

“Heaven's Light is Our Guide”

Rajshahi University of Engineering and Technology



Course code: 1202

Course title: Circuits & Systems – II Sessional

Report Number: 02

Experiment Name: **Study of the relation between phase current and line current in a delta connected 3 – ϕ balanced system.**

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Experiment 2

2.1 Name of the Experiment: Study of the relation between phase current and line current in a delta connected 3 – ϕ balanced system.

2.2 Theory: In a balanced 3 – ϕ Y - Δ system, phase currents are:

$$I_{ab} = \frac{V_{ab}}{Z_{\Delta}}, I_{bc} = \frac{V_{bc}}{Z_{\Delta}} \text{ and } I_{ca} = \frac{V_{ca}}{Z_{\Delta}}$$

The line currents can be obtained from applying KCL. So, the line currents will be:

$$I_A = I_{ab} - I_{ca}, I_B = I_{bc} - I_{ab} \text{ and } I_C = I_{ca} - I_{bc}$$

Since $I_{CA} = I_{AB} \angle -240^\circ$,

$$I_A = I_{ab} - I_{ca} = I_{ab} (1 - 1 \angle -240^\circ) = I_{ab} (1 + 0.5 - j0.866) = I_{ab} \sqrt{3} \angle 30^\circ$$

Now, if we consider the magnitude only, we get the relation between phase and line current as,

$$I_P = \frac{I_L}{\sqrt{3}} \dots \dots \dots (1)$$

2.3 Required Apparatus:

1. Source
2. VARIAC
3. Voltmeter
4. Ammeter
5. Resistor
6. Multimeter
7. Connecting wires

2.4 Circuit Diagram:

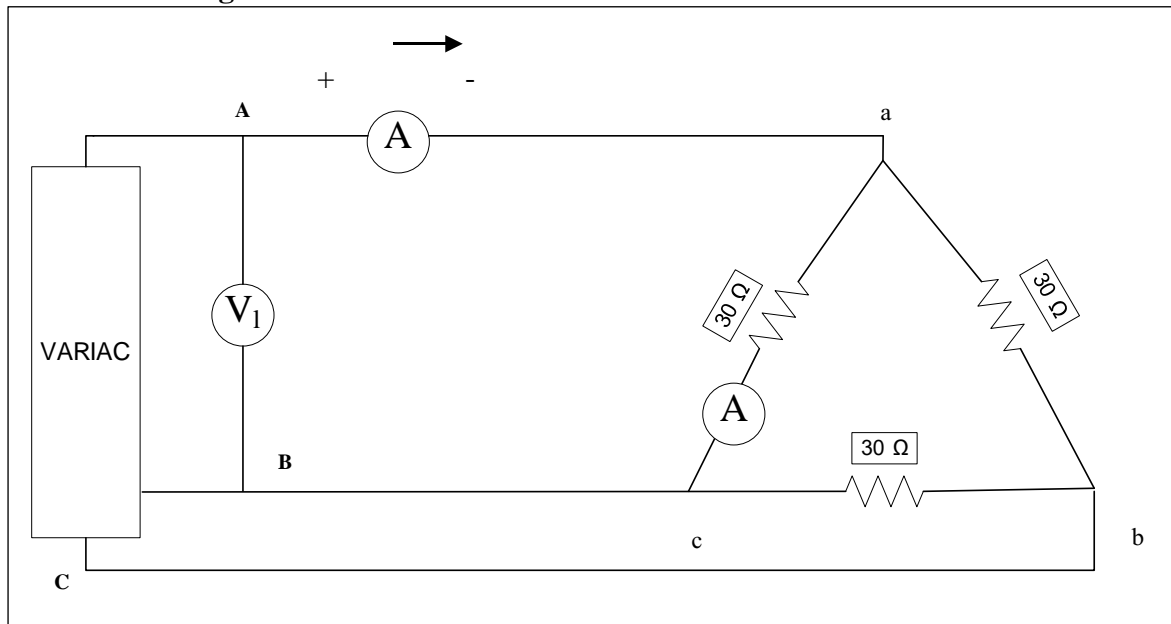


Fig: A balanced 3 – ϕ Y - Δ system

2.5 Calculation:

1. Reading 1:

Line current, $I_L = 2.25$ A

Measured phase current, $I_{P(m)} = 1.26$ A

Calculated phase current, $I_{P(calc)} = 1.29$ A

$$\text{Error} = \frac{|I_{P(calc)} - I_{P(m)}|}{I_{P(calc)}} \times 100\% = \frac{|1.29 - 1.26|}{1.29} \times 100\% = 2.32\%$$

2. Reading 2:

Line current, $I_L = 0.72$ A

Measured phase current, $I_{P(m)} = 0.39$ A

Calculated phase current, $I_{P(calc)} = 0.41$ A

$$\text{Error} = \frac{|I_{P(calc)} - I_{P(m)}|}{I_{P(calc)}} \times 100\% = \frac{|0.41 - 0.39|}{0.41} \times 100\% = 4.87\%$$

3. Reading 3:

Line current, $I_L = 1.28$ A

Measured phase current, $I_{P(m)} = 0.7$ A

Calculated phase current, $I_{P(calc)} = 0.74$ A

$$\text{Error} = \frac{|I_{P(calc)} - I_{P(m)}|}{I_{P(calc)}} \times 100\% = \frac{|0.74 - 0.7|}{0.74} \times 100\% = 5.4\%$$

4. Reading 4:

Line current, $I_L = 1.87 \text{ A}$

Measured phase current, $I_{P(m)} = 1.04 \text{ A}$

Calculated phase current, $I_{P(calc)} = 1.08 \text{ A}$

$$\text{Error} = \frac{|I_{P(calc)} - I_{P(m)}|}{I_{P(calc)}} \times 100\% = \frac{|1.08 - 1.04|}{1.08} \times 100\% = 3.7\%$$

5. Reading 5:

Line current, $I_L = 2.79 \text{ A}$

Measured phase current, $I_{P(m)} = 1.59 \text{ A}$

Calculated phase current, $I_{P(calc)} = 1.61 \text{ A}$

$$\text{Error} = \frac{|I_{P(calc)} - I_{P(m)}|}{I_{P(calc)}} \times 100\% = \frac{|1.61 - 1.59|}{1.61} \times 100\% = 1.24\%$$

$$\therefore \text{Average error} = \frac{2.32 + 4.87 + 5.4 + 3.7 + 1.24}{5} = 3.506\%$$

2.6 Table for Studying Relation Between Line and Phase Voltage:

Serial No	Line Current, I_L (A)	Measured Phase Current, $I_{P(m)}$ (A)	Calculated Phase Current, $I_{P(calc)}$ (A)	Percentage of Error (%)	Line Voltage, V_L (V)	Phase Voltage, V_P (V)
1	41.47	23.5	24.07	2.32	39.0	38.3
2	34.1	19	19.69	4.87	12.84	12.83
3	55.5	31.4	32.04	5.4	22.15	21.83
4	63.6	35.6	36.72	3.7	32.17	31.6
5	71.7	40.5	41.4	1.24	47.3	47.1

2.7 Result:

Average percentage of error: 3.506%

2.8 Discussion:

Performing the experiment above, we could prove the relation between phase and line current in a 3 – ϕ balanced Y - Δ system. After all the calculations, we figured our error margin was 3.506% which is negligible. This little error margin certifies that, the line current is $\sqrt{3}$ times that of phase current.

2.9 References:

1. Fundamentals of Electric Circuits by Charles K. Alexander and Mathew N. O. Sadiku.