1 Lexer

The Lexer reads the proof code and produces the list of tokens that represents it.

```
module Lexer where
import Data.Char
import Data.List.Split
```

These tokens are represented as LexerTokens, and are as follows

```
data Token = BOF
              ID String
              LParen
              RParen
              LBrack
              RBrack
              Arrow
              Exists
              ForAll
              Number Integer Integer
              OpAdd
              OpSub
              OpMul
              OpDiv
              OpMod
              0pLT
              OpGT
              OpAnd
              0p0r
              Negation
              Bottom
              Comma
              {\tt Colon}
              Туре
              TypeOf
              Val
              EOF
            deriving (Show)
```

The string itself is chopped up by the munch function, which uses the simplified maximal munch algorithm to produce tokens.

```
munch :: String → (Token, String)
munch = extractTokenStr Start ""
```

As you may have noticed, the actual munching is performed by extract-TokenStr, while munch simply serves as an entry point. Before defining that, however, we require a few helper definitions.

First are the states which the state machine used for munching can be in:

```
data State = Start | Identifier | Numeric | NumericPoint | Single |
PossibleArrow
```

Then, we have a few helper functions which can identify classes of characters. is Ident checks that a character is a valid character for an identifier, i.e. alphanumeric, or an underscore.

isSingle checks that a character is one of the characters that makes up a whole token on its own.

```
\mathtt{isIdent} \; :: \; \mathtt{Char} \; \to \; \mathtt{Bool}
isIdent c = isAlphaNum c || c == '_'
\mathtt{isSingle} \, :: \, \mathtt{Char} \, \to \, \mathtt{Bool}
isSingle c = c 'elem' "()[]\Leftrightarrow+-,=%*/: "
\texttt{extractTokenStr} \; :: \; \texttt{State} \; \rightarrow \; \texttt{String} \; \rightarrow \; \texttt{String} \; \rightarrow \; \texttt{(Token, String)}
extractTokenStr state token code = case state of
  Start
                      \rightarrow case code of
     '.' : rest

ightarrow extractTokenStr NumericPoint ".0" rest
     '-' : rest

ightarrow extractTokenStr PossibleArrow "-" rest
     1 : rest | isAlpha 1 || 1 == '_'

ightarrow extractTokenStr Identifier [1] rest
     \texttt{n} \; : \; \texttt{rest} \; \mid \; \texttt{isDigit} \; \; \texttt{n} \; \; \rightarrow \; \texttt{extractTokenStr} \; \; \texttt{Numeric} \; \; [\texttt{n}] \; \; \texttt{rest}
     o : rest \mid isSingle o \rightarrow extractTokenStr Single [o] rest
     w : rest \mid isSpace w \rightarrow extractTokenStr Start [] rest
                                      \rightarrow error $ "Lexer could not process character
             sequence " ++ code -- TODO: LexerError

ightarrow case code of
  Identifier
     l : rest \mid isIdent l \rightarrow extractTokenStr Identifier (l : token)
            rest
                                      → (convertToToken token, code)
  Numeric
                       \rightarrow case code of
     '.' : rest
                                      \rightarrow extractTokenStr NumericPoint ('.' : token)
```

The strings extracted by extractTokenStr, other than the numeric ones, are converted to actual tokens by convertToToken. This function expects that the token be written backwards because that's how extractTokenStr makes them.

Is that a stupid design for this function? Probably, but I think it will be ok.

```
{\tt convertToToken} \; :: \; {\tt String} \; \to \; {\tt Token}
convertToToken "" = Arrow
convertToToken ">-" = Arrow
convertToToken "(" = LParen
convertToToken ")" = RParen
convertToToken "[" = LBrack
convertToToken "]" = RBrack
convertToToken "<" = OpLT
convertToToken ">" = OpGT
convertToToken "-" = OpSub
{\tt convertToToken} \ "+" = {\tt OpAdd}
{\tt convertToToken} \ {\tt "/"} = {\tt OpDiv}
convertToToken "*" = OpMul
convertToToken "%" = OpMod
convertToToken ":" = Colon
convertToToken "," = Comma
{\tt convertToToken} \ {\tt ""} = {\tt Exists}
convertToToken "stsixe" = Exists
convertToToken "" = ForAll
{\tt convertToToken} \ "{\tt llarof"} = {\tt ForAll}
convertToToken " " = Negation
convertToToken "" = Bottom
convertToToken "dna" = OpAnd
convertToToken "" = OpAnd
convertToToken "ro" = OpOr
convertToToken "" = OpOr
```

```
convertToToken "epyt" = Type
convertToToken "foepyt" = TypeOf
convertToToken "lav" = Val
convertToToken t = ID $ reverse t
```

The munch function is finally used by lexify, which will continually munch the text until no text remains, producing the full list of munched tokens.

```
doLexify :: String → [Token]
doLexify [] = [EOF]
doLexify code = token : doLexify rest
  where (token, rest) = munch code

lexify :: String → [Token]
lexify code = BOF : doLexify code
```