

Conditional Dependency and More INLA

Example (Tokyo rainfall dependency graph)

$$\left. \begin{array}{l} y_t | \tau_t \stackrel{\text{iid}}{\sim} \text{Bin}(n_t, \pi(\tau_t)) \\ \text{for } \pi(\tau_t) = \frac{1}{1 + e^{-\tau_t}} \end{array} \right\} \text{data model}$$

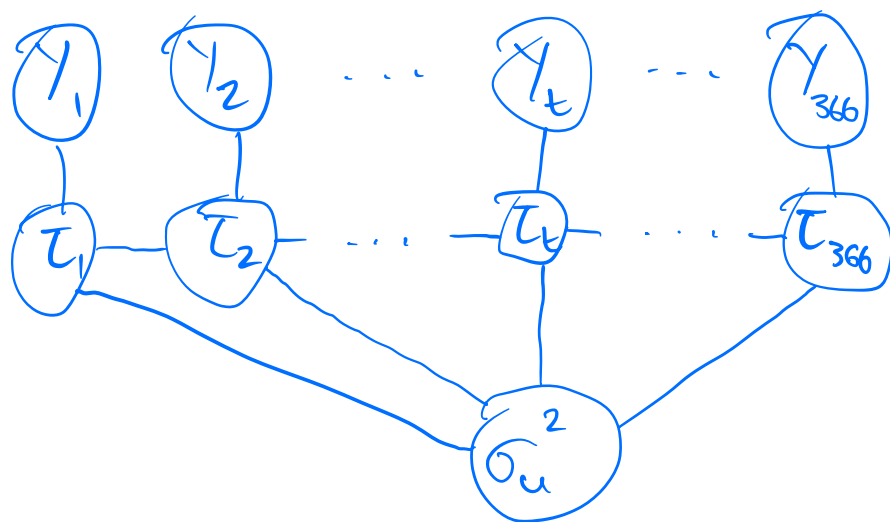
↑ "expit" or "inverse logit" function

$$\left. \begin{array}{l} \tau_t = \tau_{t-1} + u_t, \quad u_t | \sigma_u^2 \stackrel{\text{iid}}{\sim} N(0, \sigma_u^2) \\ t=2, \dots, 366 \\ \sigma_u^2 \sim \text{Inv-Gamma}(\alpha, \beta) \end{array} \right\} \begin{array}{l} \text{latent} \\ \text{model} \\ \text{hyperprior} \end{array}$$

Note: when drawing a conditional dependency graph, we first may need to reparameterize to explicitly state conditional dependencies (particularly for "=" statements).

$$\tau_t | \tau_{t-1}, \sigma_u^2 \sim N(\tau_{t-1}, \sigma_u^2), \quad t=2, \dots, 366$$

Now for the conditional dependency graph:



This represents the model's conditional dependencies.

For example, removing τ_1 , we cannot reach Y_2 from Y_1 . Main idea: Y_1, \dots, Y_{366} are conditionally independent given \vec{Z} .

Note: This idea of paths after removing the conditioning variable representing conditional dependence does not apply when conditioning on the Y_i 's. For more information look up "d-separation".