



# Rechnernetze - Computer Networks

## Problem Set 8: Internetworking & Routing

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## 1.1 Difference between forwarding, switching and routing:

- ▶ **Forwarding:** router-local action of transferring a packet from an input link interface to the appropriate output link interface.
- ▶ **Switching:** moving packets between devices on the same network.
- ▶ **Routing:** a network-wide process that determine the end-to-end paths that packets take from source to destination.



## 1.2 Link-state vs. distance-vector routing

### ▶ **Link-state routing**

- ▶ Nodes intercommunicate with all other nodes via broadcast ...
- ▶ and provide the costs of the directly connected links
- ▶ Requires knowledge of the entire network topology

### ▶ **Distance-vector routing**

- ▶ Only neighbouring nodes exchange information ...
- ▶ they provide each least-cost estimates from itself to all other (known) nodes
- ▶ Requires only connections to the neighbours and no topology information



## 1.3 Link cost selection

- ▶ Can be chosen arbitrarily
- ▶ Often associated with a network metric, e.g., bandwidth, delay
- ▶ Can force traffic to flow along a certain path

## 1.4 Drawbacks of dynamic link weights

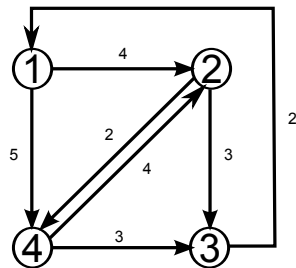
- ▶ More responsive to network changes
- ▶ Can cause routing instabilities such as routing loops and oscillations

## 1.5 Internet routing

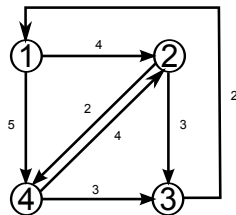
- ▶ Interconnected autonomous systems (ASes)
- ▶ Intra-domain (local) routing within each AS
- ▶ Inter-domain routing: edge routers forward packets to neighbouring ASes

## 2.1 Plot the topology:

$$E = \begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \end{pmatrix}, \quad C = \begin{pmatrix} 0 & 4 & 0 & 5 \\ 0 & 0 & 3 & 2 \\ 2 & 0 & 0 & 0 \\ 0 & 4 & 3 & 0 \end{pmatrix}$$



$$E = \begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \end{pmatrix}$$



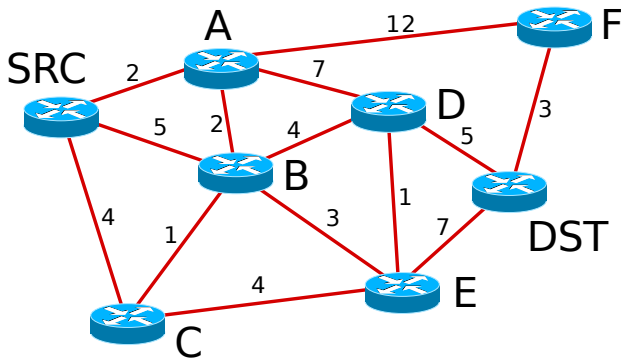
- ▶  $E$  denotes the nodes that are reachable in one step
- ▶  $E^2$  denotes the number of two step paths
- ▶  $E^3$  denotes the number of three step paths ...

$$E^2 = \begin{pmatrix} 0 & 1 & 2 & 1 \\ 1 & 1 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 \end{pmatrix}, \quad E^3 = \begin{pmatrix} 2 & 1 & 2 & 1 \\ 1 & 1 & 1 & 2 \\ 0 & 1 & 2 & 1 \\ 1 & 2 & 1 & 1 \end{pmatrix}, \quad E^4 = \begin{pmatrix} 2 & 3 & 2 & 3 \\ 1 & 3 & 3 & 2 \\ 2 & 1 & 2 & 1 \\ 1 & 2 & 3 & 3 \end{pmatrix}$$



$$E + E^2 + E^3 + E^4 = \begin{pmatrix} 4 & 6 & 6 & 6 \\ 3 & 5 & 6 & 5 \\ 3 & 3 & 4 & 3 \\ 3 & 5 & 6 & 5 \end{pmatrix}$$

Since all matrix elements are non-zero, all nodes are reachable.



Least-cost path SRC  $\rightarrow$  DST ?





Denote

- ▶  $c(i, j)$  the cost of link  $e_{i,j}$  from node  $i$  to node  $j$ 
  - ▶  $c(i, j) = \infty$  if link  $e_{i,j}$  does not exist
- ▶  $d(i)$  cost (distance) from the source to node  $i$
- ▶  $p(i)$  predecessor of node  $i$  on the least-cost path from the source to node  $i$
- ▶  $M$  set of nodes for which least-cost paths are uniquely determined

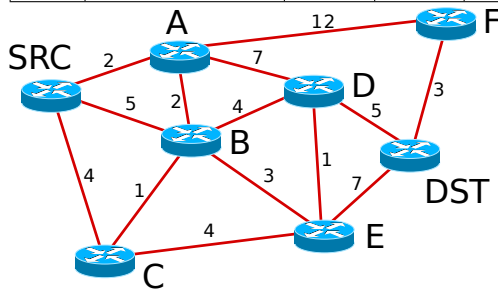


```
1:  $M = \{a\}$ 
2: for all nodes  $i$  do
3:   if link  $e_{a,i}$  exists then
4:      $d(i) = c(a, i)$ 
5:   else
6:      $d(i) = \infty$ 
7:   end if
8: end for
9: repeat
10:  find a node  $j$  not in  $M$  such that  $d(j)$  is minimal
11:  add  $j$  to  $M$ 
12:  for all nodes  $k$  not in  $M$  do
13:    if  $d(k) > d(j) + c(j, k)$  then
14:       $d(k) = d(j) + c(j, k)$ 
15:       $p(k) = j$ 
16:    end if
17:  end for
18: until all nodes in  $M$ 
```

# 3.1 Dijkstra's Algorithm - Example



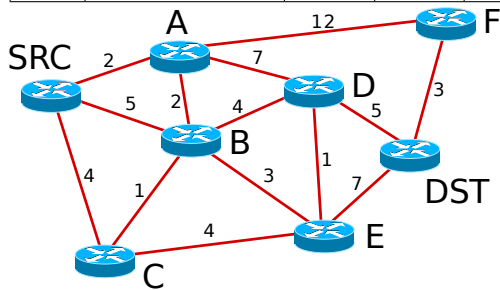
step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	$2_{SRC}$	$5_{SRC}$	$4_{SRC}$	$\infty$	$\infty$	$\infty$	$\infty$



# 3.1 Dijkstra's Algorithm - Example



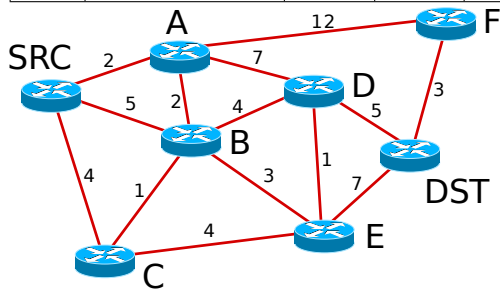
step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	$2_{SRC}$	$5_{SRC}$	$4_{SRC}$	$\infty$	$\infty$	$\infty$	$\infty$
1	SRC,A		$4_A$	$4_{SRC}$	$9_A$	$\infty$	$14_A$	$\infty$



# 3.1 Dijkstra's Algorithm - Example



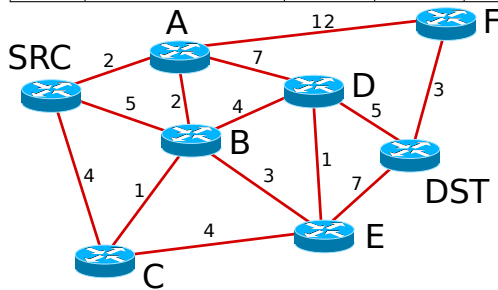
step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	$2_{SRC}$	$5_{SRC}$	$4_{SRC}$	$\infty$	$\infty$	$\infty$	$\infty$
1	SRC,A		$4_A$	$4_{SRC}$	$9_A$	$\infty$	$14_A$	$\infty$
2.1	SRC,A,B			$4_{SRC}$	$8_B$	$7_B$	$14_A$	$\infty$



# 3.1 Dijkstra's Algorithm - Example



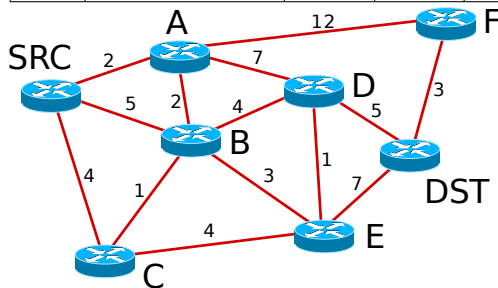
step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	$2_{SRC}$	$5_{SRC}$	$4_{SRC}$	$\infty$	$\infty$	$\infty$	$\infty$
1	SRC,A		$4_A$	$4_{SRC}$	$9_A$	$\infty$	$14_A$	$\infty$
2.1	SRC,A,B			$4_{SRC}$	$8_B$	$7_B$	$14_A$	$\infty$
2.2	SRC,A,C		$4_A$		$9_A$	$8_C$	$14_A$	$\infty$



# 3.1 Dijkstra's Algorithm - Example



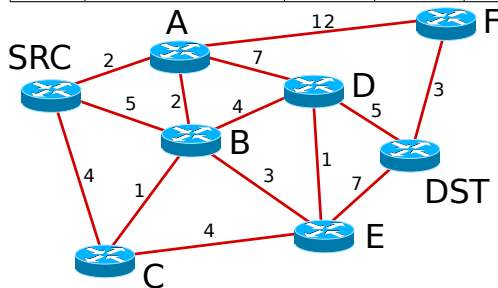
step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	<b>2</b> <sub>SRC</sub>	5 <sub>SRC</sub>	4 <sub>SRC</sub>	∞	∞	∞	∞
1	SRC,A		<b>4</b> <sub>A</sub>	<b>4</b> <sub>SRC</sub>	9 <sub>A</sub>	∞	14 <sub>A</sub>	∞
2	SRC,A,B			<b>4</b> <sub>SRC</sub>	8 <sub>B</sub>	<b>7</b> <sub>B</sub>	14 <sub>A</sub>	∞
3	SRC,A,B,C				8 <sub>B</sub>	<b>7</b> <sub>B</sub>	14 <sub>A</sub>	∞



# 3.1 Dijkstra's Algorithm - Example



step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	<b>2<sub>SRC</sub></b>	5 <sub>SRC</sub>	4 <sub>SRC</sub>	∞	∞	∞	∞
1	SRC,A		<b>4<sub>A</sub></b>	<b>4<sub>SRC</sub></b>	9 <sub>A</sub>	∞	14 <sub>A</sub>	∞
2	SRC,A,B			<b>4<sub>SRC</sub></b>	8 <sub>B</sub>	<b>7<sub>B</sub></b>	14 <sub>A</sub>	∞
3	SRC,A,B,C				8 <sub>B</sub>	<b>7<sub>B</sub></b>	14 <sub>A</sub>	∞
4	SRC,A,B,C,E				<b>8<sub>B</sub></b>		14 <sub>A</sub>	14 <sub>E</sub>

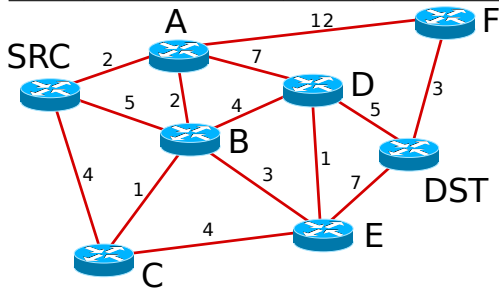




# 3.1 Dijkstra's Algorithm - Example



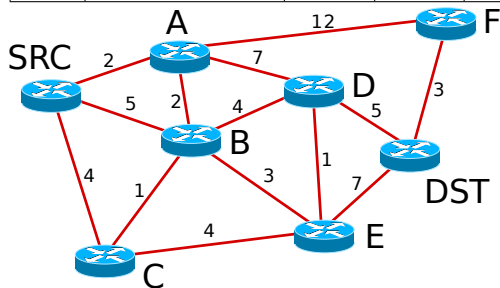
step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	<b>2<sub>SRC</sub></b>	5 <sub>SRC</sub>	4 <sub>SRC</sub>	∞	∞	∞	∞
1	SRC,A		<b>4<sub>A</sub></b>	<b>4<sub>SRC</sub></b>	9 <sub>A</sub>	∞	14 <sub>A</sub>	∞
2	SRC,A,B			<b>4<sub>SRC</sub></b>	8 <sub>B</sub>	<b>7<sub>B</sub></b>	14 <sub>A</sub>	∞
3	SRC,A,B,C				8 <sub>B</sub>	<b>7<sub>B</sub></b>	14 <sub>A</sub>	∞
4	SRC,A,B,C,E				<b>8<sub>B</sub></b>		14 <sub>A</sub>	14 <sub>E</sub>
5	SRC,A,B,C,E,D						14 <sub>A</sub>	<b>13<sub>D</sub></b>



# 3.1 Dijkstra's Algorithm - Example



step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	<b>2<sub>SRC</sub></b>	5 <sub>SRC</sub>	4 <sub>SRC</sub>	∞	∞	∞	∞
1	SRC,A		<b>4<sub>A</sub></b>	<b>4<sub>SRC</sub></b>	9 <sub>A</sub>	∞	14 <sub>A</sub>	∞
2	SRC,A,B			<b>4<sub>SRC</sub></b>	8 <sub>B</sub>	<b>7<sub>B</sub></b>	14 <sub>A</sub>	∞
3	SRC,A,B,C				8 <sub>B</sub>	<b>7<sub>B</sub></b>	14 <sub>A</sub>	∞
4	SRC,A,B,C,E				<b>8<sub>B</sub></b>		14 <sub>A</sub>	14 <sub>E</sub>
5	SRC,A,B,C,E,D						14 <sub>A</sub>	<b>13<sub>D</sub></b>
6	SRC,A,B,C,E,D,DST						<b>14<sub>A</sub></b>	



# 3.1 Dijkstra's Algorithm - Example

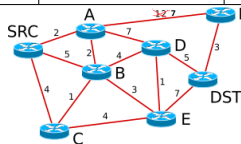


step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	<b>2</b> <sub>SRC</sub>	5 <sub>SRC</sub>	4 <sub>SRC</sub>	∞	∞	∞	∞
1	SRC,A		<b>4</b> <sub>A</sub>	<b>4</b> <sub>SRC</sub>	9 <sub>A</sub>	∞	14 <sub>A</sub>	∞
2	SRC,A,B			<b>4</b> <sub>SRC</sub>	8 <sub>B</sub>	<b>7</b> <sub>B</sub>	14 <sub>A</sub>	∞
3	SRC,A,B,C				8 <sub>B</sub>	<b>7</b> <sub>B</sub>	14 <sub>A</sub>	∞
4	SRC,A,B,C,E				<b>8</b> <sub>B</sub>		14 <sub>A</sub>	14 <sub>E</sub>
5	SRC,A,B,C,E,D						14 <sub>A</sub>	<b>13</b> <sub>D</sub>
6	SRC,A,B,C,E,D,DST						<b>14</b> <sub>A</sub>	
7	SRC,A,B,C,E,D,DST,F							

The least-cost path from *SRC* to *DST* has a cost of **13** over the path **SRC-A-B-D-DST**.

Link A-F Cost: 12  $\rightarrow$  7

step	M	d(A)	d(B)	d(C)	d(D)	d(E)	d(F)	d(DST)
init	SRC	$2_{SRC}$	$5_{SRC}$	$4_{SRC}$	$\infty$	$\infty$	$\infty$	$\infty$
1	SRC,A		$4_A$	$4_{SRC}$	$9_A$	$\infty$	$14_A$ <del><math>14_A</math></del> $9_A$	$\infty$
2	SRC,A,B			$4_{SRC}$	$8_B$	$7_B$	$14_A$ <del><math>14_A</math></del> $9_A$	$\infty$
3	SRC,A,B,C				$8_B$	$7_B$	$14_A$ <del><math>14_A</math></del> $9_A$	$\infty$
4	SRC,A,B,C,E				$8_B$		$14_A$ <del><math>14_A</math></del> $9_A$	$14_E$
5	SRC,A,B,C,E,D						$14_A$ <del><math>14_A</math></del> $9_A$	$13_D$ $13_D$
6	SRC,A,B,C,E,D,DST <del>SRC,A,B,C,E,D,DST</del> $SRC,A,B,C,E,D,F$						$14_A$ <del><math>14_A</math></del>	$12_F$
7	SRC,A,B,C,E,D,DST,F <del>SRC,A,B,C,E,D,DST,F</del> $SRC,A,B,C,E,D,F,DST$							



The least-cost path from *SRC* to *DST* has then a cost of **12** over the path **SRC-A-F-DST** (instead of *SRC* – *A* – *B* – *D* – *DST*).



## Denote

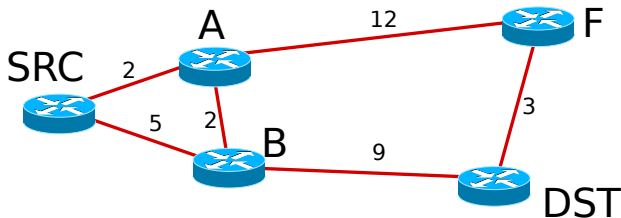
- ▶  $D^x$  distance table of node  $x$ 
  - ▶ example:  $D^x(y, z) = 4$  route to destination  $y$  has cost 4 via next hop  $z$
- ▶  $F^x$  forwarding table of node  $x$ 
  - ▶ example:  $F^x(y) = (4, z)$  shortest path to destination  $y$  via next hop  $z$  has cost 4

## Mode of operation

- ▶ node  $z$  computes the shortest path to destination  $y$  as
$$c(z, y) = \min_w \{D^z(y, w)\}$$
- ▶ node  $z$  stores the next hop  $w$  that achieves the minimum in its forwarding table  $F^z(y) = (c(z, y), w)$
- ▶ node  $z$  sends its forwarding table to its neighboring node  $x$
- ▶ node  $x$  computes  $D^x(y, z) = c(x, z) + c(z, y)$



```
1: for all neighbors  $y$  do
2:    $D^x(y, y) = c(x, y)$ 
3: end for
4: for all destinations  $z$  do
5:   send  $\min_w \{D^x(z, w)\}$  to all neighbors  $y$ 
6: end for
7: loop
8:   if  $c(x, y)$  for neighbor  $y$  changes by  $d$  then
9:     update  $D^x(z, y) = D^x(z, y) + d$  for all destinations  $z$ 
10:  else if updated  $c(y, z)$  received from neighbor  $y$  then
11:    recompute  $D^x(z, y) = c(x, y) + c(y, z)$ 
12:  end if
13:  if a new  $\min_w \{D^x(z, w)\}$  exists for any destination  $z$  then
14:    send new  $\min_w \{D^x(z, w)\}$  to all neighbors  $y$ 
15:  end if
16: end loop
```



Least-cost path SRC → DST ?

## 4.1 Distance Vector Algorithm Example



**initialization:** the distance vector of each host  $x$  is initialized with the link cost  $c(x, y)$  to the direct node neighbors  $y$ :

$$D^x(y, y) = c(x, y)$$

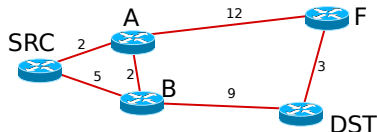
$D^S$	A	B
A	2	
B		5
F		
D		

$D^A$	S	B	F
S	2		
B		2	
F			12
D			

$D^B$	S	A	D
S	5		
A		2	
F			
D			9

$D^F$	A	D
S		
A	12	
B		
D		3

$D^D$	B	F
S		
A		
B	9	
F		3



Each node sends an update to all of its neighbors.



**T=1**

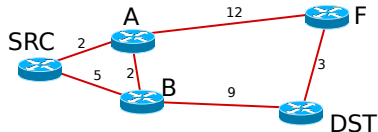
$D^S$	A	B
A	<b>2</b>	7
B	<u><b>4</b></u>	5
F	<u><b>14</b></u>	
D		<u><b>14</b></u>

$D^A$	S	B	F
S	2	7	
B	7	<b>2</b>	
F			<b>12</b>
D		<u><b>11</b></u>	15

$D^B$	S	A	D
S	5	<u><b>4</b></u>	
A	7	<b>2</b>	
F		14	<u><b>12</b></u>
D			<b>9</b>

$D^F$	A	D
S	<u><b>14</b></u>	
A	<b>12</b>	
B	14	<u><b>12</b></u>
D		<b>3</b>

$D^D$	B	F
S	<u><b>14</b></u>	
A	<u><b>11</b></u>	15
B	<b>9</b>	
F		<b>3</b>

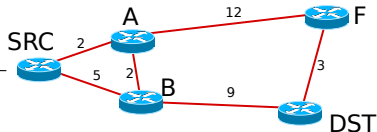


Each node sends an update to all of its neighbors when a cheaper path is discovered

**T=2**

$D^S$	A	B	$D^A$	S	B	F	$D^B$	S	A	D
A	<b>2</b>	7	S	<b>2</b>	6	26	S	5	<b>4</b>	23
B	<b>4</b>	5	B	6	<b>2</b>	24	A	7	<b>2</b>	20
F	<b>14</b>	16	F	16	14	<b>12</b>	F	19	14	<b>12</b>
D	<u><b>13</b></u>	14	D	16	<b>11</b>	15	D	19	13	<b>9</b>

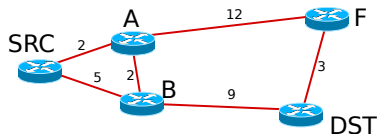
$D^F$	A	D	$D^D$	B	F
S	<b>14</b>	17	S	<u><b>13</b></u>	17
A	<b>12</b>	14	A	<b>11</b>	15
B	14	<b>12</b>	B	<b>9</b>	15
D	23	<b>3</b>	F	21	<b>3</b>



**T=3**

$D^S$	A	B	$D^A$	S	B	F	$D^B$	S	A	D
A	<b>2</b>	7	S	<b>2</b>	6	26	S	5	<b>4</b>	22
B	<b>4</b>	5	B	6	<b>2</b>	24	A	7	<b>2</b>	20
F	<b>14</b>	16	F	16	14	<b>12</b>	F	19	14	<b>12</b>
D	<b>13</b>	14	D	15	<b>11</b>	15	D	17	13	<b>9</b>

$D^F$	A	D	$D^D$	B	F
S	<b>14</b>	16	S	<b>13</b>	17
A	<b>12</b>	14	A	<b>11</b>	15
B	14	<b>12</b>	B	<b>9</b>	15
D	23	<b>3</b>	F	21	<b>3</b>



Distance vectors reached stable-state, no more updates sent

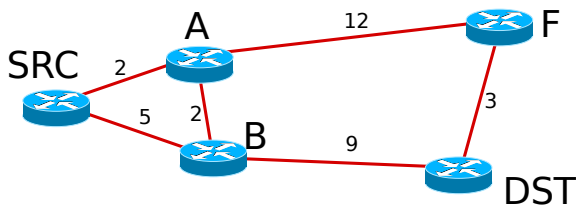


Example, Forwarding table for A after step 3:

$D^A$	S	B	F
S	<b>2</b>	6	26
B	6	<b>2</b>	24
F	16	14	<b>12</b>
D	15	<b>11</b>	15

$F^A$	
S	2,S
B	2,B
F	12,F
D	11,B

## 4.2 Distance Vector Algorithm Example



Path SRC  $\rightarrow$  DST ?

After  $t=1$ : SRC  $\rightarrow$  B  $\rightarrow$  DST

After  $t=2$ : SRC  $\rightarrow$  A  $\rightarrow$  B  $\rightarrow$  DST