## **Practice 3**

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We start importing the necessary packages and the three images we will start playing with.

#### In [1]:

```
import cv2
import numpy as np
import matplotlib.pyplot as plt

def plot(im, cmap='gray', title=None, size=(10,5)):
    %matplotlib inline
    plt.figure(figsize=size)
    plt.imshow(im, cmap=cmap)
    if title is not None:
        plt.title(title)
    plt.show()
```

#### In [2]:

```
L=cv2.imread("L.jpg")[:,:,::-1]

C=cv2.imread("C.jpg")[:,:,::-1]

R=cv2.imread("R.jpg")[:,:,::-1]

plot(np.hstack((L,C,R)), size=(30,5))

print(" L", 45*" ", "C", 45*" ", "R")
```



Note we name the left image as L, the center image as C and the right one R.

#### General Routines we will be using

Let us now define the functions to get the homography sending pixel coordinates of one image plane to the pixel positions of another camera plane. With it, we will be able to get any image as seen from the camera extrinsics of another image.

To get this homography we will employ the Direct Linear Transform method. For that we need to manually choose some corresponding points between the first and the rest of images, so we also define functions for that.

#### In [2]:

```
def choose_points(image, num_points=-1):
        %matplotlib tk
        plt.imshow(image)
        plt.title("Choose the points of correspondence")
        points = plt.ginput(n=num_points, timeout=-1, show_clicks=True)
        plt.show()
         return points
def build homography from m to mp(m points, mp points):
        # mp alpha Hm
        # turned into Bh=0
        B = np.zeros((len(m points)*2, 9), dtype=np.float64)
        for k, (mp, m) in enumerate(zip(mp points, m points)):
                 B[k*2:(k+1)*2, :] = np.array([[0,0,0,-m[0], -m[1], -1, mp[1]*m[0], mp[1]*m[1], mp[1]], mp[1], mp[1
                                                                     [m[0], m[1], 1, 0,0,0, -mp[0]*m[0], -mp[0]*m[1], -mp[0]]])
        u,s,vt = np.linalg.svd(B)
        h = vt.T[:,-1]
        H = h.reshape(3,3)
        H = H/H[2,2]
        # st now if we take [m']=Hm we know which pixel in image of m should be correspondent with m'
        return H
def homog_ops(H, inputs): # inputs expected to be [3,N] or [ 2,N]
        if inputs.shape[0]==2:
                 inputs = np.vstack((inputs, np.ones(inputs.shape[-1])))
         out = H@inputs
        return (out/out[-1, :])[:-1,:]
def image_of_mp_as_seen_from_m( H_m_to_mp, image_m, image mp ):
         # Image of m' as seen from image m-s camera
        image_mp_as_m = np.zeros(image_m.shape, image_m.dtype)
        dest_xys = np.array(np.meshgrid(
                                           np.arange(image_m.shape[1]), np.arange(image_m.shape[0]))
                                                 ).reshape(-1, image_m.shape[1]*image_m.shape[0])
        # [2 (x,y), image_m.shape[0]*image_m.shape[1]] both dest_xys and look_up_mps
        look up mps = np.round( homog ops( H m to mp, dest xys ) ).astype(int)
        is\_out\_of\_bounds = (look\_up\_mps[0]>=0) & (look\_up\_mps[0]<image\_mp.shape[1]) & \
                                                    (look up mps[1] \ge 0) & (look up mps[1] < image mp.shape[0])
        # [image m.shape[0]*image m.shape[1]]
        for dest_m, look_up_mp, is_out in zip(dest_xys.T, look_up_mps.T, is_out_of_bounds):
                 if is out:
                          image_mp_as_m[dest_m[1], dest_m[0], :] = image_mp[look_up_mp[1], look_up_mp[0], :]
         return image_mp_as_m
```

#### Get the Corresponding points manually

Get the corresponding points of the the left image (L) with the center one (C) and the right one (R) with the center one, since we are looking to get a homography from the side images to the center image.

#### In [5]:

```
pointsLC = []
pointsRC = []
pointsLC.append(choose_points(L))
pointsLC.append(choose_points(C, len(pointsLC[0])))
pointsRC.append(choose_points(R))
pointsRC.append(choose_points(C, len(pointsRC[0])))
```

#### In [6]:

```
print(f"Gathered {len(pointsLC[0])} and {len(pointsRC[0])} points for each pair (L,C) and (R,C) respectively")
```

Gathered 27 and 32 points for each pair (L,C) and (R,C) respectively

## Get the Homographies from the C image to the L and R for an output to input strategy

For this we use the routines we implemented in the beginning.

#### In [6]:

```
H_C_to_L = build_homography_from_m_to_mp(pointsLC[1], pointsLC[0]) # m is C mp are the rest
H_C_to_R = build_homography_from_m_to_mp(pointsRC[1], pointsRC[0]) # m is C mp are the rest
imageL_from_C = image_of_mp_as_seen_from_m(H_C_to_L, C, L)
imageR_from_C = image_of_mp_as_seen_from_m(H_C_to_R, C, R)
plot(np.hstack((imageL_from_C,C,imageR_from_C)), size=(30,5))
```



We clearly see that both L and R gave us more information than just the registered portions. We can get the whole images by computing where the four edges of L and R go in the projective plane of C, using the inverse homographies to those computed ones. Then, we will be able to define the whole canvas from the camera extrinsics of C that leaves no pixel of any of the three images out. We will get each of the images there and we will then blend them using the average intensities where the pixels get superimposed.

So first, get the four edges in C's coordinate system for C,L and R and get the rectangular canvas that gets all of them inside.

#### In [3]:

```
def get_edges_of_mp_in_m(H_m_to_mp, m):
    H_mp_to_m = np.linalg.inv(H_m_to_mp)
    mp_edges = np.array([[0,0], [0,m.shape[0]], [m.shape[1], m.shape[0]], [m.shape[1], 0]]).T
    return homog_ops( H_mp_to_m, mp_edges ) #[2, 4]
```

#### In [7]:

```
L_edges_in_C = get_edges_of_mp_in_m(H_C_to_L, L)
R_edges_in_C = get_edges_of_mp_in_m(H_C_to_R, R)
C_edges_in_C = np.array([[0,0], [0,C.shape[0]], [C.shape[1], C.shape[0]], [C.shape[1], 0]]).T

# in the coordinates of the C image:
min_width = np.ceil(min([L_edges_in_C[0].min(), R_edges_in_C[0].min(), 0]))
max_width = np.ceil(max([L_edges_in_C[0].max(), R_edges_in_C[0].max(), C.shape[1]]))
min_height = np.ceil(min([L_edges_in_C[1].min(), R_edges_in_C[1].min(), 0]))
max_height = np.ceil(max([L_edges_in_C[1].max(), R_edges_in_C[1].max(), C.shape[0]]))
```

#### In [4]:

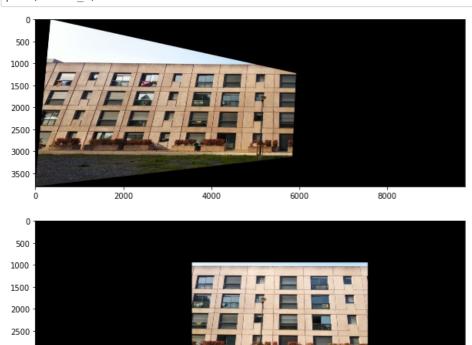
#### In [8]:

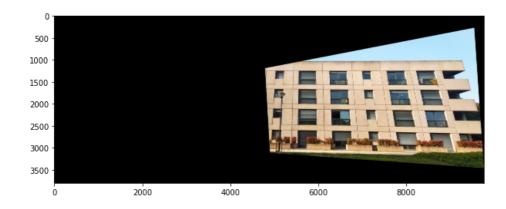
```
canvas = np.zeros( (int(max_height-min_height), int(max_width-min_width), 3), dtype=C.dtype )

canvas_L = fill_canvas_with_mp(H_C_to_L, L, canvas.copy(), min_width, min_height)
canvas_R = fill_canvas_with_mp(H_C_to_R, R, canvas.copy(), min_width, min_height)
canvas_C = fill_canvas_with_mp(np.array([[1,0,0],[0,1,0],[0,0,1]]), C, canvas.copy(), min_width, min_height)
```

#### In [10]:

```
plot(canvas_L)
plot(canvas_C)
plot(canvas_R)
```





6000

4000

8000

We can first attempt a simple blending, by simply getting one of the values of the images:

## In [11]:

3000 3500

2000

```
canvas_simple = np.where(canvas_C==0, canvas_R, canvas_C)
canvas_simple = np.where(canvas_simple==0, canvas_L, canvas_simple)
plot(canvas_simple, size=(30,5))
```



Even if it is not that perceptible for C and R, for C and L, the tonality change is very abrupt. We can improve this by getting the average of the images wherever they get superimposed.

#### In [12]:



Which is a way more reasonable result!

Finally, let us crop the result such that no black pixel without information is shown.

#### In [13]:

```
w_left = int(abs(L_edges_in_C[0,0]-L_edges_in_C[0,1]))
w_right = -int(abs(R_edges_in_C[0,2]-R_edges_in_C[0,3]))
h_top = int(-min_height)
h_bot = int(C.shape[0]-max_height)

blended_crop = blended[h_top:h_bot,w_left:w_right]
plot(blended_crop, size=(30, 10))
```



# **Automatic Corresponding Point Detection**

We will employ a SIFT keypoint detector, with which to generate some descriptors of the locality of each keypoint in each image. Then, we can use a FLANN based keypoint matcher (instead of a brute force one), which will use an approximate nearest neighbour sort of method. We will filter the best matches (which are a reasonable distance apart) and we will use these matches to build the homography from one plane to the other one, just as we did manually. Yet, since there will be way more found correspondances than we did manually, where lots of them will be for sure noisy, it would be better to do a RANSAC employing the homography building technique, say DLT like we did, as the fitter for each RANSAC iteration.

For this openCV provides us with a findHomography() function, with a parameter allowing RANSAC to be used. Then we will be able to proceed as we did before.

At this point, since the procedure here and in what follows will be equivalent, we will create a function that does all this "homography+registering"-like pipeline for any two pairs of image. In a way that if we wish to do this for several images in a row, we can iteratively apply it to a pair, then the result with another image of the set etc.

```
def detect_filter_keypoints_get_matches_find_ransac_homography_make_collage_crop_to_valid( image_from, image_into
):
    if len(image_from.shape)==3: # then it is a color image
        image from g = cv2.cvtColor(image from, cv2.COLOR RGB2GRAY)
        image into g = cv2.cvtColor(image into, cv2.COLOR RGB2GRAY)
   # Initiate SIFT detector
   sift = cv2.SIFT create()
    # find the keypoints and descriptors with SIFT
   keys from, descr from = sift.detectAndCompute(image from g,mask=None)
   keys_into, descr_into = sift.detectAndCompute(image into g,mask=None)
   # FLANN parameters - faster matcher than brute force
   FLANN INDEX KDTREE = 1
   index_params = dict(algorithm = FLANN_INDEX_KDTREE, trees = 5)
    search params = dict(checks=50) # or pass empty dictionary
   flann = cv2.FlannBasedMatcher(index_params, search_params)
   matches = flann.knnMatch(descr from, descr into, k=2)
   # store all the good matches as per Lowe's ratio test.
   good_ones = []
    for m,n in matches:
       if m.distance < 0.7*n.distance:
            good ones.append(m)
   # gather the correspondances we will pass to the RANSAC homography generator
   pts_from = np.float32([ keys_from[m.queryIdx].pt for m in good_ones ]).reshape(-1,1,2)
   pts into = np.float32([ keys into[m.trainIdx].pt for m in good ones ]).reshape(-1,1,2)
    # Generate best homography using RANSAC
   H_into_to_from, mask = cv2.findHomography(pts_into, pts_from, cv2.RANSAC, 5.0) # get homography from image_in
to to image_from for output-input strategy
    # get the resulting RANSAC inliers
   inlier match mask = mask.ravel().tolist()
    # plot the inlier matches for sanity check
   draw params = dict(matchColor = (0,255,0), # draw matches in green color
                       singlePointColor = None,
                       matchesMask = inlier match mask, # draw only inliers
                       flags = 2)
   detected_inlier_match_im = cv2.drawMatches(image_from_g,keys_from, image_into_g, keys_into, good_ones,None,**
draw params)
    # generate the canvas for the whole image
    from_edges_in_from = get_edges_of_mp_in_m(H_into_to_from, image_from)
    into_edges_in_into = np.array([[0,0], [0, image_into.shape[0]], [image_into.shape[1], image_into.shape[0]], [
image into.shape[1], 0]]).T
   # decide the size of the canvas
   min width = np.ceil(min([from edges in from[0].min(), 0]))
   max width = np.ceil(max([from edges in from[0].max(), image into.shape[1]]))
   min_height = np.ceil(min([from_edges_in_from[1].min(), 0]))
   max_height = np.ceil(max([from_edges_in_from[1].max(), image_into.shape[0]]))
   canvas = np.zeros( (int(max height-min height), int(max width-min width), 3), dtype=image into.dtype )
   # fill the canvas for each view
   canvas from = fill canvas with mp(H into to from, image from, canvas.copy(), min width, min height)
    canvas into = fill canvas with mp(np.array([[1,0,0],[0,1,0],[0,0,1]]), image into, canvas.copy(), min width,
min_height)
    # Blend them using the average trick we explained in the previous section
   mask_from = np.where(canvas_from.mean(axis=2)!=0, 1, 0)
   mask_into = np.where(canvas_into.mean(axis=2)!=0, 1, 0)
   mask backg = np.where((canvas from.mean(axis=2)==0) & (canvas into.mean(axis=2)==0) , 1, 0)
   mask_total = mask_from + mask_into + mask_backg
   blended = ((canvas into.astype(np.float64)+canvas from.astype(np.float64)
                                                  )/mask total[:,:,np.newaxis]).astype(np.uint8)
    return blended, detected_inlier_match_im
```

Lets apply it to L,C and then to L+C, R. We can also see the inlier keypoints that were left in the RANSAC.

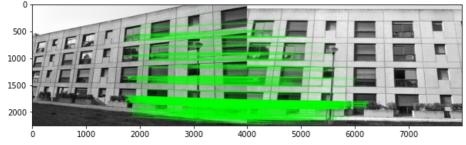
#### In [15]:

```
blendedLC, inliersLC = detect_filter_keypoints_get_matches_find_ransac_homography_make_collage_crop_to_valid(imag
e_from=L, image_into=C)
```

#### In [17]:

plot(blendedLC)
plot(inliersLC)





#### In [18]:

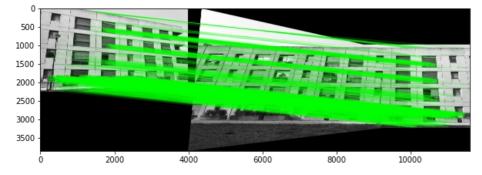
 $blendedLCR, in liers LC_R = detect\_filter\_keypoints\_get\_matches\_find\_ransac\_homography\_make\_collage\_crop\_to\_valid(image\_from=R, image\_into=blendedLC)$ 

#### And here the result:

#### In [20]:

plot(blendedLCR)
plot(inliersLC R)

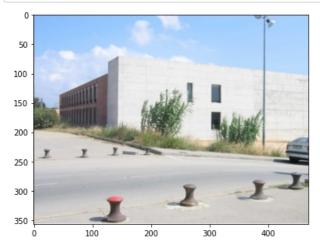




As we see, the result is at least visually, as good as what we would have obtained manually!

We can also apply this pipeline to the images given in the practice guide to get:

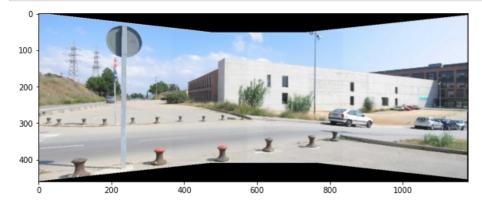
#### In [18]:





#### In [19]:

plot(cummulative\_mosaic1)



As we see, the pipeline works perfectly well!

# **Cylindrical Projection**

In the practice guide, we are given the coordinate transformation that suffers a plane tangent to a cylinder when the plane is conically projected over the cylinder, with the projection pole inside the cylinder and over its rotation axis.

This means that, since if we have multiple images taken by just rotating the camera projection axis, all of them are tangent to a same cylinder, for each of them we can apply the geometrical transofrmation given by the formulas to get how the image would be formed as projected on the cylinder (conically). Because all of these images are tangent to the same cylinder where the projection pole is on the main axis of the cylinder, we know that these projections over the cylinder will necessarily be parts of the same image. Thus, they should be registrable in principle by simple translations. To do this registering, we could use visually corresponding points and then get their relative translations in the cylinder's surface. The registering will only involve translations horizontal and vertically (vertically as well if the images were not taken really parallel to each other). Alternatively, we could employ an automatic interesting point detection, or we could register the images pairwise using Fourier phase correlation or such.

Yet another way to do this, allowing imperfect rotation of the camera along its camera axis (thus allowing the images not to be registrable with simple translations), is by generating homographies linking the cylindrically projected images. In principle, if a simple shift should be enough, then a translation is also a homography, so the result should be the same. Yet, we allow a bit more flexibility this way.

As for the equations of the cylindrical projection, we will assume the projection center is aligned with the image center (typically the value obtained in the camera calibrations). For the focal and scale factor, since we are using an FV-5 camera of a Xiaomi Redmi 5, we know the focal is about 35 mm long, with 1.3 microns per pixel. This means, in pixels, the focal is about 27000 pixels. Thus, we will need to choose f and s in the order of the thousands of pixels. We find that about 3000 gives us a reasonably curved cylinder as to try the 360 degree picture.

#### In [21]:

```
def centered conical projection onto cylinder( image in tangent plane, f=3000, s =3000 ):
           result = np.zeros((image in tangent plane.shape[0], image in tangent plane.shape[1],3), dtype=np.uint8) # we
know geometrically that the size of the output will be smaller than the input
          dest xys = np.array(np.meshgrid(
                                          np.arange(result.shape[1]), np.arange(result.shape[0]))
                                                   ).reshape(-1, result.shape[1]*result.shape[0]) #[2, resultHxresultW]
          c_in = np.array(image_in_tangent_plane.shape)[:2]//2 # [h//2, w//2] aprox center
           c out = np.array(result.shape)[:2]//2
           dest_xys_shifted = dest_xys - c_out[::-1, np.newaxis]
           look up xs input = np.round(f*np.tan(dest xys shifted[0]/s)).astype(int) + c in[1]
          look\_up\_ys\_input = np.round(f/s*dest\_xys\_shifted[1]*np.sqrt(1+(np.tan(dest\_xys\_shifted[0]/s))**2)).astype(int the context of the context of
          is out of bounds = (look\_up\_xs\_input>=0) & (look\_up\_xs\_input<image\_in\_tangent\_plane.shape[1]) & \setminus
                                                                (look_up_ys_input>=0) & (look_up_ys_input<image_in_tangent_plane.shape[0])</pre>
          for dest_can, look_up_x, look_up_y, is_out in zip(dest_xys.T, look_up_xs_input, look_up_ys_input, is_out_of_b
ounds):
                     if is out:
                                result[dest can[1],dest can[0], :] = image in tangent plane[ look up y, look up x, :]
          return result
```

#### In [69]:

```
projectedL = centered_conical_projection_onto_cylinder(L)
plot(projectedL)
projectedC = centered_conical_projection_onto_cylinder(C)
plot(projectedC)
projectedR = centered_conical_projection_onto_cylinder(R)
plot(projectedR)
```







#### In [70]:

blendedLC\_cyl, inliersLC\_cyl = detect\_filter\_keypoints\_get\_matches\_find\_ransac\_homography\_make\_collage\_crop\_to\_va
lid(image\_from=projectedL, image\_into=projectedC)

blendedLCR\_cyl, inliersLC\_R\_cyl = detect\_filter\_keypoints\_get\_matches\_find\_ransac\_homography\_make\_collage\_crop\_to \_valid(image\_from=projectedR, image\_into=blendedLC\_cyl)

plot(blendedLC\_cyl)
plot(blendedLCR\_cyl)





As said, in reality the cylindrically projected images should be registrable with a simple translation (no projective change) if they were really tangent to the same cylinder of same projection pole. Yet, when the homography is generated we find a little perspective change as well! This is clearly due to the fact that the images are really not tangent to the same projection pole cylinder! (which is rather very hard to achieve by hand).

# 360: personal camera

After we have taken several photos as to build a 360 image, we will merge different continguous images in a pyramid-like organization (to safe resources) until we arrive to the 360 view.

```
In [ ]:
```

```
images=[]
images_cyl=[]
for i in range(1, 19):
    images.append(cv2.imread(f"360 1/{i}.jpg")[:,:,::-1])
    images_cyl.append(centered_conical_projection_onto_cylinder(images[-1], f=1000, s=1000))
cummulative mosaic1 = images cyl[0]
for im cyl in images cyl[1:4]:
    plot(cummulative mosaic1)
    cummulative_mosaic1, inliers = detect_filter_keypoints_get_matches_find ransac homography make collage crop t
o valid(
                        image from=im cyl, image into=cummulative mosaic1)
cummulative mosaic2 = images cyl[3]
for im cyl in images cyl[3:7]:
    plot(cummulative mosaic2)
    cummulative mosaic2, inliers = detect filter keypoints get matches find ransac homography make collage crop t
o valid(
                        image from=im cyl, image into=cummulative mosaic2)
cummulative_mosaic3 = images_cyl[6]
for im cyl in images cyl[6:10]:
    plot(cummulative_mosaic3)
    cummulative mosaic3, inliers = detect filter keypoints get matches find ransac homography make collage crop t
o valid(
                        image from=im cyl, image into=cummulative mosaic3)
cummulative mosaic4 = images cyl[9]
for im cyl in images cyl[9:13]:
    plot(cummulative mosaic4)
    cummulative_mosaic4, inliers = detect_filter_keypoints_get_matches_find_ransac_homography_make_collage_crop_t
o valid(
                        image_from=im_cyl, image_into=cummulative_mosaic4)
cummulative_mosaic5 = images_cyl[12]
for im cyl in images cyl[12:16]:
    plot(cummulative mosaic5)
    cummulative mosaic5, inliers = detect filter keypoints get matches find ransac homography make collage crop t
o_valid(
                        image from=im cyl, image into=cummulative mosaic5)
cummulative mosaic6 = images cyl[15]
for im cyl in images cyl[15:]:
    plot(cummulative mosaic6)
    cummulative mosaic6, inliers = detect filter keypoints get matches find ransac homography make collage crop t
o valid(
                        image from=im cyl, image into=cummulative mosaic6)
print("Obtained Cummulative mosaics:")
plot(cummulative_mosaic1)
plot(cummulative_mosaic2)
plot(cummulative_mosaic3)
plot(cummulative mosaic4)
plot(cummulative mosaic5)
plot(cummulative mosaic6)
```

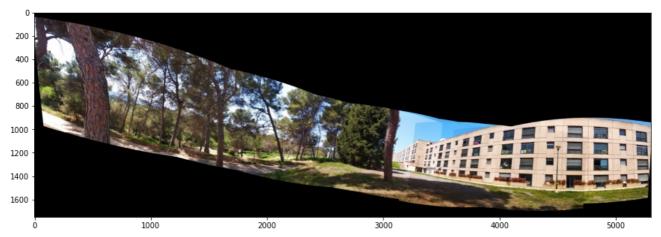
## In [ ]:

```
cumml12, = detect filter keypoints get matches find ransac homography make collage crop to valid(cummulative mo
saic2, cummulative_mosaic1)
plot(cumml12)
cumml126, _ = detect_filter_keypoints_get_matches_find_ransac_homography_make_collage_crop_to_valid(cummulative_m
osaic6, cumml12)
plot(cumml126)
cumml45.
          = detect filter keypoints get matches find ransac homography make collage crop to valid(cummulative mo
saic4, cummulative mosaic5)
plot(cumml45)
cumml453,
           = detect filter keypoints get matches find ransac homography make collage crop to valid(cummulative m
osaic3, cumml45)
plot(cumml453)
```

#### In [14]:

 $\label{eq:plot_cumml453} $$ plot(cumml453[400:1500,50:5000], size=(30,5)) $$ plot(cumml126[120:,200:5500], size=(30,5)) $$ $$$ 





For the last merging, we will downscale the images, because if not the RAM cannot generate a big enough canvas.

#### In [ ]:

```
from skimage.transform import downscale_local_mean
cumml126_small = centered_conical_projection_onto_cylinder(
    downscale_local_mean(cumml126[120:,200:5500], (4,4,1)).astype(np.uint8), f=800, s=800)
cumml453_small = centered_conical_projection_onto_cylinder(
    downscale_local_mean(cumml453[400:1500,50:5000], (4,4,1)).astype(np.uint8), f=800, s=800)
plot(cumml453_small)
plot(cumml126_small)
```

#### In [49]:

#### In [52]:

plot(total[100:550, 100:1600], size=(30,10))



Certainly the camera was not rotated as expected!

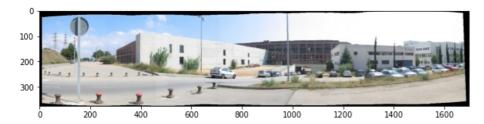
# 360 practice guide images

Lets now try a 360 image using the images given by the practice guide.

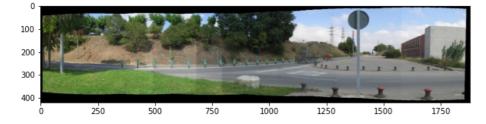
#### In [22]:

```
images=[]
images_cyl=[]
for i in range(1, 19):
    images.append(cv2.imread(f"360_2/{i}.png")[:,:,::-1])
    images_cyl.append(centered_conical_projection_onto_cylinder(images[-1], f=650, s=650))
cummulative_mosaic1 = images_cyl[0]
for im cyl in images cyl[1:7]:
    #plot(cummulative mosaic1)
    cummulative mosaic1, inliers = detect filter keypoints get matches find ransac homography make collage crop t
o valid(
                        image from=im cyl, image into=cummulative mosaic1)
cummulative mosaic2 = images cyl[6]
for im_cyl in images_cyl[6:13]:
    #plot(cummulative mosaic2)
    cummulative_mosaic2, inliers = detect_filter_keypoints_get_matches_find_ransac_homography_make_collage_crop_t
o valid(
                        image from=im cyl, image into=cummulative mosaic2)
cummulative_mosaic3 = images_cyl[12]
for im_cyl in images_cyl[12:]:
    #plot(cummulative_mosaic3)
    cummulative mosaic3, inliers = detect filter keypoints get matches find ransac homography make collage crop t
o valid(
                        image from=im cyl, image into=cummulative mosaic3)
print("Obtained Cummulative mosaics:")
plot(cummulative mosaic1)
plot(cummulative mosaic2)
plot(cummulative_mosaic3)
```

#### Obtained Cummulative mosaics:

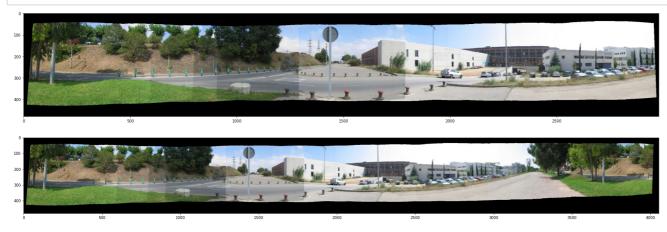






#### In [23]:

cumml13, \_ = detect\_filter\_keypoints\_get\_matches\_find\_ransac\_homography\_make\_collage\_crop\_to\_valid(cummulative\_mo
saic3, cummulative\_mosaic1)
plot(cumml13, size=(30,5))
cumml360, \_ = detect\_filter\_keypoints\_get\_matches\_find\_ransac\_homography\_make\_collage\_crop\_to\_valid(cummulative\_m
osaic2, cumml13)
plot(cumml360, size=(30,5))



We can see that the brightness change of the images is transferred to the final mosaic. A bit of image pre-processing to make all the images have the same range of light should correct this undesired effect.

# **END**