## 1 AST

The AST is the internal representation of a proof program.

```
module AST where
  data AST = Scope [AST] -- DeclList
             ID String AST -- name ArgumentList
             ArgumentList [AST] -- [Annotation]
             TypeOf AST -- Value
             Annotation String AST -- name Type
             Let AST AST AST -- ID Type Body
             Arrow AST AST -- Annotation Type
             Function AST AST -- ID Body
             Application AST AST -- Function Value
             Exists AST AST -- Annotation Body
             IntroExists AST AST -- Type Value [will this need another
               argument?]
             ElimExists AST AST -- Exists Body [how does this work again?
                does it need another argument too?]
             And AST AST -- Type Type
             IntroAnd AST AST -- Left Right
             ElimAndLeft AST AST -- And Body
             ElimAndRight AST AST -- And Body
             Or AST AST -- Type Type
             IntroOrLeft AST AST -- Or Value
             IntroOrRight AST AST -- Or Value
             ElimOr AST AST AST -- Or LeftBody RightBody
             Contradiction
            ElimContradiction AST AST -- Contradiction Body [does this
               have a body? contradiction usually means done]
           -- [will this need equality type and reflexivity?]
           -- value nodes
           | VNatural Int -- Value
            VFloat Float -- Value [is this needed? or just define as a
               pair or in STL]
            VChar Char -- Value [is this needed? or just define as an
               int or in STL]
             VBoolean Bool -- True/False
             VCons AST AST -- Head Tail
             VEmpty -- empty list
            VSymbol String -- For
             VNull -- the empty value
           VUndefined -- the non-existent value
           -- induction [do these need that 4th param like last time?]
           -- this needs a way to write induction in the code!!
           | IndNatural AST AST AST -- Int BodyS BodyZ
             IndBoolean AST AST AST -- Bool BodyT BodyF
            IndList AST AST AST -- List BodyL BodyE [is this correct?]
```

```
| Insert
| BuiltIn String -- name
deriving (Show, Eq)
```