

# nonconform: Conformal Anomaly Detection (Python)

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DOI: 10.xxxxx/draft

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Submitted: 01 January 1970 Published: unpublished

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## Summary

The ability to quantify uncertainty represents a fundamental requirement for Al systems operating in safety-critical and high-stakes domains and is essential for reliable decision-making. The software package nonconform addresses this challenge in the context of unsupervised anomaly detection in form of one-class classification problems (Petsche & Gluck, 1994). Specifically, the package implements methods from conformal anomaly detection (Laxhammar & Falkman, 2010), based on the overarching principles of conformal inference (Lei & Wasserman, 2013; Papadopoulos et al., 2002; Vovk et al., 2005) for statistically principled uncertainty quantification.

The library integrates with pyod (Chen et al., 2024; Zhao et al., 2019) anomaly detection models and converts anomaly scores to statistically valid p-values that can be systematically adjusted using methods that control the False Discovery Rate (FDR) (Bates et al., 2023; Benjamini & Hochberg, 1995). Rather than relying on anomaly scores and arbitrarily set thresholds, this approach provides statistical guarantees by calibrating detector models to align anomaly scores with their empirical false alarm rates.

### Statement of Need

The field of anomaly detection comprises methods for identifying observations that either deviate from the majority of observations or otherwise do not *conform* to an expected state of *normality*. The typical procedure leverages anomaly scores and thresholds to distinguish in-distribution data from out-of-distribution data. However, this approach does not provide statistical guarantees regarding its estimates. A major concern in anomaly detection is the rate of False Positives among proclaimed discoveries. Depending on the domain, False Positives can be expensive. Triggering *false alarms* too often results in *alert fatigue* and eventually renders the detection system ineffective and impractical.

In the context of anomaly detection, uncertainty quantification directly translates to controlling the rate of False Positive (*Type I Error*) while preserving sensitivity to genuine anomalies. In practice, it is necessary to control the proportion of False Positives relative to the entirety of proclaimed discoveries (the number of triggered alerts), measured by the FDR that may be expressed in practice as:

$$FDR = \frac{ ext{Efforts Wasted on False Alarms}}{ ext{Total Efforts}}$$

- 4 (Benjamini et al., 2009; Benjamini & Hochberg, 1995).
- Framing anomaly detection tasks as sets of statistical hypothesis tests, with  $H_0$  claiming that the data is *normal* (no *discovery* to be made), enables controlling the FDR when statistically
- p-values (or test statistics) are available. When conducting multiple simultaneous



- hypothesis tests, it is furthermore necessary to adjust for multiple testing, as fixed significance
  levels would lead to inflated overall error rates.
- 40 The nonconform package provides the tools necessary for creating anomaly detectors whose
- outputs can be statistically controlled to cap the FDR at a nominal level among normal
- 42 instances under exchangeability. It provides wrappers for a wide range of anomaly detection
- models (e.g. Autoencoder, IsolationForest, One-Class SVM etc.) complemented by a rich range
- 44 of conformalization strategies to compute classical conformal p-values or modified weighted
- conformal p-values (Jin & Candès, 2023) using different strategies that make them suitable for
- application even in low-data regimes (Hennhofer & Preisach, 2024). The need for weighted
- oconformal p-values arises when the underlying statistical assumption of exchangeability is
- violated due to covariate shift between calibration and test data.

### 49 Statistical Validity

The methods implemented in nonconform require data to satisfy the statistical assumption of exchangeability, meaning the joint probability distribution remains unchanged under any permutation of the observation order. Simply put, data points can be shuffled without affecting their statistical properties. With that, exchangeability relaxes the IID assumption by allowing dependence between observations, as long as the order doesn't matter. This accommodates domains like survey sampling without replacement, cross-sectional data analysis, quality control, fraud detection, and medical diagnostics where samples are independently collected. Timeseries and autocorrelated data are unsuitable as temporal ordering carries information that would be lost under permutation, violating exchangeability. However, when exchangeability holds, the methods support batch as well as batch-streaming and purely online deployments through integration with respective batch and online FDR control methods (see e.g. onlineFDR package<sup>1</sup>).

# Acknowledgements

- This work was conducted in part within the research projects *Biflex Industrie* (grant number 01MV23020A) and *AutoDiagCM* (grant number 03EE2046B) funded by the *German Federal Ministry of Economic Affairs and Climate Action (BMWK)*.
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<sup>1</sup>https://github.com/OliverHennhoefer/online-fdr



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