

Moral AI IQP

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April 2019

Abstract

Artificial intelligence is being deployed in increasingly autonomous systems where it will have to make moral decisions. However, the rapid growth in artificial intelligence is outpacing the research in building explainable systems. In this paper, a number of problems around one facet of explainable artificial intelligence, training data, is explored. Possible solutions to these problems are presented. Additionally, the human decision-making process in unavoidable accident scenarios is explored through qualitative analysis of survey results.

Acknowledgements

1. Professor Therese Smith
2. Professor Yunus Telliel
3. Griffin Tabor

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Chapter 1

Introduction

This work has two primary goals. First, we seek to demonstrate how a neural network can learn a bias and empirically determine the severity of that bias. Classification accuracy testing will be employed to evaluate the trained neural network and determine if any bias was learned, and, if so, the severity of that bias. Second, we also seek to understand the decision-making process in humans behind making moral decisions in unavoidable accident scenarios, i.e., dilemmas. This part of the research will be done by surveying a group of people and performing qualitative analysis on the survey results. These results serve not only as a way to understand this decision-making process but also as a language and structure we can use to craft communications with those unfamiliar with artificial intelligence.

Chapter two provides an overview of what explainable AI is and the current demands for it, in addition to covering prior research into how humans think when presented with a dilemma. Chapter three discusses the architecture, training, and testing of a neural network and what questions we asked in the aforementioned survey. Chapter four analyses the neural network testing results and the survey results. Chapter five concludes this work and provides avenues for future inquiry.

Chapter 2

Background

Introduce background readings (maybe not first?).

Autonomous vehicle technology is growing rapidly and AI is a key piece of that technology. As this technology gets closer to attaining full autonomy, the AI deployed in these systems will have greater responsibility than ever. These AI systems must be explainably fair, i.e., they must both make decisions using only the least amount of information necessary for optimal performance and make those decisions predictably and correctly. For example, the AI in an autonomous vehicle does not need to be supplied with information about a pedestrian's race, even though race may be an impactful trait in other fields, especially medical fields [2]. Furthermore, these AI systems must also be explainable for legal reasons, such as determining which party is at fault in the event of a car accident or, in the European Union, complying with a user's "right to explanation" [8].

The demand for explainable AI is increasing, as illustrated by DARPA's Explainable Artificial Intelligence (XAI) program [10]. This program aims to develop explainable AI systems such as in Figure 2.1. There has also been a symposium focusing on AI inclusivity towards marginalized peoples [6, 1]. This symposium illustrates the increasing need to discuss AI fairness and inclusivity in a way that non-technical people can understand. One facet of this need that this paper addresses is the question of specifically how much one needs to care about possible biases in the various stages of AI architecture. Not all AI research involving morally responsible AI systems has a focus on explainability, however. NVIDIA trained an end-to-end convolutional neural network, which "[maps] raw pixels from a single front-facing camera directly to steering commands" [5]. With this approach, the AI will have to respond directly to pedestrians and other external stimuli.

We must also address the ethical and moral side of AI. A reflection on ethics is critical to avoid building irresponsible AI systems. These systems affect, or will affect in the near future, many people's lives. Take, for exam-

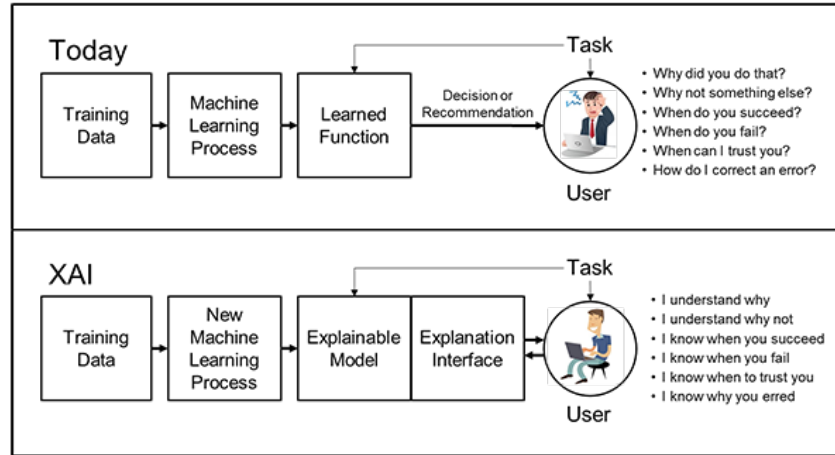


Figure 2.1: DARPA's XAI Concept [9]

ple, the case of an autonomous vehicle. By allowing autonomous vehicles in our society, we are accepting the dangers they bring in exchange for the benefits they provide; among these dangers are injury and loss of life to those involved in vehicular accidents. Those developing AI systems therefore have a responsibility to improve these systems and reduce the dangers associated with their use. They also have a responsibility to "assess, and try to inform others of, the possible social consequences" of these systems [12]. We can then conclude that building AI systems carries with it moral responsibility. This realization can also be seen in a proposed bill, the "Algorithmic Accountability Act of 2019" by Senator Wyden, which would have the Federal Trade Commission "create regulations requiring companies under its jurisdiction to conduct impact assessments of highly sensitive automated decision systems", require companies "assess their use of automated decision systems", and require companies "correct any issues they discover during the impact assessments" [3]. This bill is effectively an effort to extend anti-discrimination laws to "automated decision systems", which, as of late, are typically AI systems.

The software architects, engineers, and researchers which build AI systems must address moral concerns about explainability and fairness in their products. However, they may be morally uncertain with respect to how they can address these concerns. Resolving this moral uncertainty is a nontrivial problem. Simply choosing a resolving act based on personal preference is clearly unacceptable. A "Continue Deliberating" strategy is equivalent to an instance of the previous strategy, so it is also unacceptable [12]. An ethical framework, then, is required to resolve this uncertainty. The work of Bhargava and Kim [12] proposes an "Expected Moral Value" approach which acts

as an ethical meta-framework one can use to resolve this moral uncertainty. While this cannot act as a universal solution, it shows progress in the right direction and serves as a starting point of inquiry for those building AI systems.

Moving to the domain of how humans think about dilemmas, we look towards the Moral Machine experiment [4], which is prior research into people’s preferences in moral dilemmas. This experiment involved an online survey in which participants are shown a moral dilemma involving an autonomous vehicle, passengers, and pedestrians. In each dilemma, the participant must choose between inaction, which typically results in the certain death of the pedestrians, and action, which typically results in the certain death of the passengers. The study revealed three strong global preferences towards sparing humans over animals, sparing more lives rather than fewer, and sparing younger lives rather than older. The study also showed that some preferences vary between countries depending on that country’s propensity towards egalitarianism.

Chapter 3

Methods

3.1 Data Generation

The data is generated using a graphical model to control the conditional probabilities for the states of each variable. The variables in the model correspond directly to the attributes of a person. Figure 3.1 is a rendering of the graphical model. For example, people in the first option could be more likely to jaywalk than people in the second option, producing a data set which is biased towards/against jaywalkers. When combined with control over the number of people in each option, this method can produce both subtle and strong bias. The code for the domain of each attribute of a person is in Figure 3.2. The Python library pgmpy is used to create the graphical model and infer each variable's probability distribution. These distributions are then used to pick elements from each variable's domain. This process is repeated for each attribute of each person and for the number of people in each option of a dilemma, forming a complete dilemma. The number of dilemmas generated is specified programmatically using the `TrainMetadata` class, which captures the number of dilemmas to generate and the maximum number of people per option.

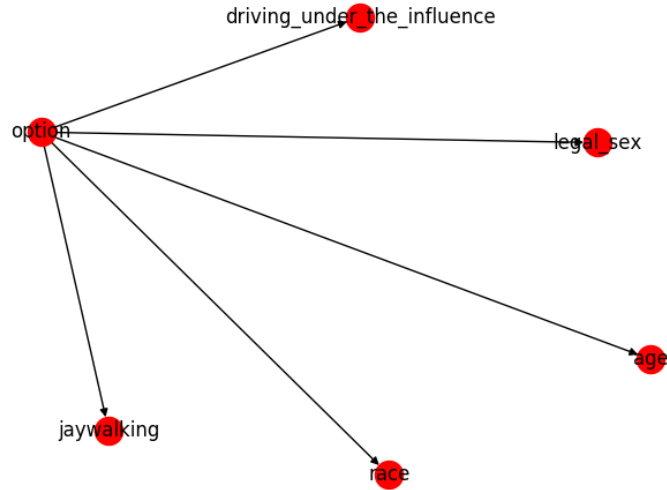


Figure 3.1: The graphical model.

```

age_states = [10, 20, 30, 40, 50, 60]
race_states = [Race.white, Race.black, Race.asian,
               Race.native_american, Race.other_race]
legal_sex_states = [LegalSex.male, LegalSex.female]
jaywalking_states = [False, True]
driving_under_the_influence_states = [False, True]

```

Figure 3.2: Python code for the bracketed attributes of a Person

3.2 Data Bracketing

Attributes are one-hot encoded (i.e., mapped using an indicator function) so the neural network is resilient to unspecified attributes. Age is bracketed by increments of 10 years. Some example encoded ages are shown in Table 3.1. Boolean attributes are encoded into three increments, as shown in Table 3.2.

Age (yr)	unspecified	1-10	11-20	21-30	31-40	41-50	51-60
unspecified	1	0	0	0	0	0	0
0	0	1	0	0	0	0	0
3	0	1	0	0	0	0	0
16	0	0	1	0	0	0	0
42	0	0	0	0	0	1	0

Table 3.1: Example age attribute encoding.

Value	unspecified	false	true
unspecified	1	0	0
false	0	1	0
true	0	0	1

Table 3.2: Example boolean attribute encoding.

3.3 Data Storage

Data is stored using the JSON format using a serialization process called pickling via the Python library `jsonpickle`. This process was chosen because it produces easily machine-readable files and because JSON is a popular data storage format. The purpose of storing the generated data sets is to keep the data consistent between test iterations and to share the data. Both the training and test data sets are pickled after generation.

3.4 Neural Network Model

There are two primary requirements of the neural network used in the experiments. First, the network must classify the training data. In other words, when given a dilemma, the network must classify that dilemma by picking which option to avoid. For example, in a dilemma with two options of three and four people, respectively, the correct classification is the second option because it allows the autonomous vehicle to save more people. In the case where a dilemma has two or more options of equal size, the earlier option is chosen.

Second, the network must be easy to train, meaning that the time required to train the network must be small (on the order of minutes or less) and the hardware resources required to train the network must be minor. Testing the network requires training it many times, so the time required to train the network must be small. Additionally, the network will be trained on personal machines, so any hardware requirements must be easy to meet.

There are three models which were considered when deciding on what network to use. First, an autoencoder: autoencoders are trained using un-

supervised learning, so labeling the data is not necessary (want to avoid imparting a set of morals). This model would perform dimensionality reduction, and perhaps learn to ignore noise (i.e., uniformly distributed attributes) in the data set, but would be unable to classify the dilemmas.

Second, an autoencoder in combination with a simple neural network trained using supervised learning: this model solves the classification problem which the previous model failed at, but introduces unnecessary complexity to the research. The intent of this research is not to build a neural network capable of guiding a real autonomous vehicle, so this model was deemed unnecessarily complex.

Lastly, a recurrent neural network (RNN) with long short-term memory (LSTM). This option was considered because RNN's are capable of accepting variable-length sequential data. We thought the network may need to handle variable-length data, but the engineering challenge that design posed was traded in favor of both limiting the maximum number of people in an option and bracketing the data as covered in section 3.2. Additionally, this network does not directly solve the classification problem, so it is only marginally applicable for this research.

The final neural network chosen is a simple, shallow, feed-forward network with one hidden layer trained using supervised learning, pictured in Figure 3.3. The input layer has dimensionality equal to the number of attributes per person (after one-hot encoding) multiplied by the number of options per dilemma multiplied by the maximum number of people per option. The output layer has dimensionality equal to the number of options per dilemma. The hidden layer has dimensionality equal to the average of that of the input and output layers. An example implementation in Keras of the model can be seen in Figure 3.4.

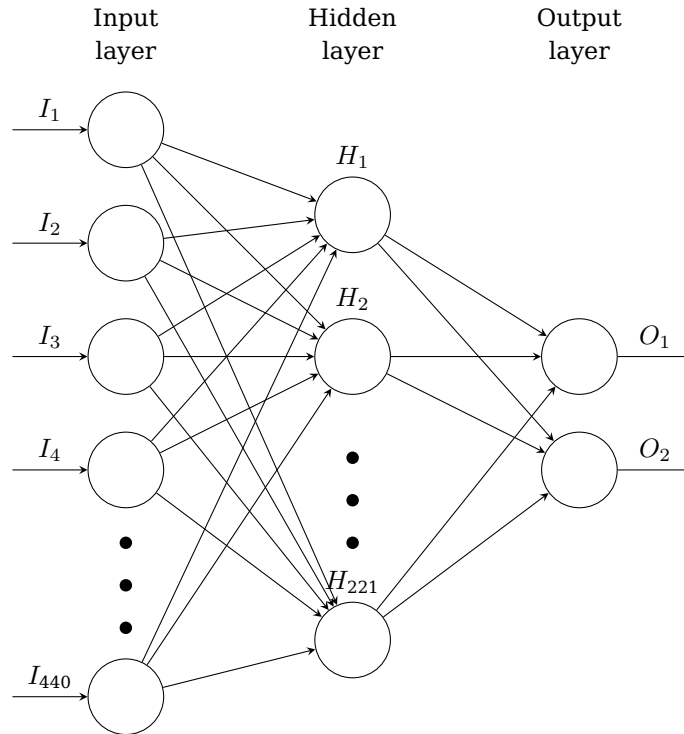


Figure 3.3: A shallow feed-forward neural network with one hidden layer.

```
output_dim = 2
input_dim = 22 * output_dim * \
    train_metadata.max_num_people_per_option

model.add(Dense(units=input_dim, activation='relu',
    input_dim=input_dim))
model.add(Dense(units=round((input_dim + output_dim) / 2),
    activation='relu'))
model.add(Dense(units=output_dim, activation='softmax'))
```

Figure 3.4: The Keras code for the neural network model.

3.5 Neural Network Training

The training data given to the network is categorical, so the categorical cross entropy loss function is used. As the network is quite simple, a stochastic gradient descent optimizer suffices. Training happens over 5 epochs with a batch size of 32. An example implementation in Keras can be seen in Figure 3.5; additionally, Figure 3.6 provides a simple visualization of the dimensionality of the network.

```
model.compile(loss=losses.categorical_crossentropy,  
              optimizer='sgd',  
              metrics=[metrics.categorical_accuracy])  
  
model.fit(train_data, train_labels, epochs=5, batch_size=32)
```

Figure 3.5: The Keras code for the neural network model.

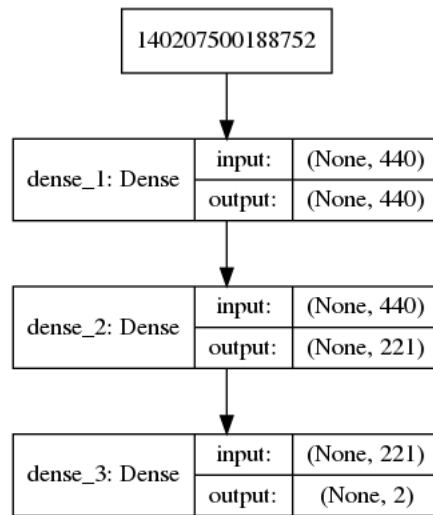


Figure 3.6: The dimensions of the neural network used in this research.

3.6 Neural Network Testing

The neural network is tested using Keras to evaluate the classification accuracy and loss against a test data set. The test data is generated using a

graphical model in the same manner as the training data; however, it is important to note that in this step, the test data is generated separately from the training data: it is not a sampled subset of the training data. Each training data set is tested five times. Each iteration involves training the neural network on the training data set and evaluating its performance against a test data set to collect classification accuracy and loss information. The results of all five iterations are averaged to produce an average classification accuracy and loss. Many training data sets are generated and tested against the same test data set. Each data point in Figure A.2 corresponds to a unique training data set. All data points in the figure are tested against the same test data set.

The test result naming format, seen, for example, in the caption of Figure A.2, reproduced here in Figure 3.7, contains all the information necessary to understand the characteristics of the test data set. The name can be split into three sections. First, "40-60" refers to the probability distribution of people among the two options: $P(O_1) = 0.4$, $P(O_2) = 0.6$ (and for any dilemma with two options, $P(O_2) = P(\neg O_1)$). Second, "100-0" refers to the probability distribution of jaywalking for those in the first option. $P(\neg J \mid O_1) = 1$, $P(J \mid O_1) = 0$. Finally, "0-100" refers to the probability distribution of jaywalking for those in the second option. $P(\neg J \mid O_2) = 0$, $P(J \mid O_2) = 1$.

Classification accuracy against test 40-60 100-0 0-100

Figure 3.7: The title of Figure A.2

3.7 Survey

A group of primarily engineering-focused undergraduate college students was surveyed. These students were in attendance of an introductory ethics course, so their responses are likely more ethically sensitive than those of an average individual. The responses discussed later are still useful in crafting communications with those outside of AI research, but might not extend as easily towards the general public. Participation in the survey was voluntary and each question in the survey was optional. The survey question are:

1. If you had to choose between two accident scenarios, one in which a single person would certainly be killed, and the other which some number of people, a cluster of people, might be able to escape, how many people would that cluster have to contain (could be infinite), before you would choose the single person scenario?
2. Please describe thoughts that went through your mind as you weighed the choice above.

3. Would you trust AI to be race-blind if it were tested for not having racial bias?
4. What would you need to know about the test, to feel protected against race-bias in AI?

Chapter 4

Findings and Analysis

4.1 Response to Bias

Our research found that the AI became biased when the training data featured a strong trend not present in the test data. For purposes of a control test, a test data set was generated with uniformly distributed people and a uniformly distributed jaywalking probability. Figure A.14 shows the result of this test. In this scenario, $P(J)$ is observed to be independent of $P(O_1)$. When $P(J | O_1) < 0.1$, the neural network classifies dilemmas incorrectly. This trend continues as $P(J | O_1)$ decreases, thereby increasing the severity of the bias in the training data set. A similar but opposite trend occurs when $P(J | O_1) > 0.9$.

Observing the contour plot in Figure A.2, one can see that classification accuracy decreases abnormally (i.e., differently than in the control in Figure A.14) when $P(O_1) > 0.6$ and $P(J | O_1) < 0.2$. In this area, the training data set consists mostly of people in the first option. Most people in the first option are not jaywalkers and most people in the second option are. Therefore, the training data set is biased to prefer non-jaywalkers because they appear disproportionately frequently in the (larger) first option. The neural network, now having learned this trend, is tested against a test data set in which most people are in the second option. Those in the first option are not jaywalkers and those in the second option are. The network tends to select the first option because it contains far fewer jaywalkers than the second option, despite the first option being smaller than the second and therefore the incorrect choice. This causes the network's classification accuracy to decrease in this region. The trend continues as $P(O_1)$ increases while $P(J | O_1)$ decreases, thereby increasing the severity of the bias in the training data set. Another view into the network's decisions is Figure A.4, which shows the real value of $P(J)$ when the network classified a dilemma incorrectly. In the areas of the contour plot corresponding to Figure A.2's

areas of worst accuracy, we can see that the real value of $P(J)$ is close to zero. In other words, the network performs worst when it picks an option because that option is absent of jaywalkers (i.e., when the network makes a decision based on the bias it learned rather than the rule used to label the test data set). This is further evidence that the network has learned a bias against jaywalkers. A similar but opposite trend occurs when $P(O_1) < 0.4$ and $P(J | O_1) > 0.8$.

4.2 Avoiding Bias

Three ways for the neural network to learn a bias

1. Flaws in data

- (a) Any information which is not strictly necessary for the neural network to make effective decisions should not be given to the network. This especially affects end-to-end networks such as the convolutional neural network in [5] because these systems have an enormous variety of (sometimes) unfiltered data given to them. This approach can increase the risk of the neural network learning a bias.

2. Flaws in AI architecture

- (a) This research uses a simple, shallow neural network to reduce architectural complexity. Deeper networks, specifically deep convolutional networks, undoubtedly perform better, but these network architectures suffer from increased design complexity and increased training difficulty [11].
- (b) Neural networks used for image-based object detection suffer from predictive inequality in detecting people of differing skin tones [13]. Those with skin tones in the Fitzpatrick range [1, 3] are more accurately identified than those with skin tones in the [4, 6] range. Furthermore, this problem persists between networks of different architectures. Although the authors of that research propose a different loss function which decreases predictive inequality, one could imagine a totally different system which does not use color cameras at all. Infrared cameras may serve as a good replacement because they produce images which are easier to filter with traditional computer vision techniques than images from color cameras are.

3. Flaws in testing

- (a) If one is concerned that a system may be less able to measure some attribute in a certain environment, then the testing for the system may want to overrepresent that attribute. In the context of [13], the test data set used might consist of a majority of images of people with skin tones in the Fitzpatrick range [4, 6], regardless of whether the system is expected to operate in an environment consistent with that skin tone distribution or not.
- (b) If a system should be equally sensitive to all of its inputs, then those input should be represented equally during testing, even if a different distribution of inputs is expected to be encountered when the system is deployed. In the case of autonomous vehicles, this research assumed the neural network should treat all people equally, but in reality this is a region-specific measure. The Moral Machine experiment measured strong regional preferences for various aspects of decision-making during dilemmas [4]. For example, Eastern countries showed an almost nonexistent preference for sparing the young compared to Western and Southern countries. Southern countries showed a strong preference for sparing females compared to Western and Eastern countries. Not all regional preferences can be reliably accounted for, however. Some preferences, such as the Eastern countries stronger preference for sparing the lawful compared to Western and Southern countries, is not entirely enforceable by AI systems. Some instances of lawfulness classification could be reliable, such as detecting jaywalkers, but others, such as detecting unlawful intoxication, are most likely difficult. There is, of course, the question of whether or not autonomous vehicles should contain any regional preferences or whether they should be totally fair; however, that is outside the scope of this paper.

4.3 Survey Results

Thirty-five survey responses were collected. We found several themes in these responses, which are summarized in Figure A.1 and explained in greater detail here:

1. Humans can be flawed
 - Humans can have bias.
 - Flaws in humans can lead to flaws in AI systems design and in data sets.
2. Data can be flawed

- AI systems trained on flawed data will show flawed performance.
3. Value saving more lives over fewer
 - This is consistent with one of the Moral Machine experiment's findings [4].
 4. Unwillingness to kill
 - Killing is generally unjustifiable; therefore, an action that causes a greater number of people to be spared is not necessarily desirable.
 - If there is an option with a chance that people might not die, that option is more desirable than an option containing one person who will certainly be killed, despite the prior option containing more people.
 5. Demand for testing
 - Because both humans and data can be flawed, testing must be employed to validate the fairness of the AI system.
 - These tests must have great breadth and cover many scenarios and people, especially minorities.
 - The data used for training and testing should be transparent.
 - The methods of testing should be transparent.
 - Good testing methodologies and good results can lead to trust in AI systems.

How to address these concerns

- People can be flawed
 - This can be addressed with architectural approaches to AI system design. We can restrict what features the neural network has access to. We can evaluate different sensor technologies and select the sensor that performs best in the system's expected operating environment. We can employ low-level safety mechanisms to catch some erroneous decisions the neural network may make.
 - Should I explain the restriction layer in more detail here? Perhaps link to a publication, if there is one?
- Data can be flawed
 - This can be addressed with sensitivity studies. This research provides a format to determine an neural network's sensitivity to flawed data.

- People have varying opinions of how an autonomous vehicle should react in dilemma situations.
 - An AI system operating an autonomous vehicle is in control at all times. The system must decide what to do in a dilemma. There is no inaction: choosing inaction is equivalent to choosing an action with the same result as inaction. Therefore, the system must be programmed, either explicitly through traditional techniques or implicitly through machine learning, to respond a specific way in a dilemma. Not all end-users may find the system's programming ethically acceptable.
 - Some survey respondents expressed interest in a "personal AI" solution in which the end-user of an autonomous vehicle can input their preferences to modify how the AI will react in a dilemma.
 - A personal AI system brings with it a number of ethical questions
 - * What parameters should be tunable? Certainly the end-user should not be able to tell the AI to prefer one race over another.
 - * Should the set of tunable parameters be regulated such that all autonomous vehicles are required to have the same set of tunable parameters?
 - * How liable is the autonomous vehicle manufacturer and any other parties involved in training/testing the AI system?
 - * How liable is the end-user in tuning their autonomous vehicle (perhaps a tuning decision they made caused greater personal injury than if they had chosen a different option).

Chapter 5

Conclusion and Future Work

5.1 Conclusion

1. Our research found that AI becomes biased when ?. Therefore, one must take a certain amount of care in dealing with bias in data (how much?).
2. In order to avoid training biased AI, we recommend formatting training data such that ?.
3. We also recommend that
 - Teams that work with AI, especially teams which create or train AI, should include social scientists.
 - AI could be verified by 3rd party groups in addition to a team's internal testing.

5.2 Future Work

- Explanations, whether of AI decisions, architecture, or other, must be delivered in a way that the user can understand. As Gilpin puts it, "The success of this goal is tied to the cognition, knowledge and biases of the user: for a system to be interpretable, it must produce descriptions that are simple enough for a person to understand using a vocabulary that is meaningful to the user" [7]. This paper has attempted to show specifically how much care one must take in dealing with bias in data, but more attention is needed in other areas of AI systems architecture.

- Repeat this work's sensitivity testing on current state-of-the-art models and determine their sensitivity to bias in training data.
- Develop a software library to report correlations in data. This library would accept a data set, analyse it to find any and all correlations between different attributes, and report those correlations and their associated strengths. The intent is to use this software to proactively detect possible false correlations in data sets before they are used for training or testing.

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Appendix A

Figures

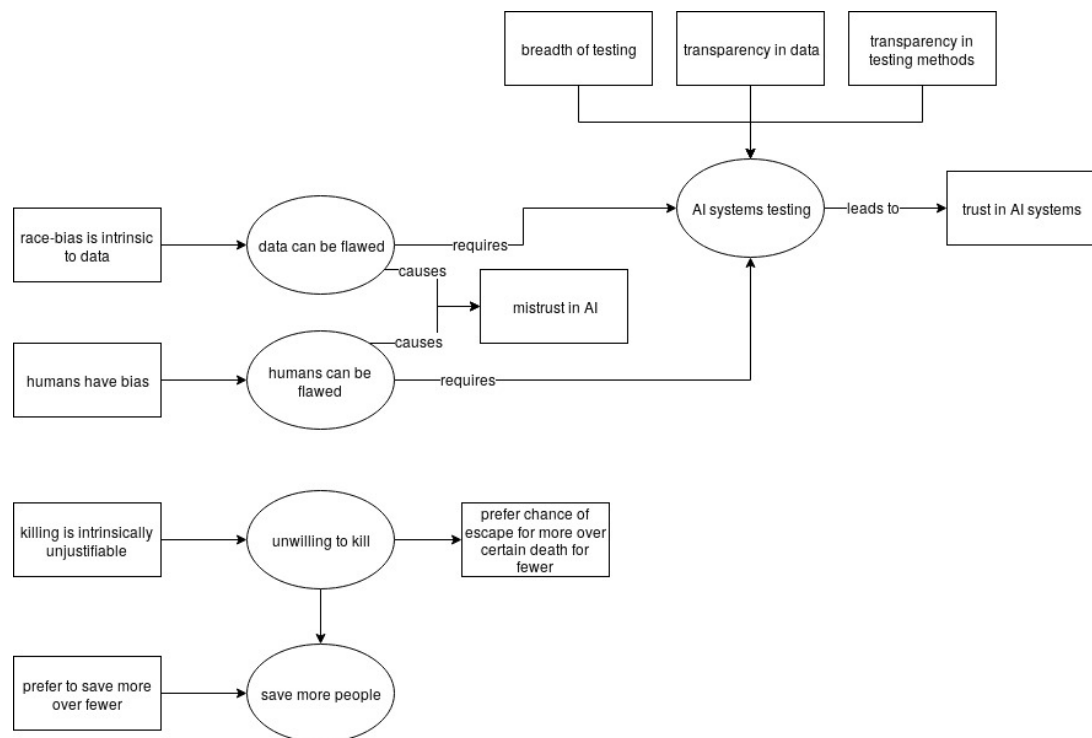


Figure A.1: Qualitative analysis of the survey results.

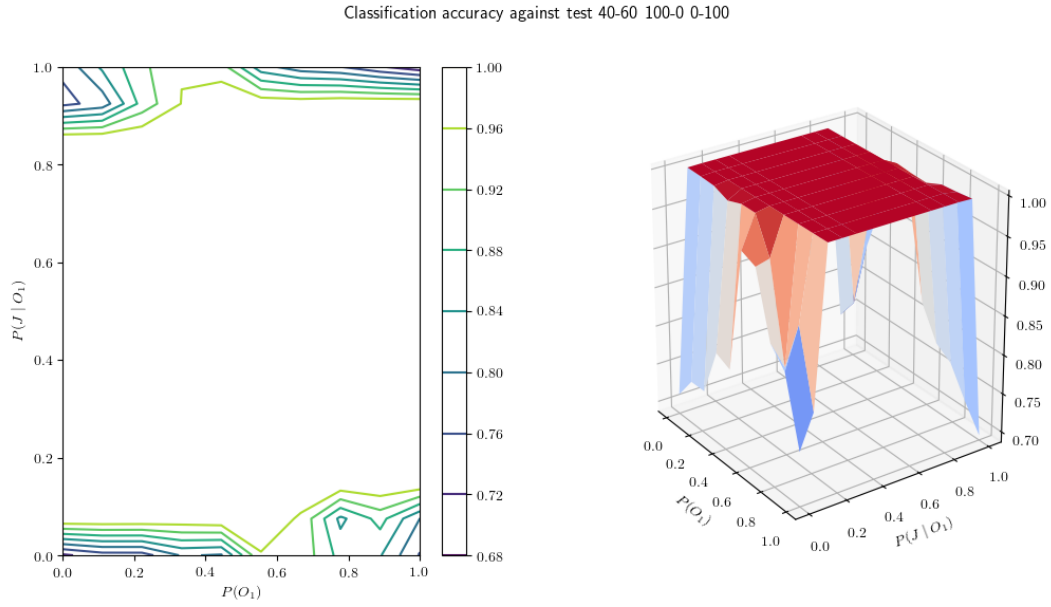


Figure A.2: The classification accuracy against test 40-60 100-0 0-100.

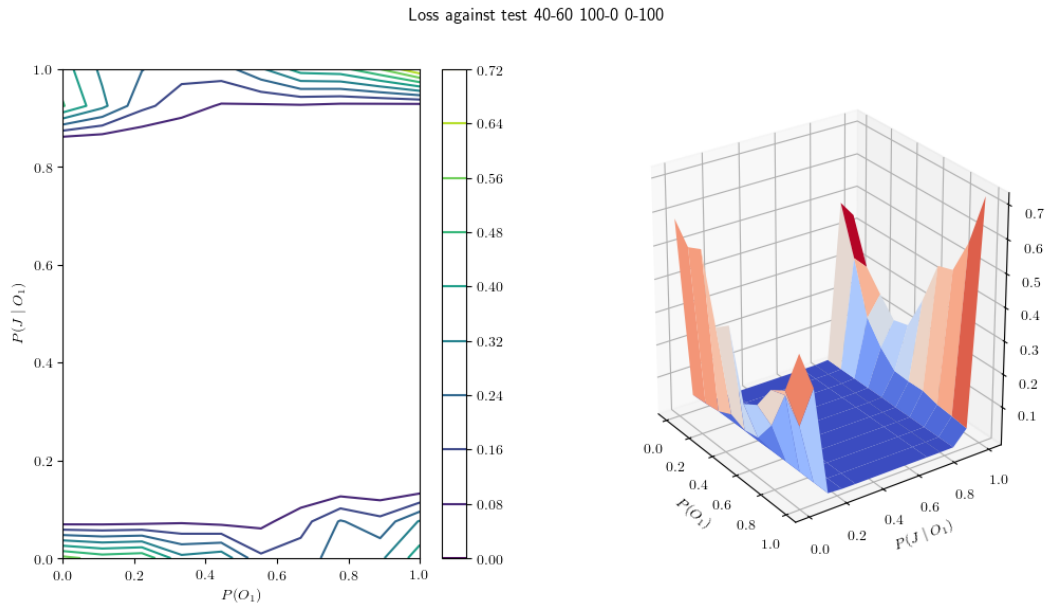


Figure A.3: The loss against test 40-60 100-0 0-100.

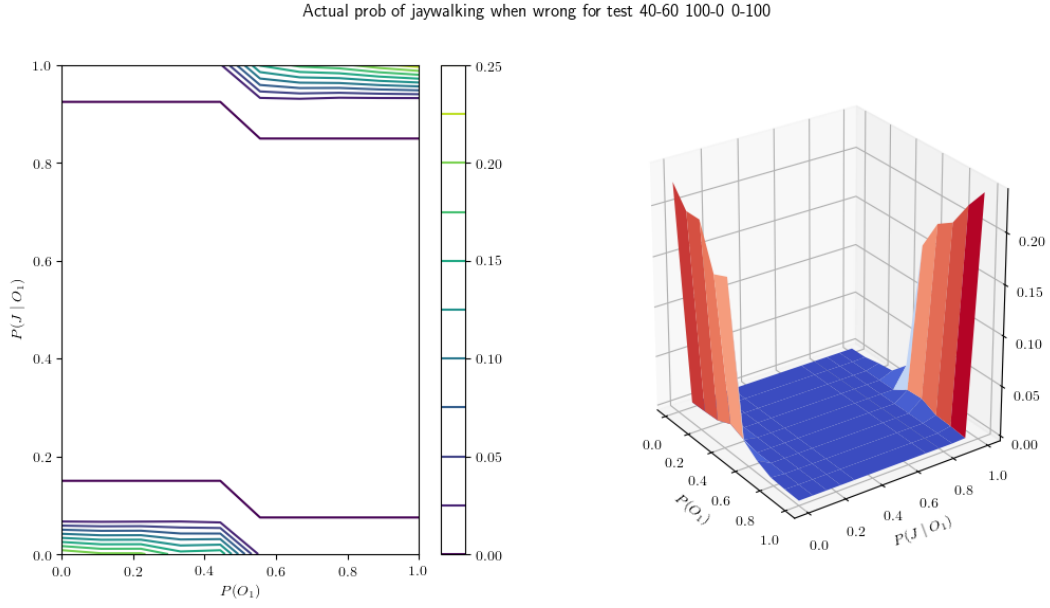


Figure A.4: The actual jaywalking probability when classified incorrectly against test 40-60 100-0 0-100.

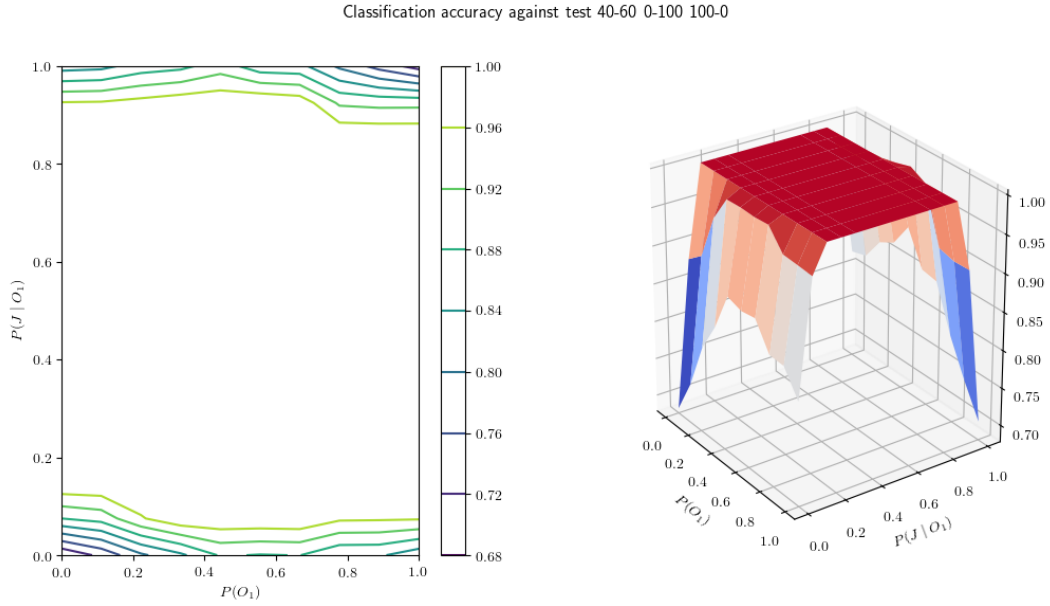


Figure A.5: The classification accuracy against test 40-60 0-100 100-0.

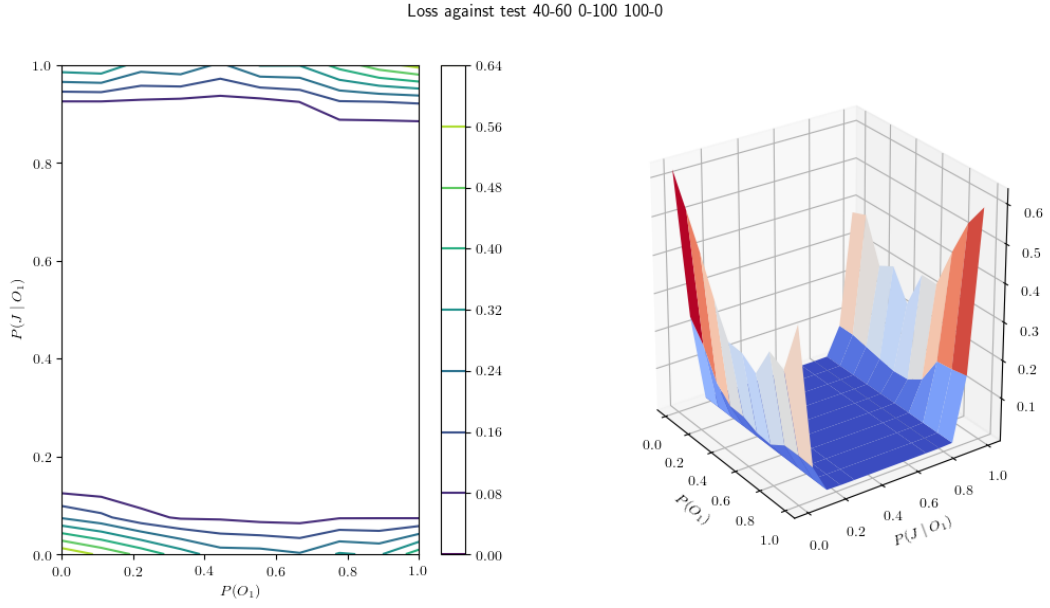


Figure A.6: The loss against test 40-60 0-100 100-0.

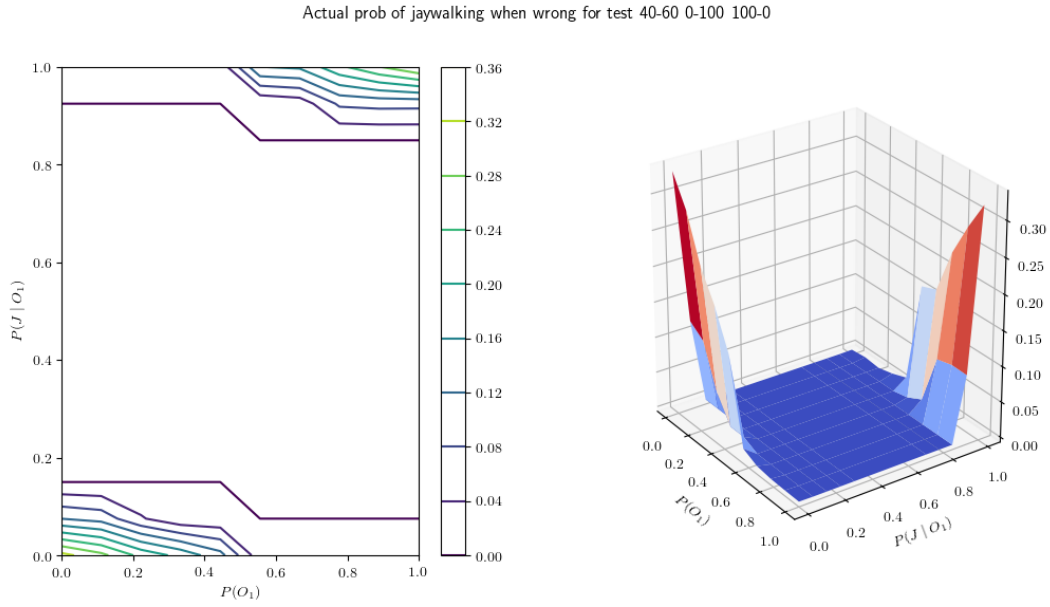


Figure A.7: The actual jaywalking probability when classified incorrectly against test 40-60 0-100 100-0.

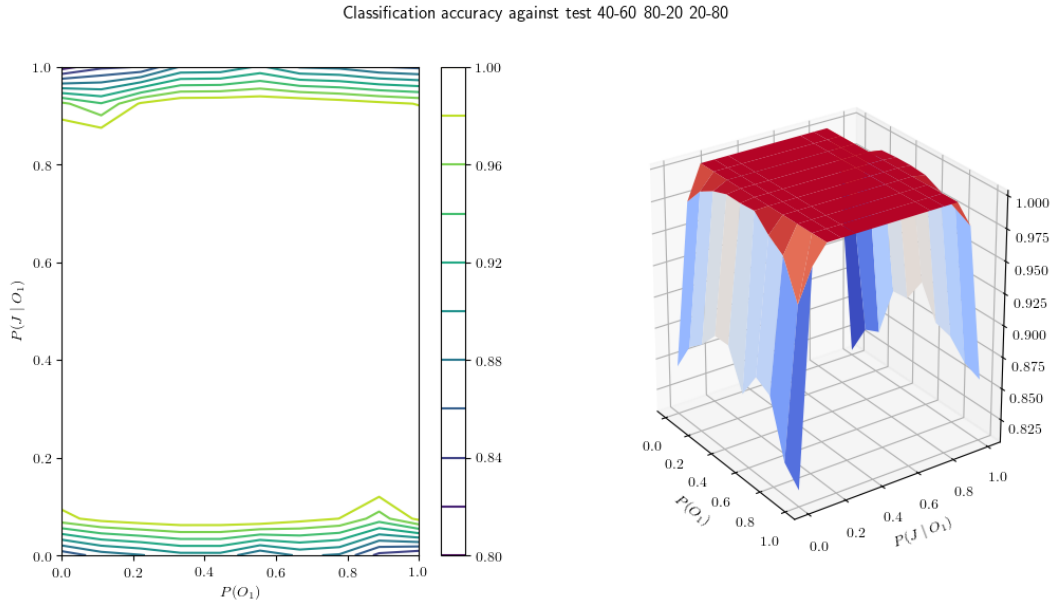


Figure A.8: The classification accuracy against test 40-60 80-20 20-80.

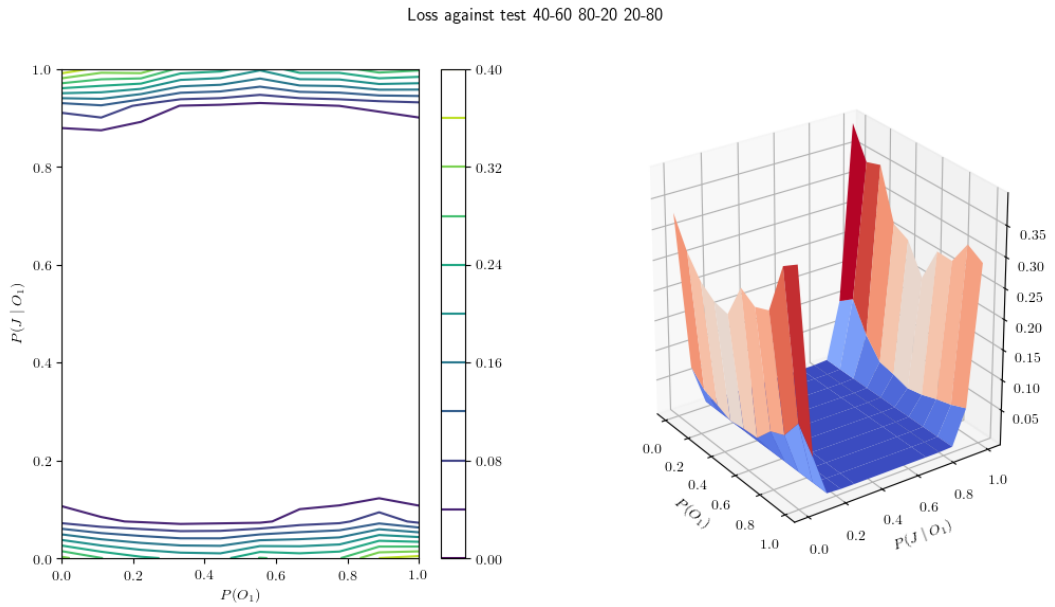


Figure A.9: The loss against test 40-60 80-20 20-80.

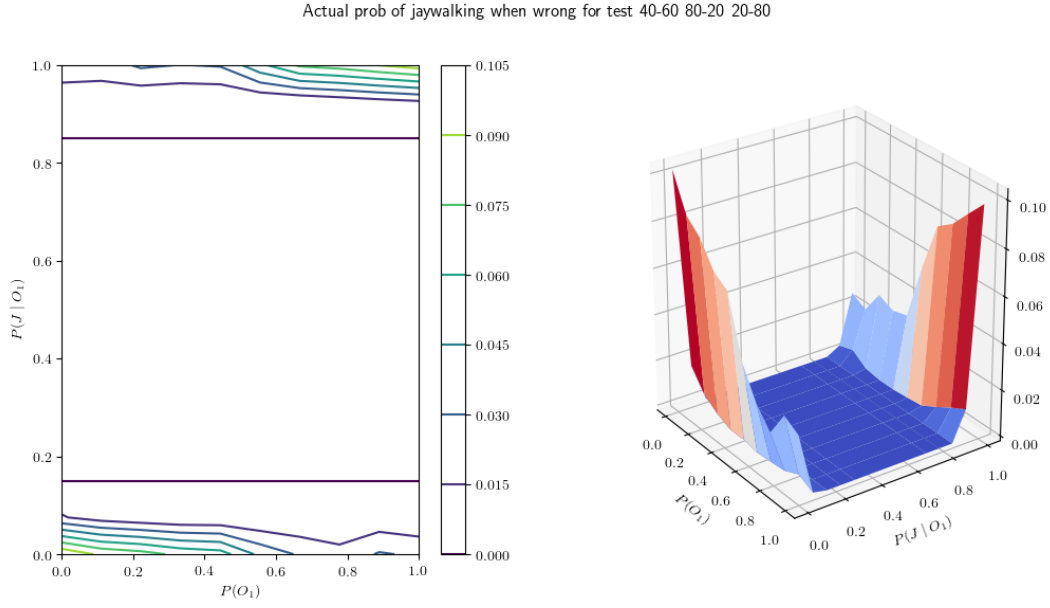


Figure A.10: The actual jaywalking probability when classified incorrectly against test 40-60 80-20 20-80.

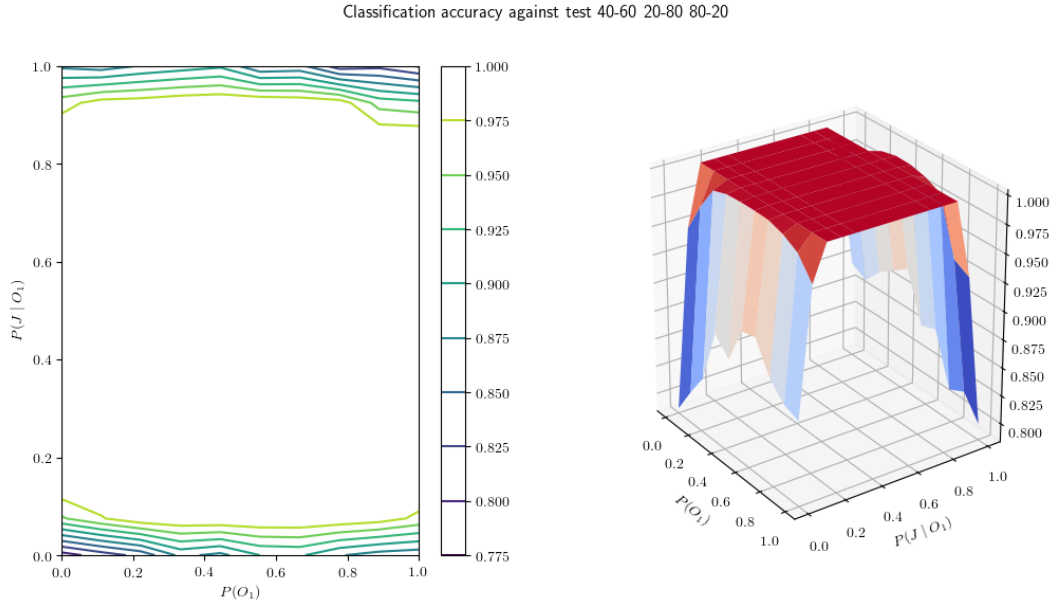


Figure A.11: The classification accuracy against test 40-60 20-80 80-20.

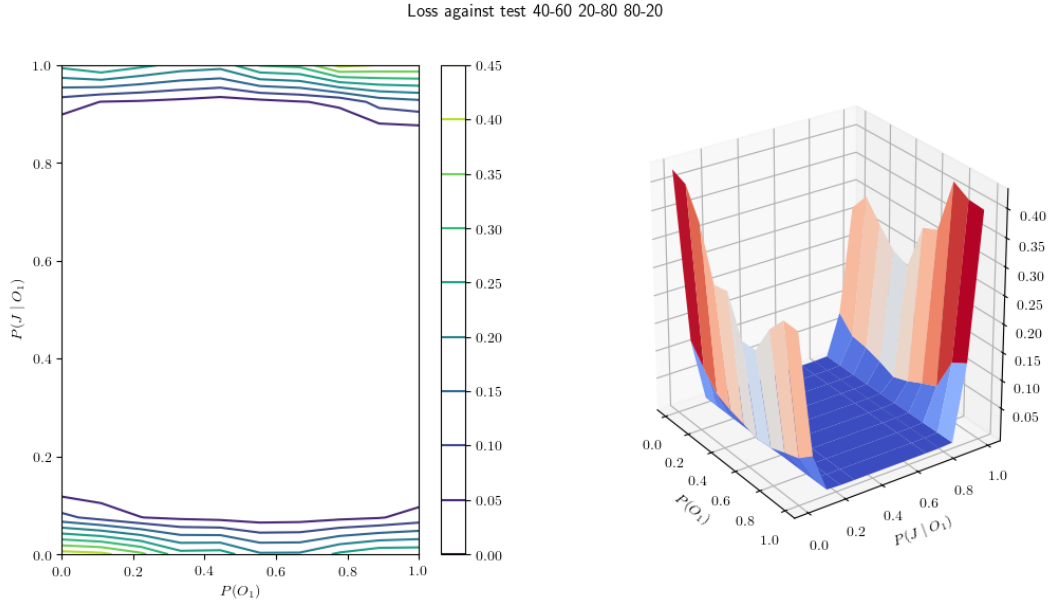


Figure A.12: The loss against test 40-60 20-80 80-20.

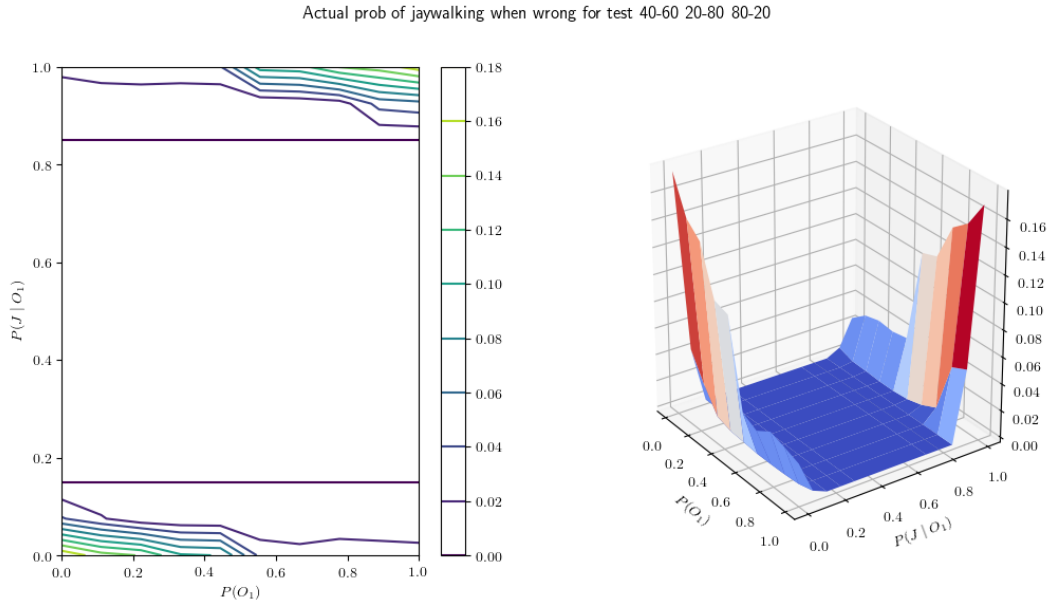


Figure A.13: The actual jaywalking probability when classified incorrectly against test 40-60 20-80 80-20.

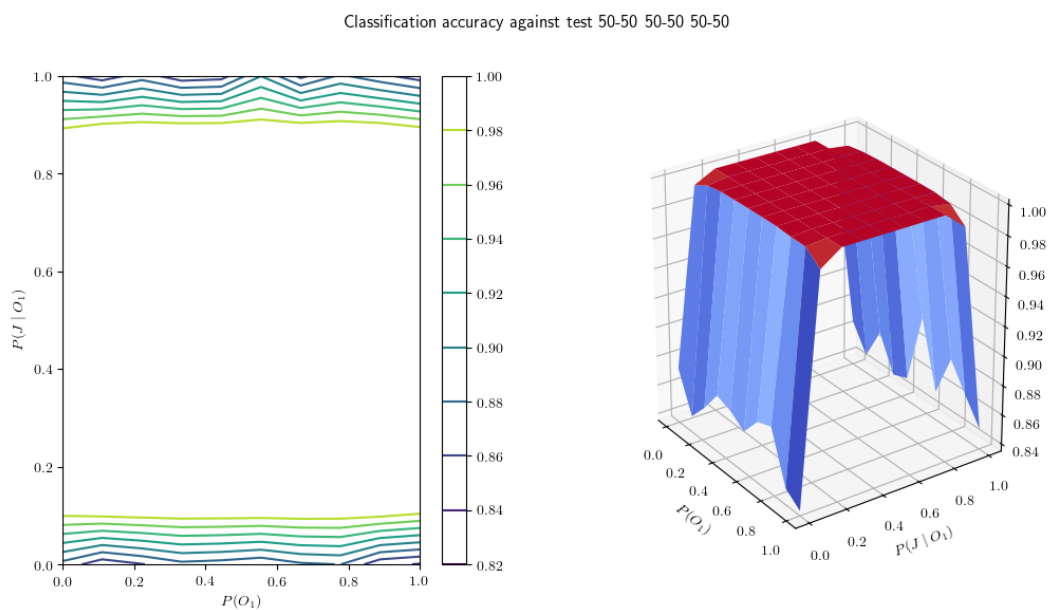


Figure A.14: The classification accuracy against test 50-50 50-50 50-50.

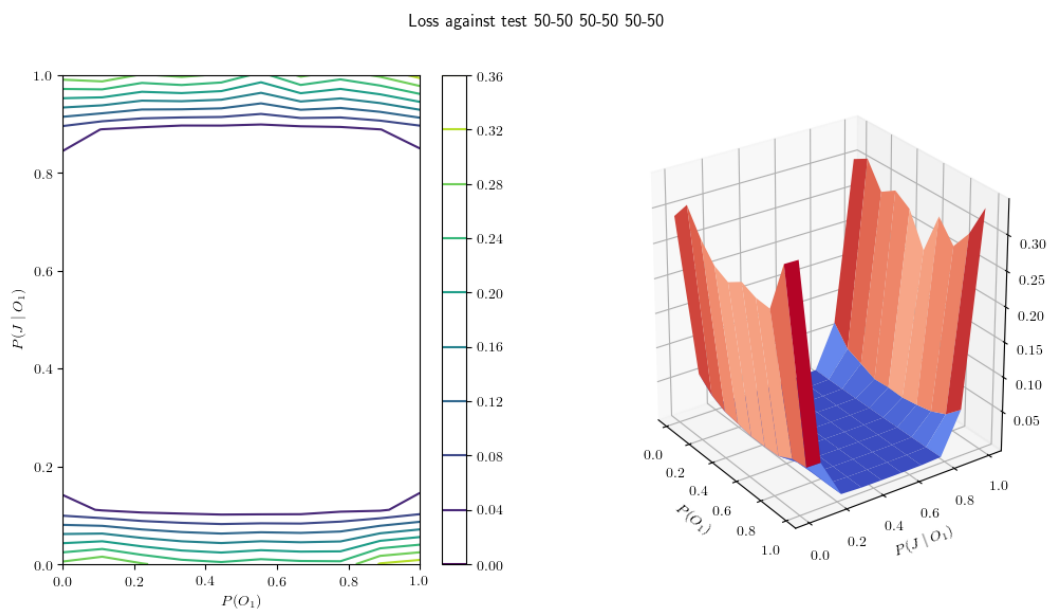


Figure A.15: The loss against test 50-50 50-50 50-50.

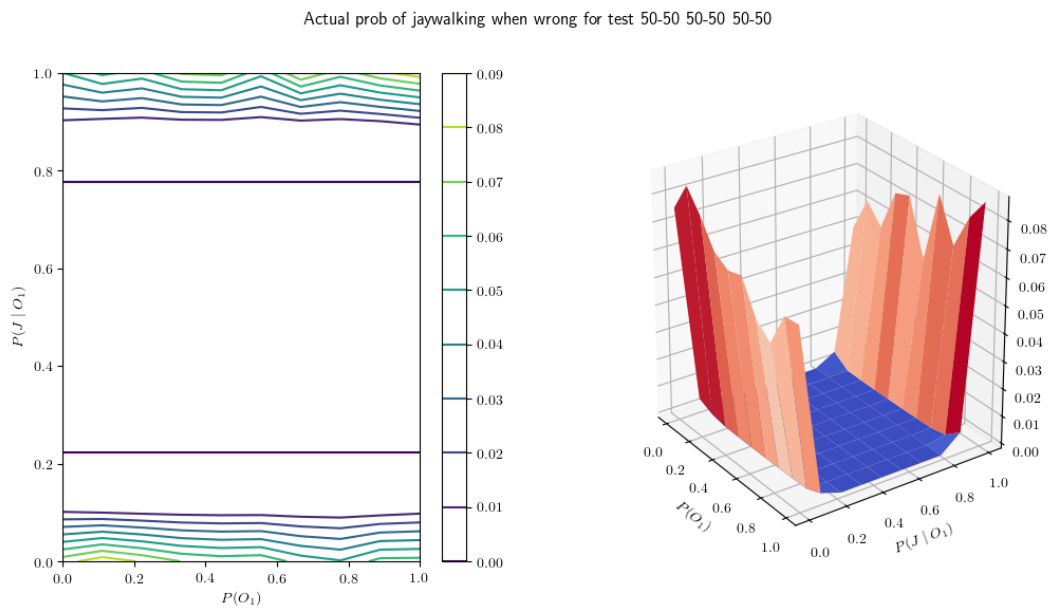


Figure A.16: The actual jaywalking probability when classified incorrectly against test 50-50 50-50 50-50.