DA5401 Assignment 5

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This assignment aims to deepen the understanding of the challenges in real-world machine learning, specifically in **multi-label classification**, by utilizing advanced **non-linear dimensionality reduction techniques** such as **t-SNE** and **Isomap**. Visually inspect the data for issues such as noisy labels, outliers, and hard-to-learn data points, sparking curiosity about data veracity in a biological context.

Dataset

Yeast Dataset: The feature matrix X and the binary multi-label matrix Y (with 14 labels) are standard files available from the <u>Mulan</u> <u>Repository</u> or other machine learning data repositories.

The task is to apply t-SNE and Isomap to the feature vectors to visually expose these data quality issues, thereby understanding the challenges a classifier would face.

Importing libraries

```
import numpy as np
import scipy as sp
import pandas as pd

import matplotlib.pyplot as plt
import seaborn as sns

from sklearn.manifold import Isomap
from sklearn.manifold import TSNE
from sklearn.preprocessing import StandardScaler
from sklearn.metrics import silhouette_score
```

Tasks

Part A: Preprocessing and Initial Setup

1. Data Loading

```
from google.colab import drive
drive.mount('/content/drive')

Drive already mounted at /content/drive; to attempt to forcibly remount, call drive.mount("/content/drive", force_remount=True)

data = sp.io.arff.loadarff("/content/drive/MyDrive/yeast.arff")
df = pd.DataFrame(data[0])
```

```
print(data[0].shape)
(2417,)
```

2. Dimensionality Check

```
print("The length of the data is: " , len(data[0]))
print(df.shape)
df.head()
```

```
The length of the data is: 2417
(2417, 117)
       Att1
                 Att2
                          Att3
                                    Δ++4
                                              Att5
                                                        Att6
                                                                 Δtt7
                                                                           A++8
                                                                                     Δ††9
                                                                                              Att10 ... Class5 Class6 Cl
0 0.004168 -0.170975 -0.156748 -0.142151 0.058781 0.026851
                                                              0.197719
                                                                       0.041850
                                                                                 0.066938 -0.056617
                                                                                                            b'0'
                                                                                                                    b'0'
1 -0.103956
             0.011879 -0.098986 -0.054501 -0.007970
                                                    0.049113 -0.030580
                                                                       -0.077933
                                                                                 -0.080529
                                                                                          -0.016267
                                                                                                            b'0'
                                                                                                                    b'0'
   0.509949
             0.401709 0.293799
                                 b'0'
                                                                                                                    b'0'
                                                                        0.013646 -0.040666 -0.024447
   0.119092
             0.004412 -0.002262
                                 0.072254
                                          0.044512 -0.051467
                                                              0.074686 -0.007670
                                                                                 0.079438
                                                                                           0.062184
                                                                                                            b'0'
                                                                                                                    b'0'
   0.042037
             0.007054 -0.069483 0.081015 -0.048207
                                                    0.089446 -0.004947
                                                                        0.064456 -0.133387
                                                                                           0.068878
                                                                                                            b'1'
                                                                                                                    b'1'
5 rows × 117 columns
```

The size of the data indicates that it contains 2417 rows or samples and 117 features + class variables. Now, the next task will be to separate the class variables from the features for further processing.

Thus from the above, we can see that there are 103 columns as features and 14 Class variables. The Class variables are what we will be analysing further in this assignment. The Class variables are stored as 'Class1', 'Class2' in the dataframe df.

```
print(df.isnull().sum())
print("Number of total missing elements are: " , df.isnull().sum().sum())
Δ++1
Att2
           a
Att3
           a
Att4
           0
Att5
           0
Class10
Class11
           0
Class12
           0
Class13
           0
Class14
           a
Length: 117, dtype: int64
Number of total missing elements are: 0
```

Thus, we can see that there are no null values and the data is clean for us to use. We would not need to remove the null samples or replace them with the mean/ median.

```
for col_name in df.columns[103:]:
    print(col_name, " has unique elements as ", df[col_name].value_counts())
Class1 has unique elements as Class1
b'0'
       1655
b'1'
        762
Name: count, dtype: int64
Class2 has unique elements as Class2
       1379
b'0'
b'1'
       1038
Name: count, dtype: int64
Class3 has unique elements as Class3
       1434
b'0'
h'1'
        983
Name: count, dtype: int64
Class4 has unique elements as Class4
b'0'
       1555
b'1'
        862
Name: count, dtype: int64
Class5 has unique elements as Class5
b'0'
       1695
b'1'
        722
Name: count, dtype: int64
Class6 has unique elements as Class6
```

```
h'a'
        1820
b'1'
         597
Name: count, dtype: int64
Class7 has unique elements as Class7
b'0'
        1989
b'1'
        428
Name: count, dtype: int64
Class8 has unique elements as Class8
        1937
b'0'
b'1'
        480
Name: count, dtype: int64
Class9 has unique elements as Class9
b'0'
        2239
b'1'
        178
Name: count, dtype: int64
Class10 has unique elements as Class10
       2164
b'1'
        253
Name: count, dtype: int64
Class11 has unique elements as Class11
h'0'
        2128
b'1'
        289
Name: count, dtype: int64
Class12 has unique elements as Class12
b'1'
        1816
b'0'
        601
Name: count, dtype: int64
Class13 has unique elements as Class13
b'1'
       1799
b'0'
        618
Name: count, dtype: int64
Class14 has unique elements as Class14
b'0'
        2383
b'1'
         34
Name: count, dtype: int64
```

3. Label Selection for Visualization

The columns were present in the format b'O' or b'1', so that had to be cleaned and replaced.

```
feature cols = [col for col in df.columns if col.startswith('Att')]
label_cols = [col for col in df.columns if col.startswith('Class')]
for col in label cols:
    df[col] = df[col].apply(lambda x: int(x.decode('utf-8')) if isinstance(x, bytes) else int(x))
Y = df[label_cols]
print("Label matrix shape:", Y.shape)
print("Sample:\n", Y.head())
Label matrix shape: (2417, 14)
Sample:
    Class1 Class2 Class3 Class4 Class5 Class6 Class7 Class8 Class9 \
0
        0
                0
                        0
                                0
                                         0
                                                 0
                                                                         0
                                                                 1
                                         0
                                                                          0
        0
                0
                                                 0
1
                        1
                                1
2
                                0
                                         0
                                                         0
                                                                 0
                                                                         0
        0
                1
                        1
                                                 0
3
        0
                0
                        1
                                1
                                         0
                                                 0
                                                         0
                                                                 0
                                                                         0
4
        0
                0
                        1
                                1
                                         1
                                                 1
                                                                          0
   Class10 Class11 Class12 Class13
                                        Class14
0
         a
                  a
                           1
                                    1
                                              a
                  0
                           0
                                    0
                                              0
1
2
                  0
                           1
                                              0
                  0
                                              0
4
         0
                  0
                           0
                                    0
                                              0
```

```
label_counts = Y.sum(axis=1)
single_label_rows = Y[label_counts == 1]
multi_label_rows = Y[label_counts > 1]
single_label_counts = single_label_rows.sum(axis=0).sort_values(ascending=False)
print("The single label plots are:\n", single_label_counts)
top_two_single_labels = single_label_counts.head(2).index.tolist()
print("Top 2 single-label classes:", top_two_single_labels)
The single label plots are:
Class1
            32
Class2
            0
Class3
            0
Class4
Class5
Class6
            0
Class7
Class8
Class9
```

```
Class10 0
Class11 0
Class12 0
Class13 0
Class14 0
dtype: int64
Top 2 single-label classes: ['Class1', 'Class2']
```

Thuis, we see that Single Class samples belong to only Class 1. The top 2 classes can be taken as 1 and any other, for ease we choose 2 here.

```
multi label combinations = multi label rows.apply(
    lambda row: tuple(row.index[row == 1]), axis=1
most_common_combo = multi_label_combinations.value_counts().idxmax()
print("5 most common combinations are:\n", multi_label_combinations.value_counts()[:5])
print("Most frequent multi-label combination:", most_common_combo)
5 most common combinations are:
 (Class3, Class4, Class12, Class13)
                                      237
(Class4, Class5, Class12, Class13)
                                      233
(Class1, Class2, Class12, Class13)
                                      172
(Class1, Class2)
(Class2, Class3, Class12, Class13)
                                     117
Name: count, dtype: int64
Most frequent multi-label combination: ('Class3', 'Class4', 'Class12', 'Class13')
```

```
def categorize row(row):
    active_labels = [lbl for lbl in label_cols if row[lbl] == 1]
    if len(active_labels) == 1:
        if active_labels[0] == top_two_single_labels[0]:
            return f"Single_{top_two_single_labels[0]}
        elif active_labels[0] == top_two_single_labels[1]:
            return f"Single_{top_two_single_labels[1]}'
    if tuple(active_labels) == most_common_combo:
        return "Multi_Common"
    return "Other"
df['viz_label'] = Y.apply(categorize_row, axis=1)
print("\nVisualization Label Distribution:\n", df['viz_label'].value_counts())
Visualization Label Distribution:
viz_label
Other
                 2148
Multi_Common
                 237
Single_Class1
                  32
Name: count, dtype: int64
```

Now the label selection for visualization has been done. Moving on to the standardization of the data part.

Dimensionality reduction techniques such as t-SNE and Isomap rely heavily on pairwise distances (Euclidean or geodesic) between data points to uncover meaningful low-dimensional structures. If features are not on a similar scale, features with larger numerical ranges will dominate the distance computations, leading to biased or misleading embeddings.

4. Scaling

```
X = df[feature_cols].values
scaler = StandardScaler()
X_scaled = scaler.fit_transform(X)

print("Mean of standardized features :", X_scaled.mean(axis=0).mean(), " which is approximately 0. ")
print("Std of standardized features :", X_scaled.std(axis=0).mean())

Mean of standardized features : 1.1987417163186414e-18 which is approximately 0.
Std of standardized features : 1.0
```

Part B: t-SNE and Veracity Inspection

1. t-SNE Implementation

```
X_{emb_input} = X_{scaled}
labels_for_color = df['viz_label']
perplexities = [5, 30, 50]
fig, axes = plt.subplots(1, 3, figsize=(18, 6))
for ax, perp in zip(axes, perplexities):
    tsne = TSNE(n_components=2, perplexity=perp, random_state=42, init='pca')
    X_tsne = tsne.fit_transform(X_emb_input)
    sns.scatterplot(
         x=X_tsne[:, 0],
         y=X_tsne[:, 1],
         hue=labels_for_color,
         palette="tab10",
         s=20,
         alpha=0.8,
         ax=ax
    ax.set_title(f"t-SNE Visualization (Perplexity = {perp})")
    ax.legend(bbox_to_anchor=(1.05, 1), loc='upper left')
plt.tight_layout()
plt.show()
                                                                                                         t-SNE Visualization (Perplexity = 50)
      t-SNE Visualization (Perplexity = 5)
                                                       t-SNE Visualization (Perplexity = 30)
                                       Multi Commo
                                                                                         Multi Commor
                                                                                                                                          Multi Common

    Multi_co...
    Single_Class1

                                       Single Class1
```

Now, we have to figure out which value of perplexity is the most optimal for our dataset.

```
labels_for_color = df['viz_label']
X_{emb_input} = X_{scaled}
perplexities = np.linspace(5, 50, 10)
for i in range(len(perplexities)):
   perp = perplexities[i]
    tsne = TSNE(n_components=2, perplexity=perp, random_state=42, init='pca')
    X_tsne = tsne.fit_transform(X_emb_input)
   sil_score = silhouette_score(X_tsne, labels_for_color)
    print(f"Perplexity: {perp}, Silhouette Score: {sil_score}")
    print(perp, tsne.kl_divergence_)
Perplexity: 5.0, Silhouette Score: -0.10062385350465775
5.0 2.04784893989563
Perplexity: 10.0, Silhouette Score: -0.09379613399505615
10.0 2.225541353225708
Perplexity: 15.0, Silhouette Score: -0.04202289134263992
15.0 2.2599754333496094
Perplexity: 20.0, Silhouette Score: -0.08609097450971603
20.0 2.2383103370666504
Perplexity: 25.0, Silhouette Score: -0.05814149230718613
25.0 2.2043683528900146
Perplexity: 30.0, Silhouette Score: -0.05727535858750343
30.0 2.182413101196289
Perplexity: 35.0, Silhouette Score: -0.07789736241102219
35.0 2.157132863998413
Perplexity: 40.0, Silhouette Score: -0.0806664526462555
40.0 2.1263887882232666
Perplexity: 45.0, Silhouette Score: -0.08686140179634094
```

```
45.0 2.097517728805542
Perplexity: 50.0, Silhouette Score: -0.09558380395174026
50.0 2.0777950286865234
```

Perplexity Selection and Evaluation

To quantitatively determine an appropriate perplexity for t-SNE, I evaluated a range of values between 5 and 50, computing both the Silhouette Score (cluster separation) and KL Divergence (embedding loss).

Perplexity	Silhouette Score	KL Divergence	
5	-0.1006	2.048	
10	-0.0938	2.226	
15	-0.0420	2.260	
20	-0.0861	2.238	
30	-0.0573	2.182	
40	-0.0807	2.126	
50	-0.0956	2.078	

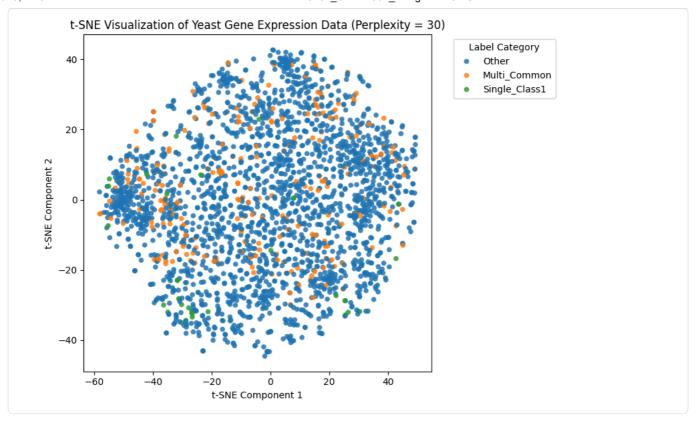
The Silhouette Score peaked around perplexity = 15, indicating relatively better separation between functional categories, while KL divergence decreased for larger perplexities, suggesting improved global consistency.

Hence, a moderate perplexity of 15-30 provides a balanced trade-off between local clustering fidelity and global structure preservation, making it a suitable choice for subsequent visualizations.

Thus, we are taking the optimal value as 30 as a tradeoff between KL divergence and Silhouetter Score.

2. Visualization

```
tsne_final = TSNE(n_components=2, perplexity=30, random_state=42, init='pca')
X_tsne_final = tsne_final.fit_transform(X_scaled)
tsne_df = pd.DataFrame({
    'TSNE1': X_tsne_final[:, 0],
    'TSNE2': X tsne final[:, 1],
    'viz_label': df['viz_label']
plt.figure(figsize=(8, 6))
sns.scatterplot(
   data=tsne_df,
    x='TSNE1', y='TSNE2',
   hue='viz_label',
   palette='tab10',
   s=30, alpha=0.85, edgecolor='none'
plt.title("t-SNE Visualization of Yeast Gene Expression Data (Perplexity = 30)")
plt.xlabel("t-SNE Component 1")
plt.ylabel("t-SNE Component 2")
plt.legend(title='Label Category', bbox_to_anchor=(1.05, 1), loc='upper left')
plt.tight_layout()
plt.show()
```



3. Veracity Inspection

The 2D t-SNE plot above shows the embedding of yeast gene expression data, colored according to a simplified class index (Single_Class1), Multi_Common, Other). From the plot, several data veracity issues can be visually identified:

1. Noisy / ambiguous

Observation: There are a few green points (Single_Class1) and orange points (Multi_Common) that are deeply embedded within the large blue cluster (Other).

Interpretation: These points likely correspond to **noisy or ambiguous labels**, where the assigned functional category does not match the local neighborhood of similar gene expression profiles. Possible reasons include:

- · Multi-functional genes being misclassified as a single class.
- · Experimental or annotation errors in labeling.

Implication: A classifier would receive conflicting signals for these points, potentially reducing overall accuracy in these locregions.

2. Outliers

Observation: A few points are isolated or located far away from the main mass of points, forming tiny distant clusters.

Interpretation: These represent outliers in the gene expression data. Potential causes include:

- Experimental noise or rare measurement errors.
- Extreme biological conditions or unusual gene expression patterns.

Implication: Outliers can distort distance-based models and complicate classification boundaries, making robustdeling more challenging.

3. Hard-to-Learn Samples

Observation: Some regions in the plot show **heavy mixing of colors**, particularly where orange (Multi_Common) points overlap with blue (Other) points.

Interpretation: These areas correspond to **hard-to-learn samples**, where the feature space does not provide clear separation between classes. Biologically, these genes may have **overlapping functional roles** or similar expression patterns.

Implication: Simple classifiers (like linear models) would likely struggle here, as the decision boundaries are complex and non-linear. More sophisticated models or additional feature engineering would be required distinguish these samples accurately.

Summary Table

Issue	Visual Signature	Possible Cause		
Noisy/Ambiguous Labels	Points of one color embedded in another cluster	Mislabeling or multi-functional genes	Conflic	tin
Outliers	Isolated or distant points	Rare biological conditions or experimental noise	1	ed
Hard-to-Learn Samples	Mixed-color dense regions	Overlapping gene functions sections consistently formatted. Do you want me to do that next?		

Part C: Isomap and Manifold Learning

1. Isomap Implementation

```
isomap = Isomap(n_components=2, n_neighbors=10)
X_isomap = isomap.fit_transform(X_scaled)

isomap_df = pd.DataFrame({
    'ISOMAP1': X_isomap[:, 0],
    'ISOMAP2': X_isomap[:, 1],
    'viz_label': df['viz_label']
})
```

Fundamental Difference Between Isomap and t-SNE

Isomap focuses on preserving the global structure of the data. It computes geodesic distances (shortest paths along the data manifold) between all pairs of points, ensuring that far-apart relationships and overall manifold shape are retained in the lower-dimensional space.

In contrast, t-SNE emphasizes preserving the local structure — it models pairwise similarities so that nearby points in the high-dimensional space remain close in the embedding, while distant points are less constrained.

Thus, Isomap is better for revealing broad manifold geometry, whereas t-SNE excels at uncovering fine-grained local clusters.

Aspect	t-SNE	Isomap
Preserves	Local neighborhood structure (focuses on nearby points)	Global manifold geometry (considers long-range relationships)
Distance Metric	Probabilistic similarity (conditional probabilities)	Geodesic distances along the manifold
Strength	Highlights fine-grained clusters, local separability	Retains large-scale topology, continuous manifolds
Weakness May distort global layout (clusters may appear arbitrarily spaced)		Sensitive to noise/outliers; struggles if manifold is not well-connected
Best for Cluster analysis, local density visualization		Understanding global data continuity or manifold shape

Visualization

```
plt.figure(figsize=(8, 6))
sns.scatterplot(
    data=isomap_df,
    x='ISOMAP1', y='ISOMAP2',
    hue='viz_label',
    palette='tab10',
    s=30, alpha=0.85, edgecolor='none'
)
plt.title("Isomap Visualization of Yeast Gene Expression Data (n_neighbors = 10)")
plt.xlabel("Isomap Component 1")
plt.ylabel("Isomap Component 2")
plt.legend(title='Label Category', bbox_to_anchor=(1.05, 1), loc='upper left')
plt.tight_layout()
plt.show()
```

Isomap Visualization of Yeast Gene Expression Data (n_neighbors = 10)

3. Comparison and Curvature Analysis

Comparison of Isomap vs. 1-SNE



In the context of the yeast gene expression data, Isomap tends to better preserve the global structure of the data, revealing how different clusters relate to each other in the overall manifold. It captures smooth transitions between functional categories, indicating potential biological relationships among gene functions. On the other hand, t-SNE emphasizes local relationships, creating well-separated clusters for nearby points but often distorting large, scale distances. Hence, while t-SNE provides clearer local groupings, Isomap gives a more coherent picture of the entire data topology and inter-cluster connectivity.

Data Manifold and Curvature

The Isomap visualization suggests that the gene expression data likely lies on a highly curved and complex manifold. This curvature reflects nonlinear dependencies among genes — for example, co-expression patterns that vary across multiple biological pathways. A highly curved manifold means that a simple linear classifier would struggle, as decision boundaries would need to adapt to these