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```

1 Section1

1.1 basic

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define ll long long
4
5 int main() {
6
7 cout << "for define \n";
8 return 0;
9 }</pre>
```

2 Section2 Math

2.1 GCD

```
1 | #include < iostream >
  using namespace std;
  int GCD(int x,int y){
3
       while(y != 0){
5
           return GCD(y,x%y);
6
7
       return x;
8 }
10 int main(){
11
       int a,b;
12
       cin>>a>>b;
       int gcd = GCD(a,b);
13
14
       int lcm = a*b/gcd;
15
       cout << "最大公因數為: "<<gcd<< '\n';
16
       cout << "最小公倍數為: "<<1cm<< '\n';
17
18
       return 0;
19 }
```

3 Section3 String

3.1 string

```
#include < iostream >
    #include < string >
    using namespace std;
  5
    int main(){
    //初始化字串
   6
        string s1 = "", s2 = "";
  7
        long long a;
        int b;
  10
    //吃整行(含空格)
  11
1
  12
         getline(cin,s1);
1
  13
2
  14
    //compare,assign,串接
  15
        s1 == s2;
  16
        s1 = s2;
  17
        s1 += s2[i];
  18
3
  19
    //字串切割, i:起始位置, 1en:幾個
  20
        s1 = s1.substr(i,len);
3
    //轉成數字或數字轉字串
  23
        s1 = to_string(a);
        s2 = to_string(b);
  24
  25
        a = stoll(s1);
        b = stoi(s2);
  26
    //判斷數字,字母
  29
         isdigit(s1[i]);
  30
         isalpha(s2[i]);
  31
         return 0;
  32 }
```

4 Section4 小工具

4.1 permutation

```
1 | #include < iostream >
  #include < algorithm >
  using namespace std;
5
  int main(){
      string a = "abc";
6
      string b = "cba";
7
  //一定要先排序,才會有全部的組合
8
      sort(a.begin(),a.end());
9
10
  //產生組合的迴圈
11
12
          cout <<a<<"\n";
13
14
      }while(next_permutation(a.begin(),a.end()));
15
  //檢查b字串是否為a字串可排出結果
16
17
      bool isSamePer =
          is_permutation(a.begin(),a.end(),b.begin());
18
  //產生上一個排列結果
19
20
      prev_permutation(a.begin(),a.end());
21
22
      return 0;
23 }
```

4.2 高斯消元

```
1 #define maxn 500+5
2 int A[maxn][maxn];
3 int guassian_elimination(int m, int n){
4    int r,i,j,k,u;
5    i=j=0;
6   while(i<m && j<n){
7    r=i;</pre>
```

```
for(k=i; k<m; k++){//找為1的值
8
         if(A[k][j]){
9
10
           r=k;
           break;
11
12
       }
13
       if(A[r][j]){
14
15
         if(r!=i){//換到first row
16
           for(k=0; k<n; k++)</pre>
17
              swap(A[r][k],A[i][k]);
18
         for(u=i+1; u<m; u++){</pre>
19
   //需要減時,該row才減第一個row
20
           if(A[u][j]){
21
22
              for(k=0; k<n; k++)</pre>
                A[u][k]^=A[i][k];
23
24
           }
         }
25
26
         i++;
27
       }
28
       j++;
29
     }
     return n-i;// free variable數量
30
31 }
```

4.3 最大流

```
1 #define N 105
2 int path[N],adj[N][N];
4 memset(adj,0,sizeof(adj));
5 //建雙向邊
6 for(int i=0,u,v,w; i<c; i++){
       scanf("%d %d %d",&u,&v,&w);
       adj[u][v] += w;
8
9
       adj[v][u] += w;
10 }
11
12 \mid int flow = 0;
13 while(true){
14
       memset(path,0,sizeof(path));
15
       queue < int > Q;
16
17
       path[s] = s;
       Q.push(s);
18
   //BFS找路徑
19
       while(!Q.empty() && !path[t]){
20
           int now = Q.front();
21
22
           Q.pop();
23
           for(int i=1; i<=n; i++){</pre>
               if(!path[i] && adj[now][i]>0){
24
25
                   Q.push(i);
                   path[i] = now;
26
27
           }
28
29
       }
  //完全沒有路到t就break
30
31
       if(!path[t])
32
           break:
       int min_flow = 1e9;
33
   //找最窄的路
34
35
       for(int from=path[t], to=t; from!=to;
           from=path[to=from]){
36
           min_flow = min(min_flow,adj[from][to]);
       }
37
   //更新該路徑所有邊的額度
38
39
       for(int from=path[t], to=t; from!=to;
           from=path[to=from]){
           adj[from][to] -= min_flow;
40
41
           adj[to][from] += min_flow;
42
43
       flow += min_flow;
44 }
```

5 Section5 Graph

5.1 kruskal

```
1 #define maxn 200005
  #define MP make_pair
3 int N, M;
4 int par[maxn], Rank[maxn];
  vector<pair<int,int>> G[maxn*2];//雙向邊,所以X2
7
  struct edge{
       int x,y,w;
9
       bool operator<(const edge& rhs) const{</pre>
10
           return w<rhs.w;</pre>
11
12
  }e[maxn*2]; //雙向邊,所以 X2
13
14
  int Find(int a){
       return par[a] == a?a:(par[a] = Find(par[a]));
15
16
  }
17
  bool Union(int a, int b){
18
       a = Find(a);
19
       b = Find(b);
20
21
       if(a==b) return false;
22
       int tmp = Rank[a] + Rank[b];
       if(Rank[a]>=Rank[b]){
23
           Rank[a] = tmp;
24
25
           par[b] = a;
26
       }
27
       else{
28
           par[a] = b;
29
           Rank[b] = tmp;
30
31
       return true;
32 }
33
34
  int kruskal(){
35
       for(int i=0; i<N; i++){</pre>
36
           G[i].clear();
           par[i] = i;
37
           Rank[i] = 1;
38
39
       int m = 0, tot = 0;
40
41
       for(int i=0,u,v,w; i<M; i++){</pre>
           scanf("%d %d %d",&u,&v,&w);
42
43
           e[m++] = edge\{u,v,w\};
44
           e[m++] = edge\{v,u,w\};
45
           tot += w;
       }
46
       sort(e,e+m);
47
48
49
       int mst = 0, cost = 0;
50
       for(int i=0,u,v,w; i<m; i++){</pre>
51
           u = e[i].x;
52
           v = e[i].y;
53
           w = e[i].w;
54
           if(Union(u,v)){
55
                cost += w;
56
                mst++;
57
                G[u].push_back(MP(v,w));
58
                G[v].push_back(MP(u,w));
59
           }
           if(mst==N-1)
60
61
                break:
       }
62
63
       return cost;
64 }
```

5.2 floyd

```
1 //N為點的個數, G為記錄路徑長的二維振烈
2 for(int k=0; k<N; k++){
3 for(int i=0; i<N; i++){
```

33

34

35

36 37

38 }

```
for(int j=0; j<N; j++){</pre>
                G[i][j]=min(G[i][j],G[i][k]+G[k][j]);
5
6
           }
7
      }
8 }
```

Dijkstra

```
1 struct Data{
2
       int u,w;
3
       bool operator<(const Data&rhs) const</pre>
4
5
            return w>rhs.w;
7
  };
   void sol(int s){
       memset(d,0x3f,sizeof(d));
10
11
       memset(vis,0,sizeof(vis));
12
       d[s] = 0:
13
       priority_queue < Data > pq;
14
       pq.push(Data{s,0});
15
16
       while(!pq.empty()){
17
           Data k = pq.top();
18
            pq.pop();
            int u = k.u;
19
            if(vis[u]) continue;
20
21
           vis[u] = 1;
22
23
            for(int i=0; i<G[u].size(); i++){</pre>
                int v = G[u][i].first, w = G[u][i].second;
24
25
                if(d[v]>d[u]+w){
                     d[v] = d[u] + w;
26
27
                     pq.push(Data{v,d[v]});
28
                }
           }
29
30
       }
31 }
```

SPFA

```
1 #define N 1005
2 #define MP make_pair
  typedef pair<int,int> PII;
5 int n,m;
6 int dis[N], cnt[N];
  vector<PII> G[N];
  bool inq[N];
8
  bool SPFA(){
10
11
       memset(dis,0x3f,sizeof(dis));
12
       memset(inq, false, sizeof(inq));
13
       memset(cnt,0,sizeof(cnt));
14
       queue<int> Q;
15
16
       dis[0] = 0;
17
       Q.push(0);
       inq[0] = true;
18
19
       while(!Q.empty()){
           int u = Q.front();
20
           Q.pop();
21
22
           inq[u] = false;
23
           for(int i=0; i<G[u].size(); i++){</pre>
24
               int v = G[u][i].first, w = G[u][i].second;
               if(dis[v]>dis[u]+w){
25
26
                   dis[v] = dis[u] + w;
27
                   if(!inq[v]){
  //如果鬆弛超過n次,代表有負環
28
29
                        if(++cnt[v]>=n)
30
                            return true;
31
                        inq[v] = true;
```

Java 6

6.1 java biginterger

}

}

}

return false;

```
1 import java.io.*;
2
  import java.util.*;
  import java.math.BigInteger;
3
  public class z {
5
      public static void main(String args[]) {
7
           Scanner cin = new Scanner(System.in);
  //Java大數資料型態: BigInteger
8
9
10
           BigInteger num = BigInteger.valueOf(1);
           BigInteger btwo = new BigInteger("2");
11
           while (cin.hasNext()){
12
               BigInteger a = BigInteger.valueOf(0);
13
               BigInteger b = BigInteger.valueOf(0);
14
15
               //讀入一整行字串
16
17
               String str = cin.next();
18
19
               //-1停止輸入
               if (str.equals("-1")) break;
20
21
               num = new BigInteger(str);
22
23
               //a += num
24
               a = a.add(num);
25
26
               //b -= num
27
               b = b.subtract(num);
28
29
           System.out.print("a+num is " + a + "\n");
           System.out.print("b-num\ is\ "+b+"\backslash n");
30
  //乘2
31
           System.out.printf("%s*2 = %s n", num,
32
               num.multiply(btwo));
33
  //除2
           System.out.printf("%s/2 = %s n n", num,
34
               num.divide(btwo));
           }
35
  //2的100次方
36
           System.out.printf("2^100 = %s\n".
37
               btwo.pow(100));
      }
38
  }
39
```

Q.push(v);

數學公式

7.1 thm

· 中文測試

```
\cdot \sum_{i=1}^{n} i^2 = \frac{n(n+1)(2n+1)}{6}
```