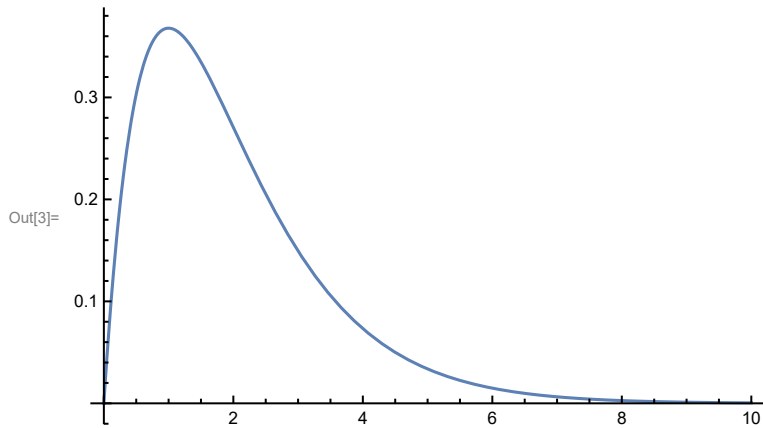


(* Jessica's Ricker model, aka, Gamma PDF kernel *)

In[1]:= **F1[a_, b_, t_] := a t Exp[-b t]**

In[3]:= **Plot[F1[1, 1, t], {t, 0, 10}]**



(* Reparameterize above model interms of the value of t that maximizes the function (peakt), and the value of y at the max (maxy) *)

In[4]:= **∂_t F1[a, b, t]**

Out[4]= $a e^{-b t} - a b e^{-b t} t$

In[5]:= **Solve[a e^{-b t} - a b e^{-b t} t == 0, t]**

Out[5]= $\left\{ \left\{ t \rightarrow \frac{1}{b} \right\} \right\}$

In[6]:= **Simplify[F1[a, b, 1 / b]]**

Out[6]= $\frac{a}{b e}$

(* Solve for original parameters (a and b) in terms of new parameters (peakt and maxy) *)

In[12]:= **Solve[{peakt == 1 / b, maxy == $\frac{a}{b e}$ }, {a, b}]**

Out[12]= $\left\{ \left\{ a \rightarrow \frac{e \text{maxy}}{\text{peakt}}, b \rightarrow \frac{1}{\text{peakt}} \right\} \right\}$

In[13]:= **FullSimplify[%]**

Out[13]= $\left\{ \left\{ a \rightarrow \frac{e \text{maxy}}{\text{peakt}}, b \rightarrow \frac{1}{\text{peakt}} \right\} \right\}$

(* Rewrite function interms of new parameters *)

```
In[14]:= FullSimplify[F1[ $\frac{e^{\text{maxy}}}{\text{peakt}}$ ,  $\frac{1}{\text{peakt}}$ , t]]
```

```
Out[14]=  $\frac{e^{1 - \frac{t}{\text{peakt}}} \text{maxy } t}{\text{peakt}}$ 
```

```
In[15]:= FullSimplify[Log[ $\frac{e^{1 - \frac{t}{\text{peakt}}} \text{maxy } t}{\text{peakt}}$ ]]
```

```
In[16]:= FullSimplify[ $1 - \frac{t}{\text{peakt}} + \text{Log}[\text{maxy}] + \text{Log}[t] - \text{Log}[\text{peakt}]$ ]
```

```
Out[16]=  $1 - \frac{t}{\text{peakt}} + \text{Log}[\text{maxy}] - \text{Log}[\text{peakt}] + \text{Log}[t]$ 
```

(* Function written in terms of new parameters, peakt and maxy *)

```
In[17]:= F1v2[peakt_, maxy_, t_] :=  $\frac{e^{1 - \frac{t}{\text{peakt}}} t \text{maxy}}{\text{peakt}}$ 
```

(* Log transformed versions of the new function *)

```
In[18]:= LF1v2[peakt_, maxy_, t_] :=  $1 - \frac{t}{\text{peakt}} + \text{Log}[\text{maxy}] - \text{Log}[\text{peakt}] + \text{Log}[t]$ 
```

(* interms of log-scale parameters, Lmaxy and Lpeakt *)

```
In[26]:= LF1v3[Lpeakt_, Lmaxy_, t_] :=  $1 - \frac{t}{\text{Exp}[L\text{peakt}]} + L\text{maxy} - L\text{peakt} + \text{Log}[t]$ 
```

(* Plot the different versions of the function to check that they are the same *)

```
In[27]:= Plot[{F1v2[2, 2, t], Exp[LF1v2[2, 2, t]], Exp[LF1v3[Log[2], Log[2], t]]}, {t, 0, 15}]
```

