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Answer:

Step1:

We fill a table of the size of the 2D map.

Step2:

We can simple solve the subproblem which is what is the minimum number of moves to reach the $point(i, j)$ with the best score $opt(i, j)$. The base cases are:

$moves(1,1) = 1$ and $moves(i, j) = 0$ for all i and j that are off the board.

Then we solve the following recursion:

$$moves(i, j) = \begin{cases} moves(i-1, j) & \text{if } opt(i-1, j) < opt(i, j-1) \\ moves(i, j-1) & \text{if } opt(i-1, j) > opt(i, j-1) \\ moves(i-1, j) + moves(i, j-1) & \text{if } opt(i-1, j) = opt(i, j-1) \end{cases}$$

It will run in $O(n^2)$.