# The kinshipsymbols package\*

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#### Abstract

This package defines consistent mathematical symbols for statistical genetics, particularly relating to the kinship model and  $F_{\rm ST}$ . In addition to providing a long list of symbols, the package has two options that alter the behavior of some of the most common symbols. Option color highlights genotypes (blue), kinship coefficients (dark green), and the standard ancestral allele frequency estimator (red), which is useful for Beamer presentations. Option noT removes the ancestral population T superscript from all symbols that contain it (for simpler presentations).

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<sup>\*</sup>This document corresponds to kinship symbols v1.02, dated 2020/05/14.

| Command | Symbol          | Description                |
|---------|-----------------|----------------------------|
| \xij    | $x_{ij}$        | Genotype                   |
| \pit    | $p_i^T$         | Ancestral allele frequency |
| \pith   | $\hat{p}_i^T$   | Sample $p_i^T$ estimator   |
| \kt     | $arphi_{jk}^T$  | Kinship coefficient        |
| \ft     | $f_i^T$         | Inbreeding coefficient     |
| \Fst    | $ec{F_{ m ST}}$ | (Wright's) Fixation index  |

Table 1: Commands for the most common statistical genetics quantities.

| Command  | Symbol                  | Description                                 |
|----------|-------------------------|---|
| \f{A}{B} | $f_B^A$                 | Inbreeding of pop. $B$ relative to pop. $A$ |
| \fl      | $f_i^{L_j}$             | Local inbreeding coefficient                |
| \fs      | $\widetilde{f}_{L_i}^T$ | Structural inbreeding coefficient           |
| \kl      | $\varphi_{jk}^{L_{jk}}$ | Local kinship coefficient                   |
| \ks      | $f_{L_{jk}}^{T}$        | Structural kinship coefficient              |
| \fpw     | $f_{L_j}^{L_{jk}}$      | Individual pairwise $F_{\rm ST}$ component  |
| \mav     | $\overline{p(1-p)}^T$   | Mean ancestral variance                     |

Table 2: Commands for more rare statistical genetics quantities.

#### 1 Introduction

This package provides macros for many common symbols involving the genotypes, kinship coefficients, and  $F_{ST}$ . Each of Tables 1 to 5 pairs a command to its symbol and its common description in the field. Note that these symbols work even when not in math mode, so it is not necessary to write  $f_{ST}$  inline,  $f_{ST}$  works! This is achieved through use of  $e_{ST}$  achieved through use of  $e_{ST}$ .

Some of these symbols accept arguments for limited flexibility. For example,  $\xij$  produces  $x_{ij}$ , but  $\xij$ [k] produces  $x_{ik}$ . Similarly,  $\times$  produces  $\varphi_{jk}^T$ , but  $\times$  below for details for each command.

Additionally, Tables 6 and 7 lists some math operators and convergence arrows defined by this package (absent in amsmath). These commands do require math mode to work.

Lastly, the package provides \sampleGenMat, which generates the cartoon genotype table shown in Fig. 1. Note that this technically generates a "tabular" table. It is meant to be used in Beamer presentations, but works in standard documents too.

The effects of the package options color and noT are visualized in Figs. 2 to 5. Each of those figures generated the symbols with a particular combination of options:

| Command              | Symbol                                       | Description   |  |
|----------------------|--|---|--|
| \ktHatNamed{example} | $\hat{\varphi}_{jk}^{T, \text{example}}$     | Named kinship estimator   |  |
| \ftHatNamed{example} | $\hat{f}_{j}^{T, \text{example}}$            | Named inbreeding estimator  |  |
| \ktHatStd            | $\hat{\varphi}_{jk}^{T,\mathrm{std}}$        | Standard kinship estimator  |  |
| \ftHatStd            | $\hat{f}_{j}^{T,\mathrm{std}}$               | Standard inbreeding estimator (I)                                       |  |
| \ftHatStdII          | $\hat{f}_j^{T,\mathrm{stdII}}$               | Alternate inbreeding estimator (II)                                     |  |
| \ftHatStdIII         | $\hat{f}_{j}^{T,\mathrm{stdIII}}$            | Alternate inbreeding estimator (III)                                    |  |
| \ktHatNew            | $\hat{arphi}_{jk}^{T,\mathrm{new}}$          | New kinship estimator   |  |
| \ktHatNewMin         | $\hat{arphi}_{\min}^{T,	ext{new}}$           | Estimator of the asymptotic minimum $\hat{\varphi}_{jk}^{T,\text{new}}$ |  |
| \ftHatNew            | $\hat{f}_{j}^{T,\mathrm{new}}$               | New inbreeding estimator  |  |
| \klHatBeagle         | $\hat{\varphi}_{jk}^{L_{jk}, \text{beagle}}$ | Beagle-based kinship estimator  |  |
| \flHatBeagle         | $\hat{f}_i^{L_j, \text{beagle}}$             | Beagle-based inbreeding estimator                                       |  |
| \Ajk                 | $A_{jk}$                                     | New kinship-related statistic   |  |
| \AMinHat             | $\hat{A}_{\min}$                             | Estimator of the asymptotic minimum $A_{jk}$                            |  |

Table 3: Commands for miscelaneous kinship and inbreeding estimators.

| Command               | Symbol                                      | Description   |  |
|-----------------------|---|---|--|
| \FstHatSample         | $\hat{F}_{\mathrm{ST},i}^{\mathrm{sample}}$ | Sample $F_{ST}$ estimator (one locus)   |  |
| \FstHatNamed{example} | $\hat{F}_{\mathrm{ST}}^{\mathrm{example}}$  | Named $F_{ST}$ estimator  |  |
| \FstHatWc             | $\hat{F}_{	ext{ST}}^{	ext{WC}}$             | Weir-Cockerham $F_{\rm ST}$ estimator   |  |
| \FstHatHudson         | $\hat{F}_{	ext{ST}}^{	ext{Hudson}}$         | Hudson Pairwise $F_{\rm ST}$ estimator  |  |
| \FstHatHudsonK        | $\hat{F}_{\mathrm{ST}}^{\mathrm{HudsonK}}$  | Generalized Hudson $F_{\rm ST}$ estimator                                     |  |
| \FstHatIs             | $\hat{F}_{	ext{ST}}^{	ext{indep}}$          | Asymptotic $F_{ST}$ estimator for indep. subpops.                             |  |
| \FstHatStd            | $\hat{F}_{	ext{ST}}^{	ext{std}}$            | Standard $F_{\rm ST}$ estimator (based on $\hat{\varphi}_{jk}^{T, \rm std}$ ) |  |
| $\P$                  | $\hat{F}'_{	ext{ST}}$                       | Standard $F_{ST}$ estimator adjusted 1  |  |
| $\P$                  | $\hat{F}_{	ext{ST}}^{\prime\prime}$         | Standard $F_{\rm ST}$ estimator adjusted 2                                    |  |
| \FstHatNew            | $\hat{F}_{	ext{ST}}^{	ext{new}}$            | New $F_{\rm ST}$ estimator  |  |

Table 4: Commands for miscelaneous  $F_{\mathrm{ST}}$  estimators.

| Command     | Symbol            | Description                                |
|-------------|-------------------|--|
| \Fit        | $F_{\mathrm{IT}}$ | Wright's total inbreeding                  |
| \Fis        | $F_{ m IS}$       | Wright's local inbreeding                  |
| \Gst        | $G_{ m ST}$       | Nei's genetic diversity measure            |
| $\GstPrime$ | $G'_{ m ST}$      | Normalized $G_{\rm ST}$                    |
| \Rst        | $R_{ m ST}$       | $F_{\rm ST}$ estimator for microsatellites |
| \PhiSt      | $\phi_{ m ST}$    | AMOVA-based differentiation measure        |

Table 5: Commands for historical quantities in statistical genetics.

| Command | Symbol               | Description       |  |
|---------|----------------------|-------------------|--|
| \E      | Е                    | Expectation       |  |
| \Var    | Var                  | Variance          |  |
| \Cov    | Cov                  | Covariance        |  |
| \round  | round                | Rounding function |  |
| \sgn    | $\operatorname{sgn}$ | Sign function     |  |
| \logit  | logit                | Logit function    |  |

Table 6: Commands for math operators.

| Command | Symbol   | Description  |
|---------|--|--|
| \toas   | $\xrightarrow{\text{a.s.}} \longrightarrow \infty$ | Almost sure convergence as $m$ goes to $\infty$            |
| \toN    | $\longrightarrow$                                  | Limit as $n$ goes to $\infty$                              |
| \toasNM | $\xrightarrow[n,m\to\infty]{n\to\infty}$           | Almost sure convergence as both $m$ and $n$ go to $\infty$ |

Table 7: Commands for math convergence arrows.

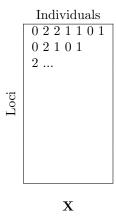


Figure 1: The cartoon genotype matrix generated by \sampleGenMat

- Fig. 2: \usepackage{kinshipsymbols} "vanilla" version (no options). This version shows symbols completely (without omitting the ancestral population T from superscripts) and without color.
- Fig. 3: \usepackage[color]{kinshipsymbols} version. Same as the vanilla version except a few common symbols gain colors:
  - The genotypes  $(x_{ij})$  become blue (and also the cartoon genotype matrix drawn by \sampleGenMat). Highlighted since this is the observed data from which inferences are drawn.
  - The kinship coefficients  $(\varphi_{jk}^T)$  become dark green. Highlighted since these are the main unknown parameters we wish to estimate.
  - The standard ancestral allele frequency estimator  $(\hat{p}_i^T)$  becomes red. Highlighted since this is a particularly problematic estimator that leads to biases in common approaches.
- Fig. 4: \usepackage[noT] {kinshipsymbols} version. Same as the vanilla version except the ancestral population T is omitted in the superscript of several symbols  $(p_i^T, \hat{p}_i^T, f_j^T, f_{L_j}^T, \varphi_{jk}^T, f_{L_jk}^T, \hat{\varphi}_{jk}^{T,\text{std}}, \hat{f}_j^{T,\text{std}}, \hat{f}_j^{T,\text{stdII}}, \hat{f}_j^{T,\text{stdIII}}, \hat{\varphi}_{jk}^{T,\text{new}}, \hat{\varphi}_{\min}^{T,\text{new}}, \hat{f}_j^{T,\text{new}}, \text{ and } \overline{p(1-p)}^T)$ . This option is provided to simplify the heavy notation in a context where T is implicit or fixed.
- Fig. 5: \usepackage[color,noT]{kinshipsymbols} version. A straightforward combination of the color and noT options described above.

## 2 Implementation

#### 2.1 Dependencies

This package requires amsmath to define the various math symbols and operators, xspace to allow inline math symbols to have appropriate spacings when used outside math mode, xcolor for color management and tricks, and colortbl and multirow for the cartoon genotype matrix.

- 1 \RequirePackage{amsmath}
- 2 \RequirePackage{xspace}
- 3 \RequirePackage{xcolor}
- 4 \RequirePackage{colortbl}
- 5 \RequirePackage{multirow}

#### 2.2 Initializing variables, modify depending on options

Then we define the special colors we want to use (in a way that is easy to tweak later if needed).

\ifcolor LaTeX boolean for whether color option is on or off.

- 6 \newif\ifcolor%
- $7 \colorfalse$ % default is false

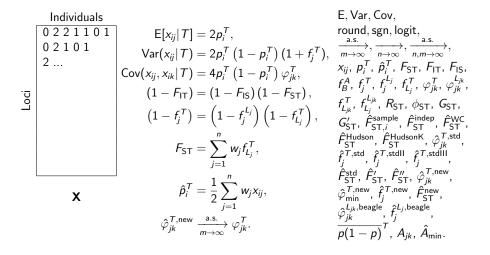


Figure 2: The vanilla version of the symbols (no colors and no omission of ancestral population T in superscripts

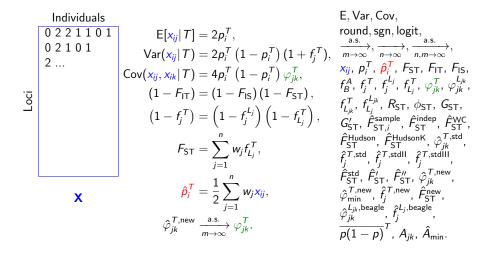


Figure 3: The color version of the symbols (with no omission of ancestral population T in superscripts

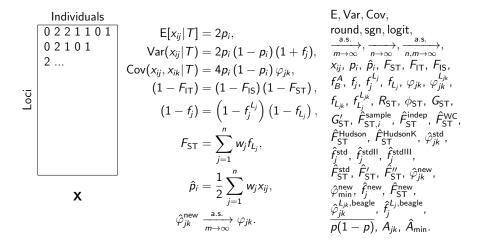


Figure 4: The noT version of the symbols (no color, with omission of ancestral population T in superscripts as appropriate

Individuals 
$$\begin{array}{c} \text{E}[\mathsf{X}_{ij}|T] = 2p_i, \\ \text{Var}(\mathsf{X}_{ij}|T) = 2p_i (1-p_i) (1+f_j), \\ \text{Cov}(\mathsf{X}_{ij},\mathsf{X}_{ik}|T) = 4p_i (1-p_i) \varphi_{jk}, \\ (1-F_{\mathsf{IT}}) = (1-F_{\mathsf{IS}}) (1-F_{\mathsf{ST}}), \\ \text{FST} = \sum_{j=1}^n w_j f_{L_j}, \\ \hat{\rho}_i = \frac{1}{2} \sum_{j=1}^n w_j \mathsf{X}_{ij}, \\ \hat{\varphi}_{jk}^{\mathsf{new}} \xrightarrow[m \to \infty]{} \varphi_{jk}. \\ \end{array} \begin{array}{c} \text{E}, \mathsf{Var}, \mathsf{Cov}, \\ \mathsf{round}, \mathsf{sgn}, \mathsf{logit}, \\ \mathsf{a.s.}, \\ \mathsf{m} \to \infty, \xrightarrow[n \to \infty]{}, \\ \mathsf{m} \to \infty, \\ \mathsf{m}$$

Figure 5: The color,noT version of the symbols (with color and omission of ancestral population T in superscripts as appropriate

genColor The hardcoded "genotype color" is blue, applied if the color package option is set.

8 \colorlet{genColor}{blue}

kinColor The hardcoded "kinship color" is a dark green, applied if the color package option is set

9 \colorlet{kinColor}{green!50!black}

pithColor The hardcoded "\pith color" is red, applied if the color package option is set.

10 \colorlet{pithColor}{red}

We also define two tricky commands to handle the ancestra population T superscript that we want to optionally omit. Note that these are internal commands not meant to be used directly outside the package.

 $\mbox{\colored}$  This is a basic superscript T that becomes blank if the noT package option is set.

11 \newcommand{\kinshipsymbols@T}{^T}

\kinshipsymbols@Ts This is a second superscript T which takes a mandatory argument that is shown next to it as text. Only the T becomes blank if the noT package option is set (the argument is shown alone as a text superscript in that case).

12 \newcommand{\kinshipsymbols@Ts}[1]{^{T,\text{#1}}}

This turns on colors if the color package option is set.

13 \DeclareOption{color}{
14 \colortrue

15 }

Similarly, this updates the commands to omit the T superscript if the noT package option is set. Note that the second command still emits the additional text passed as argument in the superscript.

```
16 \DeclareOption{noT}{
17 \renewcommand{\kinshipsymbols@T}{}
18 \renewcommand{\kinshipsymbols@Ts}[1]{^{\text{#1}}}
19 }
```

This creates a warning if any additional options are passed, then processes the options.

20 \DeclareOption\*{\PackageWarning{examplepackage}{Unknown '\CurrentOption'}} 21 \ProcessOptions\relax

#### 2.3 Commands for math operators

Here we define some trivial widely-used operators, which are not specific to statistical genetics but which are absent from the standard amsmath package.

**\E** Expectation of a random variable.

22 \DeclareMathOperator{\E}{E}

```
\Var Variance of a random variable.
23 \DeclareMathOperator{\Var}{Var}

\Cov Covariance of a random variable.
24 \DeclareMathOperator{\Cov}{Cov}

\round The rounding function.
25 \DeclareMathOperator{\round}{round}

\sgn The sign function.
26 \DeclareMathOperator{\sgn}{sgn}

\logit The logit function.
27 \DeclareMathOperator{\logit}{logit}}
```

#### 2.4 Genotypes

\xij  $x_{ij}$ : Genotype variable at locus i of individual j (default). The optional argument allows setting other individuals (\xij[k] gives  $x_{ik}$  for individual k). If the package option color is passed, then this symbol turns the color genColor (default blue).

```
28 \newcommand{\xij}[1][j]{%
29 \ensuremath{%
30 \ifcolor \textcolor{genColor}{ \fi%
31     x_{i#1}}%
32 \ifcolor } \fi%
33 }%
34 \xspace%
35 }%
```

#### 2.5 Ancestral allele frequencies

\pit  $p_i^T$ : The ancestral allele frequency at locus i. This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
36 \newcommand{\pit}{%
37 \ensuremath{%
38 p_i\kinshipsymbols@T%
39 }%
40 \xspace%
41 }%
```

\pith  $\hat{p}_i^T$ : The sample estimator of the ancestral allele frequency at locus i. The parameter being estimated has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed. If the package option color is passed, then this symbol turns the color pithColor (default red).

```
42 \neq 42 \neq 42
```

```
43 \ensuremath{%
44 \ifcolor \textcolor{pithColor}{ \fi%
45 \hat{p}_i\kinshipsymbols@T%
46 \ifcolor } \fi%
47 }%
48 \xspace%
49 }%
```

#### 2.6 Wright's $F_{ST}$

\Fst  $F_{ST}$ : Wright's Fixation index. Although the T in the subscript technically refers to the ancestral population T, in this case it is never omitted (even if the package option noT is passed) to always match the more traditional and highly recognizable notation.

```
50 \newcommand{\Fst}{%
51 \ensuremath{%
52 F_{\text{ST}}%
53 }%
54 \xspace%
55 }%
```

\Fit  $F_{\text{IT}}$ : Wright's total inbreeding coefficient. Although the T in the subscript technically refers to the ancestral population T, in this case it is never omitted (even if the package option noT is passed) to always match the more traditional and highly recognizable notation.

```
56 \newcommand{\Fit}{%
57 \ensuremath{%
58 F_{\text{IT}}}%
59 }%
60 \xspace%
61 }%
```

**\Fis**  $F_{\rm IS}$ : Wright's local inbreeding coefficient.

```
62 \newcommand{\Fis}{%
63 \ensuremath{%
64 F_{\text{IS}}%
65 }%
66 \xspace%
67 }%
```

#### 2.7 Inbreeding coefficients

\f  $f_B^A$ : The inbreeding coefficient (of  $F_{ST}$ ) of population B relative to an ancestral population A. Note that this command has two mandatory arguments.

```
68 \newcommand{\f}[2]{%
69 \ensuremath{%
70 f^{#1}_{#2}%
71 }%
```

```
72 \xspace%
73 }%
```

\ft  $f_j^T$ : The (total) inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\ft[k] gives  $f_k^T$  for individual k). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
74 \newcommand{\ft}[1][j]{%
75 \ensuremath{%
76 f_{#1}\kinshipsymbols@T%
77 }%
78 \xspace%
79 }%
```

\f1  $f_j^{L_j}$ : The local inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\f1[k] gives  $f_k^{L_k}$  for individual k).

```
80 \newcommand{\f1}[1][j]{\%
81 \ensuremath{\%}
82 f_{\#1}^{L_{\#1}}\%
83 }\%
84 \xspace\%
85 }\%
```

\fs  $f_{L_j}^T$ : The structural inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\fs[k] gives  $f_{L_k}^T$  for individual k). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
86 \newcommand{\fs}[1][j]{%
87 \ensuremath{%
88  f_{L_{#1}}\kinshipsymbols@T%
89 }%
90 \xspace%
91 }%
```

#### 2.8 Kinship coefficients

\kt  $\varphi_{jk}^T$ : The (total) kinship coefficient between the pair of individuals j and k (default). The optional argument allows setting another second individual (\kt[1] gives  $\varphi_{jl}^T$  for a second individual l). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed. If the package option color is passed, then this symbol turns the color kinColor (default dark green).

```
92 \newcommand{\kt}[1][k]{%

93 \ensuremath{%

94 \ifcolor \textcolor{kinColor}{ \fi%
```

```
\varphi_{j#1}\kinshipsymbols@T%
        95
        96
                \ifcolor } \fi%
             }%
        97
        98
             \xspace%
        99 }%
   \kl \varphi_{jk}^{L_{jk}}: The local kinship coefficient between the pair of individuals j and k.
       100 \newcommand{\kl}{%
            \ensuremath{%
       101
       102
               104
             \xspace%
       105 }%
   \ks f_{L_{ik}}^T: The structural kinship coefficient between the pair of individuals j and k.
        This parameter has a value that depends on the ancestral population T, which
        is by default denoted in the superscript, but which gets omitted if the package
        option noT is passed.
        106 \newcommand{\ks}{%
             \ensuremath{%
               f_{L_{jk}}\kinshipsymbols@T%
       108
       109
       110
            \xspace%
       111 }%
 \fpw f_{L_i}^{L_{jk}}: A component of the pairwise F_{ST} between a pair of individuals j and k
        (default). The optional argument changes the individual in the subscript only (so
        \fpw[k] gives f_{L_k}^{L_{jk}}, and is obviously intended to be used for k only). Note that
        the actual pairwise F_{ST} between j and k is given by the average of f_{L_i}^{L_{jk}} and f_{L_k}^{L_{jk}}.
        112 \mbox{newcommand} \{\pw\}[1][j] {\%}
       113 \f{L_{jk}}{L_{#1}}%
       114 }%
                Review of previous work
  \Rst R_{ST}: An F_{ST} estimator developed for microsatellites.
        115 \newcommand{\Rst}{%
             \ensuremath{%
       117
               R_{\text{ST}}%
       118
             }%
             \xspace%
       119
       120 }%
\PhiSt \phi_{ST}: An F_{ST}-like estimate based on AMOVA.
       121 \newcommand{\PhiSt}{%
             \ensuremath{%
       123
               \phi_{\text{ST}}%
```

}%

124

```
125 \xspace%
                126 }%
          \Gst G_{ST}: Nei's genetic diversity measure.
                127 \newcommand{\Gst}{\%}
                128 \ensuremath{%
                       G_{\text{st}}
                129
                130 }%
                131
                      \xspace%
                132 }%
    \GstPrime G'_{ST}: A normalized G_{ST} statistic.
                133 \newcommand{\GstPrime}{%
                134 \ensuremath{%
                        G_{\text{ST}}'%
                135
                      }%
                136
                137
                      \xspace%
                138 }%
\FstHatSample \hat{F}_{\mathrm{ST},i}^{\mathrm{sample}}: A sample F_{\mathrm{ST}} estimator for a single locus i.
                139 \newcommand{\FstHatSample}{%
                     \ensuremath{%
                140
                        141
                142 }%
                143
                      \xspace%
                144 }%
                 2.10
                          Convergence arrows
         \to
as \xrightarrow[m\to\infty]{\text{a.s.}}: Almost sure convergence as m goes to
 \infty.
                145 \newcommand{\toas}{%
                146 \xrightarrow[m \rightarrow \infty]{\text{a.s.}}
          \toN \xrightarrow[n\to\infty]{}: The limit as n goes to \infty. Optional argument changes the variable name
                 (\text{$\toN[m]$ gives } \xrightarrow[m\to\infty]{}).
                148 \newcommand{\toN}[1][n]{%
                149 \xrightarrow[#1 \rightarrow \infty]{}%
                150 }%
       \toasNM \xrightarrow[n,m\to\infty]{\text{a.s.}}: Almost sure convergence as both n and m go to \infty.
                151 \newcommand{\toasNM}{%
                152 \xrightarrow[n,m \rightarrow \infty]{\text{a.s.}}%
                153 }%
```

#### 2.11 $F_{ST}$ estimators for independent subpopulations

```
\FstHatNamed \hat{F}_{\mathrm{ST}}^{\mathrm{example}}: Base command for a named F_{\mathrm{ST}} estimator. Takes on one mandatory
                   argument—the name of the estimator—which is rendered as text.
                   154 \newcommand{\FstHatNamed}[1]{%
                         \ensuremath{%
                  156
                            \hat{F}_{\text{ST}}^{\text{text}}%
                  157
                        }%
                  158 \xspace%
                  159 }%
     \FstHatIs \hat{F}_{\mathrm{ST}}^{\mathrm{indep}}: Asymptotic F_{\mathrm{ST}} estimator for independent subpopulations.
                  160 \newcommand{\FstHatIs}{\FstHatNamed{indep}}
      \FstHatWc \hat{F}_{\mathrm{ST}}^{\mathrm{WC}}: Weir-Cockerham F_{\mathrm{ST}} estimator.
                  161 \newcommand{\FstHatWc}{\FstHatNamed{WC}}
\FstHatHudson \hat{F}_{ST}^{Hudson}: Hudson pairwise F_{ST} estimator.
                   162 \newcommand{\FstHatHudson}{\FstHatNamed{Hudson}}
\FstHatHudsonK \hat{F}_{ST}^{HudsonK}: Generalized Hudson F_{ST} estimator (for K subpopulations).
                   163 \newcommand{\FstHatHudsonK}{\FstHatNamed{HudsonK}}
```

#### Estimators based on the standard kinship

\ktHatNamed

 $\hat{\varphi}_{jk}^{T,\text{example}}$ : A generic named kinship estimator for individuals j and k (default). Mandatory argument is the name, rendered as text. The optional argument allows setting another second individual (\ktHatNamed[1]{example} gives  $\hat{\varphi}_{il}^{T,\text{example}}$  for a second individual l). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
164 \newcommand{\ktHatNamed}[2][k]{%
     \ensuremath{%
165
       \hat{\varphi}_{j#1}\kinshipsymbols@Ts{#2}%
166
167
    }%
168
     \xspace%
169 }%
```

\ktHatStd  $\hat{\varphi}_{jk}^{T,\text{std}}$ : Standard kinship estimator for individuals j and k (default). The optional argument allows setting another second individual (\ktHatStd[1] gives  $\hat{\varphi}_{il}^{T,\mathrm{std}}$  for a second individual l). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

170 \newcommand{\ktHatStd}[1][k]{\ktHatNamed[#1]{std}}

\ftHatNamed

 $\hat{f}_{\perp}^{T, \text{example}}$ : Named inbreeding coefficient estimator for individual j (default). Mandatory argument is the name, rendered as text. The optional argument allows setting another individual (\ftHatNamed[k]{example} gives  $\hat{f}_k^{T,\text{example}}$  for individual k). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
171 \newcommand{\ftHatNamed}[2][j]{%
     \ensuremath{%
       \hat{f}_{#1}\kinshipsymbols@Ts{#2}%
     \xspace%
175
176 }%
```

\ftHatStd  $\hat{f}_i^{T,\text{std}}$ : Standard inbreeding coefficient estimator (I) for individual j. The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

177 \newcommand{\ftHatStd}{\ftHatNamed{std}}

\ftHatStdII  $\hat{f}_i^{T,\text{stdII}}$ : Alternate inbreeding coefficient estimator (II) for individual j. The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

 $178 \verb|\newcommand{\ftHatStdII}{\ftHatNamed{stdII}}|$ 

\ftHatStdIII  $\hat{f}_i^{T,\text{stdIII}}$ : Alternate inbreeding coefficient estimator (III) for individual j. The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

179 \newcommand{\ftHatStdIII}{\ftHatNamed{stdIII}}

\FstHatStd  $\hat{F}_{ST}^{std}$ : Standard  $F_{ST}$  estimator (based on the standard kinship estimator).

 $180 \mbox{ \newcommand{\FstHatStd}{\FstHatNamed{std}}}$ 

\FstHatStdPrime  $\hat{F}'_{ST}$ : Standard  $F_{ST}$  estimator adjusted 1.

```
181 \newcommand{\FstHatStdPrime}{%
    \ensuremath{%
182
       \hat{F}_{\text{ST}}'%
183
184
185
     \xspace%
186 }%
```

\FstHatStdPrimeDbl

 $\hat{F}_{ST}^{"}$ : Standard  $F_{ST}$  estimator adjusted 2.

```
187 \newcommand{\FstHatStdPrimeDbl}{%
     \ensuremath{%
188
189
       \hat{F}_{\text{ST}}''%
190
     }%
191
    \xspace%
192 }%
```

#### 2.13 New kinship and $F_{ST}$ estimators

 $\hat{\varphi}_{jk}^{T,\text{new}}$ : New kinship estimator for the pair of individuals j and k (default). The optional argument allows setting another second individual (\ktHatNew[1] gives  $\hat{\varphi}_{il}^{T,\text{new}}$  for a second individual l). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

193 \newcommand{\ktHatNew}[1][k]{\ktHatNamed[#1]{new}}

\ktHatNewMin

 $\hat{\varphi}_{\min}^{T,\text{new}}$ : Estimator of the limit of the minimum value of the expectation of  $\hat{\varphi}_{jk}^{T,\text{new}}$ across all pairs of individuals. The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
194 \newcommand{\ktHatNewMin}{%
     \ensuremath{%
195
       \hat{\varphi}_{\text{min}}\kinshipsymbols@Ts{new}%
196
197
198
     \xspace%
199 }%
```

**\ftHatNew**  $\hat{f}_{j}^{T,\text{new}}$ : New inbreeding estimator for individual j (default). The optional argument allows setting other individuals (\ftHatNew[k] gives  $\hat{f}_k^{T,\text{new}}$  for individual k). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

200 \newcommand{\ftHatNew}[1][j]{\ftHatNamed[#1]{new}}

\FstHatNew

 $\hat{F}_{ST}^{new}$ : New  $F_{ST}$  estimator.

201 \newcommand{\FstHatNew}{\FstHatNamed{new}}

Ajk  $A_{jk}$ : A new statistic proportional in expectation to  $\varphi_{jk}^T - 1$  for the pair of individuals j and k (default). The optional argument allows setting another second individual (Ajk[1] gives  $A_{jl}$  for a second individual l).

```
202 \newcommand{\Ajk}[1][k]{%
     \ensuremath{%
204
       A_{j#1}%
     }%
205
206 \xspace%
207 }%
```

\AMinHat  $\hat{A}_{\min}$ : Estimator of the limit of the minimum value of the expectation of  $A_{ik}$ across all pairs of individuals.

```
208 \newcommand{\AMinHat}{%
     \ensuremath{%
209
210
       \hat{A}_{\text{min}}%
     }%
211
212
     \xspace%
213 }%
```

```
all pairs of individuals.
               214 \newcommand{\AAvgHat}{%
               215
                    \ensuremath{%
               216
                       \hat{A}_{\text{avg}}%
               217
               218
                    \xspace%
               219 }%
         \max \overline{p(1-p)}^T: Mean ancestral variance. This parameter has a value that depends on
                the ancestral population T, which is by default denoted in the superscript, but
                which gets omitted if the package option noT is passed.
               220 \newcommand{\mav}{%
               221
                     \ensuremath{%
               222
                       \overline{p(1-p)}\kinshipsymbols@T%
               223
                     \xspace%
               224
               225 }%
                2.14
                         Estimates from Beagle
               \hat{\varphi}_{jk}^{L_{jk},\text{beagle}}: Local kinship estimator based on Beagle, for the pair of individuals j
\klHatBeagle
               226 \newcommand{\klHatBeagle}{%
               227
                    \ensuremath{%
               228
                       \hat{\varphi}_{jk}^{L_{jk}},\text{beagle}}%
               229
               230
                    \xspace%
               231 }%
               \hat{f}_i^{L_j, \text{beagle}}: Local inbreeding estimator based on Beagle, for individual j (default).
\flHatBeagle
                The optional argument allows setting other individuals (\flHatBeagle[k] gives
               \hat{f}_k^{L_k,\text{beagle}} for individual k).
               232 \newcommand{\flHatBeagle}[1][j]{%
                    \ensuremath{%
               233
                       \hat{f}_{\#1}^{L_{\#1}}, \text{beagle}}%
               234
               235
                    \xspace%
               236
               237 }%
```

\AAvgHat  $\hat{A}_{avg}$ : Estimator of the limit of the average value of the expectation of  $A_{jk}$  across

#### 2.15 Cartoon genotype matrix

I use this cartoon genotype matrix often in Beamer presentations. Unfortunately I also use the color kinshipsymbols package option in my presentations, but due to a strange bug the colors do not show up in Beamer. This solution was found online: https://tex.stackexchange.com/questions/159378/cline-disappears-in-beamer

```
239 \makeatletter
              240 \@ifclassloaded{beamer}{%
                    \patchcmd\@cline
              241
                        {\arrayrulewidth\hfill}% search
              242
              243
                        {\arrayrulewidth\hfill\kern\z@}% replace
              244
                        {}% success
                        {\errmessage{Patching \string\@cline\space failed}}% failure
              245
              246 }{%
                    % nothing to do here?
              247
              248 }
              249 \makeatother
\sampleGenMat
               This is the bulky code used to generate the cartoon genotype matrix shown in
              250 \newcommand{\sampleGenMat}{%
                    \begin{tabular}{cc}%
              251
              252
                      & Individuals \\%
                      \ifcolor \arrayrulecolor{genColor} \fi% % gets applied to whole table
              253
                      \cline{2-2}%
              254
                      \multirow{10}{*}{\rotatebox[origin=c]{90}{Loci}}%
              255
                      & \multicolumn{1}{|1|}{0 2 2 1 1 0 1} \\%
              256
                      & \multicolumn{1}{|1|}{0 2 1 0 1 } \\%
              257
                      & \multicolumn{1}{|1|}{2 ...} \\%
              258
                      & \multicolumn{1}{|1|}{ } \\%
                      & \multicolumn{1}{|1|}{ } \\%
              260
                      & \multicolumn{1}{|1|}{ } \\%
              261
                      & \multicolumn{1}{|1|}{ } \\%
              262
                      & \multicolumn{1}{|1|}{ } \\%
              263
                      & \multicolumn{1}{|1|}{ } \\%
              264
              265
                      & \multicolumn{1}{|1|}{ } \\%
               266
                      \left(2-2\right)%
              267
                      & \\%
              268
                      & $\mathbf{
                        \ifcolor \textcolor{genColor}{ \fi%
              269
              270
                        \ifcolor } \fi%
              271
```

## 3 Acknowledgments

}\$ \\%
\end{tabular}%

272

273 **\** 274 **}**%

238 % after package colortbl is loaded

The symbols in this package were originally designed with John D. Storey (Alex Ochoa's postdoctoral adviser and coauthor of several papers about kinship and  $F_{\rm ST}$ ).

The package was written following Scott Pakin's guide How to Package Your LATEX package.

# Change History

| v1.00                    |   | README, and symbols $A_{jk}$ ,                              |   |
|--------------------------|---|---|---|
| General: Initial version | 1 | $\hat{A}_{avg}$ , and *Std versions                         | 1 |
| v1.01                    |   | v1.02   |   |
| General: Added NEWS,     |   | General: Added $\hat{\varphi}_{\min}^{T,\text{new}}$ symbol | 1 |

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