1 Lexer

The Lexer reads the proof code and produces the list of tokens that represents it.

```
module Lexer where
  import Data.Char
  import Data.List.Split
```

These tokens are represented as `LexerToken`s, and are as follows

```
  data Token  = BOF
              | ID String
              | Number Integer Integer
              | LParen
              | RParen
              | LBrack
              | RBrack
              | SQuote
              | DQuote
              | Arrow
              | Exists
              | ForAll
              | OpAdd
              | OpSub
              | OpMul
              | OpDiv
              | OpMod
              | OpLT
              | OpGT
              | OpAnd
              | OpOr
              | Negation
              | Bottom
              | Comma
              | Colon
              | Type
              | TypeOfType
              | True
              | False
              | TBoolean
              | TNumber
              | TList
              | TChar
```

```
          | TypeOf
          | Let
          | EOF
          deriving (Show)
```

The string itself is chopped up by the `munch` function, which uses the simplified maximal munch algorithm to produce tokens.

```
munch :: String → (Token, String)
munch = extractTokenStr Start ""
```

As you may have noticed, the actual munching is performed by `extractTokenStr`, while munch simply serves as an entry point. Before defining that, however, we require a few helper definitions.

First are the states which the state machine used for munching can be in:

```
data State = Start | Identifier | Numeric | NumericPoint | Single |
    PossibleArrow
```

Then, we have a few helper functions which can identify classes of characters.

`isIdent` checks that a character is a valid character for an identifier, i.e. alphanumeric, or an underscore.

`isSingle` checks that a character is one of the characters that makes up a whole token on its own.

```
isIdent :: Char → Bool
isIdent c = isAlphaNum c || c == '_'

isSingle :: Char → Bool
isSingle c = c `elem` "()[]<>+-,=%*/: |&'λ""

extractTokenStr :: State → String → String → (Token, String)
extractTokenStr state token code = case state of
  Start         → case code of
    '.' : rest           → extractTokenStr NumericPoint ".0" rest
    '-' : rest           → extractTokenStr PossibleArrow "-" rest
    l : rest | isAlpha l || l == '_'
                         → extractTokenStr Identifier [l] rest
```

```
    n : rest | isDigit n  → extractTokenStr Numeric [n] rest
    o : rest | isSingle o → extractTokenStr Single [o] rest
    w : rest | isSpace w  → extractTokenStr Start [] rest
    _                     → error $ "Lexer could not process character
        sequence " ++ code -- TODO: LexerError
  Identifier    → case code of
    l : rest | isIdent l  → extractTokenStr Identifier (l : token)
        rest
    _                     → (convertToToken token, code)
  Numeric       → case code of
    '.' : rest            → extractTokenStr NumericPoint ('.' : token)
        rest
    l : rest | isDigit l  → extractTokenStr Numeric (l : token) rest
    _                     → (Number (read $ reverse token) 0, code)
  NumericPoint  → case code of
    l : rest | isDigit l  → extractTokenStr NumericPoint (l : token)
        rest
    _                     → (Number (read left) (read right), code)
                             where [left, right] = map reverse $
                                 reverse $ splitOn "." token
  PossibleArrow → case code of
    '>' : rest            → extractTokenStr Single ">-" rest
    _                     → (convertToToken token, code)
  Single        → (convertToToken token, code)
```

The strings extracted by `extractTokenStr`, other than the numeric ones, are converted to actual tokens by `convertToToken`. This function expects that the token be written backwards because that's how `extractTokenStr` makes them.

Is that a stupid design for this function? Probably, but I think it will be ok.

```
convertToToken :: String → Token
convertToToken "" = Arrow
convertToToken ">-" = Arrow
convertToToken "(" = LParen
convertToToken ")" = RParen
convertToToken "[" = LBrack
convertToToken "]" = RBrack
convertToToken "<" = OpLT
convertToToken ">" = OpGT
convertToToken "-" = OpSub
convertToToken "+" = OpAdd
convertToToken "'" = SQuote
convertToToken "λ"" = DQuote
convertToToken "/" = OpDiv
convertToToken "*" = OpMul
```

```
convertToToken "%" = OpMod
convertToToken ":" = Colon
convertToToken "," = Comma
convertToToken "" = Exists
convertToToken "stsixe" = Exists
convertToToken "" = ForAll
convertToToken "llarof" = ForAll
convertToToken " " = Negation
convertToToken "" = Bottom
convertToToken "dna" = OpAnd
convertToToken "&" = OpAnd
convertToToken "" = OpAnd
convertToToken "ro" = OpOr
convertToToken "|" = OpOr
convertToToken "" = OpOr
convertToToken "epyt" = Type
convertToToken "epyT" = TypeOfType
convertToToken "foepyt" = TypeOf
convertToToken "tel" = Let
convertToToken "eurt" = Lexer.True
convertToToken "eslaf" = Lexer.False
convertToToken "looB" = TBoolean
convertToToken "rebmuN" = TNumber
convertToToken "rahC" = TChar
convertToToken "tsiL" = TList
convertToToken t = ID $ reverse t
```

The `munch` function is finally used by `lexify`, which will continually munch the text until no text remains, producing the full list of munched tokens.

```
doLexify :: String → [Token]
doLexify [] = [EOF]
doLexify code = token : doLexify rest
  where (token, rest) = munch code

lexify :: String → [Token]
lexify code = BOF : doLexify code
```