

Practical assignment 2

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Goal

 Develop a basic probabilistic constituency parser for French that is based on the CYK algorithm and the PCFG model and that is robust to unknown words

- Two parts in this introductory talk to the assignment
 - The Levenshtein edit distance algorithm (and a few words on spelling correction in general)
 - The CYK algorithm
- Both are based on dynamic programming, and share underlying ideas

Spelling correction and edit distance

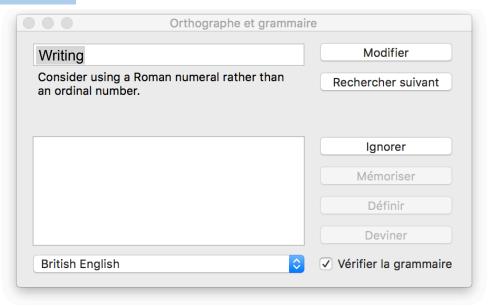


Spelling correction

- Two main application types:
 - Writign assistance

Spelling correction

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 - Writign assistance



Spelling correction

- Two main application types:
 - Writing assistance
 - Correction of texts before NLP processing
- Two subtasks:
 - Spelling error detection
 - Maybe the hardest subtask, because many erroneous spellings produce existing words!
 - Spelling error correction
 - Autocorrect: hte -> the
 - Suggested correction
 - Suggested list of possible corrections (sorted)

Types and rates

Types:

- Non-word errors (easy to detect with a large lexicon)
 vs. real-word errors (harder to detect)
- Typographical errors vs. "Cognitive" errors
- Lexical errors vs. Grammatical errors

• Rates:

- 26%: Web queries (Wang et al. 2003)
- 13%: Retyping, no backspace (Whitelaw et al. on English & German)
- 7%: Words corrected retyping on phone-sized "organiser"
- 2%: Words uncorrected on "organiser" (Soukoreff and MacKenzie 2003)
- 1-2%: Retyping (Kane and Wobbrock 2007, Gruden et al. 1983)

A non-word example

acress

Edit distance

- Creating candidate corrections
- Damereau-Levenshtein distance = minimal distance between two strings, based on a closed inventory of possible operations:
 - insertion of a character
 - deletion of a character
 - substitution of a character with another one
 - swap (transposition) between two adjacent characters
- Computed using dynamic programming
 - We fill a matrix whose (*i*,*j*) element stores the minimum number of operations needed to produce the *j*-prefix $w'_0 \dots w'_j$ of the target word from the *i*-prefix $w_0 \dots w_i$ of the source word

Levenshtein distance

```
LEVENSHTEINDISTANCE(s_1, s_2)

1 for i \leftarrow 0 to |s_1|

2 do m[i, 0] = i

3 for j \leftarrow 0 to |s_2|

4 do m[0, j] = j

5 for i \leftarrow 1 to |s_1|

6 do for j \leftarrow 1 to |s_2|

7 do if s_1[i] = s_2[j]

8 then m[i, j] = \min\{m[i-1, j]+1, m[i, j-1]+1, m[i-1, j-1]\}

9 else m[i, j] = \min\{m[i-1, j]+1, m[i, j-1]+1, m[i-1, j-1]+1\}

10 return m[|s_1|, |s_2|]

Operations: insert (cost 1), delete (cost 1), replace (cost 1)
```

On our non-word example

Words at a distance 1 from acress

Error	Candidate	Correct	Error	Туре
	Correction	Letter	Letter	
acress	actress	t	-	deletion
acress	cress	_	a	insertion
acress	caress	ca	ac	transposition
acress	access	С	r	substitution
acress	across	0	е	substitution
acress	acres	_	S	insertion
acress	acres	-	S	insertion

Edit distance and spelling errors

- 80% of errors are within edit distance 1
 - Almost all errors within edit distance 2
- We must also allow insertion of space or hyphen
 - thisidea -> this idea
 - inlaw -> in-law

anagement maagement maanagement
maangement magement magement
mamagement mamangement management management
management management management management
management management management managemenet
management managemet management management management
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management management management management
manament manamgement management management
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Candidate generation

Several options:

- 1. Run through dictionary, check edit distance with each word
- 2. Generate all words within edit distance $\leq k$ (e.g. k = 1 or 2) and then intersect them with dictionary
- 3. Use a character *k*-gram index and find dictionary words that share "most" *k*-grams with word
- Compute them fast with a Levenshtein finite state transducer
- 5. Have a precomputed hash of words to possible corrections

Refinement: weighted operations

sub[X, Y] = Substitution of X (incorrect) for Y (correct)

X												Y	(co	rrect))	/		_ \		,						
	a	b	c	d	e	f	g	h	i	j	k	1	m	n	0	p	q	r	S	t	u	v	w	х	У	Z
a	0	0	7	1	342	0	0	2	118	0	1	0	0	3	76	0	0	1	35	9	9	0	1	0	5	0
b	0	0	9	9	2	2	3	1	0	0	0	5	11	5	0	10	0	0	2	I	0	0	8	0	0	0
c	6	5	0	16	0	9	5	0	0	0	1	0	7	9	1	10	2	5	39	40	1	3	7	1	1	0
d	1	10	13	0	12	0	5	5	0	0	2	3	7	3	0	1	0	43	30	22	0	0	4	0	2	0
e	388	0	3	11	0	2	2	0	89	0	0	3	0	5	93	0	0	14	12	6	15	0	1	0	18	0
f	0	15	0	3	1	0	5	2	0	0	0	3	4	1	0	0	0	6	4	12	0	0	2	0	0	0
g	4	1	11	11	9	2	0	0	0	1	1	3	0	0	2	1	3	5	13	21	0	0	1	0	3	0
h	1	8	0	3	0	0	0	0	0	0	2	0	12	14	2	3	0	3	1	11	0	0	2	0	0	0
i	103	0	0	0	146	0	1	0	0	0	0	6	0	0	49	0	0	0	2	1	47	0	2	1	15	0
j	0	1	1	9	0	0	1	0	0	0	0	2	1	0	0	0	0	0	5	0	0	0	0	0	0	0
k	1	2	8	4	1	1	2	5	0	0	0	0	5	0	2	0	0	0	6	0	0	0	. 4	0	0	3
1	2	10	1	4	0	4	5	6	13	0	1	0	0	14	2	5	0	11	10	2	0	0	0	0	0	0
m	1	3	7	8	0	2	0	6	0	0	4	4	0	180	0	6	0	0	9	15	13	3	2	2	3	0
n	2	7	6	5	3	0	1	19	1	0	4	35	78	0	0	7	0	28	5	7	0	0	1	2	0	2
0	91	1	1	3	116	0	0	0	25	0	2	0	0	0	0	14	0	2	4	14	39	0	0	0	18	0
P	0	11	1	2	0	6	5	0	2	9	0	2	7	6	15	0	0	1	3	6	0	4	1	0	0	0
q	0	0	1	0	0	0	27	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
r	0	14	0	30	12	2	2	8	2	0	5	8	4	20	1	14	0	0	12	22	4	0	0	1	0	0
s	11	8	27	33	35	4	0	1	0	1	0	27	0	6	l	7	0	14	0	15	0	0	5	3	20	1
t	3	4	9	42	7	5	19	5	0	1	0	14	9	5	5	6	0	11	37	0	0	2	19	0	7	6
u	20	0	0	0	44	0	0	0	64	0	0	0	0	2	43	0	0	4	0	0	0	0	2	0	8	0
v	0	0	7	0	0	3	0	0	0	0	0	1	0	0	1	0	0	0	8	3	0	0	0	0	0	0
w	2	2	I	0	1	0	0	2	0	0	1	0	0	0	0	7	0	6	3	3	1	0	0	0	0	0
X.	0	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9	0	0	0	0	0	0	0
У	0	0	2	0	15	0	l	7	15	0	0	0	2	0	6	1	0	7	36	8	5	0	0	1	0	0
z	0	0	0	7	0	0	0	0	0	0	0	7	5	0	0	0	0	2	21	3	0	0	0	0	3	0

(Kernighan, Church, Gale 1990)

Refinement: weighted operations

- Such data makes it possible to compute substitution probabilities
- Can be generalised to all 4 types of operations
 - Use add-1 smoothing to allow for unseen operations

> Channel model

Candidate	Correct	Error	xlw	P(xlword)
Correction	Letter	Letter		
actress	t	-	c ct	.000117
cress	-	a	a #	.00000144
caress	ca	ac	ac ca	.00000164
access	С	r	r c	.000000209
across	0	е	e o	.0000093
acres	-	S	es e	.0000321
acres	-	S	ss s	.0000342

- Noisy channel approach: multiply channel model by language model
- We want to prefer more frequent output tokens
 - Simplest idea: unigram probability

Candidate	Correct	Error	xlw	P(xlword)	P(word)	10 ⁹ *P(xlw)P(w)
Correction	Letter	Letter				
actress	t	-	c ct	.000117	.0000231	2.7
cress	_	a	a #	.00000144	.000000544	.00078
caress	ca	ac	ac ca	.00000164	.00000170	.0028
access	С	r	r c	.000000209	.0000916	19
across	0	е	e o	.0000093	.000299	2.8
acres	_	S	es e	.0000321	.0000318	1.0
acres	-	S	ss s	.0000342	.0000318	1.0

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- Better: incorporating context
 - Simplest way: bigram language model
 - Better: with linear interpolation with unigram model to avoid unseen bigrams $P_{li}(w_k | w_{k-1}) = \lambda.P_{uni}(w_k) + (1-\lambda).P_{mle}(w_k | w_{k-1}) \\ (\text{where } P_{mle}(w_k | w_{k-1}) = \#(w_k | w_{k-1}) / \# w_{k-1}) \text{ is called the maximum likelihood estimate)}$
 - The model can also be smoothed (e.g. add-1)
- Imagine the following context for our example:

a stellar and versatile acress whose combination of sass and glamour...

 Counts from the Corpus of Contemporary American English with add-1 smoothing

```
• P(actressIversatile)=.000021   P(whoselactress) = 0.0010   P(acrossIversatile) =.000021   P(whoselacross) = 0.000006   P("versatile actress whose") = .000021 x .0010 = 210.10^{-10}   P("versatile across whose") = .000021 x .000006 = 1.10^{-10}
```

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```

The best correction is "actress"!

Real-word errors

- Much harder to detect
- Are they frequent?
 - 25-40% of spelling errors are real words (Kukich 1992)
 - More real-word errors in content produced on smartphones since the generalisation of semi-automatic correction
- General idea:
 - Guess which words could be errors
 - Produce candidates but include the original word amongst them
 - Homophones are important (phonetisation)
 - Choose best candidate with noisy channel model

The CYK algorithm



Classical CFG parsing algorithms

- Programming languages are defined by CFGs that are not ambiguous
 - Algorithms for non-ambiguous ("deterministic")
 CFGs are relatively simple (LR, LALR...)
- Natural language is ambiguous. This resulted in the development of algorithms for parsing general (i.e. not only deterministic) CFGs
 - · CYK
 - Earley
 - GLR

A membership problem

- The basic Cocke–Younger–Kasami, a.k.a. CYK (sometimes CKY) algorithm, solves a **membership problem**: it is not a parsing algorithm *per se*
 - An implementation of the CYK algorithm is a recogniser, not a parser
 - But it can easily be adapted to become a parsing algorithm
- The membership problem is simple: given an CFG and an input string, answer the following question:
 - Is the input string in the language defined by the CFG?
- The CFG must be in **Chomsky normal form**, i.e. all rewriting rules are of one of the following forms:
 - $S \longrightarrow AB$
 - S → a
 - $S \longrightarrow \epsilon$
- It is a bottom-up algorithm based on dynamic programming

Basic idea

- Iterative algorithm
- Let $u = x_1 x_2 ... x_n$ be a string to be tested for membership
 - Step 1: For each substring of u of length 1, find the set $\mathcal{S}_{i-1,i}$ of non-terminals A with a rule A $\longrightarrow x_i$
 - Step 2: for each substring $x_i x_{i+1}$ of u of length 2 find the set $\mathcal{S}_{i-1,i+1}$ of variables A that derives A $\longrightarrow x_i x_{i+1}$
 - . . .
 - Step n: for the whole string $u = x_1 x_2 ... x_n$, find the set $\mathcal{S}_{0,n}$ of variables A that derives A $\longrightarrow x_1 x_2 ... x_n$
 - Iff $S_{0,n}$ contains the axiom S, then u is in the language defined by the grammar.

Diagonal table

\$0,4			
\$0,3	S 1,4		
\$0,2	S 1,3	\$2,4	
\$0,1	S 1,2	\$2,3	S 3,4
<i>W</i> ₁	W ₂	<i>W</i> ₃	<i>W</i> 4

 $S \rightarrow AB$

 $A \rightarrow CC \mid a \mid c$

 $B \rightarrow BC \mid b$

\$ 0,4			
\$ 0,3	S 1,4		
\$0,2	S 1,3	S 2,4	
S _{0,1}	S 1,2	S 2,3	S 3,4
С	b	b	a

\$ 0,4			
\$ 0,3	S 1,4		
\$ 0,2	S 1,3	\$ 2,4	
{A,C}	{B}	{B}	{A}
С	b	р	a

 $S \rightarrow AB$

 $A \rightarrow CC \mid a \mid c$

 $B \rightarrow BC \mid b$

\$ 0,4			
\$ 0,3	S 1,4		
S 0,2	S 1,3	S _{2,4}	
\$0,1	S 1,2	S 2,3	S 3,4
С	b	b	a

\$ 0,4			
\$ 0,3	S 1,4		
{S,C}	S 1,3	\$ 2,4	
{A,C}	{B}	{B}	{A}
С	b	b	a

 $S \rightarrow AB$

 $A \rightarrow CC \mid a \mid c$

 $B \rightarrow BC \mid b$

\$ 0,4			
\$ 0,3	S 1,4		
\$0,2	S 1,3	S _{2,4}	
\$0,1	S 1,2	S 2,3	\$ 3,4
С	b	b	a

\$ 0,4			
\$ 0,3	S 1,4		
{S,C}	Ø	\$ 2,4	
{A,C}	{B}	{B}	{A}
С	b	b	a

 $S \rightarrow AB$

 $A \rightarrow CC \mid a \mid c$

 $B \rightarrow BC \mid b$

S 0,4			
\$ 0,3	S 1,4		
S 0,2	S 1,3	S 2,4	
\$0,1	S 1,2	S 2,3	S 3,4
С	b	b	а

\$ 0,4			
\$ 0,3	S 1,4		
{S,C}	Ø	{C}	
{A,C}	{B}	{B}	{A}
С	b	b	а

 $S \rightarrow AB$

 $A \rightarrow CC \mid a \mid c$

 $B \rightarrow BC \mid b$

\$ 0,4			
\$ 0,3	S 2,4		
\$ 0,2	S 1,3	S _{2,4}	
\$0,1	S 1,2	S 2,3	S 3,4
С	b	b	a

\$ 0,4			
{C}	S 1,4		
{S,C}	Ø	{C}	
{A,C}	{B}	{B}	{A}
С	b	b	а

 $S \rightarrow AB$

 $A \rightarrow CC \mid a \mid c$

 $B \rightarrow BC \mid b$

\$ 0,4			
\$ 0,3	S 1,4		
\$ 0,2	S 1,3	S _{2,4}	
\$0,1	S 1,2	S 2,3	S 3,4
С	b	b	а

\$ 0,4			
{C}	{B}		
{S,C}	Ø	{C}	
{A,C}	{B}	{B}	{A}
С	b	b	a

 $S \rightarrow AB$

 $A \rightarrow CC \mid a \mid c$

 $B \rightarrow BC \mid b$

\$ 0,4			
\$ 0,3	S 1,4		
\$ 0,2	S 1,3	S _{2,4}	
\$ 0,1	S 1,2	S 2,3	S 3,4
С	b	b	а

{S,A,C}			
{C}	{B}		
{S,C}	Ø	{C}	
{A,C}	{B}	{B}	{A}
С	b	b	а

 $S \rightarrow AB$

 $A \rightarrow CC \mid a \mid c$

 $B \rightarrow BC \mid b$

\$ 0,4			
\$ 0,3	S 1,4		
\$0,2	S 1,3	S 2,4	
\$0,1	S 1,2	S 2,3	\$ 3,4
С	b	b	a

{ S ,A,C}	=> the string is	in the language	defined by the CF
{C}	{B}		
{S,C}	Ø	{C}	
{A,C}	{B}	{B}	{A}
С	b	b	а

- We must eliminate:
 - Rules where the start symbol (the axiom) is on the right hand side
 - Rules with non-solitary terminal symbols
 - Rules with right-hand sides with more than 2 nonterminal symbols
 - Unit rules (rules with only 1 non-terminal symbol on the right-hand side)
 - Epsilon-rules (rules with an empty right-hand side)

- Eliminate the start symbol from right-hand sides
 - Introduce a new start symbol S0, and a new rule $S_0 \rightarrow S$

where S is the previous start symbol

- Eliminate rules with non-solitary terminals
 - To eliminate each rule

$$A \rightarrow X_1 \dots a \dots X_n$$

with a terminal symbol a being not the only symbol on the right-hand side, introduce, for every such terminal, a new non-terminal symbol N_a , and a new rule $N_a \rightarrow a$

Change every rule

$$A \rightarrow X_1 \dots a \dots X_n$$

 O
 $A \rightarrow X_1 \dots N_a \dots X_n$

• If several terminal symbols occur on the right-hand side, simultaneously replace each of them by its associated non-terminal symbol.

Eliminate right-hand sides with more than 2 non-terminals

```
• Replace each rule A \to X_1 \ X_2 \ ... \ X_n with more than 2 nonterminals X_1,...,X_n by rules A \to X_1 \ A_1, A_1 \to X_2 \ A_2, ..., A_{n-2} \to X_{n-1} \ X_n, where A_i are new non-terminal symbols.
```

Eliminate unit rules

• A unit rule is a rule of the form

$$A \rightarrow B$$

where A, B are non-terminal symbols. To remove it, for each rule $B \rightarrow X_1 \dots X_n$,

where $X_1 \dots X_n$ is a string of non-terminals and terminals, add rule $A \rightarrow X_1 \dots X_n$

unless this is a unit rule which has already been (or is being) removed.

 For more details, simply go to Wikipedia (on which both previous slides are based):

https://en.wikipedia.org/wiki/Chomsky_normal_form

NLP practical assignment (TD2)



Goal and instructions

- Develop a basic probabilistic parser for French that is based on the CYK algorithm and the PCFG model and that is robust to unknown words
- You will extract a PCFG from the training corpus provided, made of:
 - a probabilistic context-free grammar whose terminals are part-of-speech tags
 - a probabilistic lexicon, i.e. triples of the form (token, part-of-speech tag, probability) such that the sum of the probabilities for all triples for a given token sums to 1.
- You will reimplement the CYK algorithm, adapting it a bit in two ways: (1) to handle the existence of a lexicon; (2) to only retain the most probable way to rewrite an instantiated symbol, in order to directly extract the best (most probable) parse tree for each sentence
- Use the SEQUOIA treebank v6.0 (file in the GitHub, bracketed format):
 - Split it into 3 parts (80% / 10% / 10%)
 - Use the 80% for training (extract CFG rules + learn CFG rule probabilities)
 - Use the first 10% for development purposes (whatever you want to use it for)
 - Use the last 10% for evaluating your parser
 - IMPORTANT: Ignore the functional labels: whenever you find a hyphen in a non-terminal name, ignore it and everything that follows
 E.g.: ((SENT (PP-MOD (P En) (NP (NC 1996))) (PONCT,) (NP-SUJ (DET la) (NC municipalité)) (VN (V étudie)) (NP-OBJ (DET la) (NC possibilité) (PP (P d') (NP (DET une) (NC construction) (AP (ADJ neuve))))) (PONCT.)))

Goal and instructions

- Develop a basic probabilistic parser for French that is based on the CYK algorithm and the PCFG model and that is robust to unknown words
- Your OOV module will assign a (unique) part-of-speech to any token not included in the lexicon extracted from the training corpus.
 - The underlying idea is to assign to an OOV the part-of-speech of a "similar" word.
 - This similarity will be computed as a combination of **formal similarity** (to handle spelling errors) and **embedding similarity** (as measured by cosine similarity, i.e. scalar product between normalised vectors), to handle both spelling errors and genuine unknown words
 - You must design a reasonable way to combine these two similarities.
 - For embedding similarity, you will use the Polyglot embedding lexicon for French https://sites.google.com/site/rmyeid/projects/polyglot
 - See the tutorial with code snippets here: https://nbviewer.jupyter.org/gist/aboSamoor/6046170

Assignment deliverable

- An archive containing your code and a short report
 - See details on the GitHub page of the assignment
- Please respect the instructions given in the assignment description on the GitHub
 - Failure to do so will be penalised

https://github.com/edupoux/MVA 2019 SL/tree/master/TD %232

