

# nonconform: Conformal Anomaly Detection (Python)

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# Summary

Quantifying uncertainty is fundamental for Al systems in safety-critical, high-cost-of-error domains, as reliable decision-making depends on it. The Python package nonconform offers statistically principled uncertainty quantification for semi-supervised anomaly detection based on one-class classification (Petsche & Gluck, 1994). It implements methods from conformal anomaly detection (Bates et al., 2023; Jin & Candès, 2023; Laxhammar & Falkman, 2010), grounded in conformal inference (Lei & Wasserman, 2013; Papadopoulos et al., 2002; Vovk et al., 2005).

The package nonconform calibrates anomaly detection models to produce statistically valid p-values from raw anomaly scores. Conformal calibration uses a hold-out set  $\mathcal{D}_{\mathsf{calib}}$  of size n containing normal instances, while the model is trained on a separate normal dataset. For a new observation  $X_{n+1}$  with anomaly score  $\hat{s}(X_{n+1})$ , the p-value is computed by comparing this score to the empirical distribution of calibration scores  $\hat{s}(X_i)$  for  $i \in \mathcal{D}_{\mathsf{calib}}$ . The conformal p-value  $\hat{u}(X_{n+1})$  is defined as the normalized rank of  $\hat{s}(X_{n+1})$  among the calibration scores (Liang et al., 2024):

$$\hat{u}(X_{n+1}) \,=\, \frac{|\{i \in \mathcal{D}_{\mathsf{calib}} : \hat{s}(X_i) \leq \hat{s}(X_{n+1})\}|}{n}.$$

By framing anomaly detection as a sequence of statistical hypothesis tests, these p-values enable systematic control of the *marginal* (average) false discovery rate (FDR) (Bates et al., 2023; Benjamini & Hochberg, 1995) at a predefined significance level via appropriate statistical procedures. The library integrates seamlessly with the widely used pyod library (Chen et al., 2024; Zhao et al., 2019), extending conformal techniques to a broad range of anomaly detection models.

### Statement of Need

- A major challenge in anomaly detection lies in setting an appropriate anomaly threshold, as it directly influences the false positive rate. In high-stakes domains such as fraud detection,
- medical diagnostics, and industrial quality control, excessive false alarms can lead to alert
- 29 fatigue and render systems impractical.
- The package nonconform mitigates this issue by replacing raw anomaly scores with p-values,
- enabling formal control of the FDR. Consequently, conformal methods become effectively
- 32 threshold-free, since anomaly thresholds are implicitly determined by underlying statistical
- 33 procedures.

$$FDR = \frac{ \text{Efforts Wasted on False Alarms}}{ \text{Total Efforts}}$$

34 (Benjamini et al., 2009)



- $_{35}$  Conformal methods are nonparametric and model-agnostic, applying to any model that
- 36 produces consistent anomaly scores on arbitrarily distributed data. Their key requirement is
- 17 the assumption of exchangeability between calibration and test data, ensuring the validity of
- resulting conformal p-values.
- 39 Exchangeability only requires that the joint data distribution is invariant under permutations,
- 40 making it more general—and less restrictive—than the independent and identically distributed
- (i.i.d.) assumption common in classical machine learning.
- To operationalize this assumption, nonconform constructs calibration sets from training data
- using several strategies, including approaches for low-data regimes (Hennhofer & Preisach,
- 44 2024) that do not require a dedicated hold-out set. Based on these calibration sets, the
- package computes standard or weighted conformal p-values (Jin & Candès, 2023), which are
- 46 particularly useful under covariate shift, when exchangeability is only approximate.
- 47 These tools enable practitioners to build anomaly detectors whose outputs are statistically
- scontrolled to maintain the FDR at a chosen nominal level.
- <sup>49</sup> Overall, reliance on exchangeability makes these methods well-suited to cross-sectional data
- but less appropriate for time series applications, where temporal ordering conveys essential
- information.

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