

Oppg. 1

1. $X \sim N(225, 15^2)$

$$\begin{aligned} (a) \quad P(X > 240) &= P\left(Z > \frac{240 - 225}{15}\right) \\ &= P(Z > 1) \\ &= 1 - P(Z \leq 1) \\ &= 1 - 0.8413 \\ &= 0.1587 \end{aligned}$$

$$\begin{aligned} P(210 < X \leq 240) &= P\left(\frac{210 - 225}{15} < Z \leq 1\right) \\ &= P(-1 < Z \leq 1) \\ &= P(Z \leq 1) - P(Z \leq -1) \\ &= 0.8413 - 0.1587 \\ &= 0.6826 \end{aligned}$$

(b) $Y = \sum_{i=1}^4 X_i$

X_i uavhengig $\Rightarrow Y \sim N(900, 30^2)$

$$\begin{aligned} P(Y > 960) &= P\left(Z > \frac{960 - 900}{30}\right) \\ &= P(Z > 2) \\ &= 1 - P(Z \leq 2) \\ &= 1 - 0.9772 \\ &= 0.0228 \end{aligned}$$

$$P(Y \leq k) = 0.95$$

$$P\left(Z \leq \frac{k - 900}{30}\right) = 0.95$$

$$P(Z \leq \frac{k-900}{30}) = 0.95$$

$$\Rightarrow \frac{k-900}{30} = 1.645$$

$$\Rightarrow \underline{\underline{k = 949.35}}$$