local inbreeding coefficient.

```
78 \newcommand{\Fis}{%
79 \ensuremath{%
80 F_{\text{IS}}%
81 }%
82 \xspace%
83 }%
```

2.7 Inbreeding coefficients

\f f_B^A : The inbreeding coefficient (of F_{ST}) of population B relative to an ancestral population A. Note that this command has two mandatory arguments.

```
84 \newcommand{\f}[2]{%

85 \ensuremath{\%}

86 f^{\#1}_{\#2}\%

87 }\%

88 \xspace\%

89 }\%
```

\ft f_j^T : The (total) inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\ft[k] gives f_k^T for individual k). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
90 \newcommand{\ft}[1][j]{%
91 \ensuremath{%
92  f_{#1}\kinshipsymbols@T%
93 }%
94 \xspace%
95 }%
```

\fl $f_j^{L_j}$: The local inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\fl[k] gives $f_k^{L_k}$ for individual k).

```
96 \newcommand{\f1}[1][j]{%
97 \ensuremath{%
98  f_{#1}^{L_{#1}}%
99  }%
100 \xspace%
101 }%
```

\fs $f_{L_j}^T$: The structural inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\fs[k] gives $f_{L_k}^T$ for individual k). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
102 \newcommand{\fs}[1][j]{%
103 \ensuremath{%
104 f_{L_{#1}}\kinshipsymbols@T%
105 }%
106 \xspace%
107 }%
```

2.8 Kinship coefficients

\kt φ_{jk}^T : The (total) kinship coefficient between the pair of individuals j and k (default). The optional argument allows setting another second individual (\kt[1] gives φ_{jl}^T for a second individual l). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed. If the package option color is passed, then this symbol turns the color kinColor (default dark green).

```
108 \newcommand{\kt}[1][k]{%
109 \ensuremath{%
110 \ifcolor \textcolor{kinColor}{ \fi%
111 \varphi_{j#1}\kinshipsymbols@T%
112 \ifcolor } \fi%
113 }%
114 \xspace%
115 }%
```

\kinMat Φ^T : The matrix of (total) kinship coefficients between every pair of individuals. This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed. If the package option color is passed, then this symbol turns the color kinColor (default dark green).

```
116 \newcommand{\kinMat}{%
    117
          \ensuremath{%
    118
            \ifcolor \textcolor{kinColor}{ \fi%
    119
              \boldsymbol{\Phi}\kinshipsymbols@T%
    120
            \ifcolor } \fi%
    121
         }%
    122
          \xspace%
    123 }%
\kl \varphi_{jk}^{L_{jk}}: The local kinship coefficient between the pair of individuals j and k.
    124 \newcommand{\kl}{%
         \ensuremath{%
           126
    127
         \xspace%
    128
```

\ks $f_{L_{jk}}^T$: The structural kinship coefficient between the pair of individuals j and k. This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
130 \newcommand{\ks}{%
131 \ensuremath{%
132 f_{L_{jk}}\kinshipsymbols@T%
133 }%
134 \xspace%
135 }%
```

129 }%

\fpw $f_{L_j}^{L_{jk}}$: A component of the pairwise $F_{\rm ST}$ between a pair of individuals j and k (default). The optional argument changes the individual in the subscript only (so \fpw[k] gives $f_{L_k}^{L_{jk}}$, and is obviously intended to be used for k only). Note that the actual pairwise $F_{\rm ST}$ between j and k is given by the average of $f_{L_j}^{L_{jk}}$ and $f_{L_k}^{L_{jk}}$.

```
136 \newcommand{\fpw}[1][j]{%
137 \f{L_{jk}}{L_{#1}}%
138 }%
```

2.9 Review of previous work

```
\Rst R_{ST}: An F_{ST} estimator developed for microsatellites.
                139 \newcommand{\Rst}{%
                      \ensuremath{%
                141
                        R_{\text{st}}%
                142
                      }%
                143
                     \xspace%
                144 }%
        \PhiSt \phi_{ST}: An F_{ST}-like estimate based on AMOVA.
                145 \newcommand{\PhiSt}{%
                      \ensuremath{%
                147
                         \phi_{\text{ST}}%
                      }%
                148
                149
                      \xspace%
                150 }%
          \Gst G_{ST}: Nei's genetic diversity measure.
                151 \newcommand{\Gst}{%
                152 \ensuremath{%
                153
                        G_{\text{st}}%
                154
                155 \xspace%
     \GstPrime G'_{ST}: A normalized G_{ST} statistic.
                157 \newcommand{\GstPrime}{%
                158 \ensuremath{%
                      G_{\text{st}}, \
                160 }%
                161
                     \xspace%
                162 }%
\FstHatSample \hat{F}^{\text{sample}}_{\text{ST},i}: A sample F_{\text{ST}} estimator for a single locus i.
                163 \newcommand{\FstHatSample}{%
                     \ensuremath{%
                         \hat{F}_{\text{ST},i}^{\text{sample}}%
                166 }%
                      \xspace%
                167
                168 }%
                2.10
                          Convergence arrows
         \toas \xrightarrow[m \to \infty]{\text{a.s.}}: Almost sure convergence as m goes to \infty. Optional argument changes
                the variable name (\frac{a.s.}{n\to\infty}).
                169 \newcommand{\toas}[1][m]{%
                170 \xrightarrow[#1 \rightarrow \infty]{\text{a.s.}}
                171 }%
          \toN \xrightarrow[n\to\infty]{}: The limit as n goes to \infty. Optional argument changes the variable name
                n \to \infty ($\toN[m]$ gives \xrightarrow{m \to \infty}).
```

```
172 \newcommand{\toN}[1][n]{%
                  173 \xrightarrow[#1 \rightarrow \infty]{}%
        \toasNM \xrightarrow[n,m\to\infty]{\text{a.s.}}: Almost sure convergence as both n and m go to \infty.
                  175 \newcommand{\toasNM}{%
                  176 \xrightarrow[n,m \rightarrow \infty]{\text{a.s.}}%
                  177 }%
                  2.11
                           F_{ST} estimators for independent subpopulations
        \FstHat \hat{F}_{ST}: Unnamed F_{ST} estimator.
                  178 \newcommand{\FstHat}{%
                        \ensuremath{%
                          \hat{F}_{\text{ST}}%
                  182
                       \xspace%
                  183 }%
  \FstHatNamed \hat{F}_{\mathrm{ST}}^{\mathrm{example}}: Base command for a named F_{\mathrm{ST}} estimator. Takes on one mandatory
                  argument—the name of the estimator—which is rendered as text.
                  184 \newcommand{\FstHatNamed}[1]{%
                  185 \ensuremath{%
                         \hat{F}_{\text{ST}}^{\text{text}ST}}^{\text{text}\#1}}%
                  186
                  187
                       }%
                  188
                        \xspace%
                  189 }%
      \FstHatIs \hat{F}_{\text{ST}}^{\text{indep}}: Asymptotic F_{\text{ST}} estimator for independent subpopulations.
                  190 \newcommand{\FstHatIs}{\FstHatNamed{indep}}
      \FstHatWc \hat{F}_{\mathrm{ST}}^{\mathrm{WC}}: Weir-Cockerham F_{\mathrm{ST}} estimator.
                  191 \newcommand{\FstHatWc}{\FstHatNamed{WC}}
 \FstHatHudson \hat{F}_{ST}^{Hudson}: Hudson pairwise F_{ST} estimator.
                  192 \newcommand{\FstHatHudson}{\FstHatNamed{Hudson}}
\FstHatHudsonK \hat{F}_{ST}^{HudsonK}: Generalized Hudson F_{ST} estimator (for K subpopulations).
                  193 \newcommand{\FstHatHudsonK}{\FstHatNamed{HudsonK}}
```

2.12 Estimators based on the standard kinship

\ktHat $\hat{\varphi}_{jk}^T$: An unnamed kinship estimator for individuals j and k (default). The optional argument allows setting another second individual (\ktHat[1] gives $\hat{\varphi}_{jl}^T$ for a second individual l). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
194 \newcommand{\ktHat}[1][k]{%
195 \ensuremath{%
196 \hat{\varphi}_{j#1}\kinshipsymbols@T%
197 }%
198 \xspace%
199 }%
```

\ktHatNamed $\hat{\varphi}_{jk}^{T,\text{example}}$: A generic named kinship estimator for individuals j and k (default). Mandatory argument is the name, rendered as text. The optional argument allows setting another second individual (\ktHatNamed[1]{example} gives $\hat{\varphi}_{jl}^{T,\text{example}}$ for a second individual l). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
200 \newcommand{\ktHatNamed}[2][k]{%
201 \ensuremath{%
202 \hat{\varphi}_{j#1}\kinshipsymbols@Ts{#2}%
203 }%
204 \xspace%
205 }%
```

\ktHatStd $\hat{\varphi}_{jk}^{T,\mathrm{std}}$: Standard kinship estimator for individuals j and k (default). The optional argument allows setting another second individual (\ktHatStd[1] gives $\hat{\varphi}_{jl}^{T,\mathrm{std}}$ for a second individual l). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

206 \newcommand{\ktHatStd}[1][k]{\ktHatNamed[#1]{std}}

\ftHat \hat{f}_j^T : Unnamed inbreeding coefficient estimator for individual j (default). The optional argument allows setting another individual (\ftHat[k] gives \hat{f}_k^T for individual k). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
207 \newcommand{\ftHat}[1][j]{%
208 \ensuremath{%
209 \hat{f}_{#1}\kinshipsymbols@T%
210 }%
211 \xspace%
212 }%
```

\ftHatNamed $\hat{f}_j^{T,\text{example}}$: Named inbreeding coefficient estimator for individual j (default). Mandatory argument is the name, rendered as text. The optional argument allows setting another individual (\ftHatNamed[k]{example} gives $\hat{f}_k^{T,\text{example}}$ for individual k). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
213 \newcommand{\ftHatNamed}[2][j]{%
214 \ensuremath{%
215 \hat{f}_{#1}\kinshipsymbols@Ts{#2}%
216 }%
217 \xspace%
```

\ftHatStd $\hat{f}_j^{T,\mathrm{std}}$: Standard inbreeding coefficient estimator (I) for individual j. The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

219 \newcommand{\ftHatStd}{\ftHatNamed{std}}

```
mated parameter has a value that depends on the ancestral population T, which
                     is by default denoted in the superscript, but which gets omitted if the package
                     option noT is passed.
                      220 \newcommand{\ftHatStdII}{\ftHatNamed{stdII}}
      \ftHatStdIII \hat{f}_i^{T,\text{stdIII}}: Alternate inbreeding coefficient estimator (III) for individual j. The
                     estimated parameter has a value that depends on the ancestral population T,
                      which is by default denoted in the superscript, but which gets omitted if the
                     package option noT is passed.
                      221 \newcommand{\ftHatStdIII}{\ftHatNamed{stdIII}}
         \FstHatStd \hat{F}_{ST}^{std}: Standard F_{ST} estimator (based on the standard kinship estimator).
                      222 \newcommand{\FstHatStd}{\FstHatNamed{std}}
   \FstHatStdPrime \hat{F}'_{ST}: Standard F_{ST} estimator adjusted 1.
                     223 \mbox{newcommand{\FstHatStdPrime}{}}
                     224
                           \ensuremath{%
                              \hat{F}_{\text{st}}'
                      227
                           \xspace%
                     228 }%
\FstHatStdPrimeDbl \hat{F}_{ST}^{"}: Standard F_{ST} estimator adjusted 2.
                     229 \newcommand{\FstHatStdPrimeDbl}{%
                           \ensuremath{%
                              \hat{F}_{\text{ST}}''%
                     231
                          \xspace%
                     234 }%
                      2.13
                              New kinship and F_{ST} estimators
          \ktHatNew \hat{\varphi}_{ik}^{T,\text{new}}: New kinship estimator for the pair of individuals j and k (default). The
                     optional argument allows setting another second individual (\ktHatNew[1] gives
                     \hat{\varphi}_{il}^{T,\text{new}} for a second individual l). The estimated parameter has a value that
                     depends on the ancestral population T, which is by default denoted in the super-
                     script, but which gets omitted if the package option noT is passed.
                      235 \newcommand{\ktHatNew}[1][k]{\ktHatNamed[#1]{new}}
      \ktHatNewMin \hat{\varphi}_{\min}^{T,\text{new}}: Estimator of the limit of the minimum value of the expectation of \hat{\varphi}_{jk}^{T,\text{new}}
                     across all pairs of individuals. The estimated parameter has a value that depends
```

\ftHatStdII $\hat{f}_i^{T, \text{stdII}}$: Alternate inbreeding coefficient estimator (II) for individual j. The estimator

on the ancestral population T, which is by default denoted in the superscript, but

\hat{\varphi}_{\text{min}}\kinshipsymbols@Ts{new}%

which gets omitted if the package option noT is passed.

236 \newcommand{\ktHatNewMin}{%

\ensuremath{%

\xspace%

237

238

 $\frac{239}{240}$

241 }%

\ftHatNew $\hat{f}_j^{T,\text{new}}$: New inbreeding estimator for individual j (default). The optional argument allows setting other individuals (\ftHatNew[k] gives $\hat{f}_k^{T,\text{new}}$ for individual k). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

242 \newcommand{\ftHatNew}[1][j]{\ftHatNamed[#1]{new}}

\FstHatNew \hat{F}_{ST}^{new} : New F_{ST} estimator.

243 $\mbox{newcommand{\FstHatNew}{\FstHatNamed{new}}}$

\Ajk A_{jk} : A new statistic proportional in expectation to $\varphi_{jk}^T - 1$ for the pair of individuals j and k (default). The optional argument allows setting another second individual (\Ajk[1] gives A_{jl} for a second individual l).

```
244 \newcommand{\Ajk}[1][k]{%
245 \ensuremath{%
246 A_{j#1}%
247 }%
248 \xspace%
249 }%
```

\AMinHat \hat{A}_{min} : Estimator of the limit of the minimum value of the expectation of A_{jk} across all pairs of individuals.

```
250 \newcommand{\AMinHat}{%

251 \ensuremath{%

252 \hat{A}_{\text{min}}}%

253 }%

254 \xspace%

255 }%
```

\AAvgHat \hat{A}_{avg} : Estimator of the limit of the average value of the expectation of A_{jk} across all pairs of individuals.

```
256 \newcommand{\AAvgHat}{%

257 \ensuremath{%

258 \hat{A}_{\text{avg}}}%

259 }%

260 \xspace%

261 }%
```

\max $\overline{p(1-p)}^T$: Mean ancestral variance. This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
262 \newcommand{\mav}{%
263 \ensuremath{%
264 \overline{p(1-p)}\kinshipsymbols@T%
265 }%
266 \xspace%
267 }%
```

2.14 Estimates from Beagle

\klHatBeagle $\hat{\varphi}_{jk}^{L_{jk},\text{beagle}}$: Local kinship estimator based on Beagle, for the pair of individuals j and k.

```
268 \newcommand{\klHatBeagle}{%
                    \ensuremath{%
               269
                       \hat{\varphi}_{jk}^{L_{jk},\text{beagle}}%
               270
               271
               272
                     \xspace%
               273 }%
\flatBeagle \hat{f}_i^{L_j, \text{beagle}}: Local inbreeding estimator based on Beagle, for individual j (default).
               The optional argument allows setting other individuals (\flHatBeagle[k] gives
               \hat{f}_k^{L_k,\text{beagle}} for individual k).
               274 \newcommand{\flHatBeagle}[1][j]{%
                     \ensuremath{%
               275
               276
                       \hat{f}_{\#1}^{L_{\#1}}, \text{beagle}}%
               277
               278
                     \xspace%
               279 }%
```

2.15 Measures of association and related problems

 $\S RMSD_p$: The Signed Root Mean Square Deviation (SRMSD) of null p-values from their expectation that they have uniform quantiles.

```
280 \newcommand{\srmsdp}{%

281 \ensuremath{%

282 \text{SRMSD}_p%

283 }%

284 \xspace%

285 }%
```

\aucpr AUC_{PR}: The Area Under the Curve (AUC) for precision-recall (PR) curves, which is a proxy measure for calibrated power.

```
286 \newcommand{\aucpr}{%
287 \ensuremath{%
288 \text{AUC}_\text{PR}%
289 }%
290 \xspace%
291 }%
```

2.16 Cartoon genotype matrix

I use this cartoon genotype matrix often in Beamer presentations. Unfortunately I also use the color kinshipsymbols package option in my presentations, but due to a strange bug the colors do not show up in Beamer. This solution was found online: https://tex.stackexchange.com/questions/159378/cline-disappears-in-beamer

```
292 % after package colortbl is loaded
293 \makeatletter
294 \@ifclassloaded{beamer}{%
295 \patchcmd\@cline
296 {\arrayrulewidth\hfill}% search
297 {\arrayrulewidth\hfill\kern\z@}% replace
298 {}% success
299 {\errmessage{Patching \string\@cline\space failed}}% failure
```

```
300 }{%
                301
                     % nothing to do here?
                302 }
                303 \makeatother
\sampleGenMat This is the bulky code used to generate the cartoon genotype matrix shown in
                304 \newcommand{\sampleGenMat}{%
                305
                      \begin{tabular}{cc}%
                        & Individuals \\%
                306
                        \ifcolor \arrayrulecolor{genColor} \fi% % gets applied to whole table
                307
                        \cline{2-2}%
                308
                        \label{loci} $$\mathbf{10}_{*}{\operatorname{loci}}% $$\operatorname{corigin=c}_{90}_{Loci}% $$\operatorname{corigin=c}_{90}_{Loci}% $$
                309
                        & \mathcal{1}_{|1|}_{0 2 2 1 1 0 1} \
                310
                          \multicolumn{1}{|1|}{0 2 1 0 1 } \\%
                311
                          \multicolumn{1}{|1|}{2 ...} \\%
                312
                        & \multicolumn{1}{||1|}{ } \\%
                313
                        & \multicolumn{1}{||1|}{ } \\%
                314
                        & \multicolumn{1}{||1|}{ } \\%
                315
                316
                        & \multicolumn{1}{|1|}{ } \\%
                317
                        & \multicolumn{1}{||1|}{ } \\%
                        & \multicolumn{1}{|1|}{ } \\%
                318
                        & \multicolumn{1}{||1|}{ } \\%
                319
                        \cline{2-2}%
                320
                        & \\%
                321
                        & \X \\%
                322
                      \end{tabular}%
                323
                324 }%
```

3 Acknowledgments

The symbols in this package were originally designed with John D. Storey (Alex Ochoa's postdoctoral adviser and coauthor of several papers about kinship and $F_{\rm ST}$).

The package was written following Scott Pakin's guide How to Package Your LATEX package.

Change History

```
\hat{\varphi}_{jk}^{T}, and \hat{f}_{j}^{T} symbols (without
v1.00
                                                                          estimator name) ..... 1
     General: Initial version
                                                                v1.04
     General: Added NEWS,
                                                                     General: Added option to change variable name in \xrightarrow[m \to \infty]{\text{a.s.}} \dots \dots 1
          README, and symbols A_{ik},
          \hat{A}_{\text{avg}}, and *Std versions . . . . . . 1
                                                                v1.05
v1.02
     General: Added \hat{\varphi}_{\min}^{T,\text{new}} symbol . . . 1
                                                                     General: Added \mathbf{\Phi}^T, \mathbf{x}_i, \mathbf{X},
v1.03
                                                                          SRMSD_p, AUC_{PR}, and locus
                                                                          subscript options for p_i^T, \hat{p}_i^T. . . 1
     General: Added unnamed \hat{F}_{ST},
```

Index

Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; numbers in roman refer to the code lines where the entry is used.

A \AAvgHat 256 \Ajk 244 \AMinHat 250 \aucpr 286 B \boldsymbol 119	\FstHatStdPrime	\ktHatNewMin
C \colorfalse	\ftHatStd	$\begin{array}{c} N \\ \text{\ \ Newif\ } \dots \dots \ \ 6 \end{array}$
E \E 22 F	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	\Phi
\f	\ifcolor <u>6</u> , 30, 32, 38, 40, 46, 48, 60, 62, 110, 112, 118, 120, 307	R \round 25 \Rst 139
\Fis	K \kinColor 9 \kinMat 116 \kinshipsymbols@T 11,	S \sampleGenMat 304 \sgn 26 \srmsdp 280
\fs	$\begin{array}{c} 17,\ 54,\ 61,\ 92,\\ 104,\ 111,\ 119,\\ 132,\ 196,\ 209,\ 264\\ \\ \verb+\kinshipsymbols@Ts .\\ \underline{12},18,202,215,238\\ \end{array}$	T \toas
\FstHatIs	\k1	$\begin{array}{c} V \\ \texttt{Var} \ \ldots \ \ldots \ \underline{23} \\ X \end{array}$
$\begin{tabular}{lllllllllllllllllllllllllllllllllll$	\ktHat\named \frac{200}{206}, 206, 235 \ktHat\named \frac{235}{235}	$\begin{array}{cccccccccccccccccccccccccccccccccccc$