CISS451: Cryptography

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Chapter 1

Classical ciphers

1.1 Classical ciphers: instructions

- 1. At my website, in the Tutorials section, you'll find latex.pdf. Post LATEX questions in CCCS discord.
- 2. In thispreamble.tex, change AUTHOR and SHORTAUTHOR to your name.
- 3. To speed up compilation, in chap-classical-ciphers.tex, you might want to comment out some sections using %.
- 4. Rewrite the contents of this chapter in your own words, otherwise your book is considered plagiarized. (You probably want to make a copy of this directory.) Note that you need not rewrite the questions in the exercises. You may retain the chapter and section organization (and their titles).
- 5. Every cipher in my notes must be present in your notes. You can add extra ciphers not found in my notes. (Example: enigma, playfair, etc.)
- 6. For each cipher, have a complete definition of each cipher and then have at least one example on encryption and decryption. Include definitions of terms. Your example(s) must be different from the examples in my notes.
- 7. You must write in proper English and using proper mathematical style.
- 8. Think of your notes as the only notes you can use in an open-book test or open-book final exam. Therefore you need not include historical or pedagogical remarks (but that's up to you).
- 9. Solve as many exercises as you can. The exercises are stored in directory exercises. For instance if you see \input{exercises/abc/main.tex}, this means the question of this exercise is stored in \input{exercises/abc/question.tex} and the answer should be written in \input{exercises/abc/answer.tex}
- 10. In terms of writing style, technically speaking, in formal writings, you should not use personal noun like "I". Instead, "we" should be used.

For instance instead of saying

"I will now prove my theorem."

you should write

"We will now prove the (or our) theorem."

I use "I" just to make my notes informal. For your book, you should use the formal writing style.

11. When you are done with this chapter, comment out this section of instructions.

The subtitle: Stuff that you should not use anymore.

However some of these old stuff is important because their ideas are used in modern-day cryptography.

Here we go \dots

1.2 Shift cipher debug: classical-cipher-shift-cipher.tex

So first of all we need to establish is the mathematical representation of a cryptosystem.

A cryptosystem is made up of an Encrytpion function E(x, k) which usually requires a plaintext and a key to create a cipher text, and a decryption function D(x, k) which requires a ciphertext and a decryption key.

The feature of a good cryptosystem is then D(E(x), k) = x for a symmetric cipher so assuming is the domain for plaintext and the ciphertext is P and C so there is a bijection on the funtion $E: P \to C$ so that means that $D = E^{-1}$.

The Shift cipher is the general cipher name of the earliest cipher called the ceaser cipher. so how the cipher goes is that the key would be the amount of letters a character in the plaintext would shift hence the name shift cipher.

The encryption function would look like this E(x,k) = x+k. So in the actual cryptosystem the alphabets are in a domain of $\mathbb{Z} \pmod{26}$ so the encryption function will look like this $E(x,k) = x+k \pmod{26}$ and the decryption function would look like this D(x,k) = x-k this is because to decryption would have to reverse the operation of the encryption. The is basically the trend of how most of the ciphers go we basically find the reverse of the encryption process

Now for an example lets assume we are trying to encrypt a message with the shift cipher. Assume our plaintext is s="i am a really good boy i promise" and our key is shift by 3 first we would want to cleanup the plaintext by removing the spaces and only considering lowercase characters then we take all the letters one by one and shift all by the key 3 and also taking their mod 26. Then we consider the numerical representation of letters

i.e

$$a \to 0$$

$$b \to 1$$

$$c \to 2$$

and so on

So when shifting the letter when we have the first letter i the numeric representation of i is 8.

So applying the encryption function on i would be $8+3=11\pmod{26}$ and in the cipher text the letter would be l

Applying this encryption process the ciphertext will look like this

"ldpdjrrgerblsurplvh".

1.3 Attacking the shift cipher debug: classical-cipher-attacking-shift-cipher.tex

Now its time to attack the shift cipher. When attacking a cipher one common method is to do a brute force search with powerful technologies, today we could search through huge key spaces in seconds, for example the key space of a shift cipher is 26 beacause you could shift each letter 26 different ways. So for our computers today brute force might be a quick method but the goal of having an optimizing technique is to learn how to make a heuristic approach to breaking ciphers.

So using heuristics we would need to have a public information theory fact i.e we look at the most commonly occurring letters in the English alphabets which is e. So with this we look at the most occurring letter in our cipher text then we can deduce that that letter is corresponding to the most occurring letter in the English language.

So we compute the relative shift of both letters if we assume that was encrypted to that letter.

Remember this works best for long cipher texts, with longer cipher texts the better and the more spread out the probabilities are.

The following is a table of probabilities for each letter used in English.

Letter	Probability	
е	0.127	
t	0.091	
a	0.082	
0	0.075	
i	0.070	
n	0.067	
s	0.063	
h	0.061	
r	0.060	
d	0.043	
1	0.040	
С	0.028	
u	0.028	
m	0.024	
W	0.023	
f	0.022	
g	0.020	
У	0.020	
p	0.019	
b	0.015	
v	0.010	
k	0.008	
j	0.002	
х	0.001	
q	0.001	
Z	0.001	

Here are the frequencies of the 2-grams (of course not all 2-grams, just the top

few):

2-gram	Probability			
th	0.0271			
he	0.0233			
in	0.0203			
er	0.0178			
an	0.0161			
re	0.0141			
es	0.0132			
on	0.0132			
st	0.0125			
nt	0.0117			
en	0.0113			
at	0.0112			
ed	0.0108			
nd	0.0107			
to	0.0107			
or	0.0106			
ea	0.0100			
ti	0.0099			
ar	0.0098			
te	0.0098			
ng	0.0089			
al	0.0088			
it	0.0088			
as	0.0087			
is	0.0086			
ha	0.0083			
et	0.0076			
se	0.0073			
ou	0.0072			
of	0.0071			

and the 3-grams:

3-gram	Probability	
the	0.0181	
and	0.0181 0.0073	
ing	0.0073	
ent	0.0042	
ion	0.0042	
her	0.0036	
for	0.0034	
tha	0.0033	
nth	0.0033	
int	0.0032	
ere	0.0031	
tio	0.0031	
ter	0.0030	
est	0.0028	
ers	0.0028	
ati	0.0026	
hat	0.0026	
ate	0.0025	
all	0.0025	
eth	0.0024	
hes	0.0024	
ver	0.0024	
his	0.0024	
oft	0.0022	
ith	0.0021	
fth	0.0021	
sth	0.0021	
oth	0.0021	
res	0.0021	
ont	0.0020	

and the 4-grams:

	D 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
4-gram	Probability	
tion	0.31	
nthe	0.27	
ther	0.24	
that	0.21	
ofth	0.19	
fthe	0.19	
thes	0.18	
with	0.18	
inth	0.17	
atio	0.17	
othe	0.16	
tthe	0.16	
dthe	0.15	
ingt	0.15	
ethe	0.15	
sand	0.14	
sthe	0.14	
here	0.13	
thec	0.13	
ment	0.12	
them	0.12	
rthe	0.12	
thep	0.11	
from	0.10	
this	0.10	
ting	0.10	
thei	0.10	
ngth	0.10	
ions	0.10	
andt	0.10	

1.4 Affine cipher debug: classical-cipher-affine-cipher.tex

With the knowledge from shift cipher and how easy it is to break a shift cipher so we could do better. So how can we complicate this by adding more keys So the premise of the affine cipher is having two keys instead of one key we could have like 2.

So we could represent this cipher in a mathematical expression $E(x, (a, b)) = ax + b \pmod{26}$ with keys being a and b.

This cipher is totally fine so far but lets try to come up with the decryption function.

```
So if the cipher text x' is x' = ax + b \pmod{26}
Then the plain text x will be x = x' \cdot a^{-1} - b \cdot a^{-1} \pmod{26}
```

What does the above imply. It implies for the a part of the key it has to have an inverse in order for the cryptosystem to work. So the key space of this cipher would be cardinality of the set of invertible numbers $\phi(26)$ which are the numbers co prime to 26 multiplied by 26.

Keyspace $K = \phi(26) \cdot 26$ which is larger than the keyspace of the shift cipher.

1.5 Attacking Affine Cipher

So Attacking this cipher is basically similar to the shift cipher i.e using the probabilities of letters. So with this information we can construct a system of equations if we find the what e (this most frequent letter) is encrypted to and what the t (the second most frequent letter) is encrypted to we construct a system of equation and solve for a and b.

So assuming we want to decrypt

fflqlghsfbqiwldqbgsklkhslmklybeyoklophsoleqgyldlilhyzslksbnqglhsy fnlhmgfgslpmqllhsflulnsflylolqphsfllygsdlillhmklsosklkhslsibmvksk lylnfvfsnqgmlypsklphslehqbslqxlhsflksjdlipleykllqplphyplhslxsbply lolsgqpmqlfywmllpqlbqzslxqflifslslunbsfdlubblsgqpmqlktlylnlphyplq lslvyfpmiubyfbotfesfslydhqffslplpqlhmkliqbntlvfsimkslduplyngmfydb oldybylisnlgmlndldsfeyktlilpywslmptlphslgqkplvsfxsiplfsykqlmlclyl nlqdksfzmlclgyihmlslphypfphsleqfbnlhyklkssltlduplyklylbqzsflhsleq ubnlhyzslvbyisnlhmgksbxlmllyfxybkslvqkmpmqldldsllszsflkvqwslqxlph slkqxpsflvykkmqlktlkyzslemphlylcmdsfylnlylklssfdllhsolesfslyngmfy dbslphmlcklxqflphslqdksfzsfnsjisbbslplxqffnfyemlclphslzsmblxfqglg

slmklgqpmzsklylnlyipmqlkdlzuplxqflphslpfymlsnffsykqlsflpqlyngmplk uihlmlpfukmqlklmlpqlhmklqellnsbmiypslylnlxmlsbofynrukpsnlpsgvsfyg slpleyklpqlmlpfqnuislylnmkpfyipmlclxyipqflehmihlgmchpfphfqelylnqu dpluvqllybblhmklgslpyblfskubpkdlyfmplmllylkslkmpmzsfmlkpfugslptlq flylifyiwlmllqlslqxlhmklqellhmchyvqesflbslksktlequbnllqpfdslgqfsl nmkpufdmlclphyllylkpfqlclsgqpmqllmllyllypufslkuihlyklhmkdlulnfosp lphsfsleyklduplqlsleqgyllpqlhmgtlylnlphypleqgylleyklphslbypslifsl sfunbsftlqxlnudmquklylnlauskpmqlydbslgsgqfodf

we first have to get the frequency of the letters and get the highest frequent letter for this case that would be a appering 116 times and the second most frequent is p with 80 apperence this is done with a computer of course. With that information we can construct the system of equation.

$$s = a \cdot e + b \pmod{26}$$
$$p = a \cdot t + b \pmod{26}$$

which is

$$18 = a \cdot 4 + b \pmod{26}$$

 $15 = a \cdot 19 + b \pmod{26}$

then you solve and get a as 5 and b as 24. Then the decrypted message will be:

tosherlockholmessheisalwaysthewomanihaveseldomheardhimmentionheru nderanyothernameinhiseyessheeclipsesandpredominatesthewholeofhers exitwasnotthathefeltanyemotionakintoloveforireneadlerallemotionsa ndthatoneparticularlywereabhorrenttohiscoldprecisebutadmirablybal ancedmindhewasitakeitthemostperfectreasoningandobservingmachineth attheworldhasseenbutasaloverhewouldhaveplacedhimselfinafalseposit ionheneverspokeofthesofterpassionssavewithagibeandasneertheywerea dmirablethingsfortheobserverexcellentfordrawingtheveilfrommensmot ivesandactionsbutforthetrainedreasonertoadmitsuchintrusionsintohi sowndelicateandfinelyadjustedtemperamentwastointroduceadistractin gfactorwhichmightthrowadoubtuponallhismentalresultsgritinasensiti veinstrumentoracrackinoneofhisownhighpowerlenseswouldnotbemoredis turbingthanastrongemotioninanaturesuchashisandyettherewasbutonewo

 $\verb|mantohimandth| at woman was the late ir eneadler of dubious and question ablem \\emory$

1.6 Vigenère cipher debug: classical-cipher-vigenere-cipher.tex

To understand Vignere cipher you have to know what monoalphabetic and polyalphabetic ciphers are.

monoalphabetic ciphers are ciphers where each letters are mapped to a single character, example shift cipher and affine cipher.

monoalphabetic ciphers

polyalphabetic ciphers are ciphers that could be mapped to different character.

polyalphabetic ciphers

So you might be wondering how can you have a letter map to multiple characters, thats where vignere cipher comes in.

The premise of the Vignere cipher is to divide the plaintext and perform different shift ciphers on the amount of strings your plaintext is divided to.

Lets talk about the division of string and the key.

So the way the string is divided is based on the size of the string. Assuming my plaintext is $x_1x_2x_3x_4x_5x_6\cdots$ and my key is $k_1k_2k_3k_4$. To divide this string we look at the size of the key which is 4 so all the strings will look like this.

$$s_1 = x_1 x_5 x_9 x_{13} \cdots$$

$$s_2 = x_2 x_6 x_{10} x_{14} \cdots$$

$$s_3 = x_3 x_7 x_{11} x_{15} \cdots$$

$$s_4 = x_4 x_8 x_{12} x_{16} \cdots$$

Then encrypt it would be performing a shift cipher on all the strings with corresponding k's, so s_1 will be encrypted using k_1 and s_2 will be encrypted using k_2 and so on.

The keyspace of the cipher is 26^l where l is the size of the plaintext.

Example 1.6.1. Given a String

I want to start by saying that I love you so much. Being with you has been one of the greatest adventures of my life and I will always hold you in my heart. I'm sorry that things didn't work out the way we wanted them to. We both tried our best, but at the end of the day, trust was broken and there really isn't much we can do.

I hope you know that despite everything, I don't regret being with you, nor do I regret giving you a second chance after what you did. I know you meant it when you said you were sorry and I know you tried your best to make things right. I truly appreciate your effort. I am so honored to have been a part of your life at all. You gave me so much even when you had little to give. You were patient and kind and never stopped trying to make me happy. You've taught me to be a better, more understanding, and more open minded person. You gave me a love that I will always remember and for that, I am eternally grateful.

using key times divide and encrypt.

the first string s_1 would be

itratlouitheogevrmewlhoytrandrtynhwhdetefasbnheiuciyotieiogeiuorv ochawoiyawoderdwrosaiitacyfiheaeroflgecnydliupnkneprtepuueaeerdne mdogeeiasmntarye

second string s_2

wo tyhou cnhan free ya iwo uhirt gnkhw teetosa etytra eas cahow dtrnnritnie iuo afhukon huyrriyiut kngrpio faod vntuela shwolev watidr pyomp v gtbrusido ipnaat wlrbdhmg f

third string s_3

as biavs hgy so tetns ln la lie mytstoe eem bruttn ht wonr ln hnouteey gtenhortn anntad nutesoey koerte ghupauomntea orayvoe huiteetannse imeyehoemnt nmpneyvlhiwee faearu

fourth string s_4

nty nte obwobn haatoidly dnasth dwu wwdtoirbt derak deltwdpkh setirt gyregg s dcetiominaus anudbotstlrtrrsoobpfl toemveht oyrindet dna hyttb tod agoe droeo alam rottlal

and the fifth string s_5

 $tasgiymeiueeetduffiasymrohiiotaatotebuhodusetrymeoenapvhdebwodgiy\\ ecerydwetyiwonotyemhriyeeetorheayiaumuenatgoeedavotgkaoametrenarn\\ esumvtlyearielt$

So Encrypting all the strings are whith the key times $shift(s_i, k_i)$

$$shift(s_1,t)$$
:

 $\verb|bmktmehnbmaxhzxokfxpeahrmktgwkmrgapawxmxytlugaxbnvbrhmbxbhzxbnhko| hvatphbrtphwxkwpkhltbbmtvrybaxtxkhyezxvgrwebnigdgxikmxinnxtxxkwgx fwhzxxbtlfgmtkrx|$

$$shift(s_2,i)$$

ewbgpwckvpivnzammgiqewcpqzbovspebmmbwaimbgbzimiakipwelbzvvzqbvqmqcwinpcswvpcgzzqgqcbsvozxqwniwldvbcmtiapewtmdeibqlzxgwuxdobjzcaqlwqxviibetzjlpuvon

$$shift(s_3, m)$$

 $\label{lem:menumhetskeafqfzexzxmxuqykfefaqqqyndgffztfiazdxztzagfqqksfqztadfzmzzfmpzgfqeaqkwaqdfqstgbmgayzfqmadmkhaqtgufqqfmzzequyqkqtaqyzfzybzqkhxtuiqqrmqmdg$

$$shift(s_4, e)$$

rxcrxisfasfrleexsmhpchrewxlhayaahxsmvfxhiveohipxahtolwixmvxkcvikkw hgixmsqmreyweryhfsxwxpvxvvwssftjpxsiqzilxscvmrhixhrelcxxfxsheksihv sisepeqvsxxpep

$$shift(s_5, s)$$

lskyaqewamwwwlvmxxaskqejgzaaglsslglwtmzgvmkwljqewgwfshnzvwtogvyaqw uwjqvowlqaogfglqwezjaqwwwlgjzwsqasmemwfslygwwvsnglycsgsewljwfsjfwk menldqwsjawdl

Then joining all those string together we have

bemrlmwexskbncktgurympmxaewhiqhcesenktfwbvsaampksmaiefwxvarwhnflwz zqelxafevomzxmkmesxfgxmxxizhapqxpseemckawxhqhcurerpqejmqywgkzkxztb flagoehawvfagksaylmpqasreqasgbqhlamyxgpmnslabdmwwwgvtxaffmmifxzxmz hgybtivtgfvmlbiekuzaowgizhlamdijxixpqbazxenktawvizhgbpatwrwgofhefl smlqwhbbqinxzkxzbvsmvhvfvwzzqxtxqzkobbtcgnvavvhqdiykmfkaoqzkqhcmww vwzhuaizgwtnfijppmxqhcpmvbszsorwgqwtvfmlppqrqhceeawgayoxzqwgkzkefw qwrgpgaylkqqhqhcdfwlbfsetsqxzbvswjbotxamzgpqtxbvwvqmxwrwgvwynavlbi ywgawzsjxlfsztdqfwxvmtskbajqhcdpaymmxsetksmzihiexaaqmvpqzwgetifrwg lswtuxlemfsybdqcgneqvwiifmwgbmrvdqzhsglzinxzexgixqhlkgurymwyecxuql sixkcgndqxsnotxexbafwtjqxlxzysjxczhwkafefwqzksglysjxwbiffqzhwwxqvk

hvksmzihiexixsnxbtelbeupdttieqlzqqwfjqvsglrsjmpmxatuqxwkvmpdrodelx ngp

1.7 Attacking Vignere cipher

So The first step of breaking this cipher is to determine the length of the string. Now like how we did for shift cipher we use a public information theory fact that is the sum of the square of all the frequency is approximately 0.065 in the english language this is denoted by I(s) which is the probability of choosing two random letters to be the same.

So the goal is to find length where each division of the string are approximately 0.065.

$$I(s) = \sum_{i=0}^{25} p_i^2$$

Example 1.7.1. Given a string

bemrlmwexskbncktgurympmxaewhiqhcesenktfwbvsaampksmaiefwxvarwhnflwz zqelxafevomzxmkmesxfgxmxxizhapqxpseemckawxhqhcurerpqejmqywgkzkxztb flagoehawvfagksaylmpqasreqasgbqhlamyxgpmnslabdmwwwgvtxaffmmifxzxmz hgybtivtgfvmlbiekuzaowgizhlamdijxixpqbazxenktawvizhgbpatwrwgofhefl smlqwhbbqinxzkxzbvsmvhvfvwzzqxtxqzkobbtcgnvavvhqdiykmfkaoqzkqhcmww vwzhuaizgwtnfijppmxqhcpmvbszsorwgqwtvfmlppqrqhceeawgayoxzqwgkzkefw qwrgpgaylkqqhqhcdfwlbfsetsqxzbvswjbotxamzgpqtxbvwvqmxwrwgvwynavlbi ywgawzsjxlfsztdqfwxvmtskbajqhcdpaymmxsetksmzihiexaaqmvpqzwgetifrwg lswtuxlemfsybdqcgneqvwiifmwgbmrvdqzhsglzinxzexgixqhlkgurymwyecxuql sixkcgndqxsnotxexbafwtjqxlxzysjxczhwkafefwqzksglysjxwbiffqzhwwxqvk hvksmzihiexixsnxbtelbeupdttieqlzqqwfjqvsglrsjmpmxatuqxwkvmpdrodelx ngp

we need to find the key

computing the I(s) value of 10 different string length

Average I-value	keyLength
0.0720190990494878	5
0.05674947924604988	9
0.05595853205769283	8
0.053815997799514285	7
0.0523394211228767	6

0.05027720641212229	4
0.04814645463936731	3
0.04680577532250629	2
0.04603145033973668	1

The closest value to 0.065 is key length 5 so we can assume that the key length is 5.

The next step is getting the relative shift of all the different strings. So the Theory is that we calculate the shift relative to the first string.

 $k_1k_2k_3k_4k_5$ so the relative shift of the first string to the other strings would be given as

 $k_2 = k_1 + sft_1 \pmod{26}$ and so on. We rotate the first string against the second string so the amount of rotations would give us the relative shift but the rotation that when we perform $M(s_i, s_j)$ would be approximately 0.065.

This is to simulate I(s) so $M(s_i, s_i)$ would be

$$\sum_{l=0}^{26} p_l p_{l+k_i-k_j}$$

 $k_i - k_j$ is the relative shift.

Because if you shifted it back well you get almost the same probabilities of both strings.

Performing the above method

M value	Relative Shift
0.05920	11
0.06788	7
0.06061	15
0.07052	1
	0.05920 0.06788 0.06061

The equation for relative shift would be

$$k_1 - k_2 = 11 \pmod{26}$$

$$k_2 = k_1 - 11 \pmod{26}$$

$$k_2 = k_1 + 15 \pmod{26}$$

This means if $k_1 = 0$ then $k_2 = 15$ i.e if $k_1 = a$ then $k_2 = p$

Our key according to relative shift is [0, 15, 19, 11, 25]

with this information when we scan k_1 to be a - z we find that the key are as follows.

aptlz

bquma

crvnb

dswoc

etxpd

fuyqe

, I

gvzrf

hwasg ixbth

jycui

kzdvj

--- -- 5

laewk

mbfxl

ncgym

odhzn

peiao

qfjbp

rgkcq

shldr

times

ujnft vkogu

wlphv

xmqiw

ynrjx

zosky

To get k_1 we use frequency analysis on s_1 we see that the most frequent letter is x and the relative shift from x to e is 19 and that is relative shift from a to t so k_1 is the letter t.

When the k_1 is the letter t the key string would look like this

times

Using the assumed key to decrypt the ciphertext we get

iwanttostartbysayingthatiloveyousomuchbeingwithyouhasbeenoneoftheg reatestadventuresofmylifeandiwillalwaysholdyouinmyheartimsorrythat thingsdidntworkoutthewaywewantedthemtowebothtriedourbestbutattheen dofthedaytrustwasbrokenandtherereallyisntmuchwecandoihopeyouknowth atdespiteeverythingidontregretbeingwithyounordoiregretgivingyouase condchanceafterwhatyoudidiknowyoumeantitwhenyousaidyouweresorryand iknowyoutriedyourbesttomakethingsrightitrulyappreciateyoureffortia msohonoredtohavebeenapartofyourlifeatallyougavemesomuchevenwhenyou hadlittletogiveyouwerepatientandkindandneverstoppedtryingtomakemeh appyyouvetaughtmetobeabettermoreunderstandingandmoreopenmindedpers onyougavemealovethatiwillalwaysrememberandforthatiameternallygrateful

1.8 Substitution cipher debug: classical-cipher-substitution-cipher.tex

The substition cipher is a bit tricky to break, i will explain the premise of this cipher is that you have all the alphabets map to different alphabets. For example a could be mapped to e and f could be mapped to d and so on. The encryption is trivial but the decrytpion is difficult.

Example 1.8.1. The goal is to decrypt the following ciphertext (i.e., you need to compute the plaintext) and also to discover the key used. The substitution cipher is used.

amqtijxtheitijxnvatjhumajxltuhetlitukmoajvaotqvewm hmlojiaueecqrtgqtxlljtnhtrqtqjmximhmlajqqmtiqgbxhe bxlieftvmrmajqtggmthtxvmrtlmrmntqgjotqghmgthmlfehq ermiajxnqihtxnmubixeifehqeewmhgeomhjxntgmhqextkjis tqiajqjiotqajqqjpmoajvaieecexmquhmtiatotsajqqjpmtx lajqjrgeqjxnghmqmxvmajqamtlotqmxehrebqiamkthnmqija twmmwmhqmmxbgextabrtxumjxnjtrqbhmiatiajqiegatiatlj mwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkst xlhmqimlexrsqaebklmhqamatliamftvmtxlumthloajvajtqq evjtimojiatxtqqshjtxubkkiamfehrmhfkehjliamktiimhqe uktvctqtkreqiieatwmtqbqgjvjexefukbmqgtlmqatgmltxlh jggkjxnleoxewmhajqvamqiiamatjhotqgmvbkjthgktqimhml leoxjxfhexijxtkexnvbhwjxnojqgewmhajqrtqqjwmfehmamt liammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthw mhsvhjijvtktxlwmhsrtqimhfbktabnmqghmtlefqaebklmhqt xltvamqikjcmtuthhmkomhmiameiamhgthiqefajroajvatggm thmltuewmiamitukmqtwmfehioemxehrebqatxlqvewmhmloji akexnuktvcatjhiajqtxltumkkeojxnhethjxnhbrukjxnwejv mrtlmbgrsfjhqijrghmqqjexefiamxeiehjebqghefmqqehvat kkmxnmh

SOLUTION. The top few 1-gram frequencies of the ciphertext are

```
1gram: m:116 t:95 q:75 h:74 j:68 e:65 i:59 a:59 x:53 1:40 k:34 g:30 ...
```

The gap between the frequency of m and t is extremely large. Therefore we suspect that part of the encryption is e->m. The rest, at least up to x are most probably from t, a, o, i, n, s, h, r:

$$\{t, a, o, i, n, s, h, r\} \rightarrow \{t, q, h, j, e, i, a, x\}$$

We can try different possible assignments on the above 8 letters to 8 letters, but that's 8! = 40320 which is too big. At this point we have

We now look at 2-grams and 3-grams.

The common 2-grams are th, he, in, er, an, re, ed, on, es, st. Since we are assuming e->m, mh is either from er or ed or es. Note that er and re are common 2-grams. We also note that mh and hm are high frequency 2-grams in the ciphertext. Note further that ere is a common 3-gram and mhm is also a common 3-gram in the ciphertext. We suspect that h->r. Therefore we now have

Now we look for the. We have the -> ??m. The most commonly occurring ciphertext of this form is iam, ewm, mhm, twm. mhm is from ere which we already know so this is useless. So we are left with iam, ewm, twm. The frequency between iam and ewm is a huge 30% drop. So hopefully the -> iam. This means t->i and h->a. We have to take note of this since here we are creating two substitutions and the confidence is not as high. If we end up in a deadend, we will have to backtrack to this point. With the above two new substitutions, we have

```
amqtijx the itijxnvatjhumajx ltuhetlituk moajvaot qvewmhmlojiau eecqrt qqtx 1 ljtnhtrqtqjmximhmlajqqmtiqgbx heiliga the statement of the sta
                                                                              ----r-e----r---t---e-----here---t--
 {\tt bxlieftvmrmajqtggmthtxvmrtlmrmntqgjotqghmgthmlfehqermiajxnqihtxnmubixeifehqeewmhgeomhjxntgmhqextkjis}
                                                                         t \\ qiaj \\ qjiot \\ qaj \\ qjpmo \\ ajvai \\ eecexm \\ quhm \\ tiatot \\ saj \\ qqjpmtx \\ laj \\ qjrg \\ eqjx \\ ngh \\ mqmx \\ vmaj \\ qamtlot \\ qmx \\ ehre \\ bqiamk \\ thn \\ mqijamtlot \\ qmx \\ ehre \\ bqiamk \\ thn \\ mqijamtlot \\ qmx \\ ehre \\ bqiamk \\ thn \\ mqijamtlot \\ qmx \\ ehre \\ bqiamk \\ thn \\ mqijamtlot \\ qmx \\ ehre \\ bqiamk \\ thn \\ mqijamtlot \\ qmx \\ ehre \\ bqiamk \\ thn \\ mqijamtlot \\ qmx \\ ehre \\ e
  -ret--t---t---eherhe-t-re-t---
 \verb|xlhmqimlexrsqaebk| \verb|mhqamatliam| ftvmtxlumthloajvajtqqevjtimojiatxtqqshjtxubkkiam| fehrmhfkehjliam| ktiimhqelliam fehrmhfkehjliam| fehrmh
 --her-
 {	t mhsvhjijvtktxlwmhsrtqimhfbktabnmqghmtlefqaebklmhqtxltvamqikjcmtuthhmkomhmiameiamhgthiqefajroajvatggm
                                                            --her-
                                                                                               -ter-
                                                                                                                                                                                                                                                              --e-t---e--rre--eret-e-t-er--rt
 thmltuewmiamitukmqtwmfehioemxehrebqatxlqvewmhmlojiakexnuktvcatjhiajqtxltumkkeojxnhethjxnhbrukjxnwejv
 \verb|mrtlmbgrsfjhqijrghmqqjexefiamxeiehjebqghefmqqehvatkkmxnmh|
                                        ---r-t---re-----t-e--t-r--
 ciphertext
 1grams: m:116 t:95 q:75 h:74 j:68 e:65 i:59 a:59 x:53 1:40 k:34 g:30
 2grams: mh:25 ia:20 hm:20 aj:19 wm:18 at:16 am:16 tq:15 mq:15 xn:14 tx:14 mt:14 jx:14 xl:12 qi:12 jq:12 th:11 ml:10 ex:10 eh:10
 3grams: wmh:11 ajq:11 jxn:10 iam:10 txl:9 hml:7 ewm:7 mhm:6 otq:5 mhq:5 feh: 5 twm: 4 qqj: 4 oaj: 4 mth:4 mqi:4 mia:4 jva:4 imh:4 iat:4
 plaintext
  1grams: etaoinshr
2grams: th he in er an re ed on es st en at to nt ha nd ou ea ng as or ti is et it ar te se hi of
 3grams: the ing and her ere ent tha nth was eth for dth
 e->m. r->h. t->i. h->a
```

ent is also a common plaintext trigram. This is encrypted as m?i. The only

one that fits is mqi but the frequency of this is only 4 – so this is probably wrong.

Another high frequency plaintext 3-gram is tha. This would encrypt as ia?. We notice that iam has a high frequency. So perhaps a->m.

Now let's look at pairs of digrams.

es,st is a high frequency digram. This is encrypted as m?,?i. The only possibility is mq,qi. So we suspect s->q. This is what we have now:

```
-s-re--re--rs--eth---str---e--t--t--rs---er-
\verb|tqiajqjiotqajqqjpmoajvaieecexmquhmtiatotsajqqjpmtxlajqjrgeqjxnghmqmxvmajqamtlotqmxehrebqiamkthnmqijailamidaliti. In the context of the co
twmmwmhqmmxbgextabrtxumjxnjtrqbhmiatiajqiegatiatljmwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkstabrtxumjxnjtrqbhmiatiajqiegatiatljmwhwmxibhmiatiajqiegatiatljmwhwmxibhmiatiajqiegatiatljmwhwmxibhmiatiajqiegatiatljmwhwmxibhmiatiajqiegatiatljmwhwmxibhmiatiajqiegatiatljmwhwmxibhmiatiajqiegatiatljmwhwmxibhmiatiajqieqatiatliquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiquithiqu
                                                                                                                                                               s-reth-th-st--h-th---e-er-e-t-re-t--
--reste----sh---ersheh--the---e-r--h--h--ss
-s---stt-h--e-s-s-
                                                                                                                                                        -----es---esh--e---r
                                                                                                                                                                                                                                                                                                                          ----erh-s-hesttheh--r--s-e--
{\tt leoxjxfhexijxtkexnvbhwjxnojqgewmhajqrtqqjwmfehmamtliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthw}
                                                                                                                                                                --erh-s--ss--e--rehe--thee-es-ere---e-r--er-re-t---t--ts-er---e-r-
\verb|mhsvhjijvtktx|| \verb|wmhsrtqimhf|| bktabnmqghmtlefqaebklmhqtx|| tvamqikjcmtuthhmkomhmiameiamhgthiqefajroajvatggmiller (block of the control 
thmltuewmiamitukmqtwmfehioemxehrebqatxlqvewmhmlojiakexnuktvcatjhiajqtxltumkkeojxnhethjxnhbrukjxnwejvalianistation to the statement of the st
\verb|mrtlmbgrsfjhqijrghmqqjexefiamxeiehjebqghefmqqehvatkkmxnmh| \\
ciphertext
1grams: m:116 t:95 q:75 h:74 j:68 e:65 i:59 a:59 x:53 l:40 k:34 g:30 2grams: mh:25 ia:20 hm:20 aj:19 wm:18 at:16 am:16 tq:15 mq:15 xn:14
tx:14 mt:14 jx:14 xl:12 qi:12 jq:12 th:11 ml:10 ex:10 eh:10 3grams: wmh:11 ajq:11 jxn:10 iam:10 txl:9 hml:7 ewm:7 mhm:6 otq:5 mhq:5
                                         feh: 5 twm: 4 qqj: 4 oaj: 4 mth:4 mqi:4 mia:4 jva:4 imh:4 iat:4
                                         plaintext
1grams: e taoinshr
2grams: the in er an re ed on es st en at to nt ha nd
ou ea ng as or ti is et it ar te se hi of
3grams: the ing and her ere ent tha nth was eth for dth
e->m, r->h, t->i, h->a, s->q
```

Note that ti, is is a common plaintext 2-gram. When encrypted, this is i?,?q. Unfortunately we can't find this pattern.

We now have enough substitutions to consider multiple cases of pairs of digrams.

Consider the common plaintext digram aj,jq. With what we have at this point, the encryption is h?,?s -> aj,jq. The possibilities for h?,?s are

- he, es: Therefore e->j, but e is already encrypted as m.
- ha,as: Therefore a->j.
- hi, is: Therefore i->j.

So we have a->j or i->j. Before we make a choice, let's consider more digrams.

Consider h?, e?. h?, e? might be encrypted as at, mt. Possibilities for h?, e?

- hi,ei: But ei is not common.
- ha, ea: Therefore a->t.

Therefore a->t.

Consider h?,?r. h?,?r might be encrypted to at,th. The only possibilities for h?,?r are

- ha, ar: Therefore a->t.
- hi, ir: But ir is not common.

Therefore a->t.

Consider ?s,e? . ?s,e? might be encrypted as tq,mt. The only possibility for ?s,e? is as,ea which implies a->t.

?s,e? might be encrypted as tq,th. The only possibility for ?s,e? is as,ea which implies a->t.

e?,?r might be encrypted to mt,th. The possibilities for e?,?r are

- ed,rd: But rd is not common.
- es, sr: But sr and os not common.
- en,nr: But nr is not common.
- ea, ar: Therefore a->t.
- et,tr: But tr is not common.

All in all, this case implies a->t.

From all the above cases, it seems that a->t and i->j. (The argument for a->t is stronger.) We now have

At this point we can already see (possibly) "he sat" at line one and "that his" at line 4 and "his -hest the hair" at line 4 – perhaps "chest" is the second word?

Next, we try tx,jx. a?,i? might be encrypted as tx,jx. The possibilities for a?,i? are

- an, in: Therefore n->x.
- ar, ir: But ir is not common.

We get

```
hesatinar-tatin--hair-ehin-a-r-a-ta--e-hi-h-as-
                                                                                                       --ere--ith----
{\tt bxlieftvmrmajqtggmthtxvmrtlmrmntqgjotqghmgthmlfehqermiajxnqihtxnmubixeifehqeewmhgeomhjxntgmhqextkjis}
-n-t--a-e-ehisa--earan-e-a-e-e-as-i-as-re-are---rs--ethin-stran-e--tn-t--rs--er--erin-a-ers-na-it-
\label{tq:continuous} tqiajqjiotqajqqjpmoajvaieecexmquhmtiatotsajqqjpmtxlajqjrgeqjxnghmqmxvmajqamtlotqmxehrebqiamkthnmqija\\ asthisit-ashissi-e-hi-ht----nes-reatha-a-hissi-ean-hisi---sin--resen-ehishea--asen-r---sthe-ar-estih
uktvctqtkreqiieatwmtqbqgjvjexefukbmqgtlmqatgmltxlhjggkjxnleoxewmhajqvamqiiamatjhotqgmvbkjthgktqimhml
{\tt leoxjxfhexijxtkexnvbhwjxnojqgewmhajqrtqqjwmfehmamtliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthwliammsmqomhmukbmnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhnhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmhhtsbxlmh
    -nin-r-ntina--n--r-in--is---erhis-assi-e--rehea-thee-es-ere---e-ra--n-er-reat--a-
{\tt mhsvhjijvtktxlwmhsrtqimhfbktabnmqghmtlefqaebklmhqtxltvamqikjcmtuthhmkomhmiameiamhgthiqefajroajvatggm}
\verb|mrtlmbgrsfjhqijrghmqqjexefiamxeiehjebqghefmqqehvatkkmxnmh|
                ---irsti--ressi-n--then-t-ri--s-r--ess-r-ha--en-er
1grams: m:116 t:95 q:75 h:74 j:68 e:65 i:59 a:59 x:53 1:40 k:34 g:30
2grams: mh:25 ia:20 hm:20 aj:19 wm:18 at:16 am:16 tq:15 mq:15 xn.14 tx:14 mt:14 jx:14 xl:12 qi:12 jq:12 th:11 ml:10 ex:10 eh:10
3grams: wmh:11 ajq:11 jxn:10 iam:10 txl:9 hml:7 ewm:7 mhm:6 otq:5 mhq:5 feh: 5 twm: 4 qqj: 4 oaj: 4 mth:4 mqi:4 mia:4 jva:4 imh:4 iat:4
plaintext
1grams: e t a o i n s h r
2grams: th he in er an re ed on es st en at to nt ha nd
```

```
ou ea ng as or ti is et it ar te se hi of 3grams: the ing and her ere ent tha nth was eth for dth e->m, r->h, t->i, h->a, s->q, a->t, i->j, n->x
```

The beginning of the plaintext now reads "he sat in a." We now look at xl,ml and ex,eh.

n?,e? might be encrypted as xl,ml. The possibilities for n?,e? are

- nt, et: But t is already assigned.
- nd,ed: Therefore implies d->1.
- ng,eg: But eg is not common.

?n,?r might be encrypted as ex,eh. The possibilities for ?n,?r are

- in, ir: But i is already assigned.
- an, ar: But a is already assigned.
- on, or: This implies o->e.
- en,er: But e is already assigned.

Adding d->1 and o->e, we get

```
hesatinarotatin--hair-ehinda-roadta--e-hi-h-as-o-ered-ith-oo-s
                                                                                                                                                                                                                                                                                                                                                                                                                                         sanddia-ra-sasienteredhis
\verb|bxlieftvmrmajqtggmthtxvmrtlmrmntqgjotqghmgthmlfehqermiajxnqihtxnmubixeifehqeewmhgeomhjxntgmhqextkjiside for the contract of the contract o
 -ndto-a-e-ehisa--earan-e-ade-e-as-i-as-re-ared-orso-ethin-stran-e--tnot-orsoo-er-o-erin-a-ersona-it-
tq \verb"iajqj" iot qajqq" jpmoajva \verb"ieecexmquhmtiatots ajqq" jpmtxlajqj rgeqjxnghmqmxvmajqamtlotqmxehrebq" iamkthnmqijallotqmxehrebq iamkthnmqijallo
asthisit-ashissi-e-hi-htoo-ones-reatha-a-hissi-eandhisi--osin--resen-ehishead-asenor-o-sthe-ar-estih
a-ee-erseen--onah--an-ein-ia-s-rethathisto-hathadie-er-ent-redtodonit-o--dha-es-i
\verb|xlhmqim| lexrsqaebklmhqamatl| iamftvmtxlumthloajvajtqqevjtimojiatxtqqshjtxubkkiamfehrmhfkehjliamktiimhqelliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstalliamstall
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 e->m, r->h, t->i, h->a, s->q, a->t, i->j, n->x, d->l, o->e
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The beginning reads "he sat in a rotatin--hair-ehinda-road..." which is very likely "he sat in a rotating chair-ehinda-road...", giving us g->n and c->v. This gives us

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```

Near the middle of the first line, "-hich-asco-ered-ith" is probably "which-asco-eredwith" giving us w->o.

On the second line "orso-ethingstrange-" is probably "or something strange-", giving us m->r.

On the third line "sthe-argestiha-ee-erseen" is probably "s the largest i have ever seen." This gives us 1->k and v->w.

At this point we have

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l->k, v->w
```

At the third line "hisim-osing-resencehisheadwasenormo-sthelargestihaveeverseen" is probably "his imposing presence his head was enormous the largest i have ever seen" giving us p->g and u->b.

At line 7, "hismassive-orehead" is "his massive forehead" giving us f->f.

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mrtlmbgrsfjhqijrghmqqjexefiamxeiehjebqghefmqqehvatkkmxnmh
{\tt emadeupm-firstimpression} of the notorious professor challenger
e->m, r->h, t->i, h->a, s->q, a->t, i->j, n->x, d->l, o->e, g->n, c->v, w->o, m->r, l->k, v->w, p->g, u->b, f->f
```

The beginning "hesatinarotatingchair-ehinda-roadta-le" is "he sat in a rotating chair behind abroad table" giving us b->u.

At line 5, "restedonm-shoulder" is "rested on my shoulder" giving us y->s.

At line 8, "shouldersandachestli-ea-arrel" is "shoulders and a chest like a barrel, giving us k->c.

At line 3, "itwashissi-ewhichtookonesbreathaway" is "it was his size which took ones breath away" giving us z->p.

We now have

```
he satinar otating chair behind abroadtable which was covered with books maps and diagrams as ientered his seats punnous and the satinar of the satinar of
  bx \verb|lieftvmrmajqtggmthtxvmrtlmrmntqgjotqghmgthmlfehqermiajxnqihtxnmubixeifehqeewmhgeomhjxntgmhqextkjis
 und to face {\tt mehisappear ancemade megas piwas prepared for something strange but not for so overpowering apersonal it yet a constant of the contract of th
 asthisitwashissizewhichtookonesbreathawayhissizeandhisimposingpresencehisheadwasenormousthelargestih
  {	t twmmwmhqmmxbgextabrtxumjxnjtrqbhmiatiajqiegatiatljmwmhwmxibhmlielexjioebklatwmqkjggmlewmhrmmxijhmkst
 a veever see nu pon a human being iam sure that his tophathad iever ventured to do nit would have slipped over meentirely a constraint of the constraint o
 {\tt ndrestedonmyshouldershehadtheface} and {\tt beardwhichias} sociate {\tt withanas} {\tt syrianbulltheformerfloridthelatters} of {\tt ndrestedonmyshouldershehadtheface} and {\tt beardwhichias} {\tt sociate} {\tt withanas} {\tt syrianbulltheformerfloridthelatters} of {\tt ndrestedonmyshouldershehadtheface} and {\tt ndrestedoumyshouldershehadtheface} and {\tt ndrestedoumyshouldersheha
  {\tt uktvctqtkreqiieatwmtqbqgjvjexefukbmqgtlmqatgmltxlhjggkjxnleoxewmhajqvamqiiamatjhotqgmvbkjthgktqimhml}
 blackasalmosttohaveasuspicionofbluespadeshapedandripplingdownoverhischestthehairwaspeculiarplastered
 {\tt leoxjxfhexijxtkexnvbhwjxnojqgewmhajqrtqqjwmfehmamtliammsmqomhmukbmnhtsbxlmhnhmtiuktvcibfiqwmhsvkmthw}
  downinfrontinalongcurvingwispoverhismassiveforeheadtheeyeswerebluegrayundergreatblacktuft
 {\tt mhsvhjijvtktxlwmhsrtqimhfbktabnmqghmtlefqaebklmhqtxltvamqikjcmtuthhmkomhmiameiamhgthiqefajroajvatggmerycriticalandverymasterfulahugespreadofshouldersandachestlikeabarrelweretheotherpartsofhimwhichappedus and the statement of the statement 
  {	t thmltuewmiamitukmqtwmfehioemxehrebqatxlqvewmhmlojiakexnuktvcatjhiajqtxltumkkeojxnhethjxnhbrukjxnwejv
 aredabovethetablesavefortwoenormoushandscoveredwithlongblackhairthisandabellowingroaringrumblingvoic
 mrtlmbgrsfjhqijrghmqqjexefiamxeiehjebqghefmqqehvatkkmxnmh
 emadeupmyfirstimpressionofthenotoriousprofessorchallenger
              >m, r->h, t->i, h->a, s->q, a->t, i->j, n->x, d->l, o->e, g->n, c->v, w->o, m->r,
-, - -, -, -, -, -, -, -, -, -, -, 1->j, 1->x, 0->l

l->k, v->w, p->g, u->b, f->f, b->b, y->s, k->c, z->p

q->q, x->x, j->j
```

Note that q,x,j were not used in the plaintext. We have added q->q, x->x, j->j to the substitution key. The following is the plaintext with spaces inserted (puncuations not restored):

he sat in a rotating chair behind a broad table which was covered with books maps and diagrams as i entered his seat spun round to face me his appearance made me gasp i was prepared for something strange but not for so overpowering a personality as this it was his size which took ones breath away his size and his imposing presence his head was enormous the largest i have ever seen upon a human being i am sure that his tophat had i ever ventured to don it would have slipped over me entirely and rested on my shoulders he had the face and beard which i associate with an assyrian bull the former florid the latter so black as almost to have a suspicion of blue spade shaped and rippling down over his chest the hair was peculiar plastered down in front in a long curving wisp over his massive forehead the eyes were blue gray under great black tufts very clear very critical and very masterful a huge spread of shoulders and a chest like a barrel were the other parts of him which appeared above the table save for two enormous hands covered with long black hair this and a bellowing roaring rumbling voice made up my first impression of the

notorious professor challenger

The following programs are helpful (so go ahead and write them):

- (a) Code to print the top 1-grams, 2-grams, 3-grams. The 1-grams will help determine the character that **e** is encrypted to. The trigrams might help determine what **the** is encrypted to.
- (b) Given a character c, code that computes character(s) d such that cd and dc occurs most frequently. So if you suspect e is encrypted to r, your code will print all x such that rx and xr is common will be helpful in decoding x.
- (c) Given a collection of common 2-grams (in plaintext), a partially specified substitution, compute pairs of commonly ocurring digrams of the form xy,xz or xy,zx or xy,yz or xy,zy (i.e., there are three distinct characters in the pairs of digrams) where two of the characters have already been decrypted and the remaining one has not and has not been assigned to a plaintext character.
- (d) Instead of the above where there are two digrams, listing 4-grams where the decryption of 3 are known and one is unknown is also useful.

Index

 ${\it monoal phabetic ciphers, \, 16}$ ${\it polyal phabetic ciphers, \, 16}$

Bibliography