Modality effects in a signalling game

Intro

This script uses data compiled by *analyseData.R*.

Load libraries

```r
library(lme4)
library(sjPlot)
library(ggplot2)
library(lattice)
library(influence.ME)
```

Load data

```r
d = read.csv("../../data/FinalSignalData.csv")
```

We don't need info on every signal in each turn, just the trial time. Keep only 1st signal in each trial.

```r
d = d[!duplicated(d$trialString),]
```

Descriptive stats

Here is a graph showing the distribution of trial lengths by conditions:

The distribution of trial times is very skewed:
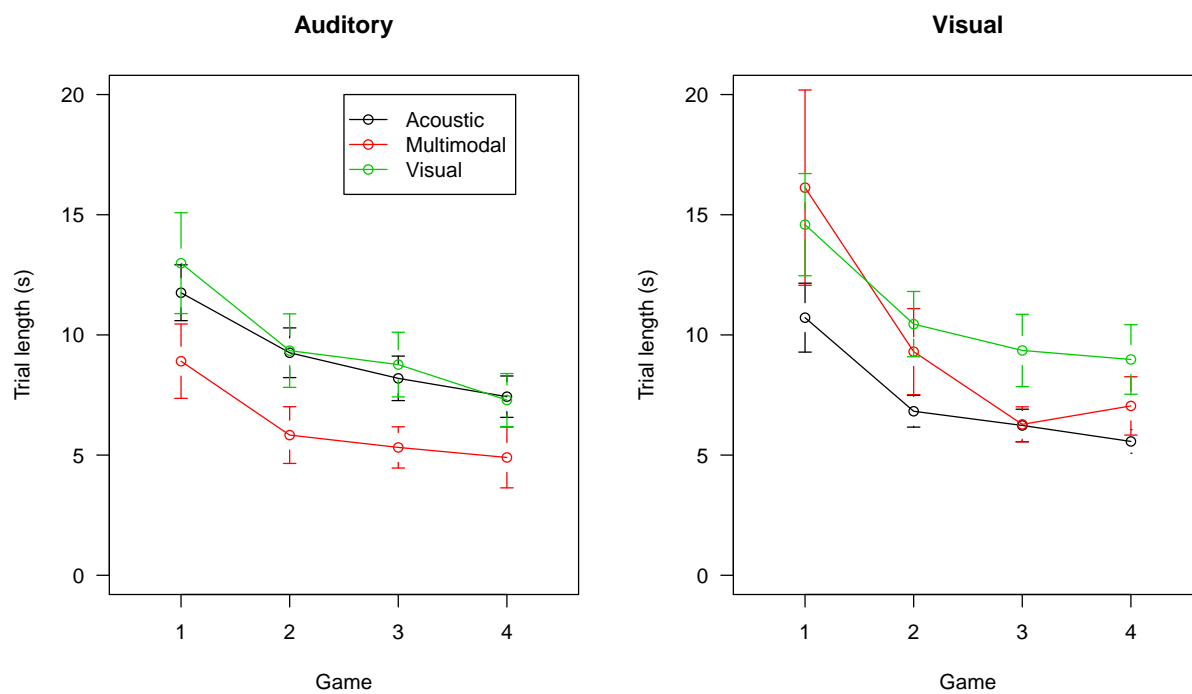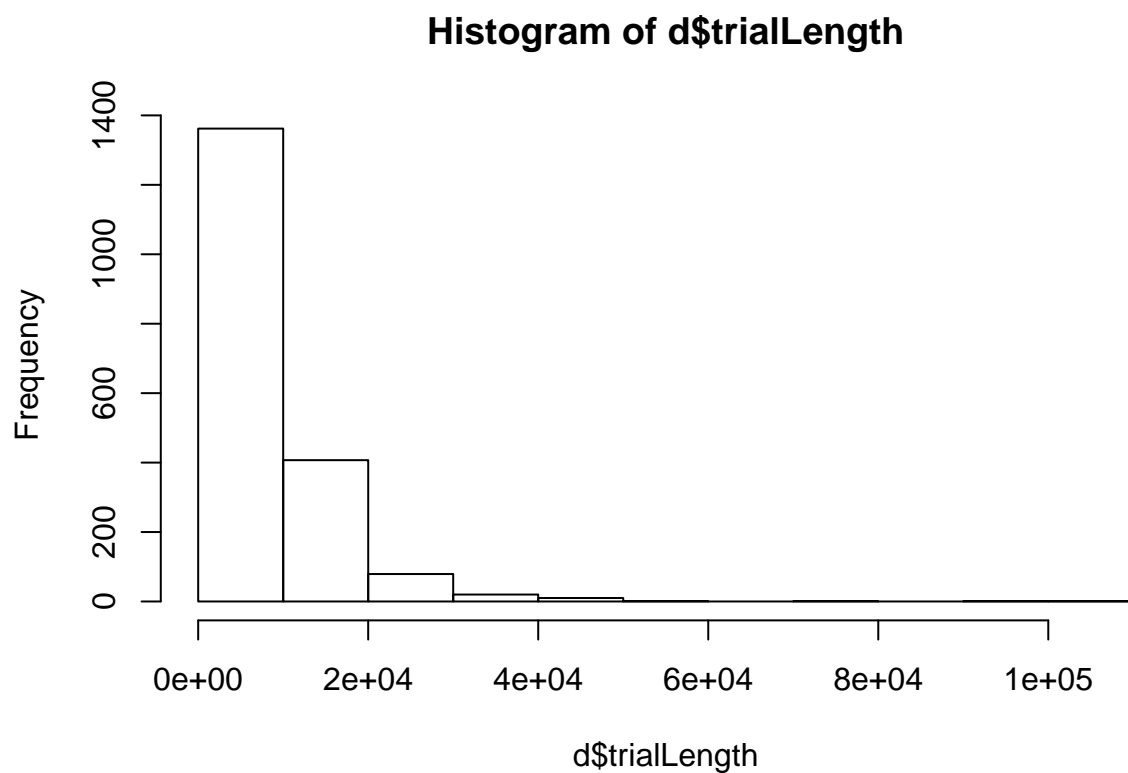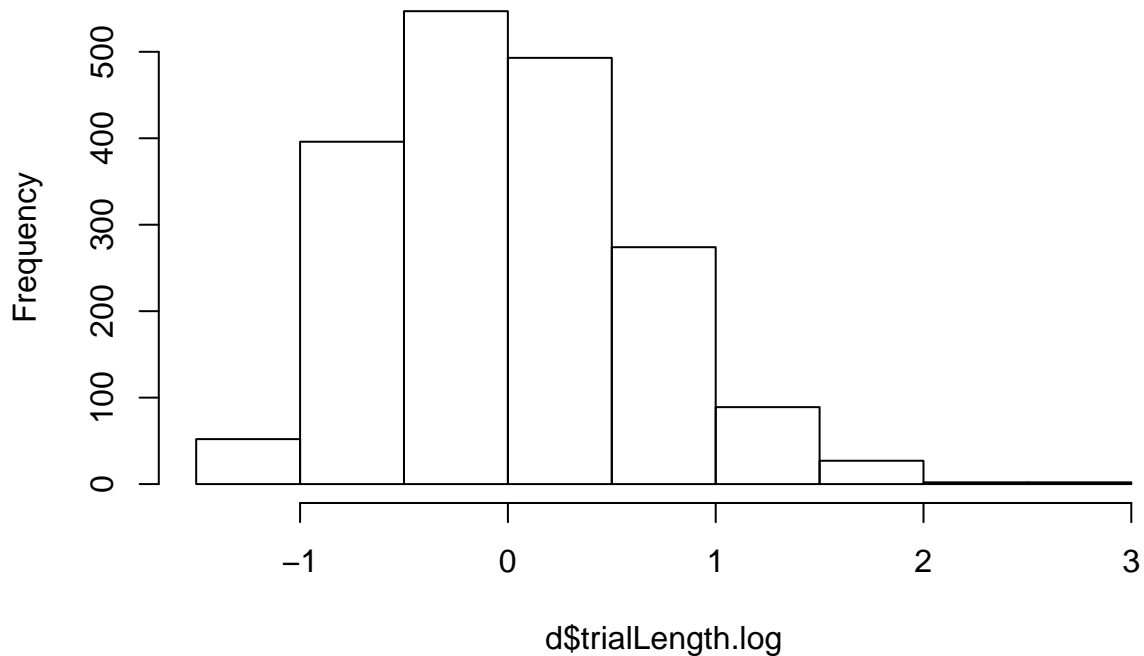
```r
hist(d$trialLength)
```

Figure 1: The efficiency of trials in different conditions

So we transform it using a log transform, then center the data.

```
d$trialLength.log = log(d$trialLength)
meanLogTrialLength = mean(d$trialLength.log)
d$trialLength.log = d$trialLength.log - meanLogTrialLength
hist(d$trialLength.log)
```

Histogram of d$trialLength.log

Make a variable to represent proportion of games played:

```
# Make a variable that represents the number of trials played
d$trialTotal = d$trial + (d$game * (max(d$trial)+1))
# Convert to proportion of games played, so that estimates reflect change per game.
d$trialTotal = d$trialTotal / 16
# Center the trialTotal variable so intercept reflects after the first game
d$trialTotal = d$trialTotal - 1
```

Make a variable for which stimuli the players experienced first.

```
firstBlock = tapply(as.character(d$condition),d$dyadNumber,head,n=1)
d$firstBlock = as.factor(firstBlock[match(d$dyadNumber,names(firstBlock))])
```

Reorder some levels so that the intercept reflects the most frequent condition.

```
d$incorrect = !d$correct
```

Mixed models

Make a series of models with random effects for dyad, director (nested within dyad) and item.

Not all random slopes are appropriate. For example, items are used in only one stimulus condition, so a random slope for condition by item is not appropriate. Similarly, each dyad only plays in one modality condition.

It's reasonable to have a random slope for trial by dyad, but this caused unreliable model convergence, so is not included.

The final random slopes were for condition and incorrectness by dyad/player, and modality condition by item.

```
# No fixed effects
m0 = lmer(trialLength.log ~ 1 +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add modality condition
modality = lmer(trialLength.log ~ 1 + modalityCondition +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add stimulus condition
cond = lmer(trialLength.log ~ 1 + modalityCondition + condition +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add trial total
game = lmer(trialLength.log ~ 1 + modalityCondition + condition + trialTotal +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
```

```
# Add interaction between condition and stimulus condition
modXcond =  lmer(trialLength.log ~ 1 + modalityCondition * condition + trialTotal +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
```

```
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : unable to evaluate scaled gradient

## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : Model failed to converge: degenerate Hessian with 1 negative
## eigenvalues
```

```
# Add interaction between condition and trial
conXgame = lmer(trialLength.log ~ 1 + (modalityCondition * condition) + trialTotal +
            (trialTotal:condition) +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add interaction between modality and trial
modXgame = lmer(trialLength.log ~ 1 + (modalityCondition * condition) + trialTotal +
            (trialTotal:condition) + (modalityCondition:game) +
            (1 + condition + incorrect |dyadNumber/playerId) +
```

```r
            (1 + modalityCondition|itemId),
          data=d)


# Add 3-way interaction
moXcoXga = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add whether the response was incorrect
incor = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            incorrect +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add the interaction between modality and incorrectness
moXincor = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            incorrect + (modalityCondition:incorrect) +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add the interaction between condition and incorrectness
coXincor = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            incorrect + (modalityCondition:incorrect) +
              (condition:incorrect) +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add the three-way interaction between condition, modality and incorrectness
coXmoXin = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            (incorrect*condition*modalityCondition)+
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)



# Add the quadratic effect of trial
gamQuad = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            I(trialTotal^2) +
            (incorrect*condition*modalityCondition)+
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add interaction between quadratic effect of trial and modality
modXgamQ = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            I(trialTotal^2) +
            (incorrect*condition*modalityCondition)+
            (modalityCondition:I(trialTotal^2)) +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
          data=d)
# Add block order
block = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            I(trialTotal^2) +
```

```
            (incorrect*condition*modalityCondition)+
            (modalityCondition:I(trialTotal^2)) +
            firstBlock +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
        data=d)
# Add interaction between block order and modality
blocXmod = lmer(trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
            I(trialTotal^2) +
            (incorrect*condition*modalityCondition)+
            (modalityCondition:I(trialTotal^2)) +
            firstBlock * modalityCondition +
            (1 + condition + incorrect |dyadNumber/playerId) +
            (1 + modalityCondition|itemId),
        data=d)
```

Results

Compare the fit of the models:

```
anova(m0,modality,cond,game,modXcond,conXgame, modXgame,
      moXcoXga,incor,moXincor,coXincor,coXmoXin,
      gamQuad,modXgamQ,block, blocXmod)
```

```
## refitting model(s) with ML (instead of REML)

## Data: d
## Models:
## m0: trialLength.log ~ 1 + (1 + condition + incorrect | dyadNumber/playerId) +
## m0:      (1 + modalityCondition | itemId)
## modality: trialLength.log ~ 1 + modalityCondition + (1 + condition + incorrect |
## modality:     dyadNumber/playerId) + (1 + modalityCondition | itemId)
## cond: trialLength.log ~ 1 + modalityCondition + condition + (1 + condition +
## cond:      incorrect | dyadNumber/playerId) + (1 + modalityCondition |
## cond:      itemId)
## game: trialLength.log ~ 1 + modalityCondition + condition + trialTotal +
## game:      (1 + condition + incorrect | dyadNumber/playerId) + (1 +
## game:      modalityCondition | itemId)
## modXcond: trialLength.log ~ 1 + modalityCondition * condition + trialTotal +
## modXcond:      (1 + condition + incorrect | dyadNumber/playerId) + (1 +
## modXcond:      modalityCondition | itemId)
## conXgame: trialLength.log ~ 1 + (modalityCondition * condition) + trialTotal +
## conXgame:      (trialTotal:condition) + (1 + condition + incorrect | dyadNumber/playerId) +
## conXgame:      (1 + modalityCondition | itemId)
## modXgame: trialLength.log ~ 1 + (modalityCondition * condition) + trialTotal +
## modXgame:      (trialTotal:condition) + (modalityCondition:game) + (1 +
## modXgame:      condition + incorrect | dyadNumber/playerId) + (1 + modalityCondition |
## modXgame:      itemId)
## moXcoXga: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
## moXcoXga:      (1 + condition + incorrect | dyadNumber/playerId) + (1 +
## moXcoXga:      modalityCondition | itemId)
## incor: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
## incor:      incorrect + (1 + condition + incorrect | dyadNumber/playerId) +
## incor:      (1 + modalityCondition | itemId)
## moXincor: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
## moXincor:      incorrect + (modalityCondition:incorrect) + (1 + condition +
## moXincor:      incorrect | dyadNumber/playerId) + (1 + modalityCondition |
## moXincor:      itemId)
## coXincor: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
## coXincor:      incorrect + (modalityCondition:incorrect) + (condition:incorrect) +
## coXincor:      (1 + condition + incorrect | dyadNumber/playerId) + (1 +
## coXincor:      modalityCondition | itemId)
## coXmoXin: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
## coXmoXin:      (incorrect * condition * modalityCondition) + (1 + condition +
## coXmoXin:      incorrect | dyadNumber/playerId) + (1 + modalityCondition |
## coXmoXin:      itemId)
## gamQuad: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
## gamQuad:      I(trialTotal^2) + (incorrect * condition * modalityCondition) +
## gamQuad:      (1 + condition + incorrect | dyadNumber/playerId) + (1 +
## gamQuad:      modalityCondition | itemId)
## modXgamQ: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
```

```
## modXgamQ:      I(trialTotal^2) + (incorrect * condition * modalityCondition) +
## modXgamQ:      (modalityCondition:I(trialTotal^2)) + (1 + condition + incorrect |
## modXgamQ:      dyadNumber/playerId) + (1 + modalityCondition | itemId)
## block: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
## block:      I(trialTotal^2) + (incorrect * condition * modalityCondition) +
## block:      (modalityCondition:I(trialTotal^2)) + firstBlock + (1 + condition +
## block:      incorrect | dyadNumber/playerId) + (1 + modalityCondition |
## block:      itemId)
## blocXmod: trialLength.log ~ 1 + modalityCondition * condition * trialTotal +
## blocXmod:      I(trialTotal^2) + (incorrect * condition * modalityCondition) +
## blocXmod:      (modalityCondition:I(trialTotal^2)) + firstBlock * modalityCondition +
## blocXmod:      (1 + condition + incorrect | dyadNumber/playerId) + (1 +
## blocXmod:      modalityCondition | itemId)
##           Df    AIC    BIC  logLik deviance   Chisq Chi Df Pr(>Chisq)
## m0        20 2694.4 2805.2 -1327.2   2654.4
## modality  22 2696.0 2817.9 -1326.0   2652.0   2.4050      2  0.3004443
## cond      23 2697.3 2824.7 -1325.7   2651.3   0.7147      1  0.3978805
## game      24 2309.0 2441.9 -1130.5   2261.0 390.3345      1  < 2.2e-16 ***
## modXcond  26 2301.2 2445.2 -1124.6   2249.2  11.7749      2  0.0027741 **
## conXgame  27 2302.9 2452.4 -1124.4   2248.9   0.3160      1  0.5740372
## modXgame  30 2303.3 2469.5 -1121.7   2243.3   5.5434      3  0.1360678
## moXcoXga  31 2302.1 2473.9 -1120.1   2240.1   3.2019      1  0.0735548 .
## incor     32 2291.1 2468.4 -1113.5   2227.1  13.0377      1  0.0003053 ***
## moXincor  34 2289.6 2478.0 -1110.8   2221.6   5.4843      2  0.0644313 .
## coXincor  35 2291.2 2485.2 -1110.6   2221.2   0.3606      1  0.5481910
## coXmoXin  37 2294.6 2499.6 -1110.3   2220.6   0.6290      2  0.7301688
## gamQuad   38 2215.8 2426.3 -1069.9   2139.8  80.8187      1  < 2.2e-16 ***
## modXgamQ  40 2212.9 2434.5 -1066.4   2132.9   6.9383      2  0.0311435 *
## block     41 2213.4 2440.6 -1065.7   2131.4   1.4471      1  0.2289883
## blocXmod  43 2216.8 2455.1 -1065.4   2130.8   0.5566      2  0.7570553
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```
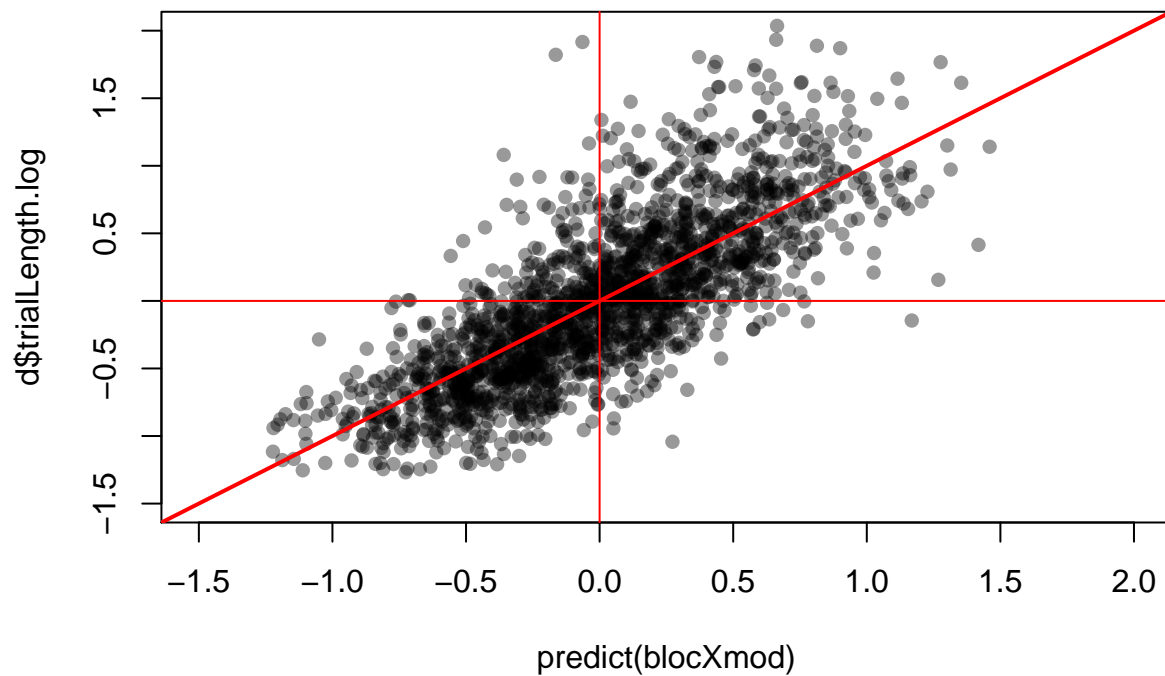
Pick final model for estimates:

```
finalModel = blocXmod
```

Check model predictions. The model predictions are in the right range and direction, fitting linear quite well:

```
plot(predict(blocXmod),d$trialLength.log, pch=16, col=rgb(0,0,0,0.4),
     ylim=c(-1.5,2),xlim=c(-1.5,2))
abline(a=0,b=1, col=2, lwd=2)
abline(h=0, col=2)
abline(v=0, col=2)
```
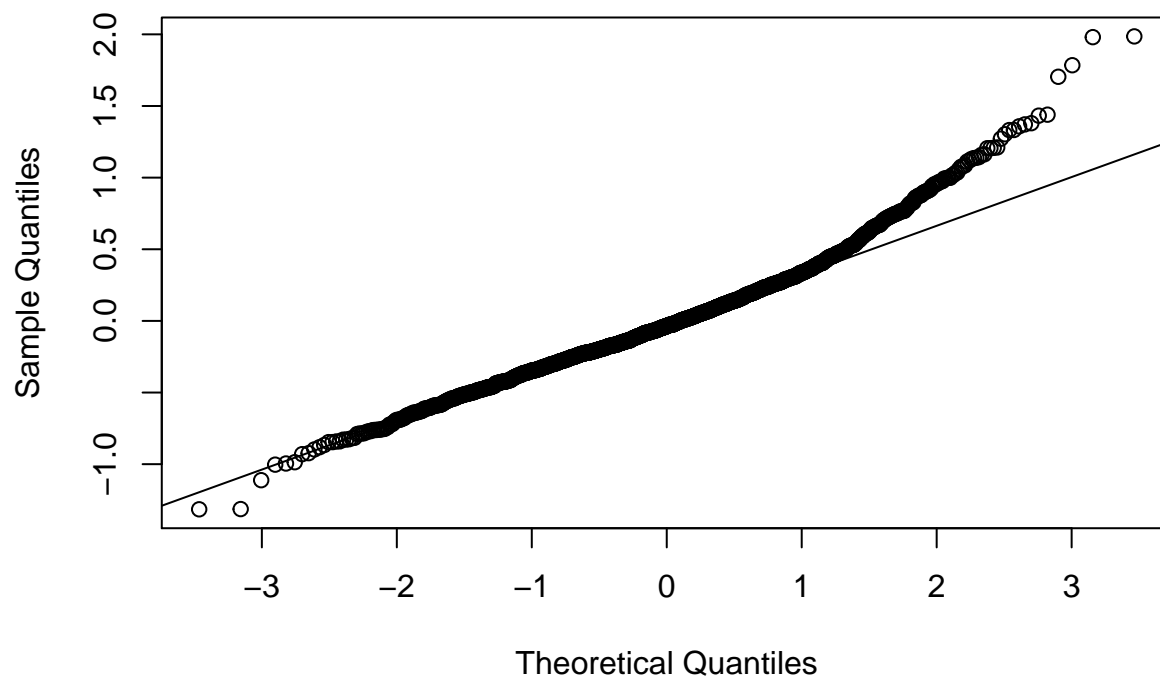
The residuals are ok, though it tends to do worse at higher values. This is expected from using the log scale.

```
qqnorm(resid(blocXmod))
qqline(resid(blocXmod))
```

Normal Q–Q Plot

Plot the fixed effects

Relabel the effects:

```r
feLabels = matrix(c(
"(Intercept)"              ,"Intercept"        ,
"modalityConditionvisual" ,"Visual modality",
"modalityConditionvocal"  , "Acoustic modality",
"conditionVisual" , "Visual stimuli",
"trialTotal"              , "Game",
"modalityConditionvisual:conditionVisual"  , "Visual modality:Visual stimuli",
"modalityConditionvocal:conditionVisual" , "Acoustic modality:Visual stimuli",
"modalityConditionvisual:trialTotal"    , "Visual modality:Game",
"modalityConditionvocal:trialTotal"     , "Acoustic modality:Game",
"conditionVisual:trialTotal"             , "Visual stimuli:Game",
"modalityConditionvisual:conditionVisual:trialTotal", "Visual modality:Visual stimuli:Game",
"modalityConditionvocal:conditionVisual:trialTotal", "Acoustic modality:Visual stimuli:Game",
"incorrectTRUE","Inorrect",
"modalityConditionvisual:incorrectTRUE","Visual modality:Incorrect",
"modalityConditionvocal:incorrectTRUE","Acoustic modality:Incorrect",
"modalityConditionvisual:I(trialTotal^2)", "Visual modality:Game^2",
"modalityConditionvocal:I(trialTotal^2)", "Acoustic modality:Game^2",
"I(trialTotal^2)","Game^2",
"firstBlockVisual","Visual stims first",
"modalityConditionvisual:firstBlockVisual","Visual modality:Visual stim first",
"modalityConditionvocal:firstBlockVisual","Acoustic modality:Visual stim first",
"modalityConditionvisual:trialTotal","Visual modality:Game",
"modalityConditionvocal:trialTotal","Acoustic modality:Game",
"conditionVisual:incorrectTRUE","Visual stimuli:incorrect",
"modalityConditionvisual:conditionVisual:incorrectTRUE","Visual modality:Visual stimuli:incorrect",
"modalityConditionvocal:conditionVisual:incorrectTRUE","Acoustic modality:Visual stimuli:incorrect"
), ncol=2, byrow = T)

feLabels2 = as.vector(feLabels[match(names(fixef(finalModel)),feLabels[,1]),2])
```

Plot the strength of the fixed effects:

```r
x = sjp.lmer(finalModel, 'fe',
        show.intercept = T,
        sort.est=NULL,
        axis.labels = feLabels2[2:length(feLabels2)],
        xlab="Trial time (ms)",
        geom.colors = c(1,1),
        show.p=F,
        show.values = F,
        string.interc="Intercept")
```

```
## Warning: replacing previous import 'lme4::sigma' by 'stats::sigma' when
## loading 'pbkrtest'

## Computing p-values via Kenward-Roger approximation. Use `p.kr = FALSE` if computation takes too long

## Warning in deviance.merMod(object, ...): deviance() is deprecated for REML
## fits; use REMLcrit for the REML criterion or deviance(.,REML=FALSE) for
## deviance calculated at the REML fit

## Warning: Deprecated, use tibble::rownames_to_column() instead.
```
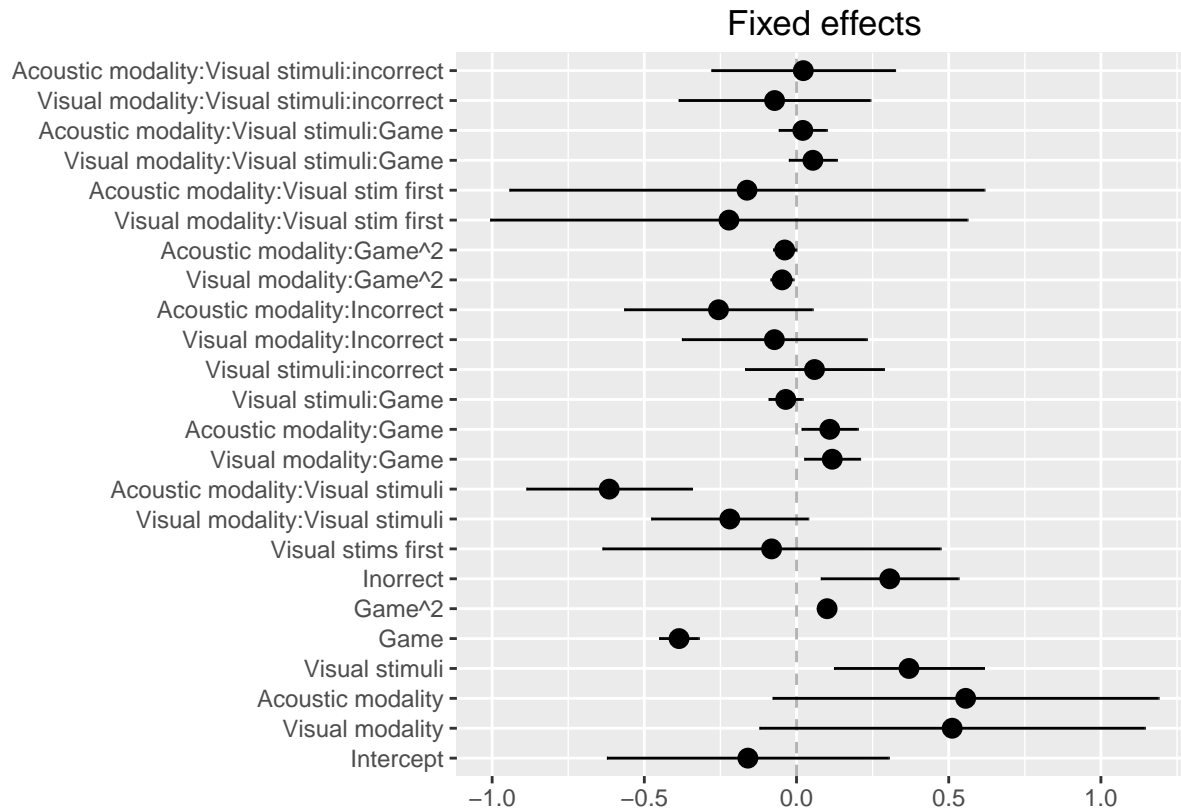
Fixed effects

Attempt plot with axes in milliseconds.

```
convertEst = function(X){
  exp(meanLogTrialLength+X) - exp(meanLogTrialLength)
}


x$plot.list[[1]]$data$estimate =convertEst(x$plot.list[[1]]$data$estimate)
x$plot.list[[1]]$data$conf.low = convertEst(x$plot.list[[1]]$data$conf.low)
x$plot.list[[1]]$data$conf.high =  convertEst(x$plot.list[[1]]$data$conf.high)

x$plot.list[[1]] +
  scale_y_continuous(limits=c(-5000,10000), name="Difference (ms)") +
  scale_x_discrete(labels=feLabels2)
```

```
## Scale for 'x' is already present. Adding another scale for 'x', which
## will replace the existing scale.
```

```
## Warning: Removed 2 rows containing missing values (geom_errorbar).
```
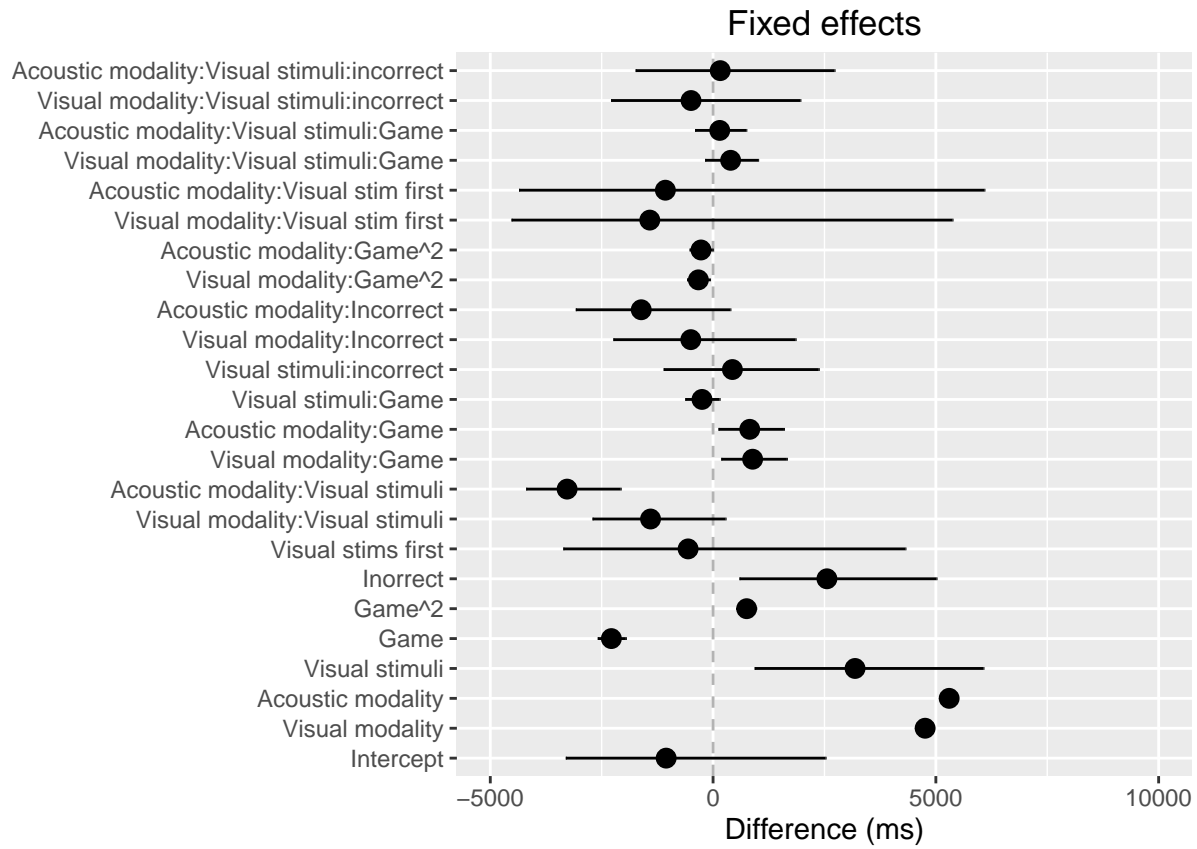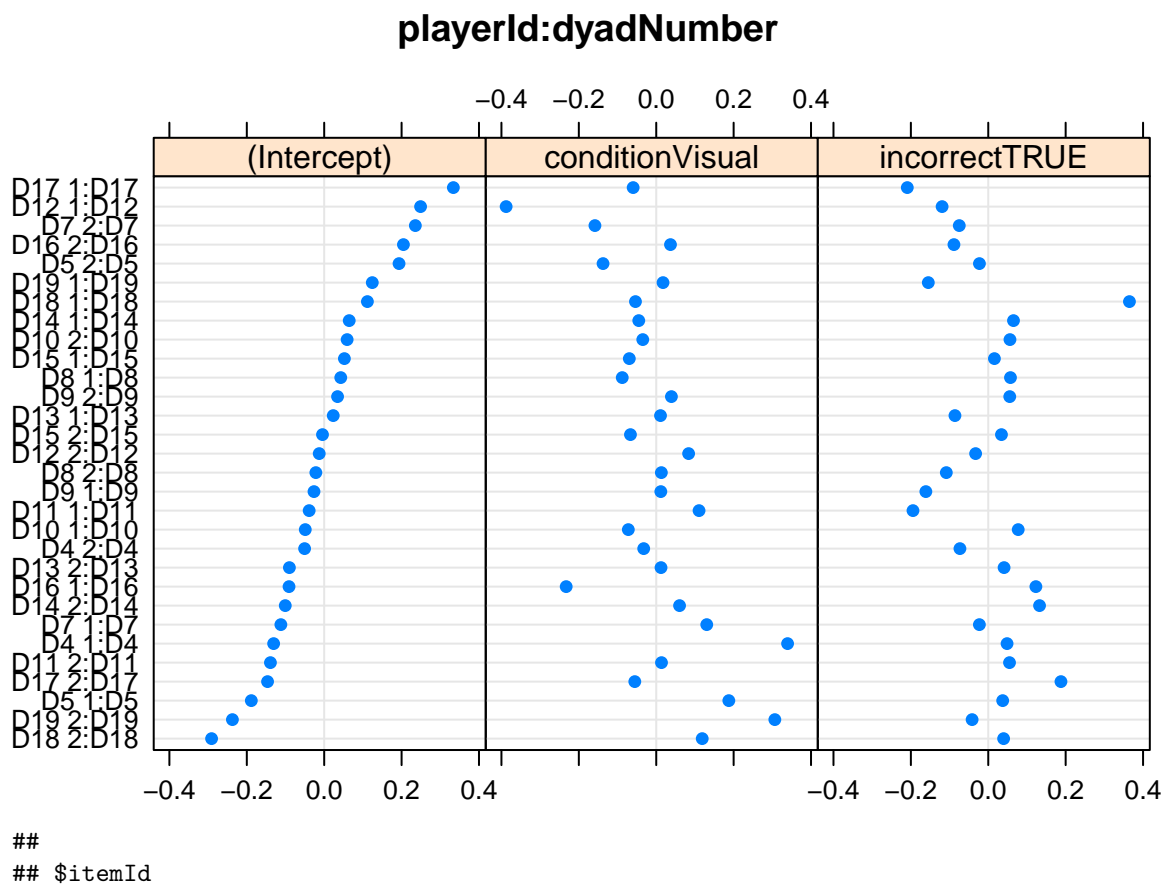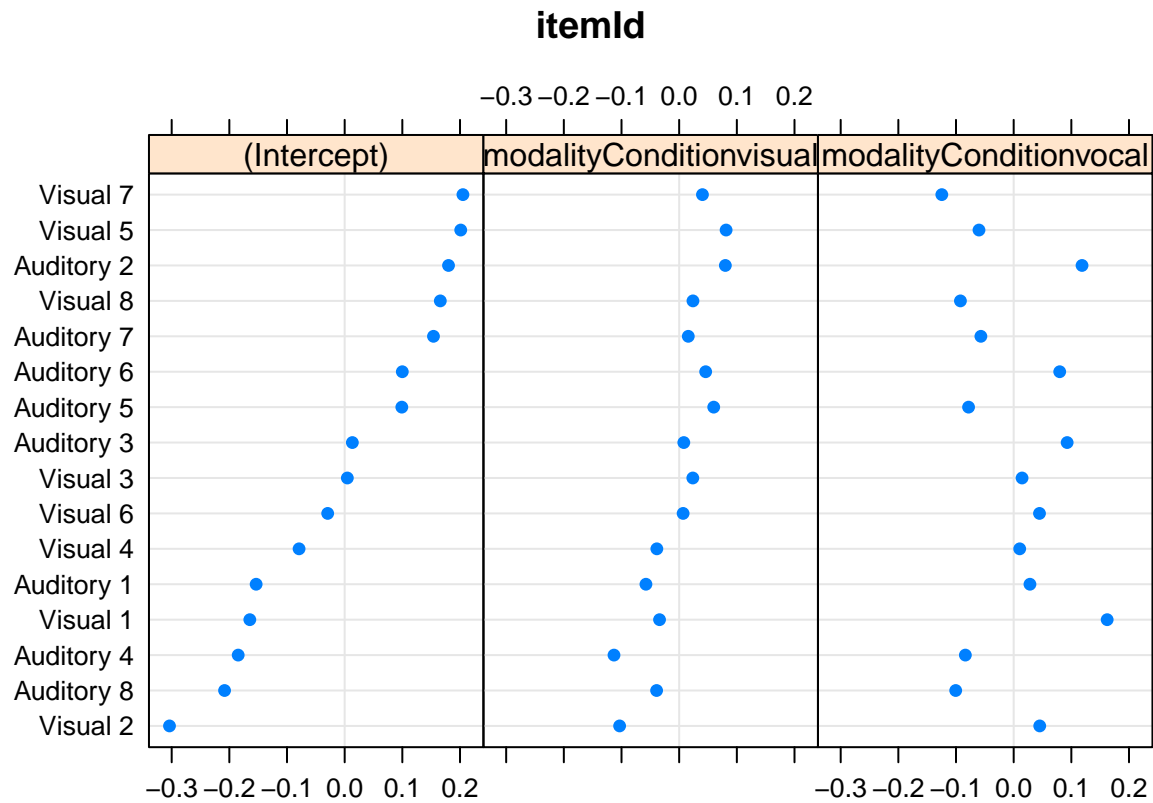
Fixed effects

Random effects

There is a reasonable amount of variaition in the random effects, suggesting that dyads and players differ. This justifies the use of mixed effects modelling.

```
dotplot(ranef(finalModel))
```

$`playerId:dyadNumber`

playerId:dyadNumber


```
##
## $itemId
```

itemId


```
##
## $dyadNumber
```

dyadNumber