




# nonconform: Conformal Anomaly Detection

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## Summary

The requirement of uncertainty quantification for AI systems has become increasingly important. In the context of anomaly detection applications, this directly translates to controlling Type I (False Positive) error rates without compromising the statistical power of the applied detection procedure. Conformal Anomaly Detection ([Laxhammar & Falkman, 2010](#)) emerges as a promising approach for providing respective statistical guarantees by calibrating a given detector model. Instead of relying on anomaly scores and arbitrarily set thresholds, this approach converts the anomaly scores to statistically valid  $p$ -values that can then be adjusted by statistical methods that control the False Discovery Rate (FDR) ([Benjamini & Hochberg, 1995](#)) within a set of tested instances ([Bates et al., 2023](#)).

The Python library nonconform is an open-source software package that provides a range of tools to enable conformal inference ([Lei & Wasserman, 2013](#); [Papadopoulos et al., 2002](#); [Vovk et al., 2005](#)) for one-class classification ([Petsche & Gluck, 1994](#)). The library computes classical and weighted conformal  $p$ -values ([Jin & Candès, 2023](#)) using different conformalization strategies that make them suitable for application even in low-data regimes ([Hennhofer & Preisach, 2024](#)). The library integrates with the majority of pyod anomaly detection models ([Chen et al., 2024](#); [Zhao et al., 2019](#)).

## Statement of Need

The field of anomaly detection comprises methods for identifying observations that either deviate from the majority of observations or otherwise do not *conform* to an expected state of *normality*. The typical procedure leverages anomaly scores and thresholds to distinguish in-distribution data from out-of-distribution data. However, this approach does not provide statistical guarantees regarding its estimates. A major concern in anomaly detection is the rate of False Positives among proclaimed discoveries. Depending on the domain, False Positives can be expensive. Triggering *false alarms* too often results in *alert fatigue* and eventually renders the detection system ineffective and impractical.

In such contexts, it is necessary to control the proportion of False Positives relative to the entirety of proclaimed discoveries (the number of triggered alerts). In practice, this is measured by the FDR, which translates to:

$$FDR = \frac{\text{Efforts Wasted on False Alarms}}{\text{Total Efforts}}$$

([Benjamini et al., 2009](#); [Benjamini & Hochberg, 1995](#)).

Framing anomaly detection tasks as sets of statistical hypothesis tests, with  $H_0$  claiming that the data is *normal* (no *discovery* to be made), enables controlling the FDR when statistically valid  $p$ -values (or test statistics) are available. When conducting multiple *simultaneous* hypothesis tests, it is furthermore necessary to *adjust* for multiple testing, as fixed *significance levels* (typically  $\alpha \leq 0.05$ ) would lead to inflated overall error rates.

39 The nonconform (*non-conformity-based anomaly detection*) package provides the tools neces-  
 40 sary for creating anomaly detectors whose outputs can be statistically controlled to cap the  
 41 FDR at a nominal level among normal instances under exchangeability. It provides wrappers for  
 42 a wide range of anomaly detectors (e.g., [Variational-]Autoencoder, IsolationForest, One-Class  
 43 SVM) complemented by a rich range of conformalization strategies (mostly depending on the  
 44 *data regime*) to compute classical conformal  $p$ -values or modified *weighted* conformal  $p$ -values.  
 45 The need for *weighted* conformal  $p$ -values arises when the underlying statistical assumption of  
 46 *exchangeability* is violated due to covariate shift between calibration and test data. Finally,  
 47 nonconform offers built-in statistical adjustment measures like Benjamini-Hochberg (Benjamini  
 48 & Hochberg, 1995) that correct obtained and statistically valid  $p$ -values for the multiple testing  
 49 problem when testing a *batch* of observations simultaneously.

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