



UNIVERSITY COLLEGE LONDON

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Computational Modelling for Biomedical Imaging - Individual Report

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April 10, 2015

## Task 1 - Registration assessment

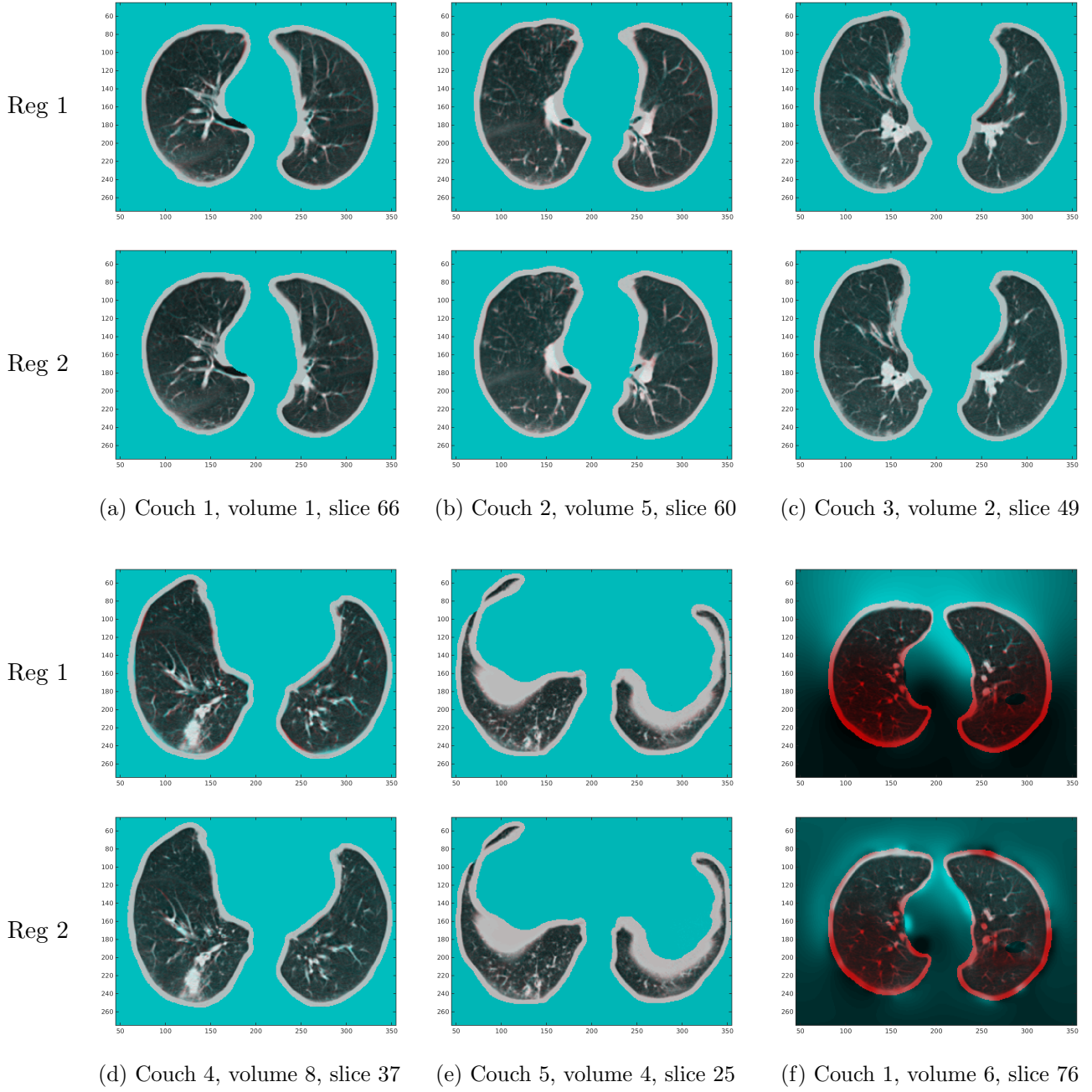


Figure 1: Registration results at several different slices and volumes for each couch position. For each subfigure, registration 1 and 2 are shown in the upper and lower figures respectively.

Figure 1 shows the registration results for a few representative slices and volumes over all couch positions. Both registrations perform equally well subfigures (1a - 1e), but yielded a bad registration in subfigure 1f. Similar bad registrations have been observed in the last slice of each volume. The images show us that there is a considerable ammount of respiratory motion across different slices which needs to be modelled. The shape of the lung is also dramatically different across different couch positions, reaching a concave shape at couch 5. Nevertheless, the segmentation and registration worked fine even for these slices.

## Task 2 & 3 - Fitting the models

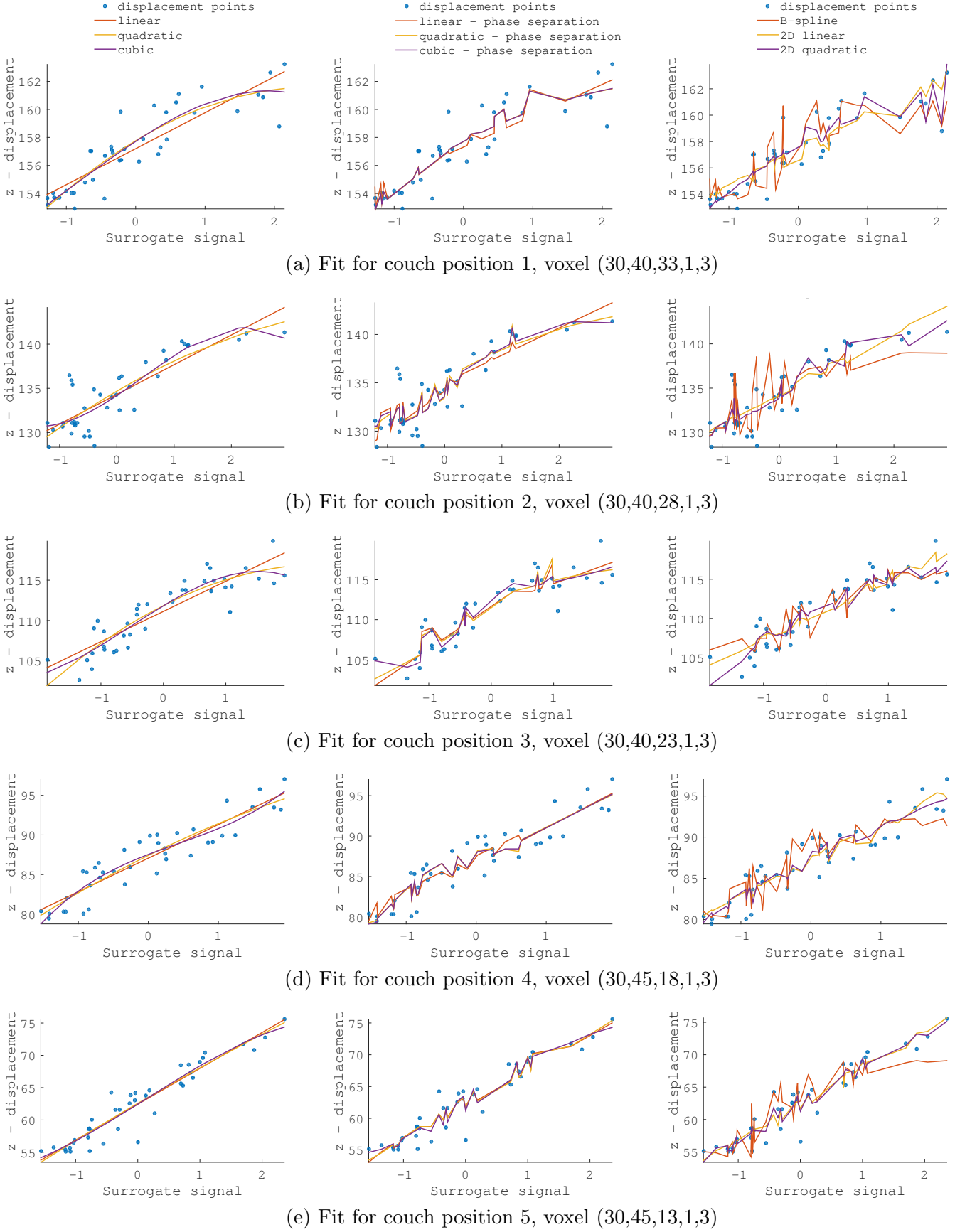


Figure 2: Fit of 9 different models across 5 voxels each from a different couch position. The first column shows the fit for the three basic models: linear, quadratic and cubic. The second column shows the same models with phase separation, while the last column shows the fit for the B-spline, 2D linear and 2D quadratic models.

I fit the models for one voxel by solving the GLM  $D = SC$  where  $D$  is the displacement along one direction,  $S$  is the matrix of surrogate signals and  $C$  are the coefficients. I chose to solve the GLM using the pseudo-inverse of  $S^T S$ , giving  $C = \text{pinv}(S^T S) S^T D$ . I used the MATLAB function `pinv` because it can better handle singularities than the function `inv`. Figure 2 shows the fit for 9 different models:

- |              |                                 |                 |
|--------------|---------------------------------|-----------------|
| 1. linear    | 4. linear - phase separation    | 7. B-spline     |
| 2. quadratic | 5. quadratic - phase separation | 8. 2D linear    |
| 3. cubic     | 6. cubic - phase separation     | 9. 2D quadratic |

These models have been fit for all CP displacements using a fast (vectorised) method where all the CP displacements are flattened into a huge matrix. The fit is plotted in figure 2 only for the given voxels for all the couch positions (one voxel/row with three groups of models for each plot).

The linear, quadratic and cubic models (plots in the column) give a reasonably good fit, especially for couch positions 4 and 5. The quadratic and cubic models don't differ much from the linear model, especially for voxels in couch positions 4 and 5. The phase separation models seem to fit outlier points better, but at the expense of extra parameters in the model. The B-spline and the 2D linear and quadratic models seem to fit the data best, but they run the risk of overfitting. The B-spline model seems to have a very oscillatory behaviour in the first few volumes, most evident in couch 2. In conclusion, all models fit these particular voxels well, and as we expected the more complex models give a better fit than the simpler models.

## Task 4 - Evaluation of the motion models

### Visual Assessment

Figure 3 shows the visual assessment for all the 9 models for couch 1, volume 1, slice 66. There is considerably more motion compared to the registration assessment in task 1. The results are quite good, with essentially no differences between the estimated deformation across the models. The motion of the outer shape of the lung has been almost perfectly estimated, with tiny errors at the top corner of the right lung. More deformation errors are found at the vasculature of the right lung. We therefore conclude that all 9 models perform equally well.



Figure 3: Visual assessment of the 9 deformation models using leave-one out cross-validation on couch 1, volume 1, slice 66.

### Deformation Field Error

Figure 4 shows the deformation field error for the 10 Cine CT volumes across all 5 couch positions. The left column shows the mean error, while the right column shows the standard deviation. The amount of motion varies slightly across the Cine CT scans but is usually less than 3mm. Similarly, standard deviation is usually below 1.2. The B-spline model seems to have larger error means and standard deviations especially in volumes from couch positions 4 and 5. The other models have similar errors across all couch positions.

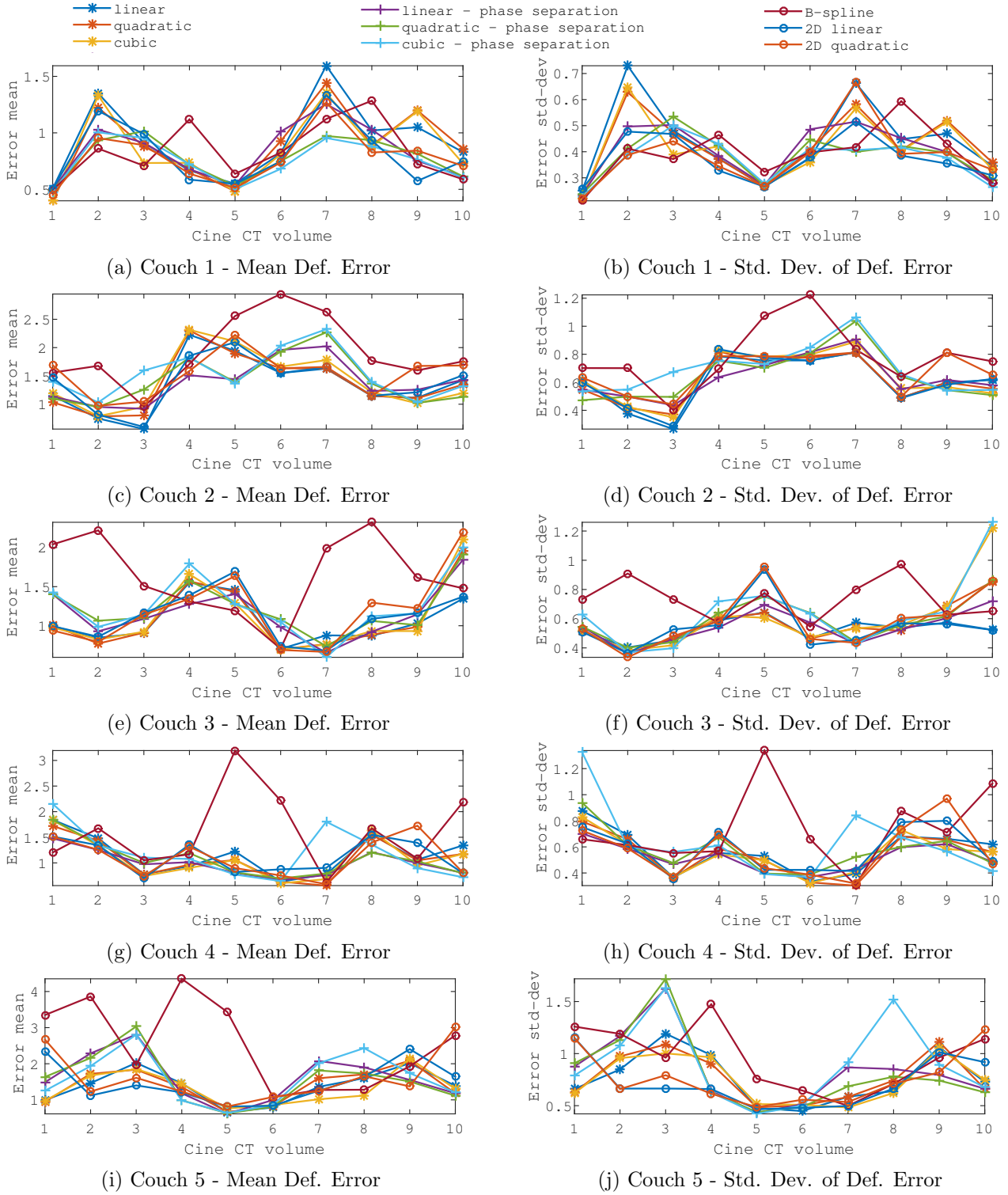


Figure 4: Deformation Error mean and standard deviation for all 5 couch positions, 10 Cine CT volumes and 9 models.

### Landmark Error

Figure 5 shows the landmark errors for all the 9 models across the 5 couch positions, this time using all 40 Cine CT volumes. Moreover, the landmark error using the original registration is also plotted in black. The landmark error is usually between 1 and 4mm. All models perform equally good, with no clear winner from the plots. In particular, the cubic - phase separation model seems to have a spike in landmark error at couch position 2, volume 24, which might be due to overfitting.

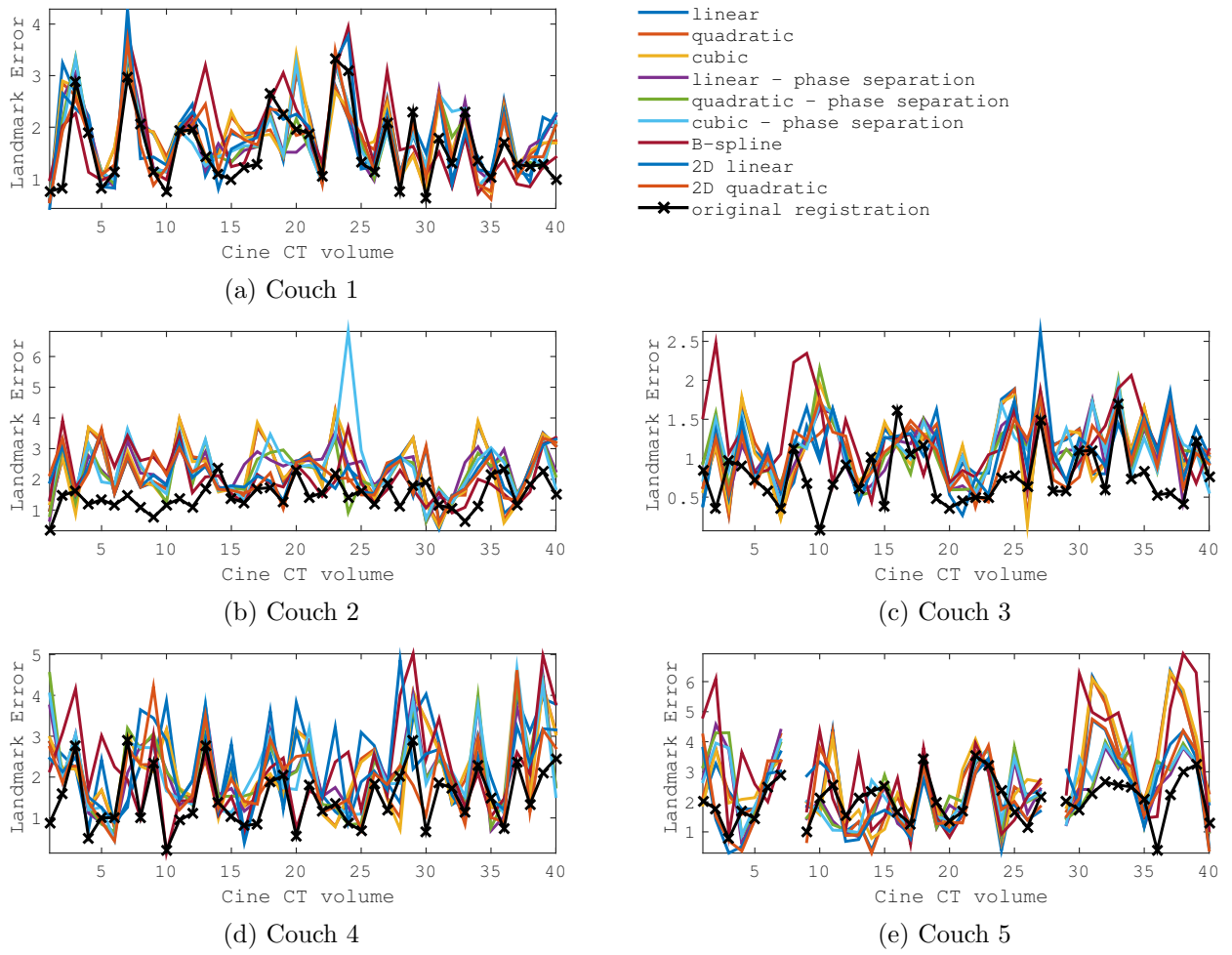


Figure 5: Landmark error for all 5 couch positions, 40 Cine CT volumes and 9 models.

## Model Ranking

### Task 5 - Parameter uncertainty

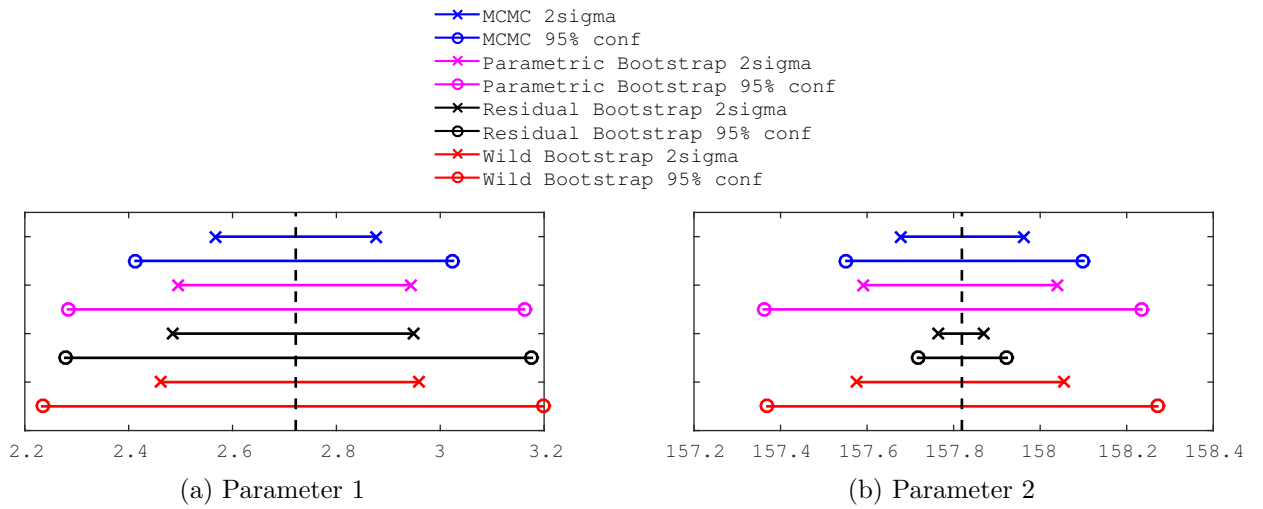


Figure 6: Parameter uncertainty for the linear model.

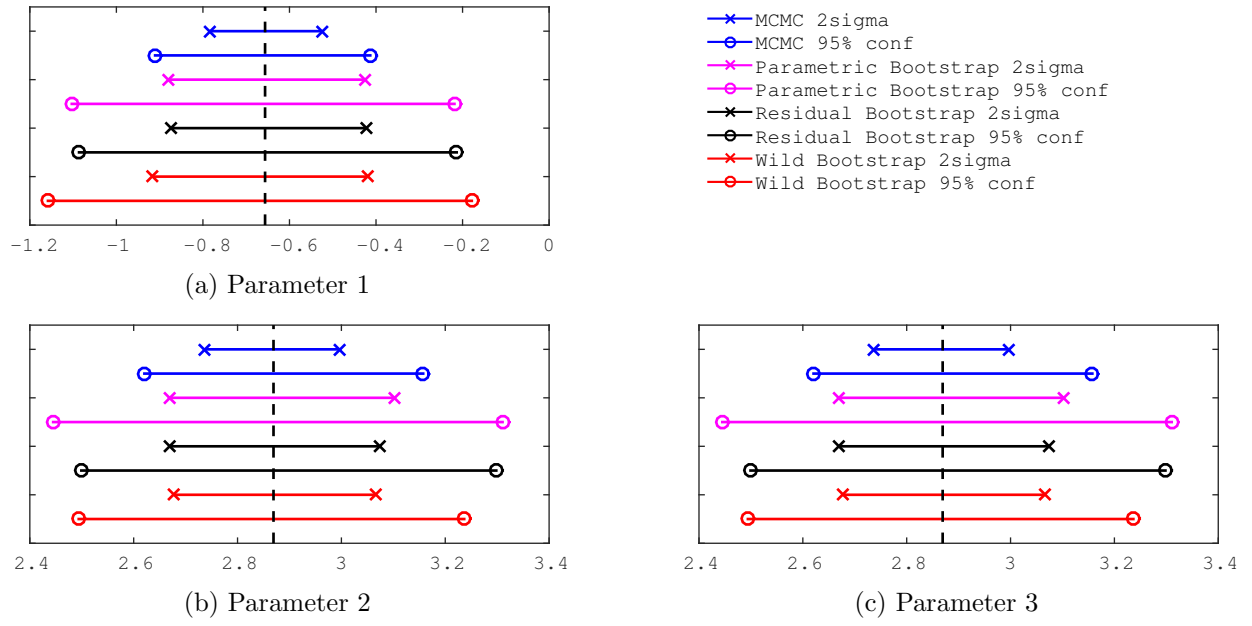


Figure 7: Parameter uncertainty for the quadratic model.

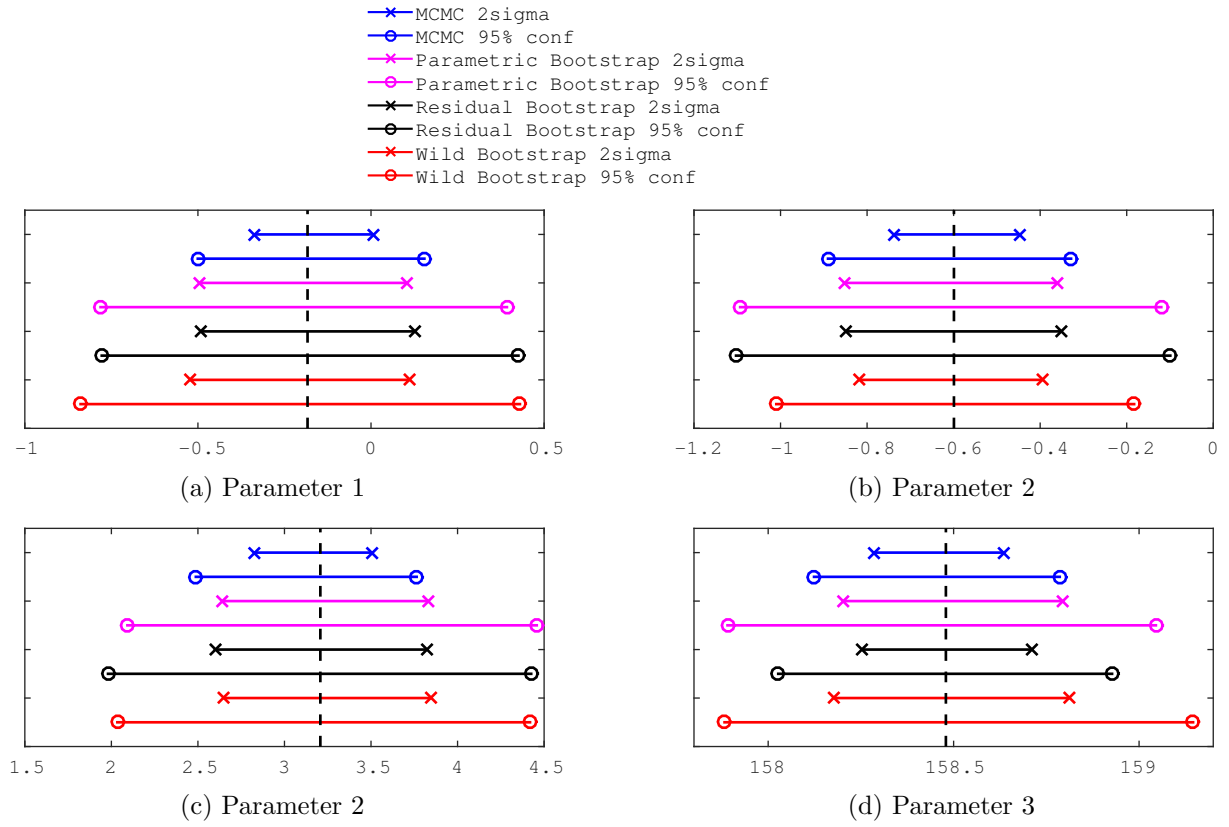


Figure 8: Parameter uncertainty for the cubic model.

## Advanced tasks