# The kinshipsymbols package\*

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#### Abstract

This package defines consistent mathematical symbols for statistical genetics, particularly relating to the kinship model and  $F_{\rm ST}$ . In addition to providing a long list of symbols, the package has two options that alter the behavior of some of the most common symbols. Option color highlights genotypes (blue), kinship coefficients (dark green), and the standard ancestral allele frequency estimator (red), which is very useful for Beamer presentations. Option noT removes the ancestral population T superscript from all symbols that contain it (for simpler presentations).

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<sup>\*</sup>This document corresponds to kinshipsymbols v1.0, dated 2019/02/01.

Command	Symbol	Description
\xij	$x_{ij}$	Genotype
\pit	$p_i^T$	Ancestral allele frequency
\pith	$\hat{p}_i^T$	Sample $p_i^T$ estimator
\kt	$arphi_{jk}^T$	Kinship coefficient
\ft	$f_i^T$	Inbreeding coefficient
\Fst	$ec{F_{ m ST}}$	(Wright's) Fixation index

Table 1: Commands for the most common statistical genetics quantities.

Command	Symbol	Description
\f{A}{B}	$f_B^A$	Inbreeding of pop. $B$ relative to pop. $A$
\fl	$f_i^{L_j}$	Local inbreeding coefficient
\fs	$\widetilde{f}_{L_i}^T$	Structural inbreeding coefficient
\kl	$\varphi_{jk}^{L_{jk}}$	Local kinship coefficient
\ks	$f_{L_{jk}}^{T}$	Structural kinship coefficient
\fpw	$f_{L_j}^{L_{jk}}$	Individual pairwise $F_{\rm ST}$ component
\mav	$\overline{p(1-p)}^T$	Mean ancestral variance

Table 2: Commands for more rare statistical genetics quantities.

#### 1 Introduction

This package provides macros for many common symbols involving the genotypes, kinship coefficients, and  $F_{ST}$ . Each of Tables 1 to 5 pairs a command to its symbol and its common description in the field. Note that these symbols work even when not in math mode, so it is not necessary to write  $f_{ST}$  inline,  $f_{ST}$  works! This is achieved through use of  $e_{ST}$  achieved through use of  $e_{ST}$ .

Some of these symbols accept arguments for limited flexibility. For example,  $\xij$  produces  $x_{ij}$ , but  $\xij$ [k] produces  $x_{ik}$ . Similarly,  $\times$  produces  $\varphi_{jk}^T$ , but  $\times$  below for details for each command.

Additionally, Tables 6 and 7 lists some math operators and convergence arrows defined by this package (absent in amsmath). These commands do require math mode to work.

Lastly, the package provides \sampleGenMat, which generates the cartoon genotype table shown in Fig. 1. Note that this technically generates a "tabular" table. It is meant to be used in Beamer presentations, but works in standard documents too.

The effects of the package options color and noT are visualized in Figs. 2 to 5. Each of those figures generated the symbols with a particular combination of options:

Command	Symbol	Description
\ktHat	$\hat{\varphi}_{jk}^{T,\mathrm{std}}$	Standard kinship estimator
\ftHat	$\hat{f}_i^{T,\mathrm{std}}$	Standard inbreeding estimator (I)
\ftHatII	$\hat{f}_i^{T, \mathrm{stdII}}$	Alternate inbreeding estimator (II)
\ftHatIII	$\hat{f}_{j}^{T,\mathrm{stdIII}}$	Alternate inbreeding estimator (III)
\ktHatPreadj	$\hat{\varphi}_{ik}^{T, \text{preadj}}$	Preadjusted kinship estimator
\ktHatPreadjMin	$\hat{\varphi}_{\min}^{T, \mathrm{preadj}}$	Asymptotic minimum value of $\hat{\varphi}_{jk}^{T,\text{preadj}}$
\ktHatNew	$\hat{\varphi}_{ik}^{T,\mathrm{new}}$	New kinship estimator
\ftHatNew	$\hat{f}_i^{T,\text{new}}$	New inbreeding estimator
\klHatBeagle	$\hat{\varphi}_{jk}^{\hat{L}_{jk}, \text{beagle}}$	Beagle-based kinship estimator
\flHatBeagle	$\hat{f}_i^{L_j, \text{beagle}}$	Beagle-based inbreeding estimator
\AMin	$A_{ m Emin}$	Asymptotic minimum value of $A_{jk}$
\AMinHat	$\hat{A}_{\mathrm{Emin}}$	Estimator of $A_{\text{Emin}}$

Table 3: Commands for miscelaneous kinship and inbreeding estimators.

Command	Symbol	Description
\FstHatSample	$\hat{F}_{\mathrm{ST},i}^{\mathrm{sample}}$	Sample $F_{ST}$ estimator
\FstHatWc	$\hat{F}_{ ext{ST}}^{ ext{WC}}$	Weir-Cockerham $F_{\rm ST}$ estimator
\FstHatHudson	$\hat{F}_{ ext{ST}}^{ ext{Hudson}}$	Hudson Pairwise $F_{\rm ST}$ estimator
\FstHatHudsonK	$\hat{F}_{\mathrm{ST}}^{\mathrm{HudsonK}}$	Generalized Hudson $F_{ST}$ estimator
\FstHatIs	$\hat{F}_{ ext{ST}}^{ ext{indep}}$	Asymptotic $F_{\rm ST}$ estimator for indep. subpops.
\FstHat	$\hat{F}_{ ext{ST}}^{ ext{std}}$	Standard $F_{\rm ST}$ estimator (based on $\hat{\varphi}_{jk}^{T,{\rm std}}$ )
\FstHatPrime	$\hat{F}'_{ ext{ST}}$	Standard $F_{ST}$ estimator adjusted 1
$\FstHatPrimeDbl$	$\hat{F}_{ ext{ST}}^{\prime\prime}$	Standard $F_{ST}$ estimator adjusted 2
\FstHatNew	$\hat{F}_{ ext{ST}}^{ ext{new}}$	New $F_{\rm ST}$ estimator

Table 4: Commands for miscelaneous  $F_{\rm ST}$  estimators.

Command	Symbol	Description
\Fit	$F_{\mathrm{IT}}$	Wright's total inbreeding
\Fis	$F_{ m IS}$	Wright's local inbreeding
\Gst	$G_{ m ST}$	Nei's genetic diversity measure
$\GstPrime$	$G'_{ m ST}$	Normalized $G_{\rm ST}$
\Rst	$R_{ m ST}$	$F_{\rm ST}$ estimator for microsatellites
\PhiSt	$\phi_{ m ST}$	AMOVA-based differentiation measure

Table 5: Commands for historical quantities in statistical genetics.

Command	Symbol	Description
\E	Е	Expectation
\Var	Var	Variance
\Cov	Cov	Covariance
\round	round	Rounding function
\sgn	$\operatorname{sgn}$	Sign function
\logit	logit	Logit function

Table 6: Commands for math operators.

Command	Symbol	Description
\toas	$\xrightarrow{\text{a.s.}} \longrightarrow \infty$	Almost sure convergence as $m$ goes to $\infty$
\toN	$\longrightarrow$	Limit as $n$ goes to $\infty$
\toasNM	$\xrightarrow[n,m\to\infty]{n\to\infty}$	Almost sure convergence as both $m$ and $n$ go to $\infty$

Table 7: Commands for math convergence arrows.

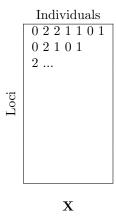


Figure 1: The cartoon genotype matrix generated by \sampleGenMat

- Fig. 2: \usepackage{kinshipsymbols} "vanilla" version (no options). This version shows symbols completely (without omitting the ancestral population T from superscripts) and without color.
- Fig. 3: \usepackage[color]{kinshipsymbols} version. Same as the vanilla version except a few common symbols gain colors:
  - The genotypes  $(x_{ij})$  become blue (and also the cartoon genotype matrix drawn by  $\sum (x_{ij})$  Highlighted since this is the observed data from which inferences are drawn.
  - The kinship and inbreeding coefficients  $(\varphi_{jk}^T$  and  $f_j^T)$  become dark green. Highlighted since these are the unknown parameters we wish to estimate.
  - The standard ancestral allele frequency estimator  $(\hat{p}_i^T)$  becomes red. Highlighted since this is a particularly problematic estimator that leads to biases in common approaches.
- Fig. 4: \usepackage[noT]{kinshipsymbols} version. Same as the vanilla version except the ancestral population T is omitted in the superscript of several symbols  $(p_i^T, \hat{p}_i^T, f_j^T, f_{L_j}^T, \varphi_{jk}^T, f_{L_{jk}}^T, \hat{\varphi}_{jk}^{T,\text{std}}, \hat{f}_j^{T,\text{std}}, \hat{f}_j^{T,\text{stdII}}, \hat{f}_j^{T,\text{stdIII}}, \hat{\varphi}_{jk}^{T,\text{preadj}}, \hat{\varphi}_{\min}^{T,\text{preadj}}, \hat{\varphi}_{jk}^{T,\text{new}}, \hat{f}_j^{T,\text{new}}, \text{ and } \overline{p(1-p)}^T)$ . This option is provided to simplify the heavy notation in a context where T is implicit or fixed.
- Fig. 5: \usepackage[color,noT]{kinshipsymbols} version. A straightforward combination of the color and noT options described above.

# 2 Implementation

#### 2.1 Dependencies

This package requires amsmath to define the various math symbols and operators, xspace to allow inline math symbols to have appropriate spacings when used outside math mode, xcolor for color management and tricks, and colortbl and multirow for the cartoon genotype matrix.

- 1 \RequirePackage{amsmath}
- 2 \RequirePackage{xspace}
- 3 \RequirePackage{xcolor}
- 4 \RequirePackage{colortbl}
- 5 \RequirePackage{multirow}

#### 2.2 Initializing variables, modify depending on options

Then we define the special colors we want to use (in a way that is easy to tweak later if needed). Note that by default these colors are all black.

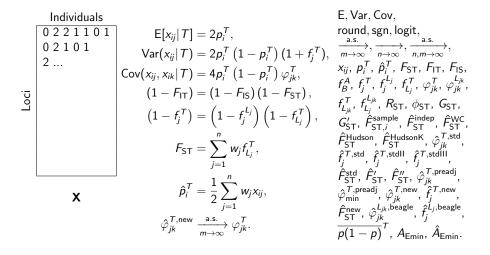


Figure 2: The vanilla version of the symbols (no colors and no omission of ancestral population T in superscripts

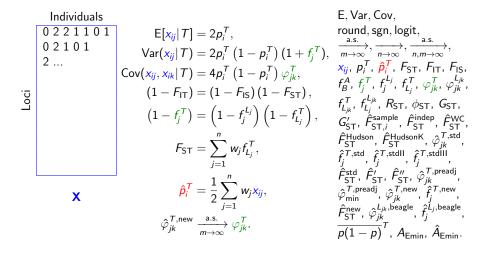


Figure 3: The color version of the symbols (with no omission of ancestral population T in superscripts

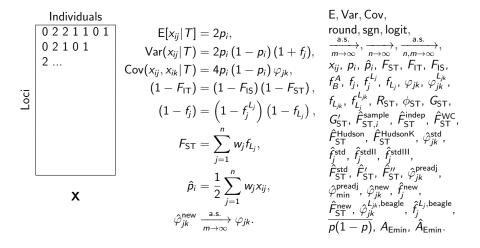


Figure 4: The noT version of the symbols (no color, with omission of ancestral population T in superscripts as appropriate

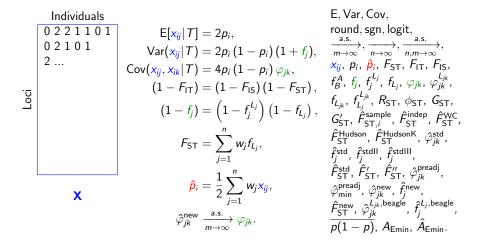


Figure 5: The color,noT version of the symbols (with color and omission of ancestral population T in superscripts as appropriate

genColor This "genotype color" is black by default, turns blue if the color package option is set.

6 \colorlet{genColor}{black}

kinColor This "kinship color" is black by default, turns a dark green if the color package option is set.

7 \colorlet{kinColor}{black}

pithColor This "\pith color" is black by default, turns red if the color package option is set.

8 \colorlet{pithColor}{black}

We also define two tricky commands to handle the ancestra population T superscript that we want to optionally omit. Note that these are internal commands not meant to be used directly outside the package.

\kinshipsymbols@T

This is a basic superscript T that becomes blank if the noT package option is set. 9  $\mbox{newcommand{\kinshipsymbols@T}{^T}}$ 

\kinshipsymbols@Ts

This is a second superscript T which takes a mandatory argument that is shown next to it as text. Only the T becomes blank if the noT package option is set (the argument is shown alone as a text superscript in that case).

10 \newcommand{\kinshipsymbols@Ts}[1]{^{T,\text{#1}}}

This turns on colors if the color package option is set.

```
11 \DeclareOption{color}{
12  \colorlet{genColor}{blue}
13  \colorlet{kinColor}{green!50!black}
14  \colorlet{pithColor}{red}
15 }
```

Similarly, this updates the commands to omit the T superscript if the noT package option is set. Note that the second command still emits the additional text passed as argument in the superscript.

```
16 \DeclareOption{noT}{
17 \renewcommand{\kinshipsymbols@T}{}
18 \renewcommand{\kinshipsymbols@Ts}[1]{^{\text{#1}}}
19 }
```

This creates a warning if any additional options are passed, then processes the options.

#### 2.3 Commands for math operators

Here we define some trivial widely-used operators, which are not specific to statistical genetics but which are absent from the standard amsmath package.

```
\E Expectation of a random variable.

22 \DeclareMathOperator{\E}{E}

\Var Variance of a random variable.

23 \DeclareMathOperator{\Var}{Var}

\Cov Covariance of a random variable.

24 \DeclareMathOperator{\Cov}{Cov}

\round The rounding function.

25 \DeclareMathOperator{\round}{round}

\sgn The sign function.

26 \DeclareMathOperator{\sgn}{sgn}

\logit The logit function.

27 \DeclareMathOperator{\logit}{logit}}
```

#### 2.4 Genotypes

\xij  $x_{ij}$ : Genotype variable at locus i of individual j (default). The optional argument allows setting other individuals (\xij[k] gives  $x_{ik}$  for individual k). If the package option color is passed, then this symbol turns the color genColor (default blue).

```
28 \newcommand{\xij}[1][j]{%
29 \ensuremath{%
30 \textcolor{genColor}{%
31     x_{i#1}%
32     }%
33     }%
34 \xspace%
35 }%
```

#### 2.5 Ancestral allele frequencies

\pit  $p_i^T$ : The ancestral allele frequency at locus i. This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
36 \newcommand{\pit}{%
37 \ensuremath{%
38 p_i\kinshipsymbols@T%
39 }%
40 \xspace%
41 }%
```

\pith  $\hat{p}_i^T$ : The sample estimator of the ancestral allele frequency at locus i. The parameter being estimated has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the

package option noT is passed. If the package option color is passed, then this symbol turns the color pithColor (default red).

```
42 \newcommand{\pith}{%
43 \ensuremath{%
44 \textcolor{\pithColor}{%
45 \hat{\p}_i\kinshipsymbols@T%
46 }%
47 }%
48 \xspace%
49 }%
```

### 2.6 Wright's $F_{ST}$

\Fst  $F_{ST}$ : Wright's Fixation index. Although the T in the subscript technically refers to the ancestral population T, in this case it is never omitted (even if the package option noT is passed) to always match the more traditional and highly recognizable notation.

```
50 \newcommand{\Fst}{%
51 \ensuremath{%
52 F_{\text{ST}}\%
53 }\%
54 \xspace\%
55 }\%
```

\Fit  $F_{\text{IT}}$ : Wright's total inbreeding coefficient. Although the T in the subscript technically refers to the ancestral population T, in this case it is never omitted (even if the package option noT is passed) to always match the more traditional and highly recognizable notation.

```
56 \newcommand{\Fit}{%
57 \ensuremath{%
58 F_{\text{IT}}}%
59 }%
60 \xspace%
61 }%
```

\Fis  $F_{IS}$ : Wright's local inbreeding coefficient.

```
62 \newcommand{\Fis}{%
63 \ensuremath{%
64 F_{\text{IS}}%
65 }%
66 \xspace%
67 }%
```

#### 2.7 Inbreeding coefficients

\f  $f_B^A$ : The inbreeding coefficient (of  $F_{ST}$ ) of population B relative to an ancestral population A. Note that this command has two mandatory arguments.

```
68 \mbox{ } \mbox{newcommand} \mbox{ } \mbox{
```

```
69 \ensuremath{%
70 f^{#1}_{#2}%
71 }%
72 \xspace%
73}%
```

\ft  $f_j^T$ : The (total) inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\ft[k] gives  $f_k^T$  for individual k). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed. If the package option color is passed, then this symbol turns the color kinColor (default dark green).

```
74 \newcommand{\ft}[1][j]{%
75 \ensuremath{%
76 \textcolor{kinColor}{%
77 f_{#1}\kinshipsymbols@T%
78 }%
79 }%
80 \xspace%
81 }%
```

\fl  $f_j^{L_j}$ : The local inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\fl[k] gives  $f_k^{L_k}$  for individual k).

```
82 \newcommand{\f1}[1][j]{%
83 \ensuremath{%
84 f_{#1}^{L_{#1}}%
85 }%
86 \xspace%
87}%
```

\fs  $f_{L_j}^T$ : The structural inbreeding coefficient of individual j (default). The optional argument allows setting other individuals (\fs[k] gives  $f_{L_k}^T$  for individual k). This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
88 \newcommand{\fs}[1][j]{%
89 \ensuremath{%
90  f_{L_{#1}}\kinshipsymbols@T%
91 }%
92 \xspace%
93 }%
```

#### 2.8 Kinship coefficients

\kt  $\varphi_{jk}^T$ : The (total) kinship coefficient between the pair of individuals j and k (default). The optional argument allows setting another second individual (\kt[1] gives  $\varphi_{jl}^T$  for a second individual l). This parameter has a value that depends on

the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed. If the package option color is passed, then this symbol turns the color kinColor (default dark green).

```
94 \newcommand{\kt}[1][k]{%
          \ensuremath{%
     95
            \textcolor{kinColor}{%
     96
               \varphi_{j#1}\kinshipsymbols@T%
     97
            }%
     99
          }%
          \xspace%
     100
     101 }%
\kl \varphi_{jk}^{L_{jk}}: The local kinship coefficient between the pair of individuals j and k.
     102 \mbox{ } \mbox{newcommand{\kl}{%}}
          \ensuremath{%
    104
            105
     106
          \xspace%
     107 }%
```

\ks  $f_{L_{jk}}^T$ : The structural kinship coefficient between the pair of individuals j and k. This parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
108 \newcommand{\ks}{%
109 \ensuremath{%
110 f_{L_{jk}}\kinshipsymbols@T%
111 }%
112 \xspace%
113 }%
```

\fpw  $f_{L_j}^{L_{jk}}$ : A component of the pairwise  $F_{\rm ST}$  between a pair of individuals j and k (default). The optional argument changes the individual in the subscript only (so \fpw[k] gives  $f_{L_k}^{L_{jk}}$ , and is obviously intended to be used for k only). Note that the actual pairwise  $F_{\rm ST}$  between j and k is given by the average of  $f_{L_j}^{L_{jk}}$  and  $f_{L_k}^{L_{jk}}$ .

```
114 \newcommand{\fpw}[1][j]{%
115 \f{L_{jk}}{L_{#1}}%
116}%
```

#### 2.9 Review of previous work

\Rst  $R_{ST}$ : An  $F_{ST}$  estimator developed for microsatellites.

```
117 \newcommand{\Rst}{%
118 \ensuremath{%}
119     R_{\text{ST}}%
120     }%
121 \xspace%
122 }%
```

```
\PhiSt \phi_{ST}: An F_{ST}-like estimate based on AMOVA.
                 123 \newcommand{\PhiSt}{%
                 124 \ensuremath{%
                         \phi_{\text{ST}}%
                 125
                 126 }%
                 127
                       \xspace%
                 128 }%
           \Gst G_{ST}: Nei's genetic diversity measure.
                 129 \newcommand{\Gst}{%
                 130 \ensuremath{%
                         G_{\text{st}}
                 131
                       }%
                 132
                 133
                       \xspace%
                 134 }%
     \GstPrime G'_{ST}: A normalized G_{ST} statistic.
                 135 \newcommand{\GstPrime}{%
                      \ensuremath{%
                 136
                         G_{\text{ST}}'%
                 137
                     }%
                 138
                 139 \xspace%
                 140 }%
                 \hat{F}_{\mathrm{ST},i}^{\mathrm{sample}} \colon A sample F_{\mathrm{ST}} estimator for a single locus i.
\FstHatSample
                 141 \newcommand{\FstHatSample}{%
                      \ensuremath{%
                          \label{f}_{\text{ST},i}^{\text{sample}}%
                 143
                 144 }%
                 145 \xspace%
                 146 }%
                           Convergence arrows
         \to
as \xrightarrow[m\to\infty]{\text{a.s.}}: Almost sure convergence as m goes to
 \infty.
                 147 \newcommand{\toas}{%
                 148 \xrightarrow[m \rightarrow \infty]{\text{a.s.}}
                 149 }%
          \toN \xrightarrow[n\to\infty]{}: The limit as n goes to \infty. Optional argument changes the variable name
                  (\$\setminus toN[m] \$ gives \xrightarrow[m\to\infty]{}).
                 150 \newcommand{\toN}[1][n]{%
                 151 \xrightarrow[#1 \rightarrow \infty]{}%
                  \xrightarrow[n,m\to\infty]{\text{a.s.}}: Almost sure convergence as both n and m go to \infty.
       \toasNM
                 153 \newcommand{\toasNM}{%
```

```
154 \xrightarrow[n,m \rightarrow \infty]{\text{a.s.}}% 155 }%
```

## 2.11 $F_{ST}$ estimators for independent subpopulations

```
\hat{F}_{\mathrm{ST}}^{\mathrm{indep}}: Asymptotic F_{\mathrm{ST}} estimator for independent subpopulations.
                     \FstHatIs
                                                                156 \newcommand{\FstHatIs}{%
                                                                                    \ensuremath{%
                                                                158
                                                                                              \hat{F}_{\text{st}}^{\text{st}}^{\text{indep}}
                                                               159
                                                               160 \xspace%
                                                               161 }%
                    \FstHatWc \hat{F}_{\mathrm{ST}}^{\mathrm{WC}}: Weir-Cockerham F_{\mathrm{ST}} estimator.
                                                                162 \mbox{ } \mbox{
                                                                                    \ensuremath{%
                                                               164
                                                                                             \hat{F}_{\text{ST}}^{\text{WC}}%
                                                               165
                                                                                  \xspace%
                                                               166
                                                               167 }%
    \FstHatHudson \hat{F}_{ST}^{Hudson}: Hudson pairwise F_{ST} estimator.
                                                               168 \newcommand{\FstHatHudson}{%
                                                               169
                                                                                    \ensuremath{%
                                                                                              \hat{F}_{\text{ST}}^{\text{Hudson}}%
                                                               170
                                                                                  }%
                                                               171
                                                               172
                                                                                    \xspace%
                                                               173 }%
\FstHatHudsonK \hat{F}_{ST}^{HudsonK}: Generalized Hudson F_{ST} estimator (for K subpopulations).
                                                               174 \newcommand{\FstHatHudsonK}{%
                                                                                    \ensuremath{%
                                                               175
                                                                                             \label{eq:linear_text_ST}^{\text{HudsonK}}%
                                                               176
                                                                177
                                                                                   }%
                                                                178
                                                                                    \xspace%
                                                                179 }%
```

#### 2.12 Estimators based on the standard kinship

\ktHat  $\hat{\varphi}_{jk}^{T,\text{std}}$ : Standard kinship estimator for individuals j and k. The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
180 \newcommand{\ktHat}{%
181 \ensuremath{%
182 \hat{\varphi}_{jk}\kinshipsymbols@Ts{std}%
183 }%
184 \xspace%
185 }%
```

```
is by default denoted in the superscript, but which gets omitted if the package
               option noT is passed.
               186 \newcommand{\ftHat}{%
                    \ensuremath{%
              187
                       \hat{f}_j\kinshipsymbols@Ts{std}%
              188
                    }%
              189
                    \xspace%
              190
              191 }%
    \ftHatII \hat{f}_j^{T, \text{stdII}}: Alternate inbreeding coefficient estimator (II) for individual j. The esti-
               mated parameter has a value that depends on the ancestral population T, which
               is by default denoted in the superscript, but which gets omitted if the package
               option noT is passed.
               192 \newcommand{\ftHatII}{%
                    \ensuremath{%
              193
               194
                       \hat{f}_j\kinshipsymbols@Ts{stdII}%
              196
                   \xspace%
              197 }%
   \ftHatIII \hat{f}_i^{T, \text{stdIII}}: Alternate inbreeding coefficient estimator (III) for individual j. The
               estimated parameter has a value that depends on the ancestral population T,
               which is by default denoted in the superscript, but which gets omitted if the
               package option noT is passed.
               198 \newcommand{\ftHatIII}{%
               199
                    \ensuremath{%
              200
                      \hat{f}_j\kinshipsymbols@Ts{stdIII}%
              201
              202
                    \xspace%
              203 }%
              \hat{F}_{ST}^{std}: Standard F_{ST} estimator (based on the standard kinship estimator).
               204 \mbox{ }\mbox{newcommand{\FstHat}{%}}
                    \ensuremath{%
              205
                       \hat{F}_{\text{ST}}^{\text{std}}%
              206
              207
              208
                    \xspace%
              209 }%
\FstHatPrime \hat{F}'_{ST}: Standard F_{ST} estimator adjusted 1.
              210 \newcommand{\FstHatPrime}{%
                    \ensuremath{%
              211
                      \hat{F}_{\text{ST}}'%
              212
                    }%
              213
              214
                    \xspace%
              215 }%
```

\ftHat  $\hat{f}_i^{T,\text{std}}$ : Standard inbreeding coefficient estimator (I) for individual j. The esti-

mated parameter has a value that depends on the ancestral population T, which

```
\FstHatPrimeDbl \hat{F}_{ST}^{"}: Standard F_{ST} estimator adjusted 2.
                  216 \newcommand{\FstHatPrimeDbl}{%
                        \ensuremath{%
                  217
                          \hat{F}_{\text{ST}}''%
                  218
                  219
                  220
                        \xspace%
                  221 }%
```

#### New kinship and $F_{ST}$ estimators 2.13

\ktHatPreadj

 $\hat{\varphi}_{ik}^{T,\text{preadj}}$ : Preadjusted kinship estimator for the pair of individuals j and k (default). The optional argument allows setting another second individual (\ktHatPreadj[1] gives  $\hat{\varphi}_{il}^{T,\text{preadj}}$  for a second individual l). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
222 \newcommand{\ktHatPreadj}[1][k]{%
223
     \ensuremath{%
       \hat{\varphi}_{j#1}\kinshipsymbols@Ts{preadj}%
224
225
226
     \xspace%
227 }%
```

\ktHatPreadjMin

 $\hat{\varphi}_{\min}^{T,\text{preadj}}$ : Minimum value of  $\hat{\varphi}_{jk}^{T,\text{preadj}}$  across pairs of individuals and in the limit of infinite loci.

```
228 \newcommand{\ktHatPreadjMin}{%
   \ensuremath{%
229
    230
231
232
   \xspace%
233 }%
```

 $\hat{\varphi}_{ik}^{T,\text{new}}$ : New kinship estimator for the pair of individuals j and k (default). The optional argument allows setting another second individual (\ktHatNew[1] gives  $\hat{\varphi}_{jl}^{T,\mathrm{new}}$  for a second individual l). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
234 \newcommand{\ktHatNew} [1] [k] {\%}
     \ensuremath{%
235
236
        \hat{\varphi}_{j#1}\kinshipsymbols@Ts{new}%
237
238
     \xspace%
239 }%
```

\ftHatNew  $\hat{f}_i^{T,\text{new}}$ : New inbreeding estimator for individual j (default). The optional argument allows setting other individuals (\ftHatNew[k] gives  $\hat{f}_k^{T,\text{new}}$  for individual k). The estimated parameter has a value that depends on the ancestral population T, which is by default denoted in the superscript, but which gets omitted if the package option noT is passed.

```
240 \newcommand{\ftHatNew}[1][j]{%
            241
                  \ensuremath{%
            242
                    \hat{f}_{\#1}\kappainshipsymbols@Ts{new}%
            243
                  }%
            244
                  \xspace%
            245 }%
            \hat{F}_{\mathrm{ST}}^{\mathrm{new}}: New F_{\mathrm{ST}} estimator.
\FstHatNew
            246 \newcommand{\FstHatNew}{\%
                  \ensuremath{%
                    248
            249
            250
                  \xspace%
            251 }%
     \AMin A_{\text{Emin}}: Minimum value of the expectation of the A_{jk} statistics across all pairs of
             individuals.
            252 \neq Min{\AMin}{%
            253
                  \ensuremath{%
            254
                    A_{\text{emin}}%
                  }%
            255
            256
                  \xspace%
            257 }%
  \AMinHat
            \hat{A}_{\text{Emin}}: Estimator of A_{\text{Emin}}.
            258 \newcommand{\AMinHat}{%
            259
                  \ensuremath{%
                    \hat{A}_{\text{Emin}}%
            260
            261
                 \xspace%
            262
            263 }%
      \max \overline{p(1-p)}^T: Mean ancestral variance. This parameter has a value that depends on
             the ancestral population T, which is by default denoted in the superscript, but
             which gets omitted if the package option noT is passed.
            264 \newcommand{\mav}{%
                  \ensuremath{%
            265
                    \overline{p(1-p)}\kinshipsymbols@T%
            266
                  }%
            267
                  \xspace%
            268
            269 }%
```

#### 2.14 Estimates from Beagle

\klHatBeagle  $\hat{\varphi}_{jk}^{L_{jk}, \text{beagle}}$ : Local kinship estimator based on Beagle, for the pair of individuals j and k.

```
270 \newcommand{\klHatBeagle}{%
               271
                     \ensuremath{%
                        \hat{\varphi}_{jk}^{L_{jk},\text{beagle}}%
               272
                     }%
               273
               274
                     \xspace%
               275 }%
                \hat{f}_{z}^{L_{j}, \mathrm{beagle}}: Local inbreeding estimator based on Beagle, for individual j (default).
\flHatBeagle
                The optional argument allows setting other individuals (\flHatBeagle[k] gives
                \hat{f}_k^{L_k,\text{beagle}} for individual k).
               276 \newcommand{\flHatBeagle}[1][j]{%
               277
                     \ensuremath{%
               278
                        \hat{f}_{\#1}^{L_{\#1}}, \text{beagle}}%
               279
                     \xspace%
               280
               281 }%
```

#### 2.15 Cartoon genotype matrix

I use this cartoon genotype matrix often in Beamer presentations. Unfortunately I also use the color kinshipsymbols package option in my presentations, but due to a strange bug the colors do not show up in Beamer. This solution was found online: https://tex.stackexchange.com/questions/159378/cline-disappears-in-beamer

```
282 % after package colortbl is loaded
283 \makeatletter
284 \@ifclassloaded{beamer}{%
285
     \patchcmd\@cline
286
         {\arrayrulewidth\hfill}% search
287
         {\arrayrulewidth\hfill\kern\z@}% replace
288
         {}% success
         {\errmessage{Patching \string\@cline\space failed}}% failure
289
290 }{%
     % nothing to do here?
291
292 }
293 \makeatother
```

\sampleGenMat This is the bulky code used to generate the cartoon genotype matrix shown in Fig. 1.

```
294 \newcommand{\sampleGenMat}{%
295
     \begin{tabular}{cc}%
296
       & Individuals \\%
       \arrayrulecolor{genColor}\cline{2-2}%
297
       \multirow{10}{*}{\rotatebox[origin=c]{90}{Loci}}%
298
       & \multicolumn{1}{||1|}{0 2 2 1 1 0 1} \\%
299
300
       & \multicolumn{1}{|1|}{0 2 1 0 1 } \\%
301
       & \multicolumn{1}{|1|}{2 ...} \\%
302
       & \multicolumn{1}{|1|}{ } \\%
       & \multicolumn{1}{|1|}{ } \\%
303
```

```
& \multicolumn{1}{|1|}{ } \\%
304
      & \multicolumn{1}{||1|}{ } \\%
305
      & \multicolumn{1}{|1|}{ } \\%
306
      & \multicolumn{1}{||1|}{ } \\%
307
      & \multicolumn{1}{||1|}{ } \\%
308
309
      \arrayrulecolor{genColor}\cline{2-2}%
310
      & \mathbf{X}}\ \\
311
    \end{tabular}%
312
313 }%
```

# **Change History**

v1.0 General: Initial version  $\dots 1$ 

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