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```
% Assignment 3 Question 3
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clc; clear; close all;
cell_all = struct2table(dir("yalefacespng"));
cell_all = cell_all.name;

matrix = zeros(243, 320, 90); % This will contain all the images
vector_matrix = zeros(77760, 90); % This will contain all the reshaped images in vector form
for i=1:90
    matrix(:, :, i) = imread('yalefacespng/' + string(cell_all(i+2)));
    vector_matrix(:, i) = reshape(matrix(:, :, i), 77760, 1);
end

% In case an image is to be seen, firstly convert it to uint8 and then
% display the reshaped image in size 243 * 320
```

Part 1. Norm Images

```
vector_norms = vector_matrix(:, 6:6:90); % All normal images
classified_person = zeros(90, 1);
image_num = 1:1:90; image_num = image_num';
true_person_num = floor((image_num-1)/6) + 1;
result = [];
correct_count = 0;

for i=1:90
    % The norm images will be 6*i kind amongst the above dataset
    % After that, use a for loop from 1:15 to check the distances
    dist = zeros(15, 1);
    for j=1:15
        dist(j) = norm(vector_norms(:, j) - vector_matrix(:, i));
    end
    classified_person(i) = find(dist == min(dist, [], "all"));
    if classified_person(i) == true_person_num(i)
        result = [result; "YES"];
        correct_count = correct_count + 1;
    else
        result = [result; "NO"];
    end
end

to_show = table(image_num, true_person_num, classified_person, result);
disp("The following table contains the Image number, Correct label of person, Classified estimate and Result");
disp(to_show)
disp("The number of images obtained correctly by comparing with the norm images is: " + correct_count);
disp("-----")
```

The following table contains the Image number, Correct label of person, Classified estimate and Result

image_num	true_person_num	classified_person	result
1	1	1	"YES"
2	1	1	"YES"
3	1	1	"YES"
4	1	12	"NO"
5	1	2	"NO"
6	1	1	"YES"
7	2	2	"YES"
8	2	2	"YES"
9	2	2	"YES"
10	2	2	"YES"
11	2	2	"YES"
12	2	2	"YES"
13	3	13	"NO"
14	3	3	"YES"
15	3	3	"YES"
16	3	12	"NO"
17	3	3	"YES"
18	3	3	"YES"
19	4	4	"YES"
20	4	4	"YES"
21	4	4	"YES"
22	4	2	"NO"
23	4	4	"YES"
24	4	4	"YES"

25	5	5	"YES"
26	5	5	"YES"
27	5	5	"YES"
28	5	12	"NO"
29	5	5	"YES"
30	5	5	"YES"
31	6	14	"NO"
32	6	6	"YES"
33	6	6	"YES"
34	6	12	"NO"
35	6	6	"YES"
36	6	6	"YES"
37	7	10	"NO"
38	7	7	"YES"
39	7	7	"YES"
40	7	12	"NO"
41	7	7	"YES"
42	7	7	"YES"
43	8	8	"YES"
44	8	8	"YES"
45	8	8	"YES"
46	8	12	"NO"
47	8	10	"NO"
48	8	8	"YES"
49	9	3	"NO"
50	9	5	"NO"
51	9	9	"YES"
52	9	12	"NO"
53	9	9	"YES"
54	9	9	"YES"
55	10	1	"NO"
56	10	1	"NO"
57	10	10	"YES"
58	10	2	"NO"
59	10	10	"YES"
60	10	10	"YES"
61	11	11	"YES"
62	11	11	"YES"
63	11	11	"YES"
64	11	11	"YES"
65	11	11	"YES"
66	11	11	"YES"
67	12	5	"NO"
68	12	2	"NO"
69	12	5	"NO"
70	12	12	"YES"
71	12	12	"YES"
72	12	12	"YES"
73	13	7	"NO"
74	13	13	"YES"
75	13	13	"YES"
76	13	12	"NO"
77	13	13	"YES"
78	13	13	"YES"
79	14	14	"YES"
80	14	14	"YES"
81	14	14	"YES"
82	14	11	"NO"
83	14	14	"YES"
84	14	14	"YES"
85	15	15	"YES"
86	15	10	"NO"
87	15	15	"YES"
88	15	12	"NO"
89	15	10	"NO"
90	15	15	"YES"

The number of images obtained correctly by comparing with the norm images is: 63  
 -----

### Part 2. First Principle Component

B - First Principal Component use to make image

```

PC_comp = zeros(77760, 15);
variance_arr = zeros(15, 1);

for i=1:15
    Z = vector_matrix(:, ((6*i) - 5):(6*i));
    Z_s = Z - mean(Z, 1);
    S_zs = cov(Z_s);
    [V, D] = eig(S_zs);
    D = sort(diag(D), 'descend');
    variance_arr(i) = D(1)/sum(D, "all");
    PC_comp(:, i) = Z*((V(:, end)).^2); % This contains the first PC of every person as each column
end

```

```

disp("We multiply by ((V(:, end)).^2) so that condition of orthogonality is " + ...
    "maintained, and also to obtain weights between 0 and 1, so that the " + ...
    "resulting number also lies in between 0 and 255")

% imshow(reshape(uint8(PC_comp(:, 2)), 243, 320))

classified_person = zeros(90, 1);
image_num = (1:1:90)';
result = [];
correct_count = 0;

for i=1:90

    dist = zeros(15, 1);
    for j = 1:15
        dist(j) = norm(PC_comp(:, j) - vector_matrix(:, i));
    end
    est_person_img = find(dist == min(dist, []), 'all'); % Minimum index is found
    if est_person_img == true_person_num(i)
        result = [result; "YES"];
        correct_count = correct_count + 1;
    else
        result = [result; "NO"];
    end
end

to_show = table(image_num, true_person_num, result);
disp("The following table contains the Image number, Correct label of person, Classified estimate and Result");
disp(to_show)
disp("The number of images obtained correctly by comparing with the first PC is: " + correct_count);
disp("-----")

```

We multiply by  $((V(:, \text{end}))^2)$  so that condition of orthogonality is maintained, and also to obtain weights between 0 and 1, so that the resulting number also lies between 0 and 255. The following table contains the Image number, Correct label of person, Classified estimate and Result

image_num	true_person_num	result
1	1	"YES"
2	1	"YES"
3	1	"YES"
4	1	"NO"
5	1	"YES"
6	1	"YES"
7	2	"YES"
8	2	"YES"
9	2	"YES"
10	2	"YES"
11	2	"YES"
12	2	"YES"
13	3	"YES"
14	3	"YES"
15	3	"YES"
16	3	"NO"
17	3	"YES"
18	3	"YES"
19	4	"YES"
20	4	"YES"
21	4	"YES"
22	4	"NO"
23	4	"YES"
24	4	"YES"
25	5	"YES"
26	5	"YES"
27	5	"YES"
28	5	"NO"
29	5	"YES"
30	5	"YES"
31	6	"NO"
32	6	"YES"
33	6	"YES"
34	6	"NO"
35	6	"YES"
36	6	"YES"
37	7	"YES"
38	7	"YES"
39	7	"YES"
40	7	"NO"
41	7	"YES"
42	7	"YES"
43	8	"YES"
44	8	"YES"
45	8	"YES"
46	8	"NO"
47	8	"YES"
48	8	"YES"

49	9	"YES"
50	9	"YES"
51	9	"YES"
52	9	"NO"
53	9	"YES"
54	9	"YES"
55	10	"YES"
56	10	"YES"
57	10	"YES"
58	10	"NO"
59	10	"YES"
60	10	"YES"
61	11	"YES"
62	11	"YES"
63	11	"YES"
64	11	"YES"
65	11	"YES"
66	11	"YES"
67	12	"NO"
68	12	"YES"
69	12	"NO"
70	12	"YES"
71	12	"YES"
72	12	"YES"
73	13	"YES"
74	13	"YES"
75	13	"YES"
76	13	"NO"
77	13	"YES"
78	13	"YES"
79	14	"YES"
80	14	"YES"
81	14	"YES"
82	14	"NO"
83	14	"YES"
84	14	"YES"
85	15	"YES"
86	15	"YES"
87	15	"YES"
88	15	"NO"
89	15	"YES"
90	15	"YES"

The number of images obtained correctly by comparing with the first PC is: 75

-----

### Part 3. Two Principle Components

```
PC_comp_both = zeros(77760, 30);
variance_arr = zeros(15, 1);

for i=1:15
    Z = vector_matrix(:, ((6*i) - 5):(6*i));
    Z_s = Z - mean(Z, 1);
    S_zs = cov(Z_s);
    [V, D] = eig(S_zs);
    D = sort(diag(D), 'descend');
    variance_arr(i) = (D(1) + D(2))/sum(D, "all");
    PC_comp_both(:, 2*i-1) = Z*((V(:, end)).^2);
    PC_comp_both(:, 2*i) = Z*((V(:, end-1)).^2);
end

classified_person_1 = zeros(90, 1);
classified_person_2 = zeros(90, 1);
image_num = (1:1:90)';
result = [];
correct_count = 0;

for i=1:90

    dist_first = zeros(15, 1);
    dist_second = zeros(15, 1);
    for j = 1:15
        dist_first(j) = norm(PC_comp_both(:, 2*j-1) - vector_matrix(:, i));
        dist_second(j) = norm(PC_comp_both(:, 2*j) - vector_matrix(:, i));
    end
    est_person_img_first = find(dist_first == min(dist_first, [], 'all'));
    est_person_img_second = find(dist_second == min(dist_second, [], 'all'));

    if (est_person_img_first == true_person_num(i)) || (est_person_img_second == true_person_num(i))
        result = [result; "YES"];
        correct_count = correct_count + 1;
    else
        result = [result; "NO"];
    end
    classified_person_1(i) = est_person_img_first;
```

```

classified_person_2(i) = est_person_img_second;
end

to_show = table(image_num, true_person_num, classified_person_1, classified_person_2, result);
disp("The following table contains the Image number, Correct label of person, Classified estimate by PC1, Classified estimate by PC2 and Result");
disp(to_show)
disp("The number of images obtained correctly by comparing with the first 2 PCs is: " + correct_count);

```

The following table contains the Image number, Correct label of person, Classified estimate by PC1, Classified estimate by PC2 and Result

image_num	true_person_num	classified_person_1	classified_person_2	result
1	1	1	12	"YES"
2	1	1	12	"YES"
3	1	1	10	"YES"
4	1	12	1	"YES"
5	1	1	12	"YES"
6	1	1	12	"YES"
7	2	2	12	"YES"
8	2	2	12	"YES"
9	2	2	12	"YES"
10	2	2	2	"YES"
11	2	2	12	"YES"
12	2	2	12	"YES"
13	3	3	10	"YES"
14	3	3	13	"YES"
15	3	3	10	"YES"
16	3	12	3	"YES"
17	3	3	10	"YES"
18	3	3	10	"YES"
19	4	4	10	"YES"
20	4	4	12	"YES"
21	4	4	12	"YES"
22	4	12	4	"YES"
23	4	4	10	"YES"
24	4	4	12	"YES"
25	5	5	12	"YES"
26	5	5	12	"YES"
27	5	5	12	"YES"
28	5	12	5	"YES"
29	5	5	12	"YES"
30	5	5	12	"YES"
31	6	14	6	"YES"
32	6	6	6	"YES"
33	6	6	6	"YES"
34	6	12	6	"YES"
35	6	6	6	"YES"
36	6	6	6	"YES"
37	7	7	10	"YES"
38	7	7	10	"YES"
39	7	7	10	"YES"
40	7	12	7	"YES"
41	7	7	10	"YES"
42	7	7	10	"YES"
43	8	8	10	"YES"
44	8	8	10	"YES"
45	8	8	10	"YES"
46	8	12	8	"YES"
47	8	8	10	"YES"
48	8	8	10	"YES"
49	9	9	9	"YES"
50	9	9	10	"YES"
51	9	9	9	"YES"
52	9	12	9	"YES"
53	9	9	9	"YES"
54	9	9	9	"YES"
55	10	10	10	"YES"
56	10	10	10	"YES"
57	10	10	10	"YES"
58	10	1	10	"YES"
59	10	10	10	"YES"
60	10	10	10	"YES"
61	11	11	11	"YES"
62	11	11	10	"YES"
63	11	11	12	"YES"
64	11	11	11	"YES"
65	11	11	10	"YES"
66	11	11	12	"YES"
67	12	1	12	"YES"
68	12	12	12	"YES"
69	12	5	12	"YES"
70	12	12	2	"YES"
71	12	12	12	"YES"
72	12	12	12	"YES"
73	13	13	13	"YES"
74	13	13	13	"YES"

75	13	13	13	"YES"
76	13	12	13	"YES"
77	13	13	13	"YES"
78	13	13	13	"YES"
79	14	14	14	"YES"
80	14	14	14	"YES"
81	14	14	14	"YES"
82	14	11	14	"YES"
83	14	14	14	"YES"
84	14	14	14	"YES"
85	15	15	10	"YES"
86	15	15	10	"YES"
87	15	15	10	"YES"
88	15	11	15	"YES"
89	15	15	10	"YES"
90	15	15	10	"YES"

The number of images obtained correctly by comparing with the first 2 PCs is: 90