

3F2 Lab Report

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Apparatus #: 2

```
In [1]: import numpy as np
import scipy.interpolate
import matplotlib.pyplot as plt

plt.rcParams['figure.figsize'] = [16, 8]
```

```
In [2]: # Define the physical constants for the pendulum experiment

g=9.81 # m/s^2
L=0.125 # distance from pendulum's centre of mass to pivot in m
a=0.016 # radius of pulley in m
m=0.32 # mass of pendulum in kg
M=0.7 # mass of carriage in kg
I=8e-5 # moment of inertia on motor shaft in kg m^2
km = 0.08 # torque motor constant in Nm/A
ka = -0.50 # amplifier constant in A/V

gamma = M/m + I/(m*np.power(a,2))

#scale factors to get physical units metres radians and seconds.
#in the crane/down position
# [x xdot Ltheta Lthetadot]=[CP CV PP PV]*Sc where,
Sc=np.diag([-1/12.5, -1/2.23, L/3.18, L/0.64])

# in the inverted position
# [x xdot Lphi Lphidot]=[CP CV PP PV]*Sp where,
Sp=np.diag([-1/12.5, -1/2.23, L/3.18, -L/0.64])

#controller amplifier gains on each measurement
opamp_c = np.diag([-20, -30, 20, -10]) # for crane controller
opamp_p = np.diag([10, 20, 30, -20]) # for inverted pendulum controller

#maximum torque from the motor in Nm
Tmax=0.4

# squares of the natural frequencies
om12=g/L
om02=om12*(1+1/gamma)

#Linearized crane model

Ac=np.array([[0, 1, 0, 0], [0, 0, om12-om02, 0], [0, 0, 0, 1], [0, 0, -om02, 0]
Cc=(ka*km/(m*a*gamma))*np.linalg.solve(Sc,opamp_c)
B=np.array([[0],[1],[0],[1]])

#Linearized inverted pendulum model
Ap=np.array([[0, 1, 0, 0], [0, 0, om02-om12, 0], [0, 0, 0, 1], [0, 0, om02, 0]])
Cp=(ka*km/(m*a*gamma))*np.linalg.solve(Sp,opamp_p)
```

```
# Sampling period
h=0.0025 #sampling period
h_sim=0.002 #simulation step size
```

Helper functions are defined here (you should not have to change these). Click to reveal and then click the vertical bar to rehide.

In [3]: # Define helper functions

```
def solver_crane(x0,tsim,tdem,xdem,p):
    x = np.copy(x0)
    x_sim = x.reshape(1,4)
    T_sim = []
    if x0[2]>0.05:
        stopped=0
    else:
        stopped = 1

    def next_state_crane(x):
        theta = x[2]/L
        sinth = np.sin(theta)
        costh = np.cos(theta)
        newx = np.empty(4)
        nonlocal stopped
        if stopped==1 and (np.abs(T/a - m*g*sinth*costh - m/L*sinth*x[3]**2)< F stati
            newx[0] = x[0]
            newx[1] = 0.0
            newx[2] = x[2]+ h_sim*x[3]+0.5*h_sim**2*(-g*sinth)
            sinth1 = np.sin(newx[2]/L)
            costh1 = np.cos(newx[2]/L)
            newx[3] = x[3] -h_sim*g*(sinth+sinth1)*0.5
        else:
            stopped=0
            x24dot =np.linalg.solve(np.array([[1+gamma,-costh],[-costh,1]]),np.array
            newx[[0,2]]=x[[0,2]]+h_sim*x[[1,3]]+0.5*(h_sim**2)*x24dot

            sinth1 = np.sin(newx[2]/L)
            costh1 = np.cos(newx[2]/L)
            x24dot1 = np.linalg.solve(np.array([[1+gamma,-costh1],[-costh1,1]]),np.
            newx[[1,3]]=x[[1,3]]+h_sim*0.5*(x24dot+x24dot1)
            if((x[1]!=0.0) & (x[1]*newx[1]<=0.0)):
                stopped= 1
        return newx

    for t in tsim:
        xd = np.interp(t,tdem,xdem)
        T= (ka*km*p@ opamp_c@ np.linalg.solve(Sc,(x-np.array([xd,0,0,0]))))[0]
        if np.abs(T)>Tmax:
            T= Tmax*np.sign(T)
        T_sim.append(T.item())
        x = next_state_crane(x)
        x_sim = np.vstack((x_sim,np.transpose(x)))
    return x_sim
# Define helper functions

def solver_pendulum(x0,tsim,tdem,xdem,p):
    x = np.copy(x0)
    x_sim = x.reshape(1,4)
    T_sim = []
```

```

if x0[2]>0.05:
    stopped=0
else:
    stopped =1

def next_state_pendulum(x):
    phi = x[2]/L
    sinphi = np.sin(phi)
    cosphi = np.cos(phi)
    newx = np.empty(4)
    nonlocal stopped
    if stopped==1 and (np.abs(T/a + m*g*sinphi*cosphi - m/L*sinphi*newx[3]**2) <
        newx[0] = x[0]
        newx[1] = 0.0
        newx[2] = x[2]+ h_sim*x[3]+0.5*h_sim**2*(g*sinphi)
        sinphi1 = np.sin(newx[2]/L)
        cosphi1 = np.cos(newx[2]/L)
        newx[3] = x[3] +h_sim*g*(sinphi+sinphi1)*0.5
    else:
        stopped=0
        x24dot =np.linalg.solve(np.array([[1+gamma,-cosphi],[cosphi,-1]]),np.array(
            newx[[0,2]]=x[[0,2]]+h_sim*x[[1,3]]+0.5*(h_sim**2)*x24dot

            sinphi1 = np.sin(newx[2]/L)
            cosphi1 = np.cos(newx[2]/L)
            x24dot1 = np.linalg.solve(np.array([[1+gamma,-cosphi1],[cosphi1,-1]]),n
            newx[[1,3]]=x[[1,3]]+h_sim*0.5*(x24dot+x24dot1)
            if((x[1]!=0.0) & (x[1]*newx[1]<=0.0)):
                stopped= 1
    return newx

for t in tsim:
    xd = np.interp(t,tdem,xdem)
    T= (ka*km*P@ opamp_p@ np.linalg.solve(Sp,(x-np.array([xd,0,0,0]))))[0]
    if np.abs(T)>Tmax:
        T= Tmax*np.sign(T)
    T_sim.append(T.item())
    x = next_state_pendulum(x)
    x_sim = np.vstack((x_sim,np.transpose(x)))
return x_sim

def loadlogdata(n,ScaleF):

    if n> 9:
        filename = 'Plot 0' + str(n) + '.csv'
    else:
        filename = 'Plot 00' + str(n)+ '.csv'

    LoadedDataCSV = np.genfromtxt(filename,delimiter=',',skip_header=16)
    # this seems to be sufficient if the offset for the header is always the same
    #print(LoadedDataCSV)
    #LoadedDataCSV = np.delete(LoadedDataCSV,-1, axis=1)
    #print(LoadedDataCSV)
    DataOfInterestCSV = np.array(LoadedDataCSV[:,[2,3,4,5,1]])
    # we now need to swap data so to place it in the following order
    # t CP CV PP PV CD
    # from an orginal order of:
    # t CD CP CV PP PV
    logdataCSV = DataOfInterestCSV*20/4095-10
    logdataCSV[:,[1,2,3]] = -logdataCSV[:,[1,2,3]]

```

```

xdata=np.concatenate([logdataCSV[:,0:4]@ScaleF, logdataCSV[:, -1:]*ScaleF[0,0]])
###
xdem = xdata[:, -1]
endtime=LoadedDataCSV[-1,0]
t = np.linspace(0,endtime,xdata.shape[0])

return xdata, xdem, t

def plot_function_crane(t0,tf,t,xdata,tsim,x_sim,p):
    ind = (t>=t0) & (t<=tf)
    plt.figure()
    plt.suptitle("Crane position with p = %s"%p, fontsize=15)

    plt.subplot(411)
    plt.plot(t[ind],xdata[ind,0], color='blue') #data
    plt.plot(tsim,x_sim[:-1,0], color='red', linestyle='--') #simulation
    plt.plot(t[ind],xdata[ind,-1], linestyle =':', color='green') # Demand
    plt.legend(['Measured','Simulated','Demand']);
    plt.ylabel("x[m]")

    plt.subplot(412)
    plt.plot(t[ind],xdata[ind,1], color='blue') #data
    plt.plot(tsim,x_sim[:-1,1], color='red', linestyle='--') #simulation
    plt.legend(['Measured','Simulated']);
    plt.ylabel("v[m/s]")

    plt.subplot(413)
    plt.plot(t[ind],xdata[ind,2], color='blue') #data
    plt.plot(tsim,x_sim[:-1,2], color='red', linestyle='--') #simulation
    plt.legend(['Measured','Simulated']);
    plt.ylabel(r"l$\Theta$[m]")

    plt.subplot(414)
    plt.plot(t[ind],xdata[ind,3], color='blue') #data
    plt.plot(tsim,x_sim[:-1,3], color='red', linestyle='--') #simulation
    plt.legend(['Measured','Simulated']);
    plt.ylabel(r"l$\omega$[m/s]")

    plt.xlabel("time [s]")

def plot_function_pendulum(t0,tf,t,xdata,tsim,x_sim,p):
    ind = (t>=t0) & (t<=tf)
    plt.figure()
    plt.suptitle("Pendulum position with p = %s"%p, fontsize=15)

    plt.subplot(411)
    plt.plot(t[ind],xdata[ind,0], color='blue') #data
    plt.plot(tsim,x_sim[:-1,0], color='red', linestyle='--') #simulation
    plt.plot(t[ind],xdata[ind,-1], linestyle =':', color='green') # Demand
    plt.legend(['Measured','Simulated','Demand']);
    plt.ylabel("x[m]")

    plt.subplot(412)
    plt.plot(t[ind],xdata[ind,1], color='blue') #data
    plt.plot(tsim,x_sim[:-1,1], color='red', linestyle='--') #simulation
    plt.legend(['Measured','Simulated']);
    plt.ylabel("v[m/s]")

    plt.subplot(413)
    plt.plot(t[ind],xdata[ind,2], color='blue') #data

```

```

plt.plot(tsim,x_sim[:-1,2], color='red', linestyle='--') #simulation
plt.legend(['Measured','Simulated']);
plt.ylabel(r'L$\Theta[m]$')

plt.subplot(414)
plt.plot(t[ind],xdata[ind,3], color='blue') #data
plt.plot(tsim,x_sim[:-1,3], color='red', linestyle='--') #simulation
plt.legend(['Measured','Simulated']);
plt.ylabel(r'L$\omega[m/s]$')

plt.xlabel("time [s]")

```

3) Crane mode

3.1) Friction measurement

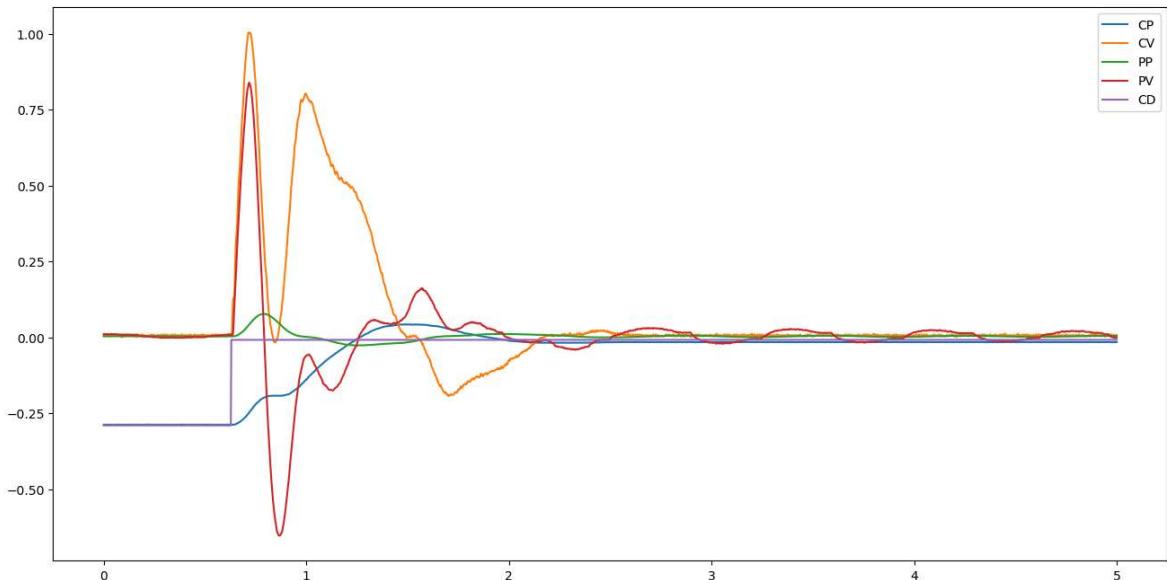
Measure the dynamic and static friction

```
In [4]: F = 1
Fstatic = 1.4 # Newton
```

3.3) Synthesis of the p_3 and p_4 controllers

```
In [5]: P = np.array([[0.35,0.15,0.45,0.05]]); 
print(np.linalg.eig(Ac-B@P@Cc)[0]) # Note that the [0] is there to ignore the se
[-8.2625171 +27.64244253j -8.2625171 -27.64244253j
 -0.96587796 +4.40876411j -0.96587796 -4.40876411j]
```

```
In [6]: ##### LOAD DATA #####
xdata, xdem, tdata = loadlogdata(1,Sc)
# in the previous Line xdem is the external input into the system.
plt.plot(tdata,xdata)
plt.legend(['CP','CV','PP','PV','CD']);
```



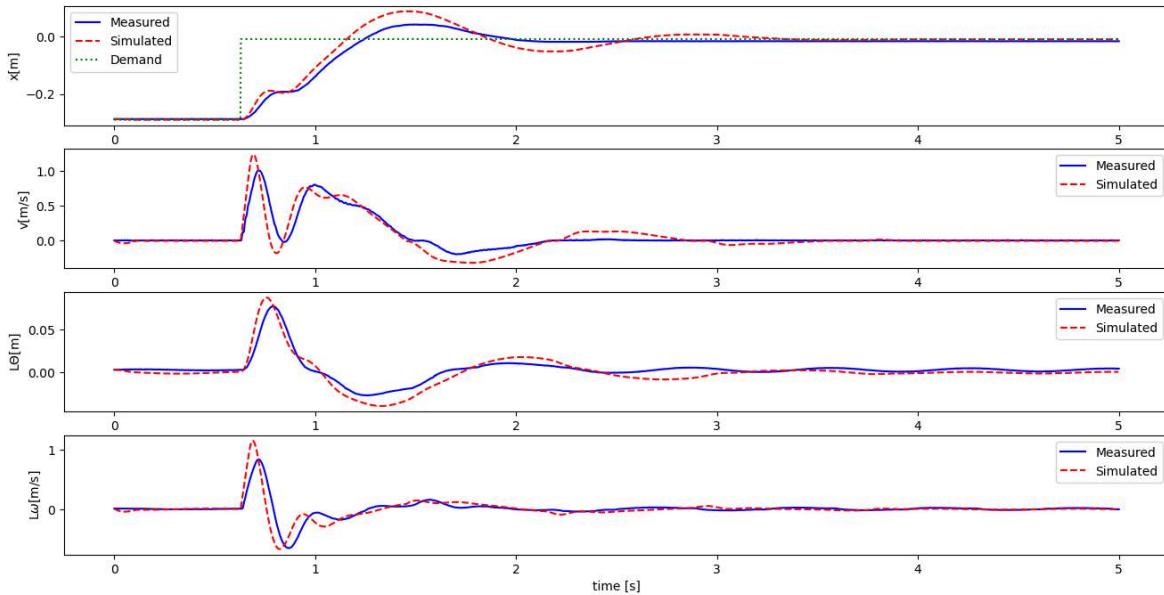
```
In [7]: t0 = 0; tf = 5 # define the simulation time to be considered

# Set up the initial conditions and time index for the simulation, this uses the

tsim = np.arange(t0,tf,h_sim)
x0=scipy.interpolate.interp1d(tdata,xdata[:, :4].T)(t0)

x_sim = solver_crane(x0,tsim,tdata,xdem,P)

plot_function_crane(t0,tf,tdata,xdata,tsim,x_sim,P)
```

Crane position with $p = [[0.35 \ 0.15 \ 0.45 \ 0.05]]$ 

Comment on the transient response and pole position

All the four poles are at the left plane, which indicates that this is a stable system.

Both the simulated plot and the measured plot show a damped oscillation which agrees that this system is stable.

The plot of carriage position shows that the system is now around critically-damped under these values of p_i .

3.4) Pole-placement

3.4a)

Use example 1 of section A.5 together with the scale factors of section A.7 to place all the closed-loop poles at $-\omega_1 = -\sqrt{78.5}$. Record your calculated values of p_1-p_4

```
In [8]: w1, w0 = 78.5, 103.3
k1 = w1
k2 = 4 * np.sqrt(w1)
k3 = 5 * w1 - w0
k4 = 0

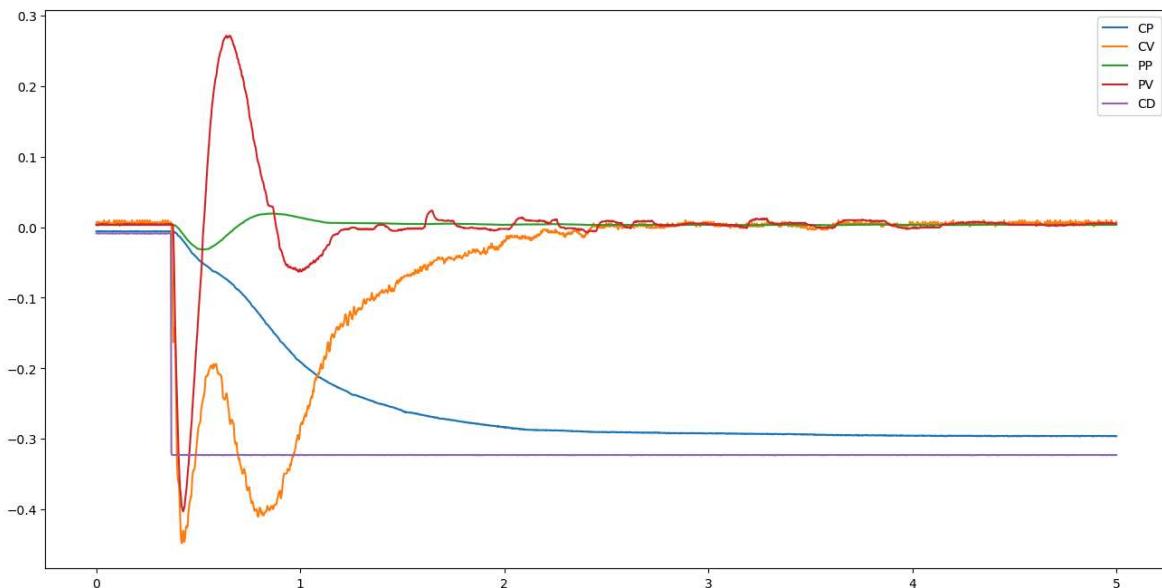
p1 = k1/617
p2 = k2/165
p3 = k3/1256
p4 = -k4/126

P = np.array([[p1, p2, p3, p4]])
print("P:", P)
print(np.linalg.eig(Ac-B@P@Cc)[0])
# Note that the [0] is there to ignore the second output of eig
```

```
P: [[0.12722853 0.21478843 0.23025478 0.]
[-11.86376287+0.j -8.47012587+2.46544622j
 -8.47012587-2.46544622j -6.67585132+0.j]]
```

```
In [9]: ##### LOAD DATA #####
xdata, xdem, tdata = loadlogdata(2, Sc)
# in the previous line xdem is the external input into the system.

plt.plot(tdata, xdata)
plt.legend(['CP', 'CV', 'PP', 'PV', 'CD']);
```

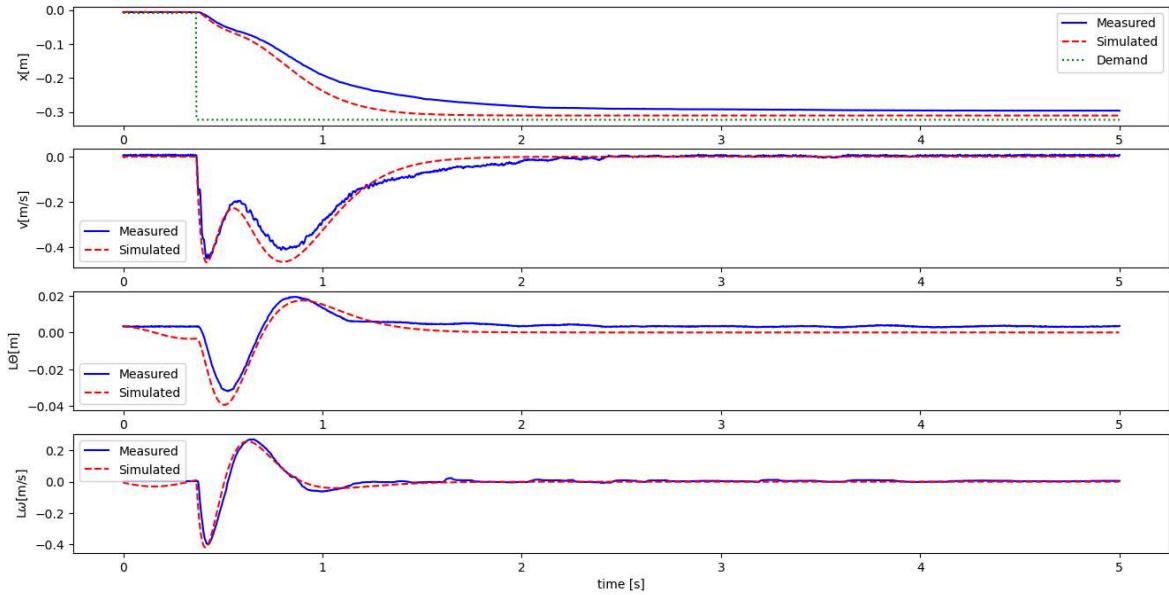


```
In [10]: t0 = 0; tf = 5 # define the simulation time to be considered

# Set up the initial conditions and time index for the simulation, this uses the
tsim = np.arange(t0, tf, h_sim)
x0=scipy.interpolate.interp1d(tdata, xdata[:, :4].T)(t0)

x_sim = solver_crane(x0, tsim, tdata, xdem, P)

plot_function_crane(t0, tf, tdata, xdata, tsim, x_sim, P)
```

Crane position with $p = [[0.12722853 0.21478843 0.23025478 0.]]$ 

Comment on the consistency with the target pole position

The measured step response has a clear discrepancy to the simulated response and the expectation from pole placement.

By placing repeated poles at $-\omega_1$, there should be no oscillation at all. However, neither the actual pole locations meet the requirements, nor the measured response shows no oscillation. This could be a result of model mismatch.

There could be some non-linearities that are ignored in this simplified model. For instance, dynamics of electric motor and non-uniform friction on the rack. For such 4th order system, little deviation of parameters would cause a great shift in pole positions. This explains why the 4 poles don't agree on the theoretical pole placement.

The measured response shows oscillation and overshoot which agrees on the form of poles. The existence of imaginary parts implies oscillation.

3.4b)

Now increase the speed of response by placing the closed-loop poles at $-\alpha, -\beta, -\omega \pm j\omega$ for suitable values of α, β and ω . Record your choice (of α, β and ω) and the corresponding potentiometer settings. Log the step response and comment. *[It is not expected that you will choose the same values as any other student!].*

```
In [11]: alpha = 12; beta = 15; omega = 8
k = np.empty(4)
k[0]=2*omega**2*alpha*beta/om12
k[1]=(2*omega**2*(alpha+beta)+2*omega*alpha*beta)/om12
```

```

k[2]=2*omega**2+2*omega*(alpha+beta)+alpha*beta-om02-k[0]
k[3]=2*omega+alpha+beta-k[1]
P=np.array([k/np.diag(Cc)])
print("alpha=", alpha, "beta=", beta, "omega =", omega)
print("P= ",P)
print(np.linalg.eig(Ac-B@P@Cc)[0])

```

```

alpha= 12 beta= 15 omega = 8
P= [[0.47559633 0.4887481  0.27313498 0.2984814 ]]
[-15.+0.j -12.+0.j -8.+8.j -8.-8.j]

```

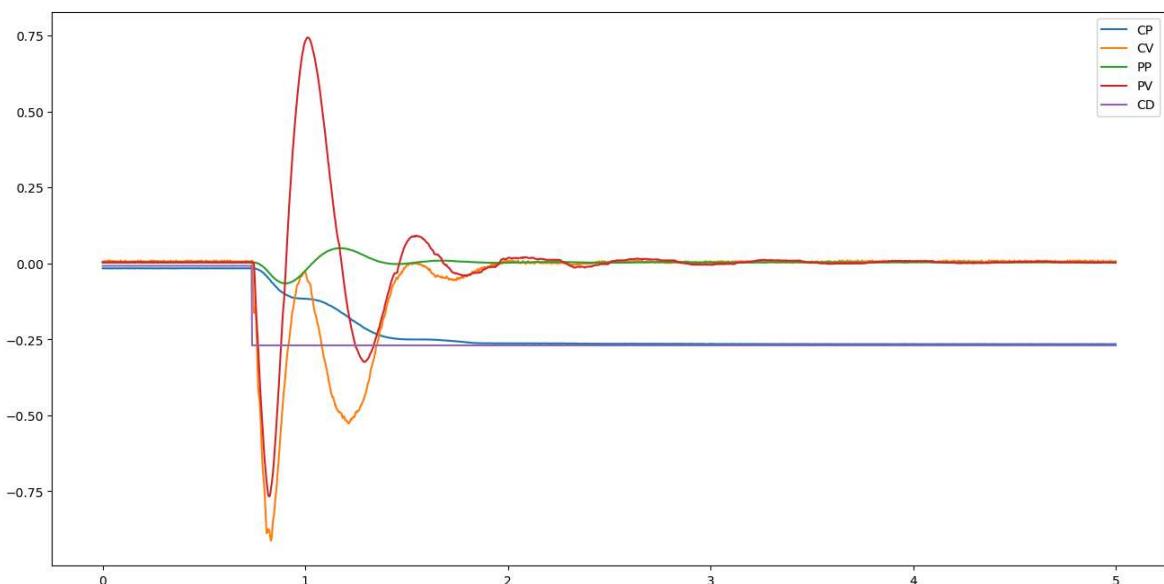
In [12]:

```

#####
# LOAD DATA #####
xdata, xdem, tdata =loadlogdata(4,Sc)
# in the previous line xdem is the external input into the system.

plt.plot(tdata,xdata)
plt.legend(['CP', 'CV', 'PP', 'PV', 'CD']);

```



In [13]:

```

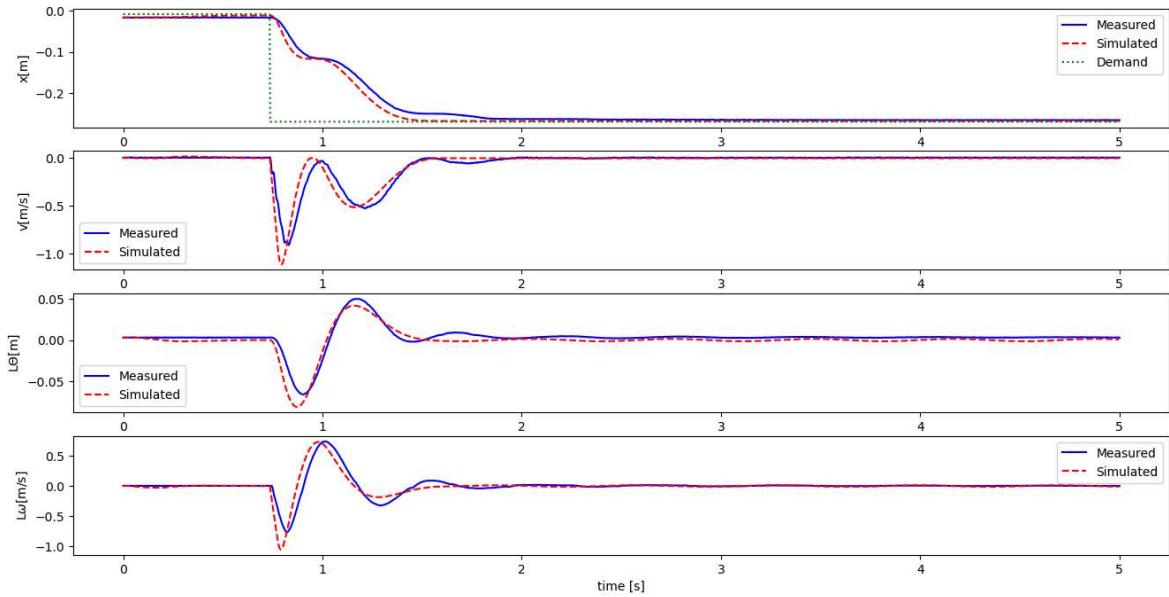
t0 = 0; tf = 5 # define the simulation time to be considered

# Set up the initial conditions and time index for the simulation, this uses the
# same data as the plot above
tsim = np.arange(t0,tf,h_sim)
x0=scipy.interpolate.interp1d(tdata,xdata[:, :4].T)(t0)

x_sim = solver_crane(x0,tsim,tdata,xdem,P)

plot_function_crane(t0,tf,tdata,xdata,tsim,x_sim,P)

```

Crane position with $p = [0.47559633 \ 0.4887481 \ 0.27313498 \ 0.2984814]$ 

Comment here on the response

The measured response agrees well to the simulated response.

By placing the poles further away from the origin, it is expected that the response decays faster. For this set of measurement, it takes around 1 second to steady-state, while it takes around 1.5 second in the previous measurement.

3.5) Variation of p_2

With the design 3.4(b) vary p_2 until instability just occurs. Log the step response just prior to the onset of oscillations, and record the value of p_2 . Use the linear model in appendix A to predict the gain k_2 at which oscillation will occur, and predict the resonant frequency $\hat{\omega}$ see section A.5). Compare these with your experimental results (note: $k_2 = 165 p_2$ — see A.7(a))

```
In [14]: p1 = 0.48
p2 = 0.22 # value used in the Lab at onset of instability
p3 = 0.27
p4 = 0.30

k1 = 617 * p1
k2 = 165 * p2
k3 = 1256 * p3
k4 = -126 * p4

"""
k2^2 (k3 + w0 - w1) + k2k4 (k3 + w0 - k1) - k1k4^2 = 0
"""

a = k3 + w0 - w1
b = k4*(k3 + w0 - k1)
c = -k1 * k4**2
k2_theory = (-b + np.sqrt(b**2 - 4*a*c))/(2*a)
```

```
p2_theory = k2_theory/165

w_r = np.sqrt(k2_theory/(k2_theory+k4) * w1)

T = (4.78 - 1.09)/12
f = 1/T

print(f'measured p2 = {p2} \ntheoretical p2 = {p2_theory:.2f} \ntheoretical k2 = {k2:.2f}')
print(f'measured oscillation frequency = {f:.2f} Hz')
print(f'theoretical oscillation frequency = {w_r/(2*np.pi):.2f} Hz')
```

measured p2 = 0.22
 theoretical p2 = 0.26
 theoretical k2 = 42.53
 measured oscillation frequency = 3.25 Hz
 theoretical oscillation frequency = 4.23 Hz

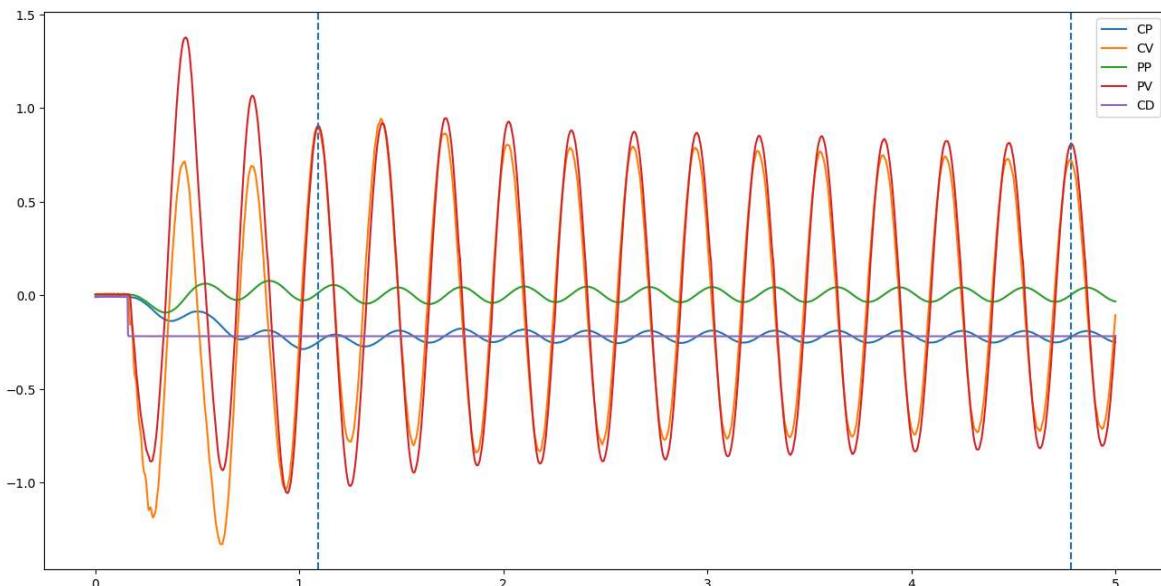
In [15]: ##### LOAD DATA #####

```
xdata, xdem, tdata = loadlogdata(5,Sc)
# in the previous line xdem is the external input into the system.

plt.plot(tdata,xdata)
plt.legend(['CP', 'CV', 'PP', 'PV', 'CD'])

# Lines to help measure the period of the oscillation in the last plot
plt.axvline(1.09, linestyle = '--')
plt.axvline(4.78, linestyle = '--')
```

Out[15]: <matplotlib.lines.Line2D at 0x2be74fe3440>



In [16]: P = np.array([[p1,p2_theory,p3,p4]])
 print("P:", P)
 print(np.linalg.eig(Ac-B@P@Cc)[0])

```
P: [[0.48 0.25776687 0.27 0.3]
 [ 0.04101444+26.57519899j 0.04101444-26.57519899j
 -2.36768528 +5.22680322j -2.36768528 -5.22680322j]]
```

In [17]: t0 = 0; tf = 5
 # define the simulation time to be considered

 # Set up the initial conditions and time index for the simulation, this uses the

```

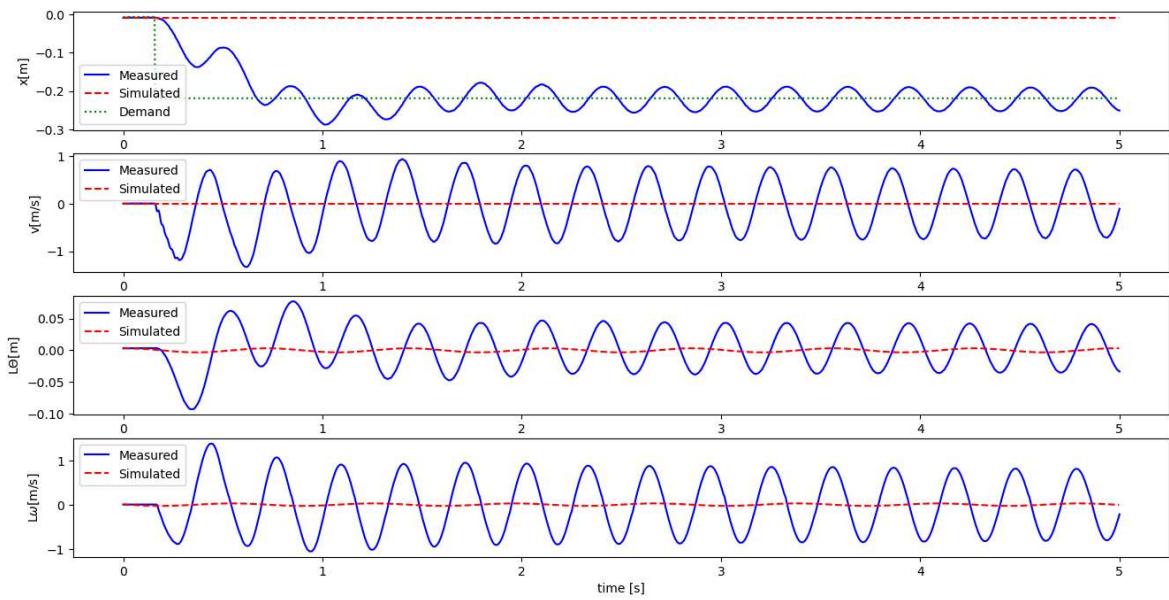
tsim = np.arange(t0,tf,h_sim)
x0=scipy.interpolate.interp1d(tdata,xdata[:,4].T)(t0)

x_sim = solver_crane(x0,tsim,tdata,xdem,P)

plot_function_crane(t0,tf,tdata,xdata,tsim,x_sim,P)

```

Crane position with p = [[0.48 0.25776687 0.27 0.3]]



Comment and discuss here section 3.5)

Value of p_2 at the onset of the oscillations: 0.22

Predicated gain k_2 : 42.4

Predicted frequency $\hat{\omega}$: 4.23 Hz

Compare with actual gain and experimental results:

The code does not initiate a simulation. The reason might be the oversimplification of the model. The non-linearity of the model only relies on a Coulomb friction model. In reality, the physical rig experiences complex friction and cable drag.

What's more, the simulation relies on the theoretical value of p_2 , which has uncertainties in physical parameters (M, L, etc.).

4) Pendulum mode

4.2) No carriage feedback

Set $p_1 = p_2 = 0$ and p_3 and p_4 to stabilize the pendulum dynamics, say $p_3 = 0.500$ and $p_4 = 0.110$. Now hold the pendulum upright and press RESET.

Manually note the force, on the pendulum, required to move the carriage - TAKE DUE CARE. Let go of the pendulum and explain the subsequent behaviour.

```
In [18]: P = np.array([[0.0, 0.0, 0.5, 0.11]])
print("P:", P)
print(np.linalg.eig(Ap-B@P@Cp)[0])
# Note that the [0] is there to ignore the second output of eig
```

```
P: [[0.  0.  0.5  0.11]]
[ 0.          +0.j        0.          +0.j
 -13.90617284+25.40781422j -13.90617284-25.40781422j]
```

Comment and discuss here section 4.2)

The carriage moves to the desired position while the inverted pendulum stays up.

4.3) Pole placement

Using example 2 in section A.5 and the data in section A.7 calculate p_i to place the closed-loop poles at $-\omega_1 = -\sqrt{78.5}$, and record your calculated values. Log the response.

```
In [19]: k1 = - w1
k2 = -4 * np.sqrt(w1)
k3 = w0 + 7 * w1
k4 = 8 * np.sqrt(w1)

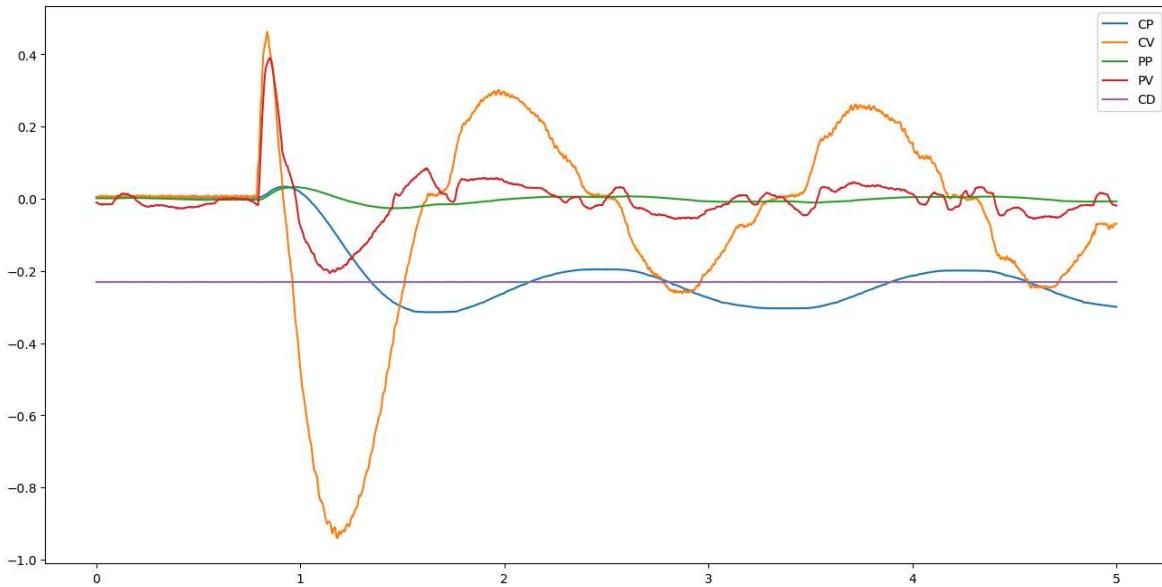
p1 = -k1 / 309
p2 = - k2 / 110
p3 = k3 / 1884
p4 = k4 / 253

P = np.array([[p1, p2, p3, p4]])
print("P:", P)
print(np.linalg.eig(Ap-B@P@Cp)[0])
# Note that the [0] is there to ignore the second output of eig
```

```
P: [[0.25404531 0.32218264 0.34649682 0.28015882]]
[-10.62609236+2.74532358j -10.62609236-2.74532358j
 -7.05158309+1.16740753j -7.05158309-1.16740753j]
```

```
In [20]: ##### LOAD DATA #####
xdata, xdem, tdata = loadlogdata(6,Sp)
# in the previous line xdem is the external input into the system.

plt.plot(tdata,xdata)
plt.legend(['CP','CV','PP','PV','CD']);
```



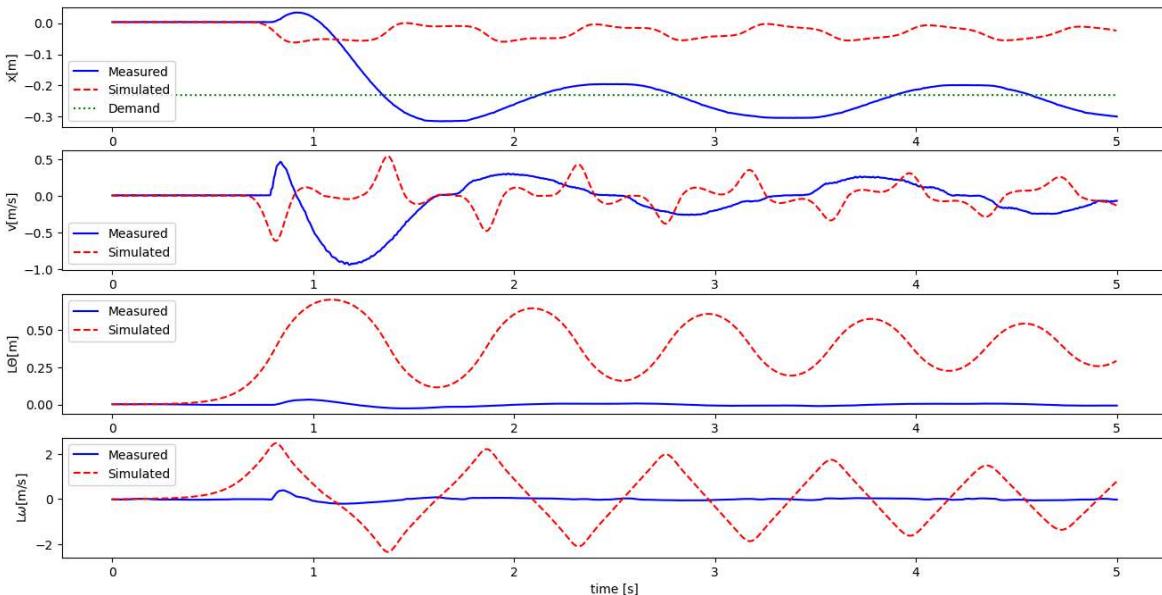
```
In [21]: t0 = 0; tf = 5 # define the simulation time to be considered

# Set up the initial conditions and time index for the simulation, this uses the
tsim = np.arange(t0,tf,h_sim)
x0=scipy.interpolate.interp1d(tdata,xdata[:,4].T)(t0)

x_sim = solver_pendulum(x0,tsim,tdata,xdem,P)

plot_function_pendulum(t0,tf,tdata,xdata,tsim,x_sim,P)
```

Pendulum position with $p = [[0.25404531\ 0.32218264\ 0.34649682\ 0.28015882]]$



4.4) Limit Cycles

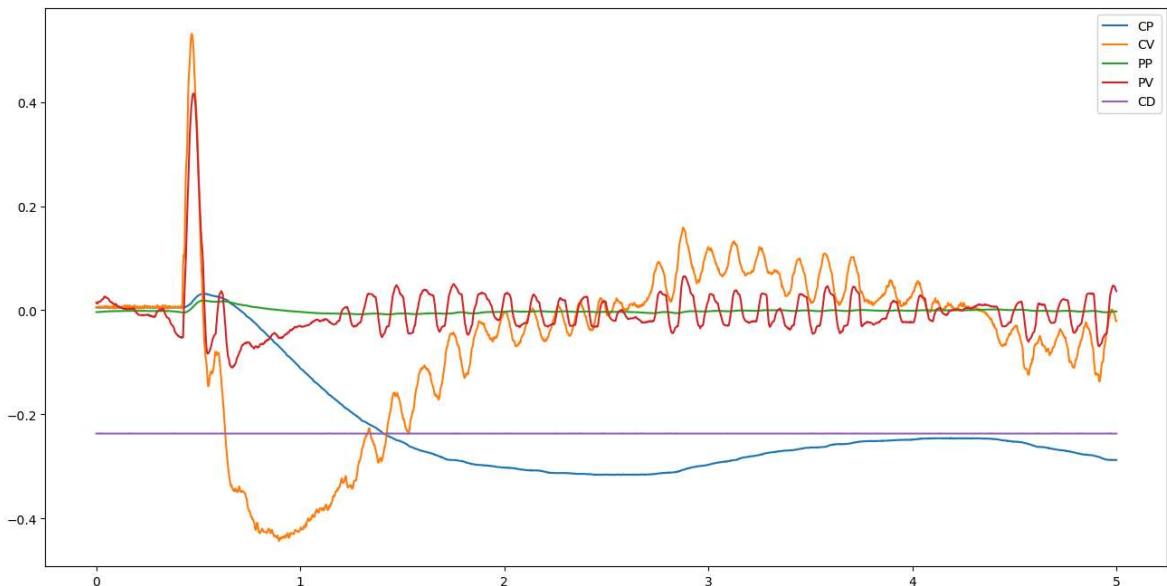
Set the potentiometers to $p_1 = 0.23$ $p_2 = 0.50$ $p_3 = 0.63$ $p_4 = 0.40$ which should give a reasonably stable response. Now reduce p_2 until large oscillations occur (i.e. the carriage nearly hits the end stops). Record your value of p_2 , and log the response. Now increase p_2 until the system is almost unstable. Record your value of p_2 , and log the response to a small step.

```
In [22]: P = np.array([[0.23, 0.5, 0.63, 0.4]])
print("P:", P)
print(np.linalg.eig(Ap-B@P@Cp)[0])
# Note that the [0] is there to ignore the second output of eig
```

```
P: [[0.23 0.5 0.63 0.4 ]]
[-20.51101586+19.4423977j -20.51101586-19.4423977j
 -2.52602118 +0.77095105j -2.52602118 -0.77095105j]
```

```
In [23]: ##### LOAD DATA #####
xdata, xdem, tdata = loadlogdata(9,Sp)
# in the previous line xdem is the external input into the system.

plt.plot(tdata,xdata)
plt.legend(['CP','CV','PP','PV','CD']);
```

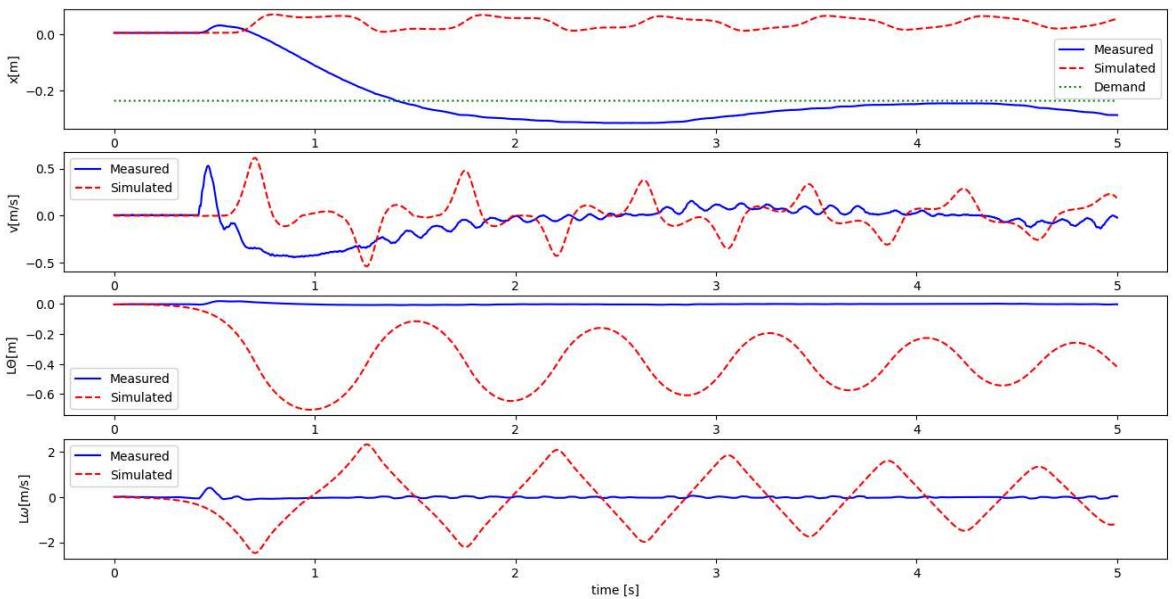


```
In [24]: t0 = 0; tf = 5 # define the simulation time to be considered

# Set up the initial conditions and time index for the simulation, this uses the
# same time points as the recorded data
tsim = np.arange(t0,tf,h_sim)
x0=scipy.interpolate.interp1d(tdata,xdata[:,4].T)(t0)

x_sim = solver_pendulum(x0,tsim,tdata,xdem,P)

plot_function_pendulum(t0,tf,tdata,xdata,tsim,x_sim,P)
```

Pendulum position with $p = [[0.23 \ 0.5 \ 0.63 \ 0.4]]$ 

Comment and discuss here section 4.4)

Value of p_2 for large oscillations: 0.42

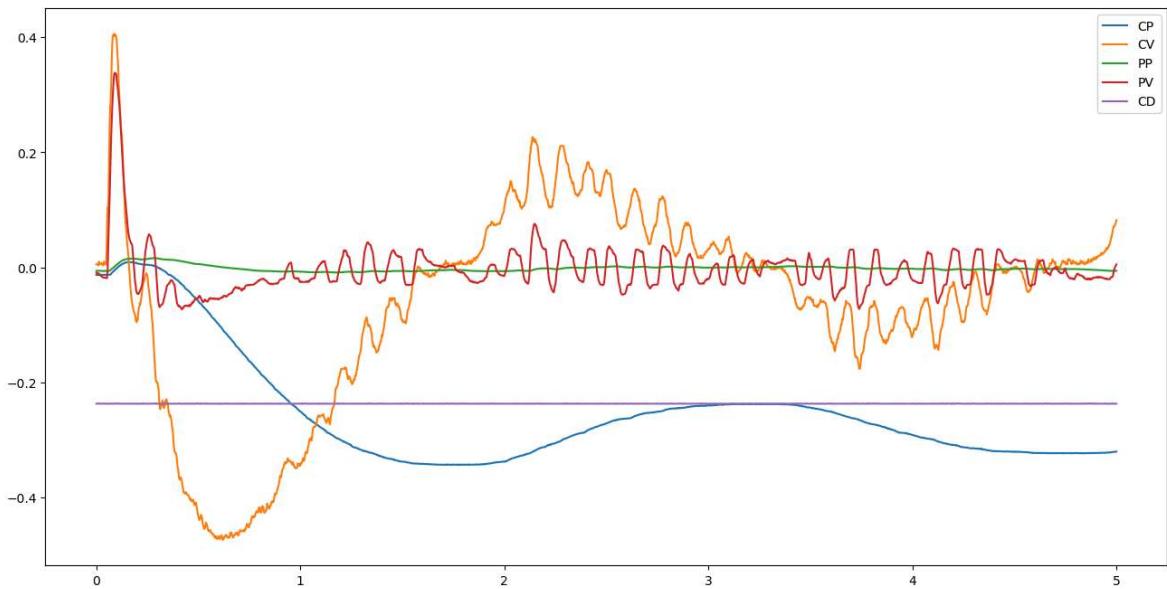
Now vary p_2

```
In [25]: P = np.array([[0.23, 0.42, 0.63, 0.4]])
print("P:", P)
print(np.linalg.eig(Ap-B@P@Cp)[0])
# Note that the [0] is there to ignore the second output of eig
```

```
P: [[0.23 0.42 0.63 0.4 ]]
[-25.38834515+12.36207684j -25.38834515-12.36207684j
 -2.05363016 +1.66411981j -2.05363016 -1.66411981j]
```

```
In [26]: ##### LOAD DATA #####
xdata, xdem, tdata = loadlogdata(7,Sp)
# in the previous line xdem is the external input into the system.

plt.plot(tdata,xdata)
plt.legend(['CP','CV','PP','PV','CD']);
```

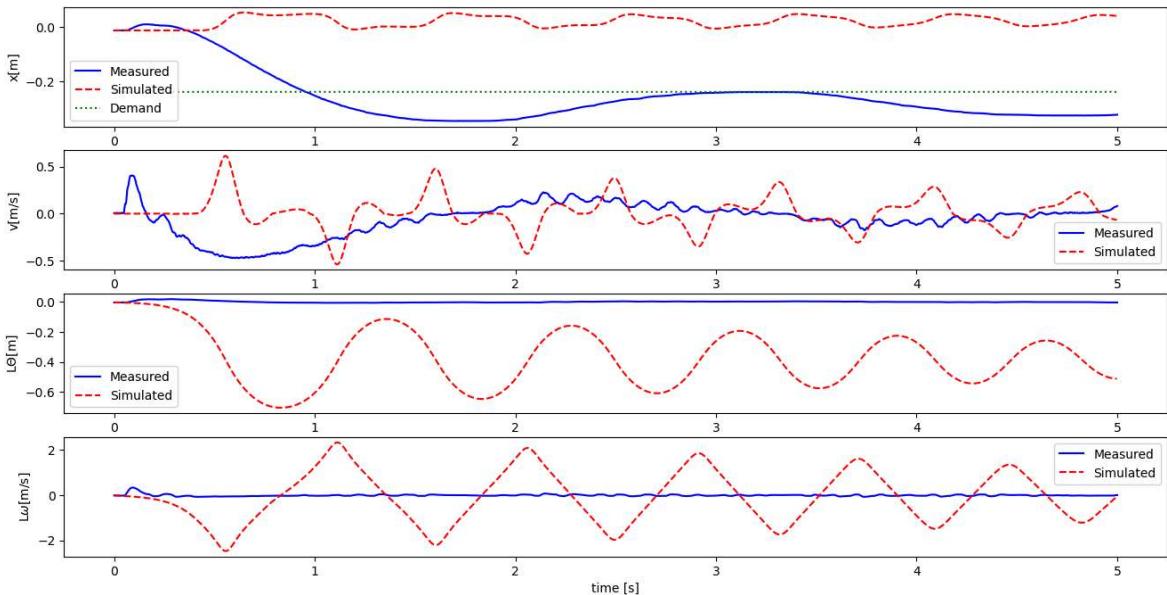


```
In [27]: t0 = 0; tf = 5 # define the simulation time to be considered

# Set up the initial conditions and time index for the simulation, this uses the
tsim = np.arange(t0,tf,h_sim)
x0=scipy.interpolate.interp1d(tdata,xdata[:,4].T)(t0)

x_sim = solver_pendulum(x0,tsim,tdata,xdem,P)

plot_function_pendulum(t0,tf,tdata,xdata,tsim,x_sim,P)
```

Pendulum position with $p = [[0.23 \ 0.42 \ 0.63 \ 0.4]]$ 

Comment and discuss here section 4.4) after changing p_2

Value of p_2 for at the onset of instability: 0.77

For small value of p2, large oscillation occurs. This corresponds to limit cycle, during which the damping of the system is reduced by a small value of p2. For such nonlinear system, a smaller damping could not dissipate energy effectively. Thus, there will be a large oscillation with low frequency.

For large value of p2, the system tends to reach instability. This infers that the system is very sensitive to velocity gain, a small noise could be amplified to make the system unstable.

4.5) No pendulum feedback

If the design of 4.3) is implemented except with $p_3 = p_4 = 0$ what would happen, and why?

```
In [28]: P = np.array([[0.25, 0.32, 0, 0]])
print("P:", P)
print(np.linalg.eig(Ap-B@P@Cp)[0])
# Note that the [0] is there to ignore the second output of eig
```

P: [[0.25 0.32 0. 0.]]
[37.96301272 8.51904027 -2.03316228 -9.20938453]

Comment and discuss here section 4.5

The carriage moves very fast and lost control. The inverted pendulum can not stand.

Feedback to the student

Content

Completeness, quantity of content: Very good | Good | Needs improvement

Has the report covered all aspects of the lab? Has the analysis been carried out thoroughly?

Correctness, quality of content: Very good | Good | Needs improvement

Is the data correct? Is the analysis of the data correct? Are the conclusions correct?

Depth of understanding, quality of discussion: Very good | Good | Needs improvement

Does the report show a good technical understanding? Have all the relevant conclusions been drawn?

Comments

...

Presentation

Attention to detail, typesetting and typographical errors:
Very good | Good | Needs improvement

Is the report free of typographical errors? Are the figures/tables/references presented professionally?

Comments

...

Raw report Mark:

The weighting of comments is not intended to be equal, and the relative importance of criteria may vary between modules. A good report should attract 4 marks.

Penalty for lateness:

1 mark / week or part week. Please refer to the online information regarding our extension policy.

Marker:

Date: