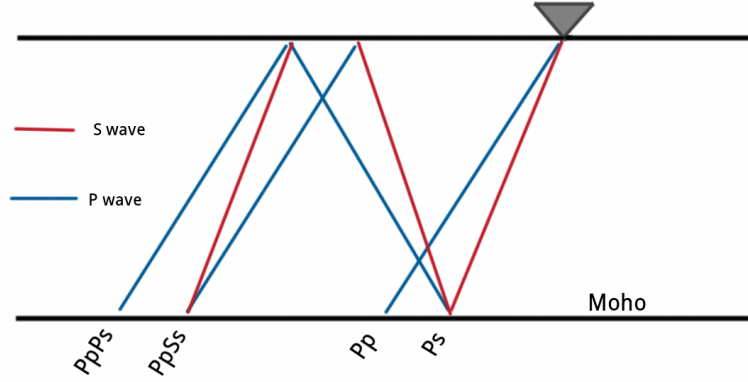


Seismograms from a seismic station are deconvolved into receiver functions which, in good conditions, contain impulsive energy at the times of the phase arrivals. The phase arrivals of interest are the direct phase t_{P_s} and two distinct reflected phases $t_{P_{ps}}$ and $t_{P_{ss}}$ which have reflected off the free surface and Moho before being recorded at the seismic station. $t_{P_{ps}}$ spends two legs of it's journey as a P-wave while $t_{P_{ss}}$ spends only one leg as a P-wave, see figure below. The difference in velocity between a P-wave and S-wave allows the use these arrivals as distinct data.



The parameter search for V_p , V_s and H is accomplished by breaking the problem into two smaller subproblems. First the reflected phase travel time equations (2) and (3) are divided by the direct arrival phase (1) to remove the dependence on crustal thickness H , (4) and (5). A gridsearch over deconvolved receiver functions is performed looking for optimal values of V_p and $\frac{V_p}{V_s}$ using equations (4) and (5) and an estimate for the direct phase travel time t_{P_s} .

Second, the best estimates for V_P and $\frac{V_p}{V_s}$ are chosen and used in a 1D line search using equations (1), (2) and (3) for H .

These best parameter estimates are used to solve the three travel time equations (1), (2) and (3) for the best estimate of a phase arrival for each receiver function and are plotted on a series of receiver functions for verification.

$$t_{Ps}(p_i) = H \left[\sqrt{\left(\frac{V_p}{V_s}\right)^2 - p_i^2 V_p^2} - \sqrt{1 - p_i^2 V_P^2} \right] \quad (1)$$

$$t_{Pps}(p_i) = H \left[\sqrt{\left(\frac{V_p}{V_s}\right)^2 - p_i^2 V_p^2} + \sqrt{1 - p_i^2 V_P^2} \right] \quad (2)$$

$$t_{Pss}(p_i) = 2H \sqrt{\left(\frac{V_p}{V_s}\right)^2 - p_i^2 V_p^2} \quad (3)$$

$$t_{Pps}(p_i) = \frac{\sqrt{\left(\frac{V_p}{V_s}\right)^2 - p_i^2 V_p^2} + \sqrt{1 - p_i^2 V_P^2}}{\sqrt{\left(\frac{V_p}{V_s}\right)^2 - p_i^2 V_p^2} - \sqrt{1 - p_i^2 V_P^2}} t_{Ps}(p_i) \quad (4)$$

$$t_{Pss}(p_i) = \frac{2\sqrt{\left(\frac{V_p}{V_s}\right)^2 - p_i^2 V_p^2}}{\sqrt{\left(\frac{V_p}{V_s}\right)^2 - p_i^2 V_p^2} - \sqrt{1 - p_i^2 V_P^2}} t_{Ps}(p_i) \quad (5)$$