

1 Lexer

The Lexer reads the proof code and produces the list of tokens that represents it.

```
module Lexer where
  import Data.Char
  import Data.List.Split
```

These tokens are represented as `LexerTokens`, and are as follows

```
data Token = BOF
           | ID String
           | Number Integer Integer
           | LParen
           | RParen
           | LBrack
           | RBrack
           | Arrow
           | Exists
           | ForAll
           | OpAdd
           | OpSub
           | OpMul
           | OpDiv
           | OpMod
           | OpLT
           | OpGT
           | OpAnd
           | OpOr
           | Negation
           | Bottom
           | Comma
           | Colon
           | Type
           | TypeOf
           | Let
           | EOF
           deriving (Show)
```

The string itself is chopped up by the `munch` function, which uses the simplified maximal munch algorithm to produce tokens.

```
munch :: String → (Token, String)
munch = extractTokenStr Start ""
```

As you may have noticed, the actual munching is performed by `extractTokenStr`, while `munch` simply serves as an entry point. Before defining that, however, we require a few helper definitions.

First are the states which the state machine used for munching can be in:

```
data State = Start | Identifier | Numeric | NumericPoint | Single |
            PossibleArrow
```

Then, we have a few helper functions which can identify classes of characters. `isIdent` checks that a character is a valid character for an identifier, i.e. alphanumeric, or an underscore.

`isSingle` checks that a character is one of the characters that makes up a whole token on its own.

```
isIdent :: Char → Bool
isIdent c = isAlphaNum c || c == '_'

isSingle :: Char → Bool
isSingle c = c `elem` "()[]<>+-,=%*/: "

extractTokenStr :: State → String → String → (Token, String)
extractTokenStr state token code = case state of
  Start      → case code of
    '.' : rest      → extractTokenStr NumericPoint ".0" rest
    '-' : rest      → extractTokenStr PossibleArrow "-" rest
    l : rest | isAlpha l || l == '_'
              → extractTokenStr Identifier [l] rest
    n : rest | isDigit n → extractTokenStr Numeric [n] rest
    o : rest | isSingle o → extractTokenStr Single [o] rest
    w : rest | isSpace w → extractTokenStr Start [] rest
    -                → error $ "Lexer could not process character
      sequence " ++ code -- TODO: LexerError
  Identifier → case code of
    l : rest | isIdent l → extractTokenStr Identifier (l : token)
    rest                → (convertToToken token, code)
  -
  Numeric    → case code of
    '.' : rest      → extractTokenStr NumericPoint ('.' : token)
```

```

        rest
    l : rest | isDigit l → extractTokenStr Numeric (l : token) rest
    -                → (Number (read $ reverse token) 0, code)
NumericPoint → case code of
    l : rest | isDigit l → extractTokenStr NumericPoint (l : token)
    rest
    -                → (Number (read left) (read right), code)
                        where [left, right] = map reverse $
                                reverse $ splitOn "." token
PossibleArrow → case code of
    '>' : rest          → extractTokenStr Single ">" rest
    -                → (convertToToken token, code)
Single              → (convertToToken token, code)

```

The strings extracted by `extractTokenStr`, other than the numeric ones, are converted to actual tokens by `convertToToken`. This function expects that the token be written backwards because that's how `extractTokenStr` makes them.

Is that a stupid design for this function? Probably, but I think it will be ok.

```

convertToToken :: String → Token
convertToToken "" = Arrow
convertToToken ">" = Arrow
convertToToken "(" = LParen
convertToToken ")" = RParen
convertToToken "[" = LBrack
convertToToken "]" = RBrack
convertToToken "<" = OpLT
convertToToken ">" = OpGT
convertToToken "-" = OpSub
convertToToken "+" = OpAdd
convertToToken "/" = OpDiv
convertToToken "*" = OpMul
convertToToken "%" = OpMod
convertToToken ":" = Colon
convertToToken "," = Comma
convertToToken "" = Exists
convertToToken "stsize" = Exists
convertToToken "" = ForAll
convertToToken "llarof" = ForAll
convertToToken " " = Negation
convertToToken "" = Bottom
convertToToken "dna" = OpAnd
convertToToken "" = OpAnd
convertToToken "ro" = OpOr
convertToToken "" = OpOr

```

```
convertToToken "epyt" = Type
convertToToken "foepyt" = TypeOf
convertToToken "tel" = Let
convertToToken t = ID $ reverse t
```

The `munch` function is finally used by `lexify`, which will continually munch the text until no text remains, producing the full list of munched tokens.

```
doLexify :: String → [Token]
doLexify [] = [EOF]
doLexify code = token : doLexify rest
  where (token, rest) = munch code

lexify :: String → [Token]
lexify code = BOF : doLexify code
```
