

$$??$$

$$r_{it} - r_{ft} = f_1(r_{mt} - r_f) + f_2(\beta_{ij} f_{jt}) + \epsilon_{it}$$

$$\begin{matrix} i = \overline{1,2,\dots,n} \\ t = \overline{1,2,\dots,T} \\ j = \overline{1,2,\dots,k} \\ f_1(\cdot) \end{matrix}$$

$$\begin{matrix} f_2(\cdot) \\ (r_{mt}- \\ r_f) \\ r_{mt} \\ r_{ft} \\ r_{it} \\ f_{jt} \\ \beta_{ij} \\ \epsilon_{it} \\ \beta_{ij} \\ \alpha_j \\ \mathcal{Q} \\ k \times \\ k \\ \sum_k \\ f_1(a) \\ f_2(a) \\ {}_1(r_{mt}-r_f)= \\ a_i+ \\ \beta_{im}(r_{mt}- \\ r_{ft}) \\ f_2(\beta_{ij}f_{jt})= \\ \sum_{j=1}^k\beta_{ij}f_{ij} \\ r_{it}=a_i+\sum_{j=1}^{k+1}\beta_{ij}f_{ij}+\epsilon_{it} \end{matrix}$$

$$\begin{matrix} a_i \\ U[-0.5,0.5] \\ \beta_{ij} \\ f_{ij} \\ \alpha_j \\ r_{mi-r_f} \\ f_{i1} \\ \beta_{\mathbf{i}} = \\ (\beta_{i1}, \beta_{i2} \cdots, \beta_{ik+1}) \\ IIDU(\mu_{\beta}- \\ 0.2, \mu_{\beta}+ \\ 0.2) \\ \mu_{\beta} \\ [n^{\alpha_j}] \\ \beta_{\mathbf{i}} \end{matrix}$$

$$r_{it} = a_i + \beta_{im}(r_{mt} - r_{ft}) + \sum_{j=1}^k \beta_{ij} f_{jt} + \epsilon_{it}$$

$$\begin{matrix} r_{mt}- \\ r_{ft} \\ \alpha_m = \\ 1 \\ \beta_m \\ T = \\ \{120,240,360\} \\ n = \\ \{100,300,500\} \\ \alpha_m = \\ 1 \\ \alpha_x = \\ \{0.5,0.7,0.9,1\} \\ a_i \\ \beta_i \\ \alpha \\ bias = \\ |\alpha - \\ \hat{\alpha}| \\ MSE = \\ \frac{1}{n} \sum_{i=1}^n (bias_i)^2 \end{matrix}$$