1 Lexer

The Lexer reads the proof code and produces the list of tokens that represents it.

```
module Lexer where import Data.Char
```

These tokens are represented as LexerTokens, and are as follows

```
data Token = ID String

| LParen
| RParen
| LBrack
| RBrack
| Arrow
| Exists
| Number Integer
```

The string itself is chopped up by the munch function, which uses the simplified maximal munch algorithm to produce tokens.

```
munch :: String → (Token, String)
munch code = (convertToToken tokenStr, rest)
where (tokenStr, rest) = extractTokenStr Start "" code
```

As you may have noticed, the actual munching is performed by extract-TokenStr, while munch simply serves as an entry point. Before defining that, however, we require a few helper definitions.

First are the states which the state machine used for munching can be in:

```
data State = Start | Identifier | Numeric | NumericPoint | Single
```

Then, we have a few helper functions which can identify classes of characters.

is Ident checks that a character is a valid character for an identifier, i.e. alphanumeric, or an underscore.

isSingle checks that a character is one of the characters that makes up a whole token on its own.

```
\mathtt{isIdent} \; :: \; \mathtt{Char} \; \to \; \mathtt{Bool}
isIdent c = isAlphaNum c || c == '_'
\mathtt{isSingle} \; :: \; \mathtt{Char} \; \to \; \mathtt{Bool}
isSingle c = c 'elem' "()[]\Leftrightarrow+-,=*/:"
extractTokenStr :: State \rightarrow String \rightarrow String \rightarrow (String, String)
extractTokenStr state token code = case state of
  Start
                       \rightarrow case code of
     '.' : rest

ightarrow extractTokenStr NumericPoint ".0" rest
     1 : rest | isAlpha 1 || 1 == '_'

ightarrow extractTokenStr Identifier [1] rest
     \texttt{n} \; : \; \texttt{rest} \; \mid \; \texttt{isDigit} \; \; \texttt{n} \; \; \rightarrow \; \texttt{extractTokenStr} \; \; \texttt{Numeric} \; \; [\texttt{n}] \; \; \texttt{rest}
     o : rest | isSingle o \rightarrow extractTokenStr Single [o] rest
     w: rest \mid isSpace w \rightarrow extractTokenStr Start [] rest
                                      \rightarrow error $ "Lexer could not process character
             sequence " ++ code -- TODO: LexerError
  Identifier

ightarrow case code of
     1: \mathtt{rest} \mid \mathtt{isIdent} \ 1 \rightarrow \mathtt{extractTokenStr} \ \mathtt{Identifier} \ (1: \mathtt{token})
           rest
                                      \rightarrow (token, code)
                       \rightarrow case code of
     '.' : rest \rightarrow extractTokenStr NumericPoint ('.' : token) rest
     1 : rest \mid isDigit 1 \rightarrow extractTokenStr Numeric (1 : token) rest

ightarrow (token, code)
  {\tt NumericPoint} \ \to \ {\tt case} \ {\tt code} \ {\tt of}
     1: rest \mid isDigit \mid 1 \rightarrow extractTokenStr NumericPoint (1: token)
           rest
                                      \rightarrow (token, code)
  Single
                       \rightarrow (token, code)
```

The strings extracted by extractTokenStr are then finally converted to actual tokens by convertToToken. This function expects that the token be written backwards because that's how extractTokenStr makes them.

```
\begin{array}{ll} {\tt convertToToken} \ :: \ {\tt String} \ \to \ {\tt Token} \\ {\tt convertToToken} \ \_ = \ {\tt LParen} \end{array}
```

The munch function is finally used by lexify, which will continually munch the text until no text remains, producing the full list of munched tokens.

```
lexify :: String → [Token]
lexify [] = []
lexify code = token : lexify rest
  where (token, rest) = munch code
```