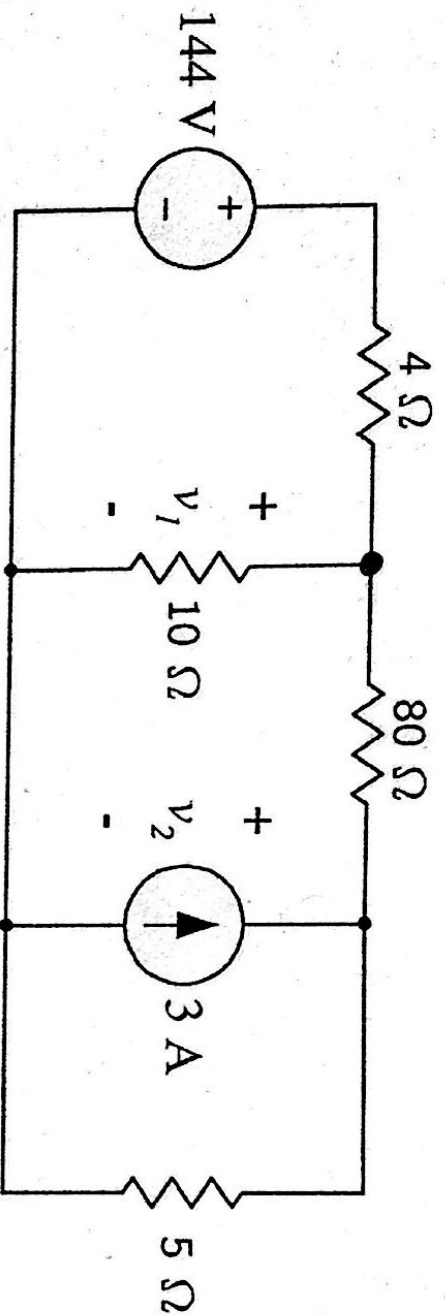


Example 3: Nodal Analysis



Solve for v_1 and v_2 .

Node I)
$$\frac{v_1 - 144}{4} + \frac{v_1}{10} + \frac{v_1 - v_2}{80} = 0$$

(20) (8)

$$20v_1 - 2880 + 8v_1 - v_1 - v_2 = 0$$

$$29v_1 - v_2 = 2880$$

Node II)
$$\frac{v_2 - v_1}{80} - 3 + \frac{v_2}{5} = 0$$

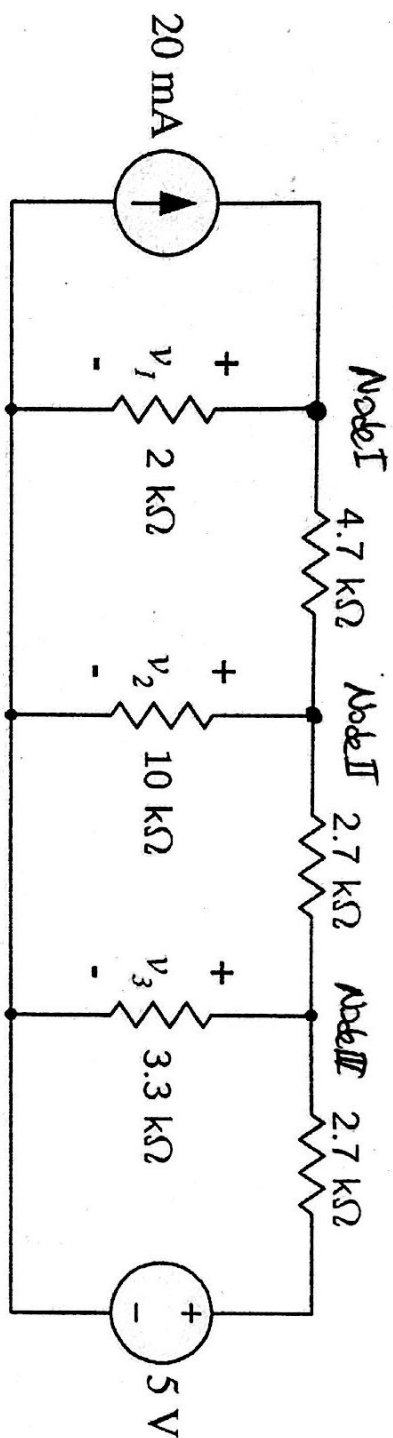
(80) (16)

$$v_2 - v_1 - 240 + 16v_2 = 0$$

$$17v_2 - v_1 = 240$$

$v_1 = 107.4 \text{ V}$
 $v_2 = 20.4 \text{ V}$

Example 4: Nodal Analysis



Solve for v_1 , v_2 , and v_3 .

$$\text{Node I)} \quad -20\text{mA} + \frac{v_1}{2\text{k}} + \frac{v_1 - v_2}{4.7\text{k}} = 0$$

$$\text{Node II)} \quad \frac{v_2 - v_1}{4.7\text{k}} + \frac{v_2}{10\text{k}} + \frac{v_2 - v_3}{2.7\text{k}} = 0$$

$$\text{Node III)} \quad \frac{v_3 - v_2}{2.7\text{k}} + \frac{v_3}{3.3\text{k}} + \frac{v_3 - 5}{2.7\text{k}} = 0$$

$$\begin{aligned} 6.7\text{V}_1 - 2\text{V}_2 &= 188 \\ -2\text{V}_1 + 20.9\text{V}_2 - 4.7\text{V}_3 &= 0 \\ -33\text{V}_2 + 93\text{V}_3 &= 165 \end{aligned}$$

$$\Rightarrow \begin{bmatrix} +6.7 & -2 & 0 \\ -2 & 20.9 & -4.7 \\ 0 & -33 & 93 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} = \begin{bmatrix} 188 \\ 0 \\ 165 \end{bmatrix}$$

$$X = A^{-1}B$$

~~$$\begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} = \begin{bmatrix} +6.7 & -2 & 0 \\ -2 & 20.9 & -4.7 \\ 0 & -33 & 93 \end{bmatrix}^{-1} \begin{bmatrix} 188 \\ 0 \\ 165 \end{bmatrix}$$~~

$$\begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} = \begin{bmatrix} 29.5 \\ 4.77 \\ 3.47 \end{bmatrix}$$