

Real-Time Certified Probabilistic Pedestrian Forecasting

Author's Response

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We would like to begin by thanking the reviewers and the editor for their careful reading and review of our paper. The comments provided were incredibly helpful and insightful, and have strengthened the paper considerably. Based on the recommendations of the reviewers and the editor, we have made several modifications to the paper including performing additional analyses with an lstm-based approach and using the Modified Hausdorff Distance metric. These additions pushed the paper beyond the eight page limit. As a result we removed all proofs from the resubmitted manuscript, but have included them instead in a supplementary technical report with our resubmission. This technical report will be posted to our websites if the paper is accepted. The changes made are summarized in detail in the letter below. Following the letter is an annotated version of the paper showing the changes made, followed by the technical report. **This letter is largely self contained, so references here are to the bibliography in this document.**

Reviewer 1

1. **This paper presents a novel real-time probabilistic forecasting method for pedestrian trajectories via observing the historical trajectories in a particular scene. The problem is well motivated, formulated and handled. The reported experimental evaluations show pivotal improvement against the current state-of-the-art.**

Thank you for the positive assessment.

2. **With the current form of the results it is hard to compare the improvements in terms of accuracy gained. This can be overcome by including results such as physical distance between predicted paths and ground truth observations. Such matrices are provided in the baseline models [1] [2] [3] with accuracy values in meters.**

Thank you for the suggestion. The objective of this paper was to develop a predictor that would be effective for use in the autonomous vehicle context. In this instance, to ensure safety it is critical that the generated set of predictions contains the ground-truth observed trajectory while including as few false positive detections as possible. Since the ROC curve plots the true positive rate (i.e. the proportion of the ground truth trajectory that is correctly identified) against the false positive rate (i.e. the proportion of the generated set that does not correspond to the ground truth trajectory), it evaluates this aforementioned safety criteria for autonomous vehicles exactly.

On the other hand the Modified Hausdorff Distance (MHD) from [4] measures the average geometric distance between the ground-truth observed trajectory and the generated set of predictions. Though popular in evaluating the geometric proximity of the ground truth trajectory and a predicted set, it is not the best way to evaluate the utility of an algorithm in the autonomous vehicle context. Specifically consider the instance of a generated set of predictions which does not contain the ground-truth observed trajectory, but is close to the ground-truth trajectory geometrically. If this generated set of predictions was used in the autonomous vehicle context, it would not preclude certain portions of the space which the person occupied. Notice that in this instance the true positive rate would be zero meaning that the generated set of predictions was not useful. Whereas the MHD would describe this generated set of predictions as informative.

Nevertheless, we addressed this concern by adding a comparison to the MHD which is summarized in the Figure 2 below and included in the resubmitted version of our manuscript. Our approach outperforms the methods proposed in [1] and [5] in the intermediate term. At short times, the method described in [5] puts more weight on the direction of the observed trajectory which results in a narrow distribution that is closer to the trajectory. If you look at Figures 3a and 3b, one can observe that the predictions generated using the method in [5] are geometrically closer to the observed trajectory but do not contain it. As a result these predictions are less appropriate in the autonomous vehicle context. At large scales, the approach described in [1] outperforms all others since it is given the endpoint of the trajectory. We have included the following passage to explain both metrics in the revised submission:

#4.4

In our analysis, we sought a metric that evaluated the utility of prediction algorithms in the autonomous vehicle context. In this instance it is critical that the generated set of predictions contains the ground-truth observed trajectory while including as few false positive detections as possible. ROC curves which plot the true positive rate (i.e. the proportion of the ground truth trajectory that is correctly identified) against the false positive rate (i.e. the proportion of the generated set that does not correspond to the ground truth trajectory), evaluate this aforementioned safety criteria for autonomous vehicles exactly. The Area Under the Curve (AUC) is a standard measure of the quality of a predictor. The closer that this AUC is to one, the better the prediction algorithm. Figure 1 shows the analysis of the AUC of each algorithm versus time.

In addition, we evaluated the Modified Hausdorff Distance (MHD) from the ground truth trajectory to a sample from the predictions at each time to provide a geometric measure of how accurate the predictions are. Figure 2 shows MHD plotted against time. Though popular in evaluating the geometric proximity of the ground truth trajectory and a predicted set, it is not the most appropriate way to evaluate the utility of an algorithm in the autonomous vehicle context. Specifically consider the instance of a generated set of predictions which does not contain the ground-truth observed trajectory but is close to the ground-truth trajectory geometrically. If this generated set of predictions was used in the autonomous vehicle context, it would not preclude certain portions of the space where the person was occupying. Notice that the true positive rate would be zero meaning that the generated set of predictions was not useful. Whereas the MHD would describe this generated set of predictions as informative.

3. How the model can incorporate the interactions among pedestrians (i.e group motion) and the influences from neighbouring pedestrians (for instances such as collision avoidance)?

Thank you for this insightful question. Since the focus of this paper was on developing a method to generate predictions at real-time for the autonomous vehicle context, we did not

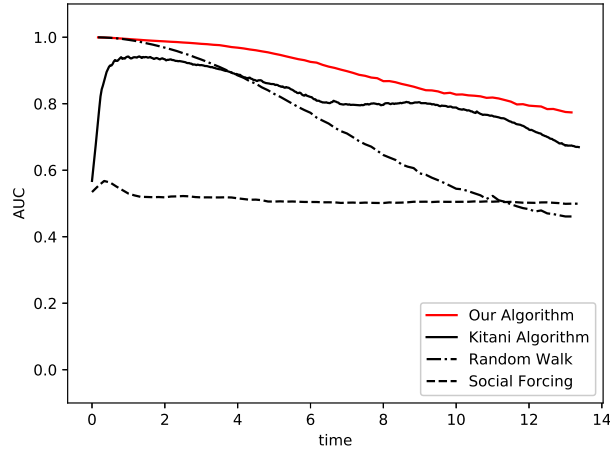


Figure 1: A comparison of the AUC of the various algorithms. Note that the initial dip in the performance of [1] is due to their confidence in their initial estimate. We sampled the S-LSTM [5] model 100 times to organically extract a less concentrated probability distribution from their algorithm, but their confidence combined with the over-reliance on social forces at moderate-to-large timescales lowered their performance.

#4.7

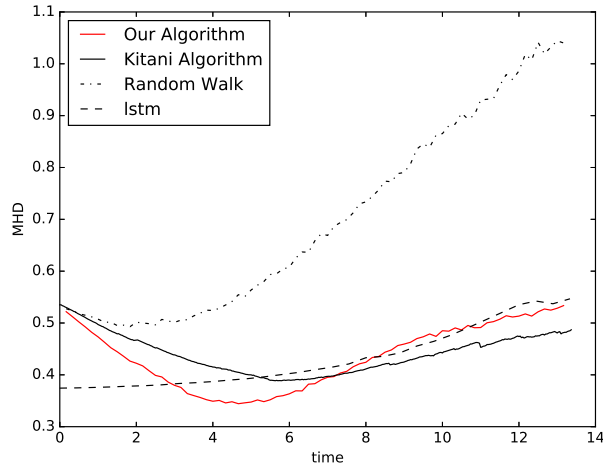


Figure 2: A comparison of the MHD from the ground truth of the pedestrian to a 1000 point samples from each distribution. The method from [5] does well at short time scales since it places a highly confident distribution at the given initial position of the pedestrian, but the method developed in this paper outperforms all others at intermediate times. At longer timescales the MHD to the trajectory of most algorithms converges. [1], which requires the end point of each trajectory, outperforms all other algorithms which assume that the end point of the trajectory is unknown.

#4.8

consider the effect of incorporating interactions between predictions. However, social forces are a natural avenue for future work, and so we included the following paragraph in the paper:

#5.1

Social forces can be incorporated into this model by including a social force F_i acting on the i th agent by letting $\ddot{x}_i = s^2 DX(x) \cdot X(x) + F_i$. Usually $F_i = \sum_j \nabla U(x_j - x_i)$ where U is an interaction potential [6]. The algorithms for generating real-time predictions would then generalize to this definition.

4. **Presentation and organisation The motivation behind choosing start/end points based clustering is not clear. Does clustering based on start/end points help to identify different motion models? Isn't it better to cluster considering the entire trajectory?**

Thank you for this relevant question. As stated in [7], the choice of clustering technique is not nearly as important as the distance metric. Our success with distance functions that took a whole trajectory was limited on the data we tested and we found more success using a custom distance metric that only considered the start and end points of a trajectory as we describe in Comment 6 to Reviewer 1. We have several hypotheses as to why this is true. For one, the spatial scale of the data we test against showcases important features (e.g. curb cuts and storefronts), which lead to clustered start points and end points. Similarly, we tested against high quality data in which trajectories with irreconcilable occlusions were rare and thus could be omitted.

5. **Do you cluster different scenes provided in campus dataset [5] (i.e Valley, Fangron) separately or all together? When motion models are learnt, are they learnt in scene specific manner or altogether?**

Thank you for noticing that this is unclear. Our algorithm trains on each scene independently, so clustering, vector field learning, and learning the potential functions are all done for each scene separately. To make this more clear, we added the following text to the paper:

#4.2

We performed a 2-fold cross validation by using 20% of the data for testing and the remainder for training within each scene. We learned separate collections of vector fields and model parameters for each fold on all of the four scenes on which we tested.

6. **The motivation behind choosing the affinity propagation clustering algorithm is not clearly stated. What is the distance measure used (i.e Euclidian) ? Not specifying such information makes reproduction of this work not feasible.**

This was an oversight on our part, thank you for noticing it. The distance used is a custom distance function. Let one trajectory A start at $(x_{A,start}, y_{A,start})$ and end at $(x_{A,end}, y_{A,end})$, and another trajectory B start at $(x_{B,start}, y_{B,start})$ and end at $(x_{B,end}, y_{B,end})$. We define the points $\mathbf{a}_1 = (x_{A,start}, y_{A,start}, x_{A,end}, y_{A,end})$, $\mathbf{a}_2 = (x_{A,end}, y_{A,end}, x_{A,start}, y_{A,start})$, and $\mathbf{b} = (x_{B,start}, y_{B,start}, x_{B,end}, y_{B,end})$. We then define our distance measure as $d(A, B) := \min \{d_e(\mathbf{a}_1, \mathbf{b}), d_e(\mathbf{a}_2, \mathbf{b})\}$, for the euclidean distance d_e in \mathbb{R}^4 . This is designed such that transposing endpoints of a trajectory doesn't matter, and so a trajectory that starts at point A and ends at point B is close to a trajectory that starts at point B and ends at point A. We have included the following clarification:

#4.1

To do this, we use a clustering algorithm on the trajectories using Affinity Propagation [8] and a custom distance measure defined on the endpoints of trajectories. Let one trajectory A start at $(x_{A,start}, y_{A,start})$ and end at $(x_{A,end}, y_{A,end})$, and another trajectory B start at $(x_{B,start}, y_{B,start})$ and end at $(x_{B,end}, y_{B,end})$. We define the points $\mathbf{a}_1 = (x_{A,start}, y_{A,start}, x_{A,end}, y_{A,end})$, $\mathbf{a}_2 = (x_{A,end}, y_{A,end}, x_{A,start}, y_{A,start})$, and $\mathbf{b} = (x_{B,start}, y_{B,start}, x_{B,end}, y_{B,end})$. We then define our distance measure as $d(A, B) := \min \{d_e(\mathbf{a}_1, \mathbf{b}), d_e(\mathbf{a}_2, \mathbf{b})\}$, for the euclidean distance d_e in \mathbb{R}^4 . This function measures the distance between the endpoints irrespective of their ordering, which means that a trajectory that starts from point A and ends at point B will be close to a trajectory that starts from point B and ends at point A. The scale of the datasets we tested on had large enough spatial scale that clustering based on endpoints captured people moving from destination to destination, e.g. from a storefront to the sidewalk at the edge of a scene. On this dataset, distance functions that utilize the entire trajectory such as DTW, LCSS, and PF from [7] and TRACCLUS from [9] did not identify pedestrian intent as well as our method did. While it is unclear why TRACCLUS underperformed on our data, PF, DTW, and LCSS appeared to put trajectories that were very similar for periods of time together even though they had very different intents.

7. **Adequacy of Citation I believe literature review section can be improved using a sub section on social force models, which is extensively applied for pedestrian trajectory forecasting. Helbing and Molnar, 1995; Koppula and Saxena, 2013; Pellegrini et al., 2010; Yamaguchi et al., 2011; Xu et al., 2012; Wang et al. 2008; Hospedales et al. 2009; Emonet et al. 2011; Yi et al. 2015.**

We agree that this adds to the paper, thank you for the suggestion. We added the following section to our literature review to reflect the relevant work:

#1.1

Many authors have approached pedestrian forecasting by deriving their motion model from interactions between pedestrians using physically motivated methods [6, 10]. Several models derive their motion models from [6] by incorporating collision avoidance through an interaction potential [11, 12, 13]. However this method suffers from not planning for other pedestrian positions at future times. Others take optical flow as input [14, 15, 16]. These approaches use variants of Hierarchical Dirichlet Processes on discretized optical flow to determine temporal motifs (i.e. classes of motion within the scene), or on a Markov model. These models are not agent based, and the lack of an explicit motion model limits their predictive power. Recently methods have been developed to predict trajectories by introducing and sampling Anticipatory Temporal Conditional Random Fields which incorporate learned affordances for humans and objects based on observed objectives within the scene [17]. Others create agent-based models based on Gaussian Processes, though they suffer issues when trained on discretized trajectories [18, 19, 20]. Most recently a method using Long Short-Term Memory (lstm) to learn pedestrian motion models without making assumptions about the manner in which agents interact and is the state-of-the-art algorithm for socially based models while also having a rapid computation time [5].

8. **Furthermore a comprehensive review on trajectory clustering algorithms is required. This should be used to motivate the reason of choosing affinity propagation algorithm in section 4. Morris and Trivedi 2009; Giannotti et al. 2007; Lee et al. 2007; Ester et al. 1996**

Thank you for this suggestion and for the list of relevant titles. We included a note about different algorithms as well as a justification for why we chose our metric which is described in Comment 6 to Reviewer 1.

Reviewer 2

1. **Keep the good work going. Interesting approach.**

Thank you for the kind comments.

2. **Need to be clearer and dive a little bit deeper into the technical approach.**

Thank you for this criticism. We strengthened the description of our method for learning the motion model and quantifying the way that we tested our data as is described in our responses to the suggestions by other reviewers.

3. **Need to use and apply more deep learning approaches such as social LSTM or other machine methods.**

Thank you for the suggestion. We hope that we have addressed this criticism by including a review of literature of social motivated models, including S-LSTM, as well as a section on how social factors can be integrated into our model. In addition, we compared our approach against S-LSTM in addition to the method proposed in [1]. We included the visualizations in Figures 3a and 3b, which are also included in our resubmission.

Reviewer 5

1. **It would be more interesting if the authors show whether the prediction algorithm would transfer the learned “knowledge” of forecasting in novel scenes.**

Thank you for your comment. Though this was not the focus of this paper, the low-dimensional parameterization of the vector fields make transfer learning more amenable. As it is, this is an immediate avenue for future work which we describe in the following addition to the text:

#5.2

We also plan to explore transfer learning using scene segmentation, as well as the semantic context descriptors and routing scores to show how vector fields can be transferred to novel scenes. It appears that the low-order parameterization and unit-length vector field of our model, make it amenable to the methods developed in [21].

2. **More statistically result is expected rather than analyzing “four different scenes”, and comparing run-time by “averaged across several agents and scenes” (how many?).**

Thank you for noticing this oversight on our part. We have modified the paper in the passages listed below to clarify the list of scenes we ran in comparison, and how many agents total were run. The set of agents used during evaluation were the same that were used to determine run times. Note that we attempted to compare on all of the scenes in the Stanford Drone Dataset, but the difficulty in getting the other models to converge in a reasonable amount of time prevented us from doing so.

#4.3

Our analysis was conducted on the Coupa, Bookstore, Death Circle, and Gates scenes from the dataset from [3], with a total of 142 trajectories analyzed.

#4.6

The run time per frame for each algorithm was generated using the mean run time for 400 frames, averaged across all of the trajectory data used in the quality analysis.

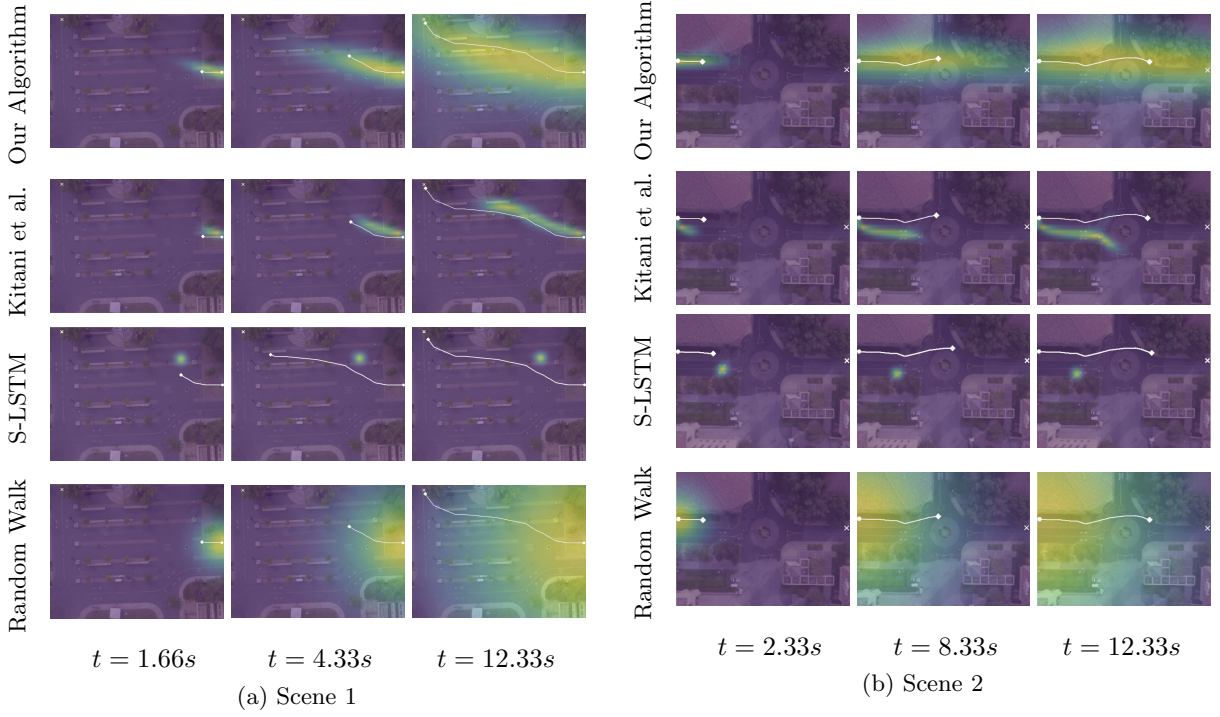


Figure 3: An illustration of the predictions generated by the various algorithms. In this figure, the dot is the start point of the test trajectory, the diamond is the position at time t , and the X is the end of the trajectory. The likelihood of detection is depicted using the viridis color palette. Notice that the Random Walk is imprecise, while the predictions generated by the algorithm in [1] are unable to match the speed of the agent and choose the wrong direction to follow the agent around the circle. The algorithm in [5] is confident and close to the trajectory at small times, but their lack of a motion model causes their prediction to compress into a point at intermediate time scales.

#4.5

3. Besides, it is better to explain the meaning of ROC and AUC in section IV.

This is a necessary clarification, thank you for the suggestion. We have included a description of ROC and AUC, as well as a justification for why we chose to evaluate the methods using this criterion in our response to Comment 2 for Reviewer 1.

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