

$$\Omega = [0,1]^2 h \mathit{vertex_matrix} \mathit{cell_matrix} \mathit{vertex_matrix} \mathit{cell_matrix}$$

Example $h = 0.5$

$$\mathit{nodes} \hat{T} = [0,1]^2 p_i$$

$$p_i(x_j) = \delta_{ij}, x_j$$

$$p_i$$

$$k\{x^i y^j, i, j = 0 \dots k\} 2 k k \frac{1}{k} k + 1$$

Remark

$$\mathit{sf_generate} k \mathit{mesh_generate} \frac{1}{k} (k+1)^2 := n$$

$$SF$$

Example SF

$A_{ij} = a(\phi_i, \phi_j)$ local see also
~~sp_assemble_local~~ hSF
 hf_eval_poly
 $sf_derivate$
 $int_gauss_weights$
 int_gauss
 $(a_{ij})^T T_{ij}$

ρ
 ρ mesh nodes i, j, j_i mesh nodes
 $rhs_integration$
 $mesh_nodes$ rep mat f hf_eval_poly
 minimal residual method conjugate gradient method $u \phi_i u$

$\phi_i u_h$
 $hf_eval_solution(x, y) u$
 $(x, y) u_h hf_eval_solution(x, y) u_h$
 $m_plot_solution hf_eval_solution u_h$
 $hf_vtk m_plot_paraview$
 $linear_solver_analytics$
 $error_map$
 $error_runge_evaluation$
 Evaluation of a Polynomial
 $p(x, y) \in R hf_eval_poly SF$

$$\begin{array}{l} Gauss\ quadrature \\ (x_1,...,x_n)^T(w_1,...,w_n)^T f \end{array}$$

$$meshgrid W_1,W_2 w_i X,Y x_i f(X,Y)$$

$$\begin{array}{l} int_gauss_vectorized int_gauss_vectorized_matrices \\ f \end{array}$$

$$repmat$$

$$A,B,C,D,E,F\in R^{3\times 3}M$$

$$\begin{array}{l} (1)0 \\ 10 \\ 10 \\ 01 \\ 01 \\ 01(\bar{})A_1\bar{B}_1 \\ \bar{A}_2\bar{B}_2 \\ A_3\bar{B}_3 \\ C_1\bar{D}_1 \\ C_2\bar{D}_2 \\ C_3\bar{D}_3 \\ E_1\bar{F}_1 \\ E_2\bar{F}_2 \\ E_3\bar{F}_3 \\ A_i iA \end{array}$$

$$\begin{array}{l} A^*A \\ Vectorization\ of\ sm_local_assembly \\ p_1,...,p_n SMlocal \end{array}$$

$$P_i p_i$$

$$.*(P_1,...,P_n)^Thf_eval_polyrepmat$$

$$P_1^TxyP_i$$