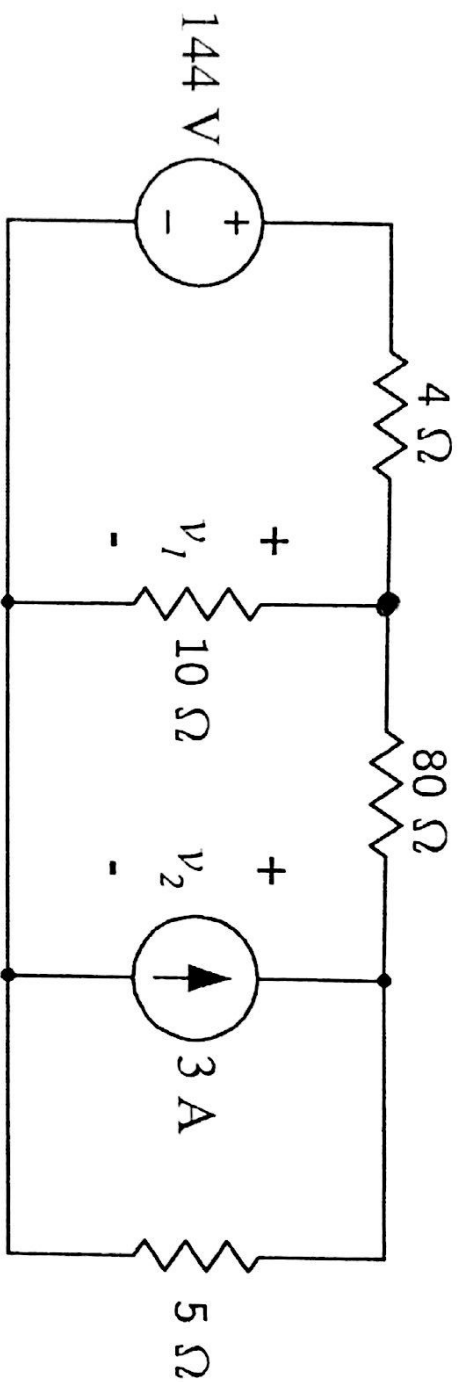


Example 3: Nodal Analysis



Solve for v_1 and v_2 .

$$\text{Node I)} \quad \frac{v_1 - 144}{4} + \frac{v_1}{10} + \frac{v_1 - v_2}{80} = 0$$

(20) (8)

$$20v_1 - 2880 + 8v_1 + v_1 - v_2 = 0$$

$$29v_1 - v_2 = 2880$$

$$\text{Node II)} \quad \frac{v_2 - v_1}{80} - 3 + \frac{v_2}{5} = 0$$

(80) (16)

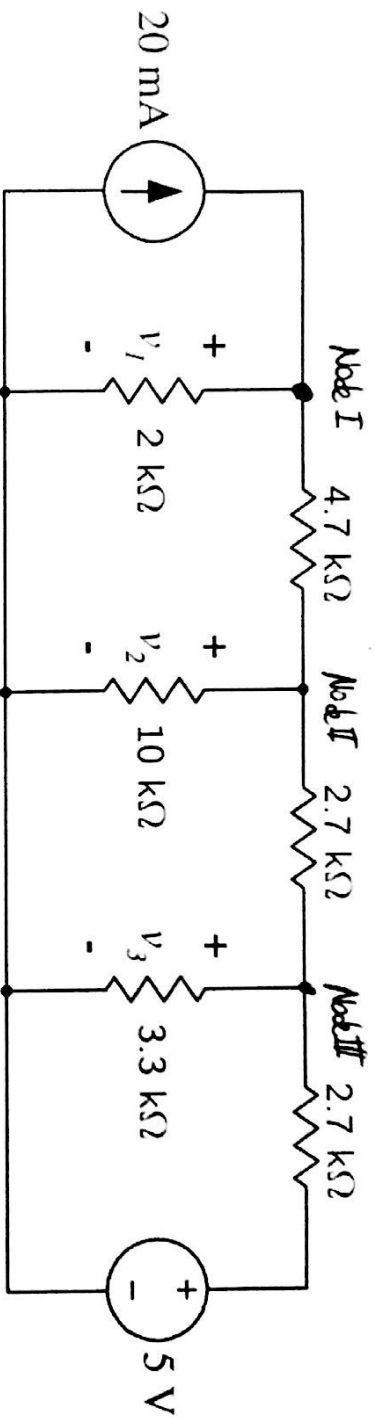
$$v_2 - v_1 - 240 + 16v_2 = 0$$

$$17v_2 - v_1 = 240$$

$$\begin{aligned} v_1 &= 100 \text{ V} \\ v_2 &= 20 \text{ V} \end{aligned}$$

$$\begin{aligned} v_1 &= 100 \text{ V} \\ v_2 &= 20 \text{ V} \end{aligned}$$

Example 4: Nodal Analysis



Solve for v_1 , v_2 , and v_3 .

$$\text{Node I)} \quad -20\text{mA} + \frac{v_1}{2\text{k}} + \frac{v_1 - v_2}{4.7\text{k}} = 0$$

$$\rightarrow 6.7v_1 - 2v_2 = 188$$

$$\text{Node II)} \quad \frac{v_2 - v_1}{4.7\text{k}} + \frac{v_2}{10\text{k}} + \frac{v_2 - v_3}{2.7\text{k}} = 0$$

$$\rightarrow -270v_1 + 866.9v_2 - 470v_3 = 0$$

$$\text{Node III)} \quad \frac{v_3 - v_2}{2.7\text{k}} + \frac{v_3}{3.3\text{k}} + \frac{v_3 - 5}{2.7\text{k}} = 0$$

$$\rightarrow -33v_2 + 93v_3 = 165$$

$$X = A^{-1}B$$

$$\begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} = \begin{bmatrix} 32.1 \\ 13.6 \\ 6.6 \end{bmatrix}$$

A

$$\begin{bmatrix} 6.7 & -2 & 0 \\ -270 & 866.9 & -470 \\ 0 & -33 & 93 \end{bmatrix}$$

$X = B$

$$\begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} = \begin{bmatrix} 188 \\ 0 \\ 165 \end{bmatrix}$$