

## Task 1 Part C

For part A, the size of the input word is  $N$ .

Since we can easily retrieve the last character of the input word, the time complexity of retrieving the last character uses  $O(1)$  time.

Now, we have to determine the time rest of the characters in the input word, and the size of the rest of the characters is  $N-1$ . Since you have to retrieve each letter in the rest of the characters, the time complexity of retrieving each letter in the rest of the characters uses  $O(N^2)$  time because there are  $N-1$  characters, and you have to do that retrieval process for  $N-1$  times.

Lastly, since all of the mathematical operations in the formula take  $O(1)$  time (i.e. multiply by 33, the XOR operation, and determining the remainder of  $2^M$ ), the final time complexity is  $O(n^2)$  because  $O(n^2)$  multiply many  $O(1)$  is still the same as  $O(n^2)$ , and  $M$  does not change the time complexity at all.

For part B, since we're looking for the worst case possible,  $N$  would be 5, as the question gives the max range for  $N$ .

From part A, we know that the time complexity of any size input word  $N$  is  $O(n^2)$ , and part A gives the equivalent hash value of the input word  $N$ . For this part, we have to figure out all 5 letter words that have the same hash value as the given input  $K$ .

Since we have to search all possible equivalent hash value of a 5 letter word that matches  $K$ , we have to check each letter in the 5 letter word, and since there are 26 letters in the alphabet, in the worst case, we have to search  $26^5$  times.

Also, for each time that we have to check if a 5 letter word has the equivalent hash value as  $K$ , in the worst case, part A's algorithm would search  $5^2$  times (from  $O(n^2)$  where  $n=5$  in this case).

Therefore, in total, in the worst case, part B's algorithm would have to search  $26^5 * 5^2 = 297034400$  times.

Hypothetically, if  $N$  didn't have a limit, then the time complexity would be  $O(26^n) * O(n^2) = O(26^n * n^2)$ .