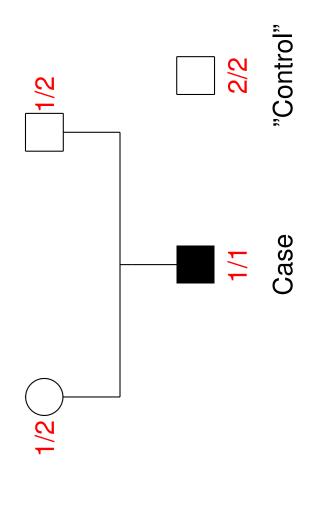
Family-based association (FBA) studies



Sample: Case-parent triads (affected child with both parents)

Method: The two parental alleles that have not been transmitted to the

affected child are combined to form the genotype of a "control" individual

Advantage: Genetic background of the "control" individual is identical to that

of the case individual

Unmatched analysis of FBA studies

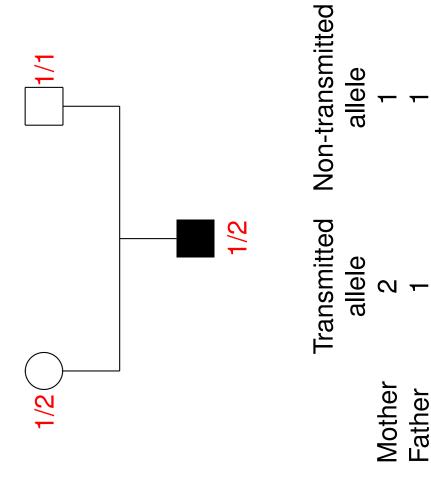
or by Armitage's trend test (c.f. CC/10). However, these kinds of analyses do case-control studies, i.e., by comparing the genotype distribution (c.f. CC/8), n nuclear families with a single affected child provide genotypes of n cases by comparing the allele distribution (c.f. CC/9) between cases and controls, obtained from the same family (i.e., the one-to-one matching of cases and not take into account the relationship between the cases and controls and n "controls". The statistical analysis can proceed exactly as for controls). It can be shown that

- for a "perfect" (i.e., randomly mating) population, unmatched analysis is slightly more powerful than matched analysis in most cases.
- for a stratified population, unmatched analysis of FBA studies can be conservative and less powerful than matched analysis.

Matched analysis of FBA studies

Each parent provides one pair of transmitted/non-transmitted alleles.

Example:



Matched analysis of FBA studies

Diallelic marker locus $\{1,2\}$, n nuclear families

	Non-trans	Von-transmitted allele	
ansmitted allele	-	2	
-	a	q	
Ø	S	p	

b: number of parents with genotype 1/2 who transmit allele 1

c: number of parents with genotype 1/2 who transmit allele 2

In case that there is no association between the alleles at the marker locus and the disease, b and c should be similar numbers.

Test statistic:

$$TDT = \frac{(b-c)^2}{b+c}$$

Null distribution: In case of no association, the distribution of the

TDT-statistic can be approximated by a χ_1^2 distribution.

Name: Transmission disequilibrium test (TDT)

TDT: Exercise

Assume that genotyping a sample of 64 families with a single affected child resulted in the following data:

	frequency	-	7	က	က	2	-	4	
—	child	2/2	1/2	2/2	1/2	1/2	2/2	2/2	
notype o	ner father (1/2	2/2	2/2	1/1	1/2	1/2	2/2	
Ger	mother	1/2	1/2	1/2	2/2	2/2	2/2	2/2	
	frequency	4	2	Ψ-	2	7	က	တ	9
	child frequency	1/1 4	1/1 5	1/2 1	1/2 5	1/1 7	1/2 3	1/1 9	1/2 6
Genotype of				1/2 1/2 1		1/1 1/1 7			

Calculate the TDT-statistic for these data.

Marker locus $\{a_1, \ldots a_k\}$ with $k \geq 2$, n nuclear families

	2	n-trar	Non-transmitted allele	ed all	<u>e e</u>
Transmitted allele	a_1	•	a_j	•	a_k
a_1	n_{11}	•	n_{1j}	•	n_{1k}
•••			•••		•••
a_i	n_{i1}	•	n_{ij}	•	n_{ik}
a_k	n_{k1}	:	n_{kj}	•	n_{kk}

 n_{ij} : number of parents with genotype a_i/a_j who transmit allele a_i

In case that there is no association between the alleles at the marker locus and the disease, n_{ij} and n_{ji} should be similar numbers.

Test statistic:

 $TDT_{SE} = \frac{k-1}{k} \sum_{i=1}^{k} \frac{(n_{i.} - n_{.i})^{2}}{n_{i.} + n_{.i} - 2n_{ii}}$

with $n_{i.} = \sum_{j=1}^k n_{ij}$ and $n_{.i} = \sum_{j=1}^k n_{ji}$

Null distribution: In case of no association, the distribution of the

 ${
m TDT}_{
m SE}$ -statistic can be approximated by a χ_{k-1}^2 distribution.

Exercise:

Show that TDT_{SE}=TDT for a diallelic marker.

Test statistic:

 $\text{TDT}_{\text{max}} = \max_{1 \le i \le k} \frac{(n_{i.} - n_{.i})^2}{n_{i.} + n_{.i} - 2n_{ii}} = \max_{1 \le i \le k} \text{TDT}^{(i)}$

where $\mathrm{TDT}^{(i)}$ is the TDT-statistic for a diallelic marker applied to

$$a_i, \bar{a}_i = \{a_1, \dots, a_{i-1}, a_{i+1}, \dots, a_k\}$$

Null distribution: The (approximate) distribution of the TDT_{max} statistic is

not known, but can be obtained by simulation.

FBA studies vs. CC studies: Pros and Cons

- sufficiently large number of affected children with both parents available. FBA studies are logistically more demanding. Especially in case of a disease with a late age of onset, it is difficult/impossible to sample a
- FBA studies are more expensive in regard to genotyping costs: Three individuals have to be genotyped for obtaining one case and one "control".

- FBA studies circumvent the problem of population stratification.
- Often, a family sample adequate for FBA analysis is already available from a previous linkage analysis.

Families with more than a single affected child

Problem:

Some or all of the families in the sample may contain two or more affected

children. How to deal with these families?

Possibilities:

1. Randomly select a single child from each family and discard additional affected children in the family. Drawback: Result of the analysis cannot be verified. Further, discarding additional affected children may waste information.

Families with more than a single affected child

2. Count, for both parents and all affected children, the pair of alleles transmitted/non-transmitted by the parent to each child.

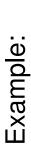
independent if there is linkage (but no association) between marker and disease locus. However, the independence of parental transmissions is an essential assumption for approximating the null distribution of the Drawback: Transmissions by one parent to different children are not TDT statistic by a χ_1^2 distribution.

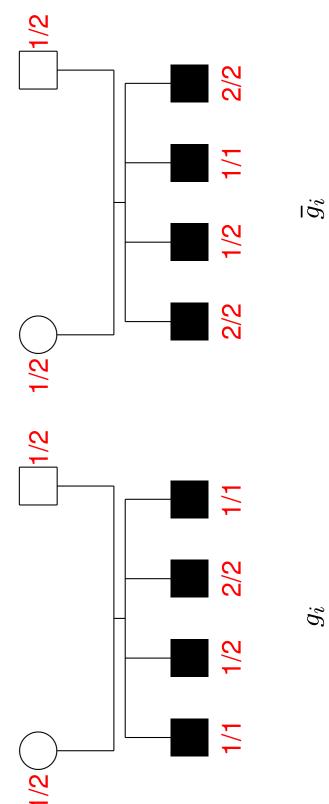
Solution: Obtain the null distribution of the TDT by an appropriate simulation procedure.

FBA/13

Families with more than a single affected child

For $1 \le i \le n$, let g_i denote the collection of observed marker genotypes of collection of genotypes that is obtained from g_i by replacing the observed genotypes of all children with the two non-transmitted parental alleles. all individuals (parents and children) in family i and let \overline{g}_i denote the





Families with more than a single affected child

- counts over the families and calculate the TDT statistic (Notation: TDT₀). transmitted/non-transmitted by the parent to each child. Sum up these 0. Count, for both parents and all affected children, the pair of alleles
 - collection of the observed marker genotypes in family i is either g_i (with probability 1/2) or \bar{g}_i (with probability 1/2). Let TDT $_j$ denote the TDT $(1 \le j \le t)$, a sample of n families is constructed such that the 1. Perform t simulation replicates. In the j-th simulation replicate statistic for the j-th simulation replicate.
- 2. The P value assigned to TDT₀ is the fraction of simulation replicates resulting in a test statistic greater or equal to TDT_0 , i.e.,

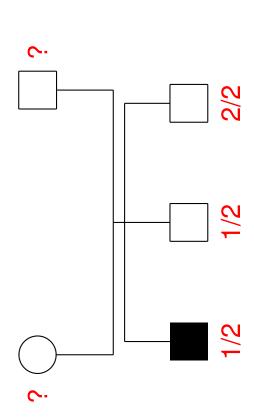
$$P = \frac{|\{j: \text{TDT}_j \ge \text{TDT}_0\}|}{\int_{t}^{t}}$$

FBA studies without parents

In FBA studies, missing parents can be compensated by unaffected

offspring.

Example:



Let $m_A\ (m_U)$ be the mean number of "1" alleles among the affected

(unaffected) children.

Example: $m_A = 0.5$, $m_U = 0.25$

FBA studies without parents: SDT

Marker: Diallelic locus {1,2}

Sample: Sibships with (at least) one affected and (at least) one unaffected

chilo

Method: Let d_+ be the number of sibships for which $m_A>m_U$ and d_- be

the number of sibships for which $m_A < m_U$

Test statistic:

$$SDT = \frac{(d_+ - d_-)^2}{d_+ + d_-}$$

Null distribution: In case of no association, the distribution of the

SDT-statistic can be approximated by a χ_1^2 distribution

Name: Sibship disequilibrium test (SDT)