

# Programmieren 1

## Enumerations and Intervals

# Lectures

#	Date	Topic	HÜ→	HÜ←
1	14.10.	Organization, computers, programming, algorithms, PostFix introduction (execution model, IDE, basic operators, booleans, naming)	1	20.10. 23:59
2	21.10.	PostFix (primitive types, functions, parameters, local variables, tests), recipe for atomic data	2	27.10. 23:59
3	28.10.	PostFix (operators, array operations, string operations), recipes for enumerations and intervals	3	3.11. 23:59
4	4.11.	Recipes for compound and variant data, iteration and recursion, PostFix (loops, association arrays, data definitions)	4	10.11. 23:59
5	11.11.	C introduction (if, variables, functions, loops), Programming I C library	5	17.11. 23:59
6	18.11.	Data types, infix expressions, C language (enum, switch)	6	24.11. 23:59
7	25.11.	Compound and variant data, C language (formatted output, struct, union)	7	1.12. 23:59
8	2.12.	C language (arrays, pointers) arrays: fixed-size collections, linear and binary search	8	8.12. 23:59
9	9.12.	Dynamic memory (malloc, free), recursion (recursive data, recursive algorithms)	9	15.12. 23:59
10	16.12.	Linked lists, binary trees, search trees	10	22.12. 23:59
online → 11	23.12.	C language (program structure, scope, lifetime, linkage), function pointers, pointer lists	11	12.1. 23:59
12	13.1.	List and tree operations (filter, map, reduce), objects, object lists	12	19.1. 23:59
13	20.1.	Dynamic data structures (stacks, queues, maps, sets), iterators, documentation tools	(13)	
14	27.1.	C language (remaining C keywords), finite state machines, quicksort	(14)	

# Review

- PostFix
  - Types, data arrays [...], executable arrays {...}, functions **f**: (...) {...} **fun**, parameters, local variables, tests
- Functions
  - Functions are named, reusable pieces of computation
  - Some parts are fixed, others (parameters) are filled with actual values (arguments) when calling the function
- How to Design Programs
  - From problem statement to well-organized solution
- Recipe for Atomic Data
  - Primitive data that cannot be subdivided further

# Preview

- Operators
- Recipe for enumerations
- Recipe for intervals
- Array operations
- Characters and Strings
- Loops

# OPERATORS

# Operators in PostFix

	Operators
arithmetic	+   -   *   /   div (integer division)   mod
relational, equality	<   <=   >   >=   = (equal)   != (not equal)
logical	and   or   not
conditional	if   cond
assignment	x!   !   vref
stack	pop   dup   swap   copy   clear
loops	loop   for   fori   break   breakif
arrays	[   ]   {   }   array   length   exec
array access	set   get   .3   .:x   .i
function definition	lam   fun   cond-fun
parameters	(   )   ->
data definition	datadef
type test	int?  flt?   num?   bool?   str?   sym?   ...
type cast	int   flt   str   sym   arr   exearr
tests	test=   test~=   test!=   test!~=   test-stats

# Short-Circuit Logical Operators

- **and** and **or** either take two Boolean operands or one array
  - Array of predicates: May not need to evaluate all of them
  - $\{p_1 \ p_2 \ \dots \ p_n\}$  and
  - $\{p_1 \ p_2 \ \dots \ p_n\}$  or
- **Short-circuit and:** Test elements one-by-one, stop on first false and return false, if no false found return true  
 $\{\{1 \text{ positive}\} \ \{0 \text{ positive}\} \ \{2 \text{ positive}\}\}$  and  

not evaluated
- **Short-circuit or:** Test elements one-by-one, stop on first true and return true, if no true found return false  
 $\{\{0 \text{ positive}\} \ \{1 \text{ positive}\} \ \{2 \text{ positive}\} \}$  or  

not evaluated

Two Boolean operands:

$p_1 \ p_2$  and

$p_1 \ p_2$  or

## cond: Conditional Operator

- Multiple cases are inconvenient with nested ifs
- **cond** operator processes conditions one-by-one
- executes first action for which condition is true
- Example:

```

10 age!
{
    { age 3 <= } { "Toddler" }      # condition 1, action 1
    { age 13 <= } { "Child" }       # condition 2, action 2
    { age 18 < } { "Teenager" }     # condition 3, action 3
    { true } { "Adult" }           # default case, action 4
} cond

```



# cond-fun: Conditional Function Operator

Function with **cond** as its body may be abbreviated to **cond-fun**

```
f: (age :Num -> :Str) {
  {
    { age 3 <= } { "Toddler" }
    { age 13 <= } { "Child" }
    { age 18 < } { "Teenager" }
    { true } { "Adult" }
  } cond
} fun
```

equivalent to

```
f: (age :Num -> :Str) {
  { age 3 <= } { "Toddler" }
  { age 13 <= } { "Child" }
  { age 18 < } { "Teenager" }
  { true } { "Adult" }
} cond-fun
```

# Stack Operators

- Stack operations allow writing functions without variables
  - But can be difficult to read
- clear: Remove all elements from stack
- pop: Remove top stack element
- dup: Duplicate top stack element
- swap: Exchange top two stack elements

# Stack Operators

```
dist: { dup * swap dup * + sqrt } ! 3 4 dist
```

Tokens	Stack	Dictionary	Comment
...! 3 4	3 4	dist → {...}	Store array in dictionary, push 3 and 4
dist	3 4	dist → {...}	Reference (execute) dist
<b>dup</b>	3 4 4	dist → {...}	Duplicate top stack element
*	3 16	dist → {...}	Multiply two top stack elements
<b>swap</b>	16 3	dist → {...}	Swap two top stack elements
<b>dup</b>	16 3 3	dist → {...}	Duplicate top stack element
*	16 9	dist → {...}	Multiply two top stack elements
+	25	dist → {...}	Add two top stack elements
sqrt	5.0	dist → {...}	Take square root of top stack element

# Type Test Operators

- type: Provide the type of an object (:Obj -> :Sym)
  - `123 type → :Int`
  
- Test whether an object as a specific type (:Obj -> :Bool)
- `int? flt? num? bool? str? sym? arr? exearr?`
  - `123 int? → true`
  - `123.456 num? → true`
  - `"hello" bool? → false`

# Type Cast Operators

- Convert the type of an object (return nil if not possible)
- int, flt, str, sym, arr, exearr
  - 67.89 int → 67
  - 67.89 str → "67.89"
  - "67.89" flt → 67.89
  - "67.89" int → 67
  - "abc" int → nil
  - "hello" arr → ["hello"]
  - [1 2 3] str → "[1 2 3]"
- round: Round floating-point to integer number
  - 67.89 round → 68 (type :Int)

Convert to string before printing:  
["hello"] str println

Output:  
[ "hello" ]

# RECIPE FOR ENUMERATIONS

# Design Recipes

- Recipe for Atomic Data
- Recipe for Enumerations
- Recipe for Intervals
- Recipe for Compound Data (Product Types)
- Recipe for Variant Data (Sum Types)

# Enumerations

- An enumeration type can represent one of a fixed number of distinct values
- Each enumerated value names a category
- Examples
  - Dog breeds (Poodle, Golden Retriever, Saint Bernard)
  - Suit of cards (diamonds ♦, clubs ♣, hearts ♥, and spades ♠)
  - Continents (Europe, Asia, Africa, etc.)
- In PostFix, such types can be represented as symbols
  - Symbols are names



# 1. Problem Statement

- Write down the problem statement as a comment.
  - What is the relevant information?
  - What should the function do with the data?

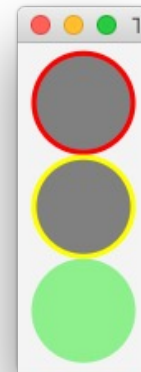
- Example

```
#<
```

Design a function that returns the duration of a traffic light phase.

Durations: red: 3 s, red-yellow: 1 s, green: 2 s, yellow: 1 s.

```
>#
```



## 2. Data Definition

- How should domain information be represented as data in the program?  
How to interpret the data as real-world information?
- Write the data definition as a list of required symbols
- Data definition
  - # enumeration of TrafficLight states:  
# :red, :red-yellow, :green, :yellow
  - # :Int represents the phase duration in milliseconds

### 3. Function Name and Parameter List

- Find a good function name
  - Short, non-abbreviated, descriptive name that describes what the function does
- Find good parameter names
  - Short, non-abbreviated, descriptive name that describes what each parameter means
- Write parameter list
  - Parameter names and types left of the arrow
  - Result type right of the arrow
- Example

`traffic-light-duration: (color :Sym -> :Int)`

## 4a. Function Stub

- Function stub returns an arbitrary value from the function's range
- The function stub is syntactically complete (can be executed)

- Example

```
traffic-light-duration: (color :Sym -> :Int) {  
    0  
} fun
```

## 4b. Purpose Statement

- Briefly describes what the function does. Ideally as a single sentence. Multiple sentences may be necessary.
- Example
  - # Duration of the given traffic light phase in milliseconds.

## 5. Examples with Expected Results

- Examples
  - Duration of red is 3 s
  - Duration of red-yellow is 1 s
  - Duration of green is 2 s
  - Duration of yellow is 1 s
- Test function
 

```
traffic-light-duration-test: {
  :red traffic-light-duration 3000 test=
  :red-yellow traffic-light-duration 1000 test=
  :green traffic-light-duration 2000 test=
  :yellow traffic-light-duration 1000 test=
  test-stats
}
```

## 6. Function Body

```
traffic-light-duration: (color :Sym -> :Int) {  
  color :red = {  
    3000 # red  
  } {  
    color :red-yellow = {  
      1000 # red-yellow  
    } {  
      color :green = {  
        2000 # green  
      } {  
        1000 # yellow  
      } if  
    } if  
  } if  
} fun
```

## 7a. Testing

- Calling the test function

`traffic-light-duration-test`

- Test results

`:red traffic-light-duration 3000 test= ✓`

`:red-yellow traffic-light-duration 1000 test= ✓`

`:green traffic-light-duration 2000 test= ✓`

`:yellow traffic-light-duration 1000 test= ✓`

`✓ All 4 tests passed`



## 7b. Review and Revise

- Review the products of the steps
  - Improve function name
  - Improve parameter names
  - Improve purpose statement
  - Improve and extend tests
- Improve / generalize the function
  - `cond` operator
  - `cond-fun` operator

## cond Operator to Handle Multiple Cases

```
traffic-light-duration: (color :Sym -> :Int) {
  {
    { color :red = } { 3000 }
    { color :red-yellow = } { 1000 }
    { color :green = } { 2000 }
    { color :yellow = } { 1000 }
  } cond
} fun
```

```
traffic-light-duration: (color :Sym -> :Int) {
  color :red = {
    3000 # red
  } {
    color :red-yellow = {
      1000 # red-yellow
    } {
      color :green = {
        2000 # green
      } {
        1000 # yellow
      } if
    } if
  } if
} fun
```

## cond-fun Operator to Handle Multiple Cases

```
traffic-light-duration: (color :Sym -> :Int) {  
  { color :red = } { 3000 }  
  { color :red-yellow = } { 1000 }  
  { color :green = } { 2000 }  
  { color :yellow = } { 1000 }  
} cond-fun
```

## cond-fun Operator to Handle Multiple Cases

```
traffic-light-duration: (color :Sym -> :Int) {
  { color :red = } { 3000 }
  { color :red-yellow = } { 1000 }
  { color :green = } { 2000 }
  { color :yellow = } { 1000 }
} cond-fun
```

```
:blue traffic-light-duration
```

## cond-fun Operator to Handle Multiple Cases

```
traffic-light-duration: (color :Sym -> :Int) {
  { color :red = } { 3000 }
  { color :red-yellow = } { 1000 }
  { color :green = } { 2000 }
  { color :yellow = } { 1000 }
} cond-fun
```

:blue traffic-light-duration

```
255 traffic-light-duration: (color :Sym -> :Int) {
```

**Error:** Expected fun to return 1 values but it returned 0 values

## cond-fun Operator to Handle Multiple Cases

```
traffic-light-duration: (color :Sym -> :Int) {
  { color :red = } { 3000 }
  { color :red-yellow = } { 1000 }
  { color :green = } { 2000 }
  { color :yellow = } { 1000 }
  { true } { color str " is not a valid color" + err }
} cond-fun
```

```
:blue traffic-light-duration
```

## cond-fun Operator to Handle Multiple Cases

```
traffic-light-duration: (color :Sym -> :Int) {
  { color :red = } { 3000 }
  { color :red-yellow = } { 1000 }
  { color :green = } { 2000 }
  { color :yellow = } { 1000 }
  { true } { color str " is not a valid color" + err }
} cond-fun
```

```
:blue traffic-light-duration
```

```
267 { true } { color str " is not a valid color" + err }
```

**Error:** :blue is not a valid color

## cond-fun Operator to Handle Multiple Cases

```
#<
Duration of the given traffic light phase in milliseconds.
@param color traffic light phase, allowed values are
        :red, :red-yellow, :green, and :yellow
@return the duration of the phase in milliseconds
>#
traffic-light-duration: (color :Sym -> :Int) {
  { color :red = } { 3000 }
  { color :red-yellow = } { 1000 }
  { color :green = } { 2000 }
  { color :yellow = } { 1000 }
  { true } { color str " is not a valid color" + err }
} cond-fun
```



# RECIPE FOR INTERVALS

# Design Recipes

- Recipe for Atomic Data
- Recipe for Enumerations
- Recipe for Intervals
- Recipe for Compound Data (Product Types)
- Recipe for Variant Data (Sum Types)

# Intervals

- Intervals represent one or more ranges of numbers
- Example: Taxation scheme with
  - No tax for goods below 1000 €
  - Moderate tax for goods between 1 k€ – 10 k€
  - High tax for goods of 10 k€ or more
- Pay attention to boundary cases
  - Interval notation is precise:  $[0, 1000)$ ,  $[1000, 10000)$ ,  $[10000, \text{inf})$
  - Brackets  $[$  and  $]$  denote inclusive boundaries
  - Parentheses  $($  and  $)$  denote exclusive boundaries
- Data definitions
  - Symbols to name each interval
  - Constants to define boundaries

# 1. Problem Statement

- Write down the problem statement as a comment.
  - What is the relevant information?
  - What should the function do with the data?

- Example

#<

A fictitious country has decided to introduce a three-stage sales tax. Cheap items below 1 k€ are not taxed. Luxury goods of 10 k€ or more are taxed at 10%. Items in between are taxed at a rate of 5%. Give a data definition and define a function that computes the amount of tax for a given item price.

>#

## 2. Data Definition

- How should domain information be represented as data in the program?  
How to interpret the data as real-world information?
- Data definition
  - Name each interval as a symbol
  - Give interpretations of data types
  - Capture the interval boundaries as constants

```
# enumeration of tax stages:
```

```
# :no-tax :low-tax :high-tax
```

```
# :Int represents Euro
```

```
1000 LOW-TAX-BOUNDARY! # interpretation: price in Euro
```

```
10000 HIGH-TAX-BOUNDARY! # interpretation: price in Euro
```

### 3. Function Name and Parameter List

- Find a good function name
  - Short, non-abbreviated, descriptive name that describes what the function does
- Find good parameter names
  - Short, non-abbreviated, descriptive name that describes what each parameter means
- Write parameter list
  - Parameter names and types left of the arrow
  - Result type right of the arrow
- Example  
`sales-tax: (price :Int -> :Int)`

## 4a. Function Stub

- Function stub returns an arbitrary value from the function's range
- The function stub is syntactically complete (can be executed)

```
sales-tax: (price :Int -> :Int) {  
    0  
} fun
```

## 4b. Purpose Statement

- Briefly describes what the function does. Ideally as a single sentence. Multiple sentences may be necessary.
- Example
  - # Returns the amount of tax for the given price.



## 5a. Examples with Expected Results

- For a price of 0 € expect a sales tax of 0 €.
- For a price of 537 € expect a sales tax of 0 €.
- For a price of 1000 € expect a sales tax of 50 € (5 %).
- For a price of 1282 € expect a sales tax of 64 € (5 %).
- For a price of 10000 € expect a sales tax of 1000 € (10 %).
- For a price of 12017 € expect a sales tax of 1202 € (10 %).

## 5b. Examples and Expected Results (Test Function)

```
sales-tax-test: {  
    0 sales-tax, 0, test=  
    537 sales-tax, 0, test=  
    1000 sales-tax, 1000 0.05 * round, test=  
    1282 sales-tax, 1282 0.05 * round, test=  
    10000 sales-tax, 10000 0.10 * round, test=  
    12017 sales-tax, 12017 0.10 * round, test=  
    test-stats  
} fun  
sales-tax-test
```

## 6. Function Body

```
# Returns the amount of tax for the given price.
sales-tax: (price :Int -> :Int) { # :Int represents Euro
  { 0 price <= price 1000 < and } { # :no-tax interval
    0
  }
  { 1000 price <= price 10000 < and } { # :low-tax interval
    price 0.05 * round
  }
  { price 10000 >= } { # :high-tax interval
    price 0.10 * round
  }
  { true } { # error: if this line is reached then price < 0
    "sales-tax, error: negative price" err
  }
} cond-fun
```

## 7. Testing

- Main function call test function  
`sales-tax-test`
- Test results
  - tax.pf, line 36: Check passed.
  - tax.pf, line 37: Check passed.
  - tax.pf, line 38: Check passed.
  - tax.pf, line 39: Check passed.
  - tax.pf, line 40: Check passed.
  - tax.pf, line 41: Check passed.
  - All 6 tests passed!

## 8. Review and Revise

- Review the products of the steps
  - Improve function name
  - Improve parameter names
  - Improve purpose statement
  - Improve and extend tests
- Improve / generalize the function
  - Constants
  - Simplify conditions (because, checked from top)
  - Templates for future functions on this data

# Constants and Simplified Conditions

0.05 LOW-TAX-RATE!

0.10 HIGH-TAX-RATE!

```
sales-tax: (price :Int -> :Int) { # :Int represents Euro
  { price 0 < } { # error
    "sales-tax, error: negative price" err
  }
  { price LOW-TAX-BOUNDARY < } { # :no-tax interval
    0
  }
  { price HIGH-TAX-BOUNDARY < } { # :low-tax interval
    price LOW-TAX-RATE * round
  }
  { true } { # :high-tax interval
    price HIGH-TAX-RATE * round
  }
} cond-fun
```

# ARRAY OPERATIONS

# Arrays Operations

```
>> [1 2 3] 0 "x" set
```

```
[ "x" 2 3 ]
```

```
>> [1 2 3] 4 append
```

```
[ 1 2 3 4 ]
```

```
>> ["hop" "skip"] ["jump" "now"] +
```

```
[ "hop" "skip" "jump" "now" ]
```

```
>> ["hop" "skip" "jump"] "fall" contains
```

```
false
```

- Arrays cannot be modified (in PostFix)
  - cannot be modified once created  
→ are immutable
- Array operations may create a new array



# Strings and Arrays are Immutable

```
"hello" s!  
s 0 "H" set    # new array on stack  
s              # old one still exists  
pop           # remove top value  
s!            # store new value  
s             # now s has new value
```

stack contents:

```
"Hello"  
"Hello" "hello"  
"Hello"  
  
"Hello"
```

# Array Operations

Create an n-element array and initialize it with the given object or executable array, call executable array for each index

- `n {...} array`
- Examples:
- `>> 3 "hello" array`  
`["hello" "hello" "hello" ]`
- `>> 5 {} array`  
`[ 0 1 2 3 4 ]`
- `>> 5 { 1 + } array`  
`[ 1 2 3 4 5 ]`

# Array Operations

```
>> [10 20 30] 20 remove      # remove element (first occurrence)
[ 10 30 ]
```

```
>> [10 20 30] 2 remove-at    # remove at index
[ 10 20 ]
```

```
>> [10 20 30] 0 9 insert     # insert at index
[ 9 10 20 30 ]
```

```
>> [10 20 30] 3 9 insert     # insert at index
[ 10 20 30 9 ]
```

# Array Operations

```
>> [10 20 30] 30 find      # get index of element
2
```

```
>> [10 20 30] 40 find      # returns nil if not found
nil
```

```
      0 1 2 3 4 5
>> [7 8 9 7 8 9] 7 1 find-from  # start at index 1
3
```

# Arrays Operations

```
>>  0 1 2 3 4
    [1 2 3 4 5] 1 3 slice # part of an array
    [ 2 3 ]      # from (inclusive), to (exclusive)
```

```
>> [1 2 3] reverse
    [ 3 2 1 ]
```

```
>> [1 2 3 4 5 6] shuffle
    [ 4 2 5 3 1 6 ]
```

```
>> sort
    [ 1 2 3 4 5 6 ]
```

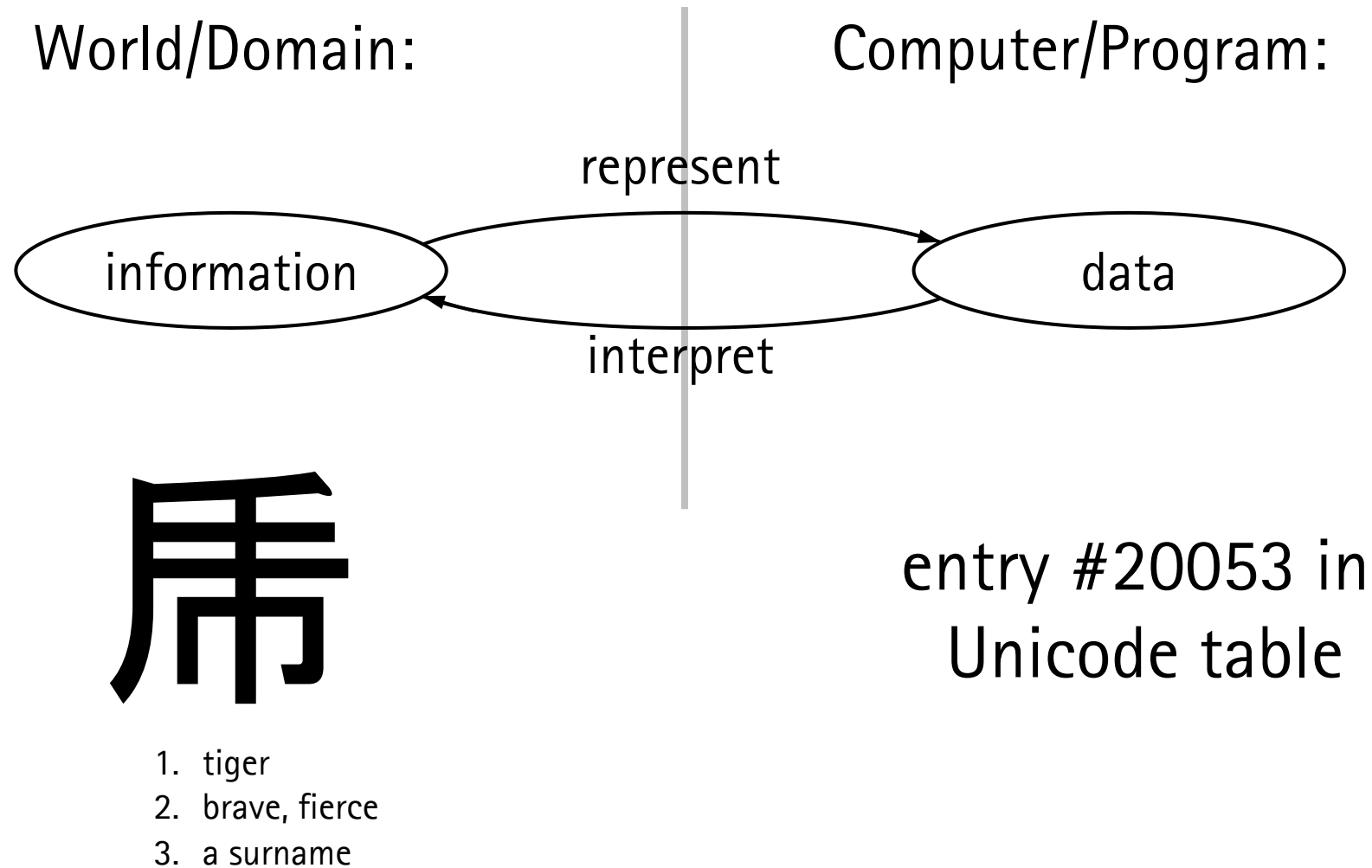
# CHARACTERS AND STRINGS

# Concatenation and Length of Strings

- `>> "what a" " lovely" + " day" +  
"what a lovely day"`

```
>> "abc" length # number of characters  
3
```

# Representing Characters





# Accessing Characters, Strings $\leftrightarrow$ Characters

```
>> "abc" 0 get      # get first character
"a"

>> "abc" str->chars
[97 98 99]          # 'a' has ASCII/Unicode value 97

>> "abc" str->chars 0 get
97                  # extract from array

>> 97 char->str      # convert ASCII/Unicode value
"a"                 # to string

>> 20053 char->str   # convert Unicode value
"厶"
```

# The ASCII Table

- ASCII = American Standard Code for Information Interchange
- Representing characters as numbers
- Interpreting numbers as characters
- Example:
  - character: A (information)
  - represented as number: 65 (data)
- Problem with ASCII: only 7 bits, not enough to encode all characters → Unicode

Decimal	Character	Meaning
0	'\0'	null character
9	'\t'	horizontal tab
10	'\n'	newline
13	'\r'	carriage return
32	' '	blank
33	'!'	
...	...	
47	'/'	
48	'0'	digits
...	...	
57	'9'	
58	':'	
...	...	
65	'A'	uppercase letters
...	...	
90	'Z'	
...	...	
97	'a'	lowercase letters
...	...	
122	'z'	
...	...	

# String Operations

- `"HELLO" lower-case → "hello"`
- `"hello" upper-case → "HELLO"`
- `" hello " trim → "hello"`
- `"hello" "l" "x" replace-first → "hexlo"`
- `"hello" "l" "x" replace-all → "hexxo"`
- `"hello" 0 remove-at → "ello"`
- `"ello" 0 "h" insert → "hello"`

# String Operations

- `"hello" "ll" contains → true`
- `"hello" "lo" find → 3`
- `"hello" "h" 1 find-from → nil`
- `"hello" 2 4 slice → "ll"`
- `"this is nice" " " split → [ "this" "is" "nice" ]`
- `"this,is,nice" "," split → [ "this" "is" "nice" ]`

# LOOPS

## for: Loop over Ranges

- General loop

```
5 x!
```

```
1 i!
```

```
{ i 10 > breakif
```

```
    i x * println
```

```
    i 1 + i!
```

```
} loop
```

- for loop over range

```
5 x!
```

```
1 11 {
```

```
    x * println
```

```
} for
```

lower upper {...} for

- lower index inclusive
- upper index exclusive

## for: Loop over Ranges

- with indices on the stack

```
1 11 {
    x * println
} for
```

- with index variable i

```
5 x!
1 11 { i!
    i x * println
} for
```

- with index variable i and lam

```
1 11 { i!
    i x * println
} lam for
```

- with lam and parameters

```
1 11 (i) {
    i x * println
} lam for
```

# Nested Loops

```
1 5 { row!
    1 10 { column!
        row print "," print column print " " print
    } for
    "" println
} for
```

## ■ Output:

```
1,1 1,2 1,3 1,4 1,5 1,6 1,7 1,8 1,9
2,1 2,2 2,3 2,4 2,5 2,6 2,7 2,8 2,9
3,1 3,2 3,3 3,4 3,5 3,6 3,7 3,8 3,9
4,1 4,2 4,3 4,4 4,5 4,6 4,7 4,8 4,9
```

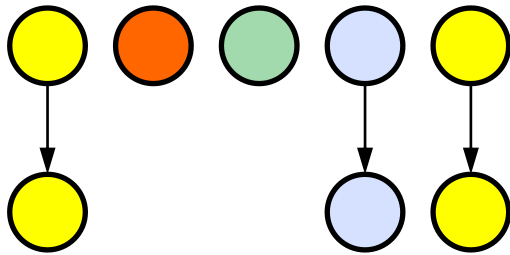


# ARRAY-PROCESSING OPERATIONS

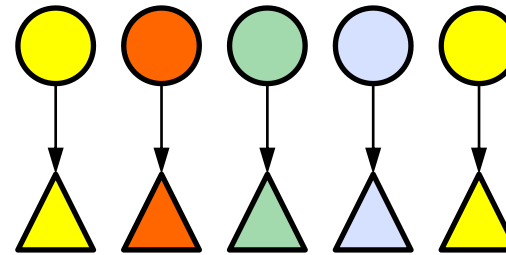
## (OPTIONAL TOPIC)

# Array-Processing Operations: filter, map, fold/reduce

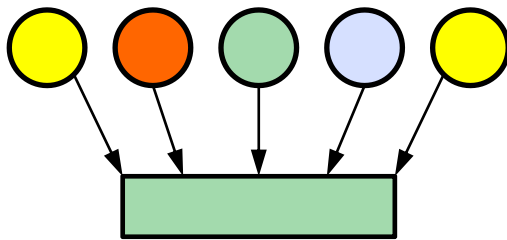
filter:



map:



fold / reduce:



- Operations on each element of an array
- Treat the array as a whole
- Powerful form of abstraction

## for: Loop over Arrays (map)

```
[10 20 30] a!
```

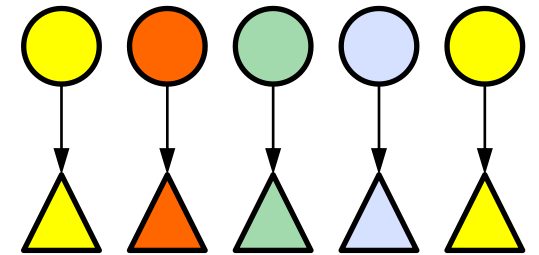
```
>> a { print } for # print each element
102030
```

```
>> [ a { 1 + } for ] # add 1 to each element, new array
[ 11 21 31 ]
```

```
>> ["peanut sauce" "rice" "vegetables"] a!
```

```
>> [a { "!" + } for]
[ "peanut sauce!" "rice!" "vegetables!" ]
```

map:



## for: Loop over Arrays (fold/reduce)

```
>> [10 20 30] a!
```

```
>> 0 a {+} for # compute the sum
```

```
60
```

```
>> ["vegetables" "rice" "pizza" "burger"] a!
```

```
>> 0 a {length +} for # total number of characters
```

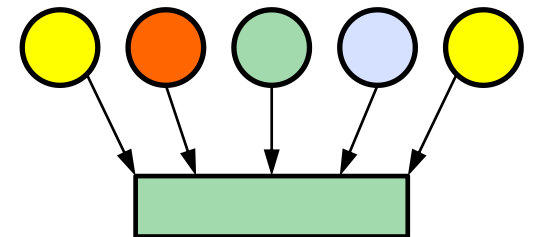
```
25
```

```
>> [1 "hello" -3.14 "world" :yummy] a!
```

```
>> 0 a { str? { 1 + } if } for # count strings only
```

```
2
```

fold / reduce:



# for: Loop over Arrays (forall)

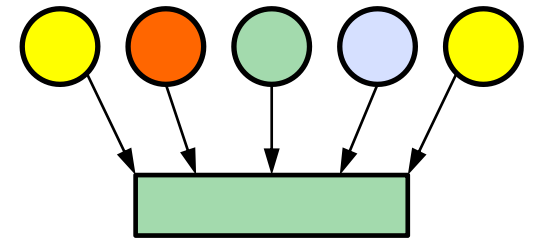
```
forall: (a :Arr, predicate :ExeArr -> :Bool) {
  true
  a {
    predicate not {
      pop false break
    } if
  } for
} fun
```

```
>> [1 2 3 4] {3 <} forall
false
>> [1 2 3 4] {5 <} forall
true
```

true iff, the  
predicate holds for  
all array elements

iff = if an only if

fold / reduce:



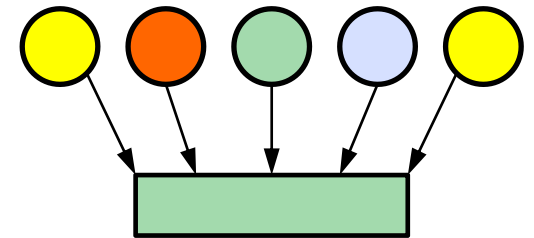
## for: Loop over Arrays (exists)

```
exists: (a :Arr, predicate :ExeArr -> :Bool) {
  false
  a {
    predicate { pop true break } if
  } for
} fun
```

true, iff the predicate  
holds for at least one  
array element

```
>> [1 2 3 4] {1 <} exists
false
>> [1 2 3 4] {2 <} exists
true
```

fold / reduce:

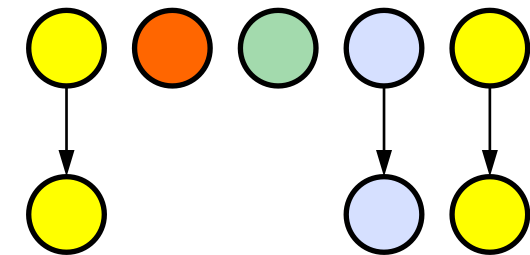


## for: Loop over Arrays (filter)

```
>> [1 "hello" -3.14 "world" :yummy] a!
>> [ a (x) { x str? { x } if } lam for ]
[ "hello" "world" ]
```

```
>>[ a { dup str? not { pop } if } for ]
[ "hello" "world" ]
```

filter:



## for: Loop over Arrays (filter)

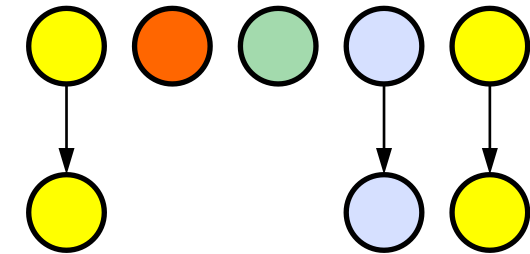
```
filter: (a :Arr, predicate :ExeArr) {
  [a { dup predicate not { pop } if } for]
} fun
```

```
>> [1 0 6 -3] { 0 > } filter
[ 1 6 ]
```

```
>> ["a" "b" 6 -3] { int? } filter
[ 6 -3 ]
```

```
>> ["a" "b" 6 -3] { str? } filter
[ "a" "b" ]
```

filter:



only keep the  
elements for which  
the predicate holds



# Summary

- Operators
  - $\{p_1 p_2 \dots\}$  and/or, cond, cond-fun, stack, types
- Enumerations
  - Fixed number of categories (:cat, :dog, :mouse)
- Intervals
  - One or more ranges of numbers
  - (:no-tax :low-tax :high-tax + interval boundaries)
- Array operations
- Characters and Strings
- Loops