

1) License Plate Laws:

Step 1: claim:

Passenger car owners waives license
plat laws at a higher rate than commercial
truck owners. Passenger cars $\rightarrow P_1$ $P_1 > P_2$
Commercial trucks $\rightarrow P_2$

Step 2: if $P_1 > P_2$ is false, then $P_1 \leq P_2$

Step 3: Hypothesis tests

$$\text{Null } H_0 = P_1 \leq P_2$$

$$H_1 = P_1 > P_2$$

Step 4: $\alpha = 0.02$

$$\begin{aligned} \text{Step 5: } \bar{P} &= \frac{x_1 + x_2}{n_1 + n_2} = \frac{239 + 45}{2049 + 334} \\ &= \frac{284}{2383} = 0.1191 \end{aligned}$$

$$\begin{aligned} \bar{q} &= 1 - \bar{P} = 1 - 0.1191 \\ &= 0.8808 \end{aligned}$$

$$\text{Step 6 : } Z = \frac{\hat{P}_1 - \hat{P}_2}{\sqrt{\frac{\bar{P}\bar{q}}{n_1} + \frac{\bar{P}\bar{q}}{n_2}}}$$

$$= \frac{\left(\frac{239}{2049} - \frac{45}{334} \right)}{\sqrt{\frac{0.8808)(0.1191)}{2049} + \frac{0.8808)(0.1191)}{334}}} - 0$$

$$= \frac{0.1166 - 0.1347}{\sqrt{0.00065 + 0.0003}}$$

$$= \boxed{-0.9468}$$

$$\text{P value} = \boxed{\approx 0.1719}$$

step 7 = A) Because the P-value
of $0.17 > \alpha (0.1)$,
we fail to reject the
null hypothesis. ($P_1 \leq P_2$)

B) Confidence Interval =

$$-0.0670 < P_1 - P_2 < 0.0310$$

2) Accuracy of fast food Drive-Through:

Step 1 : claim :

Burger King & Mac Donald's have
the same accuracy score.

$$BK = McD$$

Step 2 : Alternative hypothesis

$$BK \neq McD$$

Step 3: Hypothesis tests

$$H_0 = BK = McD$$

$$H_1 = BK \neq McD$$

Step 4: $\alpha = 0.01$

Step 5: $\bar{p} = \frac{x_1 + x_2}{n_1 + n_2} = \frac{264 + 329}{318 + 362}$

$$= 0.8720$$

$$\bar{q} = 1 - \bar{p} = 0.128$$

Step 6: $Z = \frac{(\bar{p} - \bar{q}) - (p - q)}{\sqrt{\frac{\bar{p}\bar{q}}{n_1} + \frac{\bar{p}\bar{q}}{n_2}}}$

$$= \frac{(264 - 329) - 0}{318 - 362}$$

$$\sqrt{\frac{(0.8720)(0.128)}{318}} + \frac{(0.8720)(0.128)}{362}$$

$$= \frac{0.83 - 0.9088}{318}$$

$$= \sqrt{\frac{0.111616}{318} + \frac{0.111616}{362}}$$

$$= \sqrt{0.00035 + 0.00030}$$

$$= \frac{-0.0788}{0.02843}$$

$$= \boxed{-3.091}$$

Step 7: $\boxed{P\text{-value} = 0.0020}$

Step 8: a) Since $P\text{-value} < \alpha$,
we reject the null hypothesis.

b) Confidence Interval :-

$$-0.1454 < P_2 - P_1 < -0.0120$$

Final Conclusion :- There is enough evidence that accuracy of BK doesn't equal to Mac D.

3) Regular Coke and Diet Coke :-

Step 1 : claim :-

the mean weight of Diet Coke is less than the mean weight of regular Coke.

DC = Diet Coke mean weight

RC = Regular Coke mean weight

Step 2 :- Alternative claim :-

mean weight of DC is equal or greater than RC.

Step 3 :- Hypothesis testing

$$H_0 : DC \geq RC$$

$$H_1 : DC < RC$$

Step 4 :- $\alpha = 0.1$

Step 5 :- We are using t-distribution because both are independent variable.

$$\text{Step 6 :- } t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$$\Rightarrow \frac{(0.78479 - 0.81682) - 0}{\sqrt{\frac{(0.00439)^2}{36} + \frac{(0.00781)^2}{36}}} = 0$$

$$z = \frac{-0.03203}{0.001935}$$

$$= \boxed{-22.32}$$

step - 7 :- $df = PC + RC - 2$

$$= \boxed{170}$$

$P\text{-value} = 0.0001$

Because P-value is less than 0.1 significant value, we reject the null hypothesis.

6) Confidence - Interval :-

≈ -0.034488 to -0.029638

c) Reason :-

DC weight less than RC because of the use of artificial sweetner.

4) Color and Creativity :-

Step 1 :- Claim :-

Blue enhances performance on creative task.

Step 2 :- Alternative Claim

Blue doesn't enhance performance on creativity tasks.

Step 3 :- Hypothesis testing :-

$H_0 : \mu_{\text{Blue}} \leq \mu_{\text{Red}}$ (Blue doesn't enhance)

$H_1 : \mu_{\text{Blue}} > \mu_{\text{Red}}$ (enhance)

Step 4 :- $\alpha = 0.01$

Step 5 :- f-distribution is being used because of two independent variables.

Step 6 :-

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

$$Z = \frac{(3.97 - 3.39)}{\sqrt{\frac{(0.63)^2}{36} + \frac{(0.97)^2}{35}}} = 0$$

$$Z = \frac{0.58}{0.1897} = 3.06$$

Step 7 :- $df = n_{Blue} + n_{Red} - 2$

$$= 36 + 35 - 2.$$

$$= 69$$

$$P\text{-value} = 0.0032$$

Step 8 :- Since $p\text{-value} < \alpha$,
we reject the null hypothesis.

b) Confidence Interval :-

$$(0.2638, 0.8962)$$