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Transformăm ecuația:

$$t^3 y''' = 5t^3 \ln t + 9t^3 + t^2 y'' - 3t y' + 4y$$

$$u_1 = y;$$

$$u_2 = y';$$

$$u_3 = y''$$

Scrivem funcțiile:

$$\text{function } [f_1 \ f_2 \ f_3 \ u_{10} \ u_{20} \ u_{30} \ a \ b \ h] = \text{fet}(t)$$

$$u_{10} = 0;$$

$$u_{20} = 1;$$

$$u_{30} = 3;$$

$$a = 1;$$

$$b = 2;$$

$$h = 0.1;$$

$$f_1 = @ (t, u_1, u_2, u_3) \ u_2;$$

$$f_2 = @ (t, u_1, u_2, u_3) \ u_3;$$

$$f_3 = @ (t, u_1, u_2, u_3) \ 5 * t^{1/3} * \log(t) + 9 * t^{1/3} + t^{1/2} * u_3 - 3 * t * u_2 + 4 * u_1;$$

endfunction

Funcția este una ajutătoare, iar ecuația este rezolvată de:

function $y = RK4(f1, f2, f3, u10, u20, u30, a, b, h)$

$$u1(1) = u10;$$

$$u2(1) = u20;$$

$$u3(1) = u30;$$

$$t = a : h : b$$

$$n = \text{length}(t) - 1;$$

% acum vom incepe rezolvarea propriu zisa.

for $i = 1 : n$

$$K11 = h * \text{feval}(f1, t(i), u1(i), u2(i), u3(i));$$

$$K21 = h * \text{feval}(f2, t(i), u1(i), u2(i), u3(i));$$

$$K31 = h * \text{feval}(f3, t(i), u1(i), u2(i), u3(i));$$

$$K12 = h * \text{feval}(f1, t(i) + h/2, u1(i) + K11/2, u2(i) + K21/2, u3(i) + K31/2);$$

$$K22 = h * \text{feval}(f2, t(i) + h/2, u1(i) + K11/2, u2(i) + K21/2, u3(i) + K31/2);$$

$$K32 = h * \text{feval}(f3, t(i) + h/2, u1(i) + K11/2, u2(i) + K21/2, u3(i) + K31/2);$$

$$K13 = h * \text{feval}(f1, t(i) + h/2, u1(i) + K12/2, u2(i) + K22/2, u3(i) + K32/2);$$

$$K23 = h * \text{feval}(f2, t(i) + h/2, u1(i) + K12/2, u2(i) + K22/2, u3(i) + K32/2);$$

$$K33 = h * \text{feval}(f3, t(i) + h/2, u1(i) + K12/2, u2(i) + K22/2, u3(i) + K32/2);$$

$$K14 = h * \text{feval}(f1, t(i) + h, u1(i) + K13, u2(i) + K23, u3(i) + K33);$$

$$K24 = h * \text{feval}(f2, t(i) + h, u1(i) + K13, u2(i) + K23, u3(i) + K33);$$

$$K34 = h * \text{feval}(f3, t(i) + h, u1(i) + K13, u2(i) + K23, u3(i) + K33);$$