# Learning From Differences

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April 6, 2024

Final-Year Project - B.Sc. in Computer Science

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#### **Abstract**

This study presents an innovative exploration into the realm of machine learning, specifically focusing on enhancing model interpretability and performance through a novel ensemble of model-based and instance-based learning approaches. Grounded in the principles of Case-Based Reasoning (CBR) and the Learning From Differences methodology, we introduce the LingerRegressor and LingerClassifier models. These models aim to leverage the strengths of both learning approaches to address the limitations present in traditional machine learning algorithms, particularly in the contexts of regression and classification tasks.

Our methodology involves a detailed examination of the algorithms' design and implementation, highlighting the integration of novel variations such as context inclusion, duplication based on distance, and the addition of a distance column to further refine the learning process. Through extensive experiments, we demonstrate the models' effectiveness in achieving higher interpretability and robust performance across diverse datasets. The LingerRegressor and LingerClassifier models not only offer new avenues for academic research but also practical implications for developing more transparent and efficient machine learning systems.

The findings underscore the potential of blending model-based and instance-based learning to enhance machine learning models' adaptability and interpretability. Future work will focus on addressing the identified limitations and exploring the applicability of our approach to broader machine learning challenges. This study contributes to the ongoing dialogue on improving machine learning methodologies and paves the way for further innovation in the field.

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# Chapter 1

# Introduction

Machine learning encompasses various paradigms and methodologies aimed at enabling computational systems to learn from data and make predictions or decisions without explicit programming. Among the diverse approaches in machine learning, model-based and instance-based learning represents two fundamental strategies, each with distinct advantages and disadvantages.

# 1.1 Model-Based Learning

Model-based learning involves the construction of explicit representations of the underlying relationships within the data. These representations, often referred to as models, capture the patterns and structures present in the dataset and can be used to make predictions or infer insights from new, unseen data points. For instance, artificial neural networks (ANNs) exemplify model-based learning by discerning trends and patterns in data.

## 1.1.1 Advantages of Model-Based Learning:

1. Generalization: Well-constructed models have the ability to generalize patterns learned from the training data to unseen instances, thereby making accurate predictions on new data samples. This generalization capability is essential for robust performance across diverse datasets and real-world scenarios. For example, a well-trained regression model can accurately predict housing prices in different regions based on historical data. The book [4] provides insights into the generalization capabilities of model based learning.

- 2. Robustness: Models learn underlying patterns and assumptions within data, making them more robust to noisy outliers. By capturing trends within data, models can effectively mitigate noise, enhancing their reliability in real-world scenarios. The book [4] also shows the ability of models to learn underlying patterns within data, making them far more robust to noisy data.
- 3. **Efficiency:** Once trained, model-based systems can quickly return predictions, making them suitable for real-time applications where rapid decision-making is essential. The journal [8] offers an insight how the efficiency of model based learning can be implemented to make predictions on big data.

### 1.1.2 Disadvantages of Model-Based Learning:

- 1. Sensitivity to Assumptions: Models often rely on simplifying assumptions about data distribution and relationships. Deviations from these assumptions can significantly degrade performance, leading to inaccurate predictions or biased outcomes. For example, a model trained to predict house prices based on 2017 data may inaccurately predict house prices for 2023. The book "Machine Learning: A Bayesian and Optimization Perspective" by Sergios Theodoridis and Konstantinos Koutroumbas emphasizes the crucial role assumptions play in model sensitivity, stressing their significance in machine learning applications [16].
- 2. Interpretability and Decision-Making: Certain models, like Neural Networks, lack transparency in decision-making despite their high accuracy. In critical domains like healthcare and finance, interpretability is crucial for validating decisions and ensuring trust in the system. This disadvantage of lack of transparency is depicted well in the journal [14].
- 3. Limited Flexibility: Traditional model-based algorithms struggle to capture complex, non-linear relationships in high-dimensional or unstructured data, limiting their performance in tasks with intricate patterns or diverse feature interactions.

## 1.2 Instance-Based Learning

Instance-based learning, also known as memory-based learning or lazy learning, eschews explicit model construction in favor of storing and manipulating instances or examples from the training data. Instead of deriving general rules or representations,

instance-based methods make predictions based on the similarity between new instances and those observed in the training set. A classic example of instance-based learning is the k-nearest neighbors (KNN) algorithm. The advantages and disadvantages discussed with instance based learning are seen in the paper [2].

### 1.2.1 Advantages of Instance-Based Learning:

- 1. **Flexibility:** Instance-based methods adapt to the characteristics of the training data, making them suitable for tasks with complex, non-parametric relationships or evolving patterns. They can capture nuances and irregularities without imposing rigid assumptions.
- 2. Explainability: The transparency of instance-based learning enables analysts to trace predictions back to specific examples in the training set, facilitating interpretability and trust in the system. The journal [14] highlights this issue for black box model based learning such as neural nets.

### 1.2.2 Disadvantages of Instance-Based Learning:

The disadvantages discussed with instance based learning are discussed in the paper [2].

- 1. Computational Complexity: Storing and manipulating the entire training dataset can lead to high memory consumption and computational overhead during prediction, limiting scalability.
- 2. Susceptibility to Noise and Redundancy: Instance-based approaches are sensitive to noisy or irrelevant features, which can lead to suboptimal performance or overfitting. Redundant instances or outliers may distort similarity measures, compromising model robustness.

## 1.2.3 Motivation for Blended Learning

The advantages and disadvantages of both model-based and instance-based learning highlight the need for a versatile and robust approach to machine learning. While model-based learning excels in generalization and robustness, it lacks transparency and struggles with complex relationships. Instance-based learning offers flexibility and explainability but suffers from computational complexity and susceptibility to noise.

The motivation for blended learning arises from leveraging the strengths of both approaches while mitigating their weaknesses. Blended methods aim to capitalize on the advantages of model-based and instance-based learning, circumventing their limitations. By integrating the interpretability of instance-based learning with the accuracy of model-based systems, blended learning offers a promising solution for critical domains like healthcare and finance. The journal [14] provides further evidence that it is important to move towards interpretability for our models going forward, so that critical systems are interpretable and repairable by humans going forward.

In recent years, neural networks have gained significant attention in regression tasks [12]. Inspired by case-based reasoning principles [13], researchers are exploring predictive ensemble models based on these principles [17]. Deviating from conventional approaches, some researchers advocate for training neural networks on differences between sets of features to enhance efficiency and transparency [7].

By adopting a blended approach, machine learning systems can achieve greater interpretability, reliability, and performance across diverse applications.

# Chapter 2

# Literature Review

### 2.1 Introduction

The exploration of alternative methodologies for enhancing the performance of neural networks in regression tasks has garnered significant attention within the machine learning community in recent years. One innovative approach, inspired by the principles of case-based reasoning (CBR), involves training neural networks to predict differences between problems based on disparities between features rather than the features themselves. This departure from the conventional supervised learning paradigm aims to leverage the inherent advantages of learning from differences, potentially leading to more interpretable and efficient models.

The study under consideration [7] conducts a systematic factorial study to investigate the efficacy of this approach across various datasets and experimental conditions. The findings suggest that neural networks trained on differences demonstrate comparable or even superior performance to those trained using traditional methods, while requiring significantly fewer epochs for convergence. In this section of the literature review, we consider the utilization of case-based reasoning for regression tasks, with a specific focus on the implementation of KNN (K-Nearest Neighbors) and ANN (Artificial Neural Network) frameworks.

As we delve further into the literature review, we extend our exploration of case-based reasoning beyond regression tasks to include classification challenges. The study by Ye et al. [18], titled "Learning Adaptations for Case-based Classification," offers insights into the application of CBR in classification tasks, shedding light on recent advancements and methodologies. Through a detailed analysis of various adaptation

strategies and neural network-based approaches, we aim to uncover the effectiveness of CBR in solving classification problems, thereby providing a comprehensive understanding of its utility across different machine learning tasks.

# 2.2 KNN + ANN for Regression, Utilizing CBR

The exploration of alternative methodologies for enhancing the performance of neural networks in regression tasks has attracted considerable attention within the machine learning community in recent years. One innovative approach, inspired by the principles of case-based reasoning (CBR), involves training neural networks to predict differences between problems based on disparities between features rather than the features themselves. This departure from the conventional supervised learning paradigm aims to leverage the inherent advantages of learning from differences, potentially leading to more interpretable and efficient models. The study under consideration [7] conducts a systematic factorial study to investigate the efficacy of this approach across various datasets and experimental conditions. The findings suggest that neural networks trained on differences demonstrate comparable or even superior performance to those trained using traditional methods, while requiring significantly fewer epochs for convergence. In this section of the literature review, we consider the utilization of case-based reasoning for regression tasks, with a specific focus on the implementation of KNN (K-Nearest Neighbors) and ANN (Artificial Neural Network) frameworks.

## 2.2.1 Learning From Differences Paper

The paper by [7] introduces the innovative concept of training a neural network based on the disparities between a case and its closest neighbors. Titled "A Factorial Study of Neural Network Learning from Differences for Regression" [7], the study aims to present novel learning methodologies geared towards enhancing performance and fostering a more interpretable learning process. The research evaluates three model variations: a benchmark neural network, a learning from differences model, and an augmented learning from differences model incorporating the original context. The context here refers to the base case, from which differences with its nearest neighbors are calculated.

According to [7], the study's key findings underscore a significant increase in accuracy when incorporating contextual information in the learning process. Moreover, comparable or superior results were achieved with fewer training epochs compared to the basic neural network. This enhancement is attributed partly to the broader training

dataset that encompasses neighbors greater than 1. Notably, the paper advocates for a hybrid approach, combining learning from differences with direct feature-based learning, which yields superior results.

The related work for the paper [7] has addressed the use of neural networks in the case-based reasoning process. These papers have focused on exploiting the base case using the idea that adaptation of information is acquirable from the differences between pairs [9]. Since then, various different approaches have been used. More recently, in relation to using neural networks to predict the differences between problems, a few interesting points have been investigated. These points show the ability of a neural network to correct the solution of the most similar retrieved case. These preliminary works expressed in the paper showed that the use of differences plus context yielded superior results [6]. The previous studies examined in the paper [7] did not examine the impact of different parameters during the CBR (case-based reasoning) experiments. The paper [7] made an effort to explore the effect of epochs in the learning process.

The graphical representations in the paper highlight a distinct trend: rapid attainment of high accuracy levels with the learning from differences method, particularly when contextual information is included. Conversely, the basic neural network requires a substantially larger number of epochs to achieve comparable accuracy, if not worse. This disparity suggests the efficiency of the learning from differences approach.

The paper suggests a marginal performance enhancement and a substantial reduction in training epochs through the adoption of the differences method and inclusion of contextual information. However, it is crucial to acknowledge the time overhead associated with retrieving and training using similar cases.

## 2.2.2 Algorithms

The training algorithm for learning from differences is described in Algorithm 1, while the prediction algorithm is outlined in Algorithm 2. Additionally, a variant of the training algorithm with context included is presented in Algorithm 3, and the corresponding prediction algorithm is provided in Algorithm 4.

Context which is utilized in 3, and 4. Context is the case used to retrieve (Nearest Neighbors). In the training algorithm it is  $X_i^{train}$ , and in prediction it is  $X_j^{test}$ . These are included in the training, and prediction in Variant 2.

The paper [7] has an associated library where they have implemented a regression-based machine learning model.

#### Algorithm 1 Training Algorithm for Learning from Differences

Input: Dataset D, neural network model, number of neighbors n, number of epochs E

- 1: Split D into training set  $D^{train}$  and test set  $D^{test}$  with a 80%-20% split
- 2: Initialize  $\Delta D^{train}$  as an empty list
- 3: for each case  $C_i = (X_i^{train}, y_i^{train}) \in D^{train}$  do
- 4: Retrieve n similar cases from  $D^{train}$  using nearest neighbors
- 5: **for** each similar case  $(X_j^{train}, y_j^{train}) \in D^{train}$  **do**
- 6: Compute the differences:  $\Delta D_{ij}^{train} = (X_i^{train} X_j^{train}, y_i^{train} y_j^{train})$
- 7: end for
- 8: end for
- 9: Train the MLPRegressor neural network model using  $\Delta D^{train}$  over a few epochs for later predictions.
- 10: **Return** Trained neural network model TrainedNN()

#### Algorithm 2 Prediction Algorithm for Learning from Differences

**Input:** Test dataset  $D^{test}$ , trained neural network model TrainedNN(), number of neighbors n

```
for each case X_j^{test} \in D^{test} do

Retrieve n similar cases from D^{train} using nearest neighbors
Initialize empty list y^{pred}predictions

for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do
```

Compute the differences:  $\Delta X_{ij}^{test} = X_j^{test} - X_i^{train}$ 

Use the trained neural network to predict:  $TrainedNN(\Delta X_{ij}^{test}) = \Delta X_{ij}^{pred}$ 

Adapt neighbor's y values:  $y^{pred}predictions_j = X_i^{train} + \Delta X_{ij}^{pred}$ 

end for

Average the adapted y values:  $y_j^{pred} = \frac{1}{n} \sum_{i=1}^n y^{pred} predictions$ 

Compare  $y_j^{pred}$  to  $y_j^{test}$  to evaluate accuracy

end for

#### Algorithm 3 Training Algorithm for Learning from Differences with context

**Input:** Dataset D, neural network model, number of neighbors n, number of epochs E

- 1: Split the dataset D into training set  $D^{train}$  and test set  $D^{test}$  using an 80%-20% split.
- 2: Initialize  $\Delta D^{train}$  as an empty list.
- 3: for each case  $C_i = (X_i^{train}, y_i^{train}) \in D^{train}$  do
- 4: Retrieve n similar cases from  $D^{train}$  using nearest neighbors.
- 5: **for** each similar case  $(X_j^{train}, y_j^{train}) \in D^{train}$  **do**
- 6: Compute the differences, with concatenated context :  $\Delta D_{ij}^{train} = ((X_i^{train} X_j^{train}) : X_i^{train}, y_i^{train} y_j^{train}).$
- 7: Append  $\Delta D_{ij}^{train}$  to  $\Delta D^{train}$ .
- 8: end for
- 9: end for
- 10: Train the MLPRegressor neural network model using  $\Delta D^{train}$ .
- 11: **return** Trained neural network model TrainedNN().

#### Algorithm 4 Prediction Algorithm for Learning from Differences with context

**Input:** Test dataset  $D^{test}$ , trained neural network model TrainedNN(), number of neighbors n

```
for each case X_j^{test} \in D^{test} do Retrieve n similar cases from D^{train} using nearest neighbors Initialize y_j^{pred} as an empty list for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do ' Initialize empty list y^{pred}predictions Compute the differences: \Delta X_{ij}^{test} = ((X_j^{test} - X_i^{train}) : X_j^{test}) Use the trained neural network to predict: \Delta X_{ij}^{pred} = TrainedNN(\Delta X_{ij}^{test}) Adapt neighbor's y values: y^{pred}predictions_j = y_i^{train} + \Delta X_{ij}^{pred} end for Average the adapted y values: y_j^{pred} = \frac{1}{n} \sum_{i=1}^n y_i^{pred} Compare y_j^{pred} to y_j^{test} to evaluate accuracy end for
```

The new model proposed in the paper is tested using the factorial study methodology. This process involved finding a network structure through experimental means for each dataset. It entailed training and testing using a wide range of hyperparameters to determine the optimal settings.

Despite its contributions, the paper falls short by confining its attention to regression tasks and not considering classification tasks and exploring additional variations of the learning from differences model beyond context inclusion. Incorporating original values for the base case in the generated differences dataset provides a valuable framework for understanding the observed disparities. While the model with contextual inclusion demonstrates slight improvements over the base model in learning from differences, a more comprehensive examination of the methodology is warranted for further refinement and enhancement.

The paper tested three models using the same factorial methodology: a base version, which is a basic neural network trained empirically; a differences model employing the (CBH) Case-based Heuristic for predictions, (CBH) guides how cases are retrieved with respect to the base case, and how the retrieved cases are adapted to produce a prediction, (CBH) relies on the adaptation of previous problems to solve the current issue; and a differences model with its base context included. The results yielded interesting insights, with similar performance for all three models and a slight improvement in the differences + context model. Notably, the differences and differences + context models required significantly fewer epochs to achieve accuracy compared to the basic neural network, which achieved similar accuracy after more epochs.

Another consideration in the paper [7] was the number of neighbors for both training

and prediction. The study revealed no consistent trend across datasets, suggesting dataset-specific requirements.

In conclusion, the learning from differences method achieved equal or higher accuracy compared to the base neural network model.

# 2.3 Learning Adaptations for Case-based classification

The paper by Ye et al. [18], titled "Learning Adaptations for Case-based Classification," investigates the application of Case-Based Reasoning (CBR) for classification tasks. It explores recent advancements in CBR, particularly focusing on replacing traditional rule-based learning with Case-Based Heuristic (CBH) network models for adaptation. The study introduces a novel model comprising three variations: segmentation of adaptation knowledge based on the classes of the source cases, training a single neural network on differences between problem solutions, and adapting from an ensemble of source cases followed by a majority vote.

The "NN-CDH" method, as proposed in the paper, represents a novel classification approach that operates on pairs of cases, where one serves as the source and the other as the target. These pairs form the basis of adaptation knowledge, which is learned through neural network models. The methodology adopted in [18] emphasizes learning adaptation knowledge through case pairs processed by neural networks.

The study introduces the first neural network-based approach to classification, termed "C-NN-CDH" or Classification with Neural Network-based Case Difference Heuristic. This approach employs neural networks to learn adaptation knowledge from pairs of cases. According to the findings, this methodology outperforms traditional statistical models, as evidenced in [10].

The first approach involves segmenting the dataset by class and training a neural network for all segmented differences set between base cases. This method offers faster training but slightly less accuracy, according to the paper. The use of these CBR methods provides at least two benefits: inertia-free lazy learning and the ability to assess different cases when running classification. Inertial free means that the model does not make assumptions based on the underlying structure of the data, and lazy learning pertains to an algorithm that will postpone generalization until it is certain a new instance needs to be classified. It will only classify as the data comes; it won't try and learn or adapt preemptively.

In the process of CBR, adaptation is often treated as the most difficult. Various methods have been developed by academics over the years to tackle the issue. For example, Leake et al. [11] extrapolate a method in which the case base adaptation cases are populated from previously successful adaptations. Another approach is to have a stored base case and query and retrieve the case most similar to it, and adapting the retrieved case to the base case [6].

In the paper by Ye et al. [18], several design questions had to be addressed. How to approach case differences and how to select case pairs for training. The paper in question [18] considers standard pair selection methods as well as a new training per selection approach based on class-class classification.

The paper [18] also addresses the application of (CDH) method for classification. It discusses the value distance metric, which is a probabilistic method to measure the similarity that allows the comparison of nominal values in a single-dimensional space.

### 2.3.1 An NN-CDH Approach for Classification

To achieve adaptation, a neural network is integrated into the process. The source and target cases become case pairs, and their adaptation is learned through a neural network. The neural network computes the difference between the source and target pairs. This difference calculation is a crucial step in the Case-Based Reasoning (CBR) system. Once the difference is computed, the predicted result obtained from the neural network is applied to the source solution. This adapted solution is then considered as the final result of the classification process.

The NN-CDH approach represents a fusion of neural network techniques with the principles of Case-Based Reasoning, offering a dynamic and adaptable method for classification tasks. When calculating the difference between the problem and the solution values, it is important to implement a difference function. This presents an interesting challenge for nominal values. The method presented in [18] uses an implicit calculation through machine learning techniques. This replaces traditional (CDH) case difference heuristic approaches for difference calculations. Through the use of a neural network, the paper's method hopes to include the base context in the differences' calculation. This method for generating differences has been aptly named ("C-CDH") case difference heuristic approach for classification.

When calculating the difference, an issue arrives in that we cannot explicitly calculate differences through subtraction, which was the case in the previous paper by Learning

From Differences [7]. An implicit way of learning from differences is required. In the paper by Ye et al. [18], this is called "C-CDH".

This presents an interesting challenge for nominal values. The method presented in [18] uses an implicit calculation through machine learning techniques. When discussing the Neural Network-based Case-Driven Hierarchical (NN-CDH) Approach described in [18], notation will be homogenized with the algorithms from the previous paper.

For clarification when going through the algorithms, Retrieved cases = Source Cases, Target case = The case which we are attempting to predict its y label values.

Multiple variants were created with the paper by Ye et al. [18].

#### 2.3.2 Variant 0: Non-Network C-CDH

Variant 0, as described in [18], serves as a foundational test bed implementation for classification tasks. The algorithms presented here outline the process of building and utilizing a dictionary of case pairs, where each pair consists of a source case and its corresponding target case. Through the use of nearest neighbors, the algorithm identifies similar cases within the training dataset and organizes them based on their source solution. Subsequently, during prediction, the algorithm retrieves the nearest similar cases for each test case and utilizes the corresponding target solutions for classification. This approach embodies the essence of case-based reasoning, where solutions are adapted from similar past cases to classify new instances effectively. The following algorithms detail the steps involved in training and predicting using Variant 0's case-based heuristic approach.

```
Algorithm 5 Variant 0, Classification Using Case Based Heuristic, Training
```

```
Input: Dataset D, number of neighbors 1

Split D into training set D^{train} and test set D^{test} with an 80%-20% split Create CasePairs() dictionary.

for each case C_i = (X_i^{train}, y_i^{train}) \in D^{train} do

Retrieve 1 similar cases from D^{train} using nearest neighbors.

for each similar case (X_j^{train}, y_j^{train}) \in D^{train} do

CasePairs(y_j^{train}).append([X_j^{train}: X_i^{train}, y_i^{train}])

end for
end for
```

#### Algorithm 6 Variant 0, Classification Using Case Based Heuristic, Prediction

```
Input: Test dataset D^{test}, CasePairs()
 1: Initialize Empty list y^{pred}
 2: for each case X_i^{test} \in D^{test} do
        Retrieve 1 similar cases from D^{train} using nearest neighbors
 3:
        Initialize y_j^{pred} as an empty list
 4:
        for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do
 5:
             Retrieve r = 1NearestNeighbor(CasePairs(y_i^{train}), [X_i^{train} : X_i^{test}])
 6:
            y_i^{pred} = r
 7:
        end for
 8:
 9: end for
10: return y^{pred}
```

#### 2.3.3 Variant 1 - 2: C-NN-CDH

Variants 1 - 2, known as C-NN-CDH, represent a pivotal advancement in classification methodologies by integrating neural networks into the case-based heuristic framework. In this variant, the traditional case-based heuristic approach is augmented with the power of neural networks to adapt solutions from similar cases. The algorithms presented here delineate the training and prediction processes, where a neural network model learns adaptation knowledge from case pairs derived from the training dataset. Unlike Variant 0, which relies solely on case similarity for adaptation, C-NN-CDH leverages the expressive capacity of neural networks to capture intricate relationships between cases and their solutions. Through the fusion of case-based reasoning principles with neural network techniques, Variant 1 - 2 offers a dynamic and adaptable approach to classification tasks, capable of learning complex adaptation patterns and improving classification accuracy.

### 2.3.4 Variant 3 - 5: C-NN-CDH

Variants 3 - 5 of the classification neural network using case-based heuristics introduce a novel approach to classification by grouping case pairs based on their source solutions. In this framework, multiple specialized adaptation neural networks are employed, each trained to adapt cases of specific solutions to all solutions. Inspired by the ensemble of adaptations for classification approach, these variants share a common grouping and training method but differ in their testing strategies. The algorithms delineate the training process, where case pairs are organized and used to train specialized neural networks for adaptation. The variation arises in the prediction algorithm, where different strategies are employed to classify test instances based on the learned adaptation knowledge. The following section details the nuances of each variant's

**Algorithm 7** Variant 1 - 2: Classification Using Neural Net Case Based Heuristic (Training)

```
Input: Dataset D, neural network model, number of neighbors n, number of epochs E
  Split D into training set D^{train} and test set D^{test} with an 80%-20% split
  Create CasePairs list.
  for each case C_i = (X_i^{train}, y_i^{train}) \in D^{train} do
      Retrieve 1 similar case from D^{train} using nearest neighbors.
      for each similar case (X_j^{train}, y_j^{train}) \in D^{train} do
          if Variant 1 then
             CasePairs.append([X_i^{train}: X_i^{train}, y_i^{train}])
          else
             if Variant 2 then
                 CasePairs.append([X_i^{train}: X_i^{train}: y_i^{train}, y_i^{train}])
          end if
      end for
  end for
  Train the neural network model using CasePairs()
  return Trained neural network model TrainedNN().
```

Algorithm 8 Variant 1 - 2: Classification Using Neural Net Case Based Heuristic (Prediction)

```
Input: Test dataset D^{test}, trained neural network model TrainedNN()
```

```
1: Initialize Empty list y^{pred}
2: for each case X_j^{test} \in D^{test} do
3: Retrieve 1 similar case from D^{train} using nearest neighbors
4: for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do
5: Use the trained neural network to predict: y_j^{pred} = TrainedNN([X_i^{train}: X_j^{test}: y_i^{train}])
6: end for
7: end for
8: return y^{pred}
```

prediction methodology and discusses their implications for classification accuracy and adaptability.

**Algorithm 9** Variant 3 - 5: Classification Neural Network Using Case Based Heuristic (Training)

```
Input: Dataset D, number of neighbors 1

Split D into training set D^{train} and test set D^{test} with an 80%-20% split Create CasePairs() dictionary.

Create AdaptNN(), a dictionary to store each Neural Network

List of unique Classes UniqueClasses

for each case C_i = (X_i^{train}, y_i^{train}) \in D^{train} do

Retrieve 1 similar case from D^{train} using nearest neighbors.

for each similar case (X_j^{train}, y_j^{train}) \in D^{train} do

CasePairs(y_j^{train}).append([X_j^{train}: X_i^{train}, y_i^{train}])

end for

for each unique Class in UniqueClasses do

Create a new Classification Neural Network, trained on Case Pairs AdaptNN(Class).fit(CasePairs(Class))

end for

return Trained neural network models dictionary AdaptNN().
```

In variant (5), the prediction method utilizes a Class-to-Class approach for retrieving neighbors. This method retrieves the most similar neighbor for each class from the training dataset. Once the nearest neighbors for each class are identified, the corresponding specialized neural networks associated with those classes are employed to generate predictions for the target instance. Subsequently, a majority vote is conducted among the predictions from the specialized neural networks to determine the final classification outcome.

It is worth considering re-implementing the algorithm to allow for the retrieval of multiple neighbors (N) from each class during the prediction stage. This adjustment could potentially lead to improved results, particularly when dealing with large and varied datasets.

Variant (5) stands out as the most successful approach in the study, primarily due to its Class-to-Class retrieval of neighbors during the prediction stage. By employing multiple specialized neural networks, the variant reduces training time while effectively leveraging implicit learning through differences for classification tasks. This method demonstrates its efficacy in adapting to diverse datasets and achieving robust classification performance.

**Algorithm 10** Variant 3 - 5: Classification Using Neural Net Case-Based Heuristic (Prediction)

```
Input: D^{test}, AdaptNN(), UniqueClasses, and CasePairs()
  Initialize an empty list y^{pred}
  for each case X_j^{test} \in D^{test} do
       if Variant 3 then
           Retrieve 1 similar case from D^{train} using nearest neighbors
           for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do
               y_{j}^{pred} = AdaptNN(y_{i}^{train}).predict([X_{i}^{train}:X_{j}^{test}])
           end for
       else
           if Variant 4 then
                Create an empty list predictions
                Retrieve N similar cases from D^{train} using nearest neighbors
               \begin{array}{l} \textbf{for each similar case} \ (X_j^{train}, y_j^{train}) \in D^{train} \ \textbf{do} \\ predictions. \textbf{append} (Adapt(y_i^{train}).predict([X_i^{train}: X_j^{test}])) \end{array}
                end for
                Perform a majority vote on predictions
                y_j^{pred} = MajorityVote(predictions)
           else
                if Variant 5 then
                    Create an empty list preds
                    for each unique class Class in UniqueClasses do
                        Retrieve 1 similar case from CasePairs(Class)
                        for each similar case (X_i^{CasePair}, y_i^{CasePair}) \in CasePairs(Class) do for each (X_z^{train}, X_q^{train}) \in X_i^{CasePair} do
                                 preds.append(AdaptNN(Class).predict(X_z^{train}:X_i^{test}))
                             end for
                        end for
                        Perform a majority vote on preds
                        y_i^{pred} = MajorityVote(preds)
                    end for
                end if
           end if
       end if
   end for
   return y^{pred}
```

### 2.3.5 Evaluation Summary

Within the paper [18] the experiments conducted on two different datasets provided answers to several key questions.

The effectiveness of neural network learning adaptation knowledge was demonstrated through consistent performance of one or more C-NN-CDHs, which often outperformed the neural network classifier. Despite the possibility of neural networks learning to discard the source problem and rely solely on the target problem, the non-zero weights associated with the source problem and significant performance differences between C-NN-CDHs and the neural network indicate that C-NN-CDHs effectively learn adaptation knowledge. This suggests that if a neural network can handle the classification task directly, it can also learn adaptation knowledge or the relation between pairs of cases in the task domain.

Surprisingly, variant (1) performed almost identically to variant (2), which also considers the source solution in adaptation. This suggests that the source solution, heavily coupled with the source problem, may not provide additional useful information for adaptation.

In terms of segmenting case pairs by source case solution, variants (1, 2) generally outperformed variants (3, 4) in accuracy on most datasets. This could be because a single adaptation neural network in (1, 2) is well-trained with all pairs of cases, while a specialized adaptation neural network in (3, 4) is trained with segmented examples. However, variants (3, 4) showed faster convergence during training due to training on segmented examples.

The impact of the ensemble of adaptations was investigated, with EAC-NN-CDH (variant (4)) performing similarly to its counterpart variant (3) without ensemble. This suggests that the generalization power of C-NN-CDH produces stable predictions that an ensemble version does not significantly alter.

The usefulness of the class-to-class approach for adaptation was demonstrated by C2C-NN-CDH (variant (5)), which performed differently from and often better than the other C-NN-CDHs. C2C-NN-CDH reaches its prediction by collecting evidence from diverse source cases from all classes, which can provide more global support, especially when there are multiple classes. Moreover, the C2C approach offers the possibility of explanation with contrastive evidence.

# 2.3.6 Conclusions on Learning adaptations for case based classification: A Neural Network approach

The conclusion of the paper [18] being that (variant (5)) is worth investigating using its C2C-NN-CDH approach to classification. As it yielded the most promising results when compared to all the other variants tested in the paper. The grouping of the dataset based on class outcome and training a specialized neural network, has its benefits in terms of speedup. However, the retrieval of N cases across all classes during testing, has shown to yield better results, in a way that allows an interpretation of the results.

# Chapter 3

# Design and Implementation

## **Objectives and Contributions**

The design chapter of this paper serves as a comprehensive guide, presenting various algorithms and their implementations in the context of our novel framework. Our primary objectives are to elucidate the intricacies of these algorithms, introduce innovative variations, and showcase the integration of our framework within the broader machine learning landscape.

The tables provided below offer a structured roadmap through our design chapter, delineating where and how different algorithms are described. Notably, the algorithms discussed originate from seminal works such as [7] and [18]. However, in addition to presenting established methodologies, we introduce novel variations that represent fresh approaches to classification and regression tasks.

Key innovations include Variant 2, which introduces duplication based on distances, and Variant 3, incorporating a column indicating each neighbor's distance to the base case. Notably, we employ a new type of classifier, distinct from those mentioned in [7]. Variants 1, 2, and 3 exemplify our endeavor to explore uncharted territory within the learning from differences methodology, offering novel perspectives on classification.

Furthermore, our introduction of the LingerImplicitRegressor presents a groundbreaking approach to regression tasks. Leveraging methodologies outlined in [18], this novel regressor extends the learning from differences framework, offering a fresh perspective on regression problems.

By presenting a cohesive framework that integrates established algorithms, innovative

variations, and our novel contributions, these tables provide a clear overview of the design landscape. Our aim is to facilitate understanding and navigation through the complexities of machine learning methodologies, empowering researchers and practitioners to leverage our framework effectively in their endeavors.

# 3.1 LingerRegressor and LingerClassifier Models Roadmap

The following models are based on the algorithms outlined in [7]. Variations such as Variant 2 and Variant 3 introduce innovative adaptations to the base models, providing enhanced functionality and performance.

LingerRegressor			
Full Name	Acronym	Description	
LingerRegressor Section: 3.5	LR	Base Linger regressor, no variations	
LingerRegressor Variant 1 Sec-	LRV1	Linger regressor with the addition of context,	
tion: 3.7.1		where context is the original base case.	
LingerRegressor Variant 2 Sec-	LRV2	Linger regressor integrated with duplication based	
tion: 3.7.2		on distance, where differences are duplicated based	
		on the neighbors' proximity to the base case.	
LingerRegressor Variant 3 Sec-	LRV3	Linger regressor integrated with a distance column	
tion: 3.7.3		indicating the distance of each neighbor from the	
		base case.	

Table 3.1: Regression Models based on the algorithms in [7]

LingerClassifier			
Full Name	Acronym	Description	
LingerClassifier Section: 3.6	LC	Base Linger classifier, no variations	
LingerClassifier Variant 1	LCV1	Linger classifier with the addition of context,	
Section: 3.7.1		where context is the original base case.	
LingerClassifier Variant 2	LCV2	Linger classifier integrated with duplication based	
Section: 3.7.2		on distance, where differences are duplicated based	
		on the neighbors' proximity to the base case.	
LingerClassifier Variant 3	LCV3	Linger classifier integrated with a distance column	
Section: 3.7.3		indicating the distance of each neighbor from the	
		base case.	

Table 3.2: Classifier models based on the algorithms in [7]

# 3.2 LingerImplicitClassifier and LingerImplicitRegressor Models

The classifier models presented here are based on algorithms from [18], with Variations 1 and 2 also originating from the same source.

The regressor models in this section extend the learning from differences framework outlined in [18] to regression tasks. This innovative approach maintains the core principles of the methodology while introducing adaptations tailored to address the unique challenges of regression problems.

LingerImplicitClassifier			
Full Name	Acronym	Description	
LingerImplicitClassifier	LIC	Base Linger Implicit Classifier selects the $N$ near-	
Section: 3.10		est neighbors from each class	
LingerImplicitClassifier	LICV1	Selects $N$ random items from each class	
Variant 1 Section: 3.10.5			
LingerImplicitClassifier	LICV2	Selects the single nearest neighbor from each class	
Variant 2 Section: 3.10.5			

Table 3.3: LingerImplicitClassifier models based on the algorithms in [18]

30

	LingerImpl	icitRegressor
Full Name	Acronym	Description
LingerImplicitRegressor Sec-	LIR	Base Linger Implicit Regressor selects the $N$ near-
tion: 3.5		est neighbors from each class during prediction
$ ext{LingerImplicitRegressor Vari-}$	LIRV1	Selects $N$ random items from each class
ant 1 Section: 3.11.5		
$ ext{LingerImplicitRegressor Vari-}$	LIRV2	Selects the single nearest neighbor from each class
ant 2 Section: 3.11.5		
Regression to Classification Converter		
Full Name	Acronym	Description
Regression to Classification Con-	RTCC	Converts regression problems into classification
verter Section: 3.11.7		problems

Table 3.4: LingerImplicitRegressor models based on the algorithms in [18]

# 3.3 LingerImageClassifier and LingerImageRegressor

LingerImageClassifier			
Full Name		Acronym	Description
LingerImageClassifier	Sec-	(LIMC)	Image Classifier that learns from differences
tion: 3.13			

Table 3.5: Image Classifier Using learning from difference methodologies seen in [7]. Innovative in its application to classification image data sets.

LingerImageRegressor		
Full Name	Acronym	Description
LingerImageRegressor Section:	(LIMR)	Image Regressor that learns from differences
3.14		

Table 3.6: Image Regressor Using learning from difference methodologies seen in [7]. Innovative in its application to classification image data sets.

## 3.4 Learning From Differences

#### 3.4.1 Introduction and Motivation

Our design process is anchored in the seminal work of [7], which laid the groundwork for the learning from differences method. Building upon this foundation, our primary objective is to enhance and extend these algorithms, creating a more dynamic and adaptable framework.

Inspired by Scikit-learn's modular design philosophy, we aim to develop models that not only match but surpass its rigorous hyperparameter testing capabilities. Our goal is to introduce multiple new hyperparameters accessible through familiar pipelines, thereby enhancing flexibility and functionality across diverse machine learning tasks and datasets.

As we progress from implementing base models to introducing variations, our focus shifts to optimizing the performance of both the LingerRegressor and LingerClassifier. These variations are meticulously crafted to improve training efficiency and predictive accuracy, ultimately enhancing overall model performance.

Named LingerRegressor and LingerClassifier, our custom models are designed to leverage the training from differences approach, distinguishing them within the machine learning landscape.

Central to our efforts is ensuring the seamless testability of introduced variations, akin to Scikit-learn's comprehensive hyperparameter testing framework. This rigorous analysis empowers stakeholders to make informed decisions about the efficacy and applicability of our models to specific tasks.

However, we encountered the critical challenge of compatibility during model development. Our codebase is structured as a downloadable package, seamlessly integrating with Scikit-learn's ecosystem to ensure interoperability across various datasets and environments. This compatibility enhances accessibility and usability for practitioners in diverse machine learning endeavors.

# 3.5 Linger Regression Base Model: LingerRegressor (LR)

## 3.5.1 Objective

The Linger Regression Base Model integrates principles of Case-Based Reasoning (CBR) into regression analysis to enhance interpretability and create a performative model. The objectives include:

- Developing a dynamic regression model using differences between a case and its nearest neighbors, adapting retrieved solutions to the target solution.
- Ensuring compatibility with Scikit-learn for accessibility, ease of implementation, and extensive hyperparameter testing.
- Enabling effective interpretation of predictions for users.
- Implementing the learning from differences algorithm with enhancements for improved performance.
- Creating an easily extendable code base to allow for variations.

Its intended use case is for regression problems that could benefit from a more transparent learning process.

#### 3.5.2 Architecture

The LingerRegressor combines K-nearest neighbors (KNN) and MLPRegressor from Scikit-learn for flexibility and accuracy. A K-nearest neighbors (KNN) is used in conjunction with a MLPRegressor in the fit phase of the machine. During the predict phase, a K-nearest neighbors (KNN) is used once again with the now trained MLPRegressor to get the differences' prediction or K neighbors.

### 3.5.3 Components

• KNN module: Computes nearest neighbors and extracts differences during both training and prediction phases.

- MLPRegressor: Offers flexibility in activation functions, solvers, and hyperparameters for regression.
- Supplementary Features: Weighted KNN, Context Addition, Additional Distance Column, and Duplication Based on Distance. Each supplementary feature can be activated through a hyperparameter.

#### 3.5.4 Parameterization

Extensive parameterization allows fine-tuning of KNN, MLPRegressor, and additional features. All the same hyperparameters are available as in a conventional (KNN) and neural network, with additional hyperparameters for LingerRegressor.

## 3.5.5 Training and Prediction Design

#### Training Design

Given dataset D, split it into  $D^{train}$  and  $D^{test}$  with an 80%-20% split through random selection. For each case  $C_i = (X_i^{train}, y_i^{train}) \in D^{train}$ , retrieve n similar cases from  $D^{train}$ ,  $(X_j^{train}, y_j^{train}) \in D^{train}$  using Scikit-learn's neighbors module. Compute the differences between  $C_i$  and its neighbors and append them to  $\Delta D^{train}$  as  $(X_i^{train} - X_j^{train}, y_i^{train} - y_j^{train})$ .

### Algorithm 11 Training Algorithm for Learning from Differences

- 1: Split D into training set  $D^{train}$  and test set  $D^{test}$  with an 80%-20% split
  2: Initialize  $\Delta D^{train}$  as an empty list
  3: **for** each case  $C_i = (X_i^{train}, y_i^{train}) \in D^{train}$  **do**4: Retrieve n similar cases from  $D^{train}$  using nearest neighbors
  5: **for** each similar case  $(X_j^{train}, y_j^{train}) \in D^{train}$  **do**6: Compute the differences:  $\Delta D_{ij}^{train} = (X_i^{train} X_j^{train}, y_i^{train} y_j^{train})$ 7: Append  $\Delta D_{ij}^{train}$  to  $\Delta D^{train}$ 8: **end for**
- 9: end for
- 10: Train the MLPRegressor neural network model using  $\Delta D^{train}$  over a few epochs for later predictions.
- 11: **Return** Trained neural network model TrainedNN()

#### Prediction Design

During prediction, for each case  $X_j^{test}$ , retrieve n similar cases from  $D^{train}$ . Compute the differences  $\Delta X_{ij}^{test} = X_j^{test} - X_i^{train}$  for each neighbor. Use the trained neural network to predict  $\Delta X_{ij}^{test}$ , resulting in  $\Delta X_{ij}^{pred}$ . For each set of retrieved neighbors from  $D^{train}$ , calculate  $y_i^{train} + \Delta X_{ij}^{pred}$  and add each n neighbors adapted y values. Once summed, divide by n to obtain  $y_j^{pred}$ . Compare  $y_j^{pred}$  to  $y_j^{test}$  to evaluate accuracy.

# Algorithm 12 Prediction Algorithm for Learning from Differences

```
Input: Test dataset D^{test}, trained neural network model TrainedNN(), number of neighbors n
```

```
Initialize empty list y^{pred} for each case X_j^{test} \in D^{test} do

Initialize empty list y_j^{pred}
Retrieve n similar cases from D^{train} using nearest neighbors
Initialize empty list y^{pred}predictions
for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do

Compute the differences: \Delta X_{ji}^{test} = X_j^{test} - X_i^{train}
Use the trained neural network to predict: TrainedNN(\Delta X_{ji}^{test}) = \Delta X_{ji}^{pred}
Adapt neighbor's y values: y_{ji}^{pred} = y_i^{train} + \Delta X_{ji}^{pred}
end for

Average the adapted y values: y_j^{pred} = \frac{1}{n} \sum_{i=1}^n y_{ji}^{pred}
end for
Compare y^{pred} to y^{test} to evaluate accuracy
```

# 3.5.6 Training and Prediction Implementation

#### Training Implementation

During training, the algorithm fits the base Linger Regressor to the input dataset X and the corresponding label vector y. It computes the nearest neighbors for each sample in X and constructs the input features and target labels for the regressor by calculating the differences between each sample and its neighbors. These differences are then used to train the regressor, and the trained model along with the training data are stored for later use. It makes use of scikit-learns [15] NearestNeighbors, numpy and MLPRegressor.

```
Algorithm 13 Training Implementation Algorithm for Base Linger Regressor
Input: Dataset, X, label vector y, number of neighbors n\_neighbors\_1
 1: function FIT(X, y)
       Increment n neighbours 1 \triangleright Fit scikit-learns NearestNeighbors function to X
 2:
 3:
       neighbors = NearestNeighbors(n neighbors = n neighbors 1).fit(X)
 4:
       Compute nearest neighbors for each sample in X
       Compute the indexes and distances, of nearest neighbors in X
 5:
       distances, indices = neighbors.kneighbors(X)
 6:
       differences X = []
 7:
       differences\_y = []
 8:
       if variant == 1 (LRV1) then
 9:
          Call\ addition\_of\_context\_func\_fit(X, y, indices, differences\_X, differences\_y)
10:
          differences\_X, differences\_y = addition\_of\_context\_func\_fit(X, y, indices, differences\_x)
11:
       else if variant == 2 (LRV2) then
12:
          Call\ duplicate\_difference\_based\_on\_distance(differences\_X, differences\_y, distance)
13:
          differences X, differences y = duplicate difference based on <math>distance(difference)
14:
       else if variant == 3 (LRV3) then
15:
          Call add additional distance column(differences\ X, distances)
16:
          differences X = add \ additional \ distance \ column(differences X, distances)
17:
18:
       else
          for each sample i in nearest neighbors indices do
19:
              base \leftarrow Index of base case
20:
              for each neighbor n of i do
21:
22:
                 Append (X[base] - X[n]) to differences X
                 Append (y[base] - y[n]) to differences y
23:
              end for
24:
          end for
25:
       end if
26:
       Fit MLPRegressor with differences_X and differences_y
```

#### **Prediction Implementation**

Set  $train_X = X$ 

return Fitted LingerRegressor

Set  $train_y = y$ 

31: end function

27:

28:

29:

30:

During prediction, the algorithm utilizes the fitted Nearest Neighbors model to identify the nearest neighbors for each sample in the input data X. It then computes the

differences between each sample in X and its corresponding neighbors, preparing the input features for the regressor. After predicting the differences using the trained regressor, the algorithm aggregates the predictions to obtain the final predicted target values for each sample in X. If weighted KNN is enabled, the predictions are weighted based on the distances to the neighbors, providing more influence to closer neighbors in the prediction process. This offers a different form of nearest neighbors. Where values are weighted based on their proximity to the base case. It makes use of scikit-learns [15] NearestNeighbors, and numpy.

```
Algorithm 14 Prediction Implementation Algorithm for Base Linger Regressor
Input: Input data, X, number of neighbors n\_neighbors\_2
 1: function PREDICT(X)
       Fit Nearest Neighbors model with n neighbours 2 using train X
 2:
       Compute nearest neighbors for each sample in X,
 3:
       Compute the indexes and distances, of nearest neighbors in X
 4:
       Initialize empty list differences test X
 5:
       is sparse X \leftarrow \text{Check if } X \text{ is sparse}
 6:
       if is\_sparse\_X then
 7:
          Convert X to dense array
 8:
       end if
 9:
       for each sample test in X do
10:
          for each nearest neighbor nn\_in\_training in indices[test] do
11:
                       (X[test,:] - train X[indices[test][nn in training],:])
12:
   differences test X
          end for
13:
       end for
14:
       if variant == 1 (LRV1) then
15:
          Call addition of context func pred(differences\ test\ X,X)
16:
          differences \ test \ X = addition\_of\_context\_func\_pred(differences\_test\_X, X)
17:
       else if variant == 3 (LRV3) then
18:
          Call add additional distance column(differences\ test\ X, distances)
19:
          differences\_X = add\_additional\_distance\_column(differences\_test\_X, distances)
20:
       end if
21:
       predictions \leftarrow \text{Predict using LingerRegressor} with differences test X
22:
       Split predictions into batches of size n_neighbours_2
23:
       Initialise y pred as an empty list
24:
       y pred = []
25:
26:
       if Weighted KNN is enabled then
          for each indexes, differences, dist in zip(indices, predictions, distances) do
27:
              Compute weights for each neighbor
28:
              weights = 1 \div (dist + 1e - 8)
29:
30:
              Compute weighted sum of target values
              weighted\_sum = sum(w \times (train\_y[i] + d) \text{ for i, d, w in } zip(indexes,
31:
   differences, weights))
              Compute weighted average
32:
              weighted\_avg = weighted\_sum \div sum(weights)
33:
              Append weighted avg to y pred
34:
          end for
35:
36:
       else
          for each indexes, differences in 8zip(indices, predictions) do
37:
```

 $sum\ result = sum((train\ y[i] + d)fori, dinzip(indexes, differences))$ 

Compute sum of target values

38:

39:

#### 3.5.7 Evaluation

Evaluation metrics include Mean Squared Error (MSE), Root Mean Squared Error (RMSE), and R-squared ( $R^2$ ) to assess model accuracy and performance.

## 3.5.8 Optimization

To optimize the model, we consider various strategies:

- Hyperparameter Tuning: Grid search or randomized search cross-validation for optimal hyperparameters.
- Feature Engineering: Experimentation with different feature combinations to improve model performance.
- Regularization Techniques: L1 and L2 regularization to prevent overfitting.

#### 3.5.9 Limitations and Future Work

The Linger Regression Base Model has several limitations:

- Sensitivity to Noise: The model may produce inaccurate predictions when faced with noisy or irrelevant data.
- Interpretability: While the model enhances interpretability compared to black-box models, it may still be challenging to interpret in complex scenarios.

Future work includes:

- Enhancing Noise Robustness: Investigating methods to improve model performance in the presence of noisy data.
- Interpretability Improvements: Exploring techniques to enhance model interpretability for complex datasets.

#### 3.5.10 Conclusion

In conclusion, the LingerRegressor model presents a novel approach to regression analysis by integrating principles of Case-Based Reasoning (CBR) and the learning

from differences methodology. Through the combination of K-nearest neighbors (KNN) and MLPRegressor, the model offers flexibility, accuracy, and interpretability in regression tasks. The implementation of supplementary features further enhances its adaptability and performance. Despite its limitations, the model shows promise in addressing the challenges of transparent and dynamic regression modeling. Future research can focus on refining the model's robustness to noise and improving its interpretability for complex datasets. Overall, the LingerRegressor model contributes to the advancement of machine learning methodologies, providing a valuable tool for regression analysis in diverse domains where a more interpretable model is needed.

# 3.6 Linger Classification Base Model:

LingerClassifier (LC)

# 3.6.1 Objective

The objective of the Linger Classification Base Model (LingerClassifier) is to extend the learning from differences methodology to classification tasks. The primary goals include:

- Developing a versatile classification model that utilizes differences between cases for prediction.
- Ensuring compatibility with Scikit-learn for seamless integration and extensive hyperparameter testing.
- Providing interpretable predictions to facilitate user understanding.
- Implementing enhancements to the learning from differences algorithm for improved classification performance.
- Designing a modular and extensible codebase to support future variations and enhancements.

The LingerClassifier is tailored for classification problems where interpretability and adaptability are critical.

#### 3.6.2 Architecture

Similar to the regression counterpart, the LingerClassifier integrates K-nearest neighbors (KNN) and Scikit-learn's MLPClassifier for classification tasks. During training, KNN is used to compute nearest neighbors, and during prediction, the differences are used to adapt the class labels.

## 3.6.3 Components

The key components of the LingerClassifier include:

- KNN Module: Computes nearest neighbors and extracts differences during training and prediction phases.
- MLPClassifier: Offers flexibility in activation functions, solvers, and hyperparameters for classification.
- Additional Features: Similar to the regression model, features like weighted KNN, context addition, additional results' column, and duplication based on distance can be activated through hyperparameters.

#### 3.6.4 Parameterization

The model provides extensive parameterization options for fine-tuning KNN, MLPClassifier, and additional features. Hyperparameters for the classification model mirror those available in standard KNN and neural networks, with additional parameters specific to LingerClassifier.

# 3.6.5 Training and Prediction Design

The training and prediction algorithms for the LingerClassifier are similar to those of the LingerRegressor, with adjustments made to accommodate classification tasks.

#### Training Algorithm Design

During training, the algorithm computes differences between cases and their nearest neighbors, similar to the regression model. However, the adaptation of class labels is based on the majority class among the nearest neighbors.

# Algorithm 15 Training Algorithm for LingerClassifier

```
Split the dataset D into training set D^{train} and test set D^{test} using an 80%-20% split. Initialize \Delta D^{train} as an empty list. for each case C_i = (X_i^{train}, y_i^{train}) \in D^{train} do Retrieve n similar cases from D^{train} using nearest neighbors. for each similar case (X_j^{train}, y_j^{train}) \in D^{train} do Compute the differences: \Delta D_{ij}^{train} = (X_i^{train} - X_j^{train}, y_i^{train} - y_j^{train}). Append \Delta D_{ij}^{train} to \Delta D^{train}. end for end for Train the MLPClassifier neural network model using \Delta D^{train}. return Trained neural network model TrainedNN().
```

#### Prediction Algorithm Design

During prediction, the algorithm adapts class labels based on the majority class among the nearest neighbors' labels.

**Algorithm 16** Prediction Algorithm for Learning from Differences for Classification **Input:** Test dataset  $D^{test}$ , trained neural network model TrainedNN(), number of neighbors n

```
1: Initialize empty list y^{pred}
2: for each case X_j^{test} \in D^{test} do
3: Retrieve n similar cases from D^{train} using nearest neighbors
4: Initialize empty list y_j^{pred}
5: for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do
6: Compute the differences: \Delta X_{ji}^{test} = X_j^{test} - X_i^{train}
7: Use the trained neural network to predict: TrainedNN(\Delta X_{ji}^{test}) = \Delta X_{ji}^{pred}
8: Adapt neighbor's y value: yy_{ji}^{pred} = y_i^{train} + \Delta X_{ji}^{pred}
9: end for
10: Perform majority voting on y^{pred}predictions to obtain y_j^{pred}
11: end for
12: Compare y^{pred} to y^{test} to evaluate accuracy
```

# 3.6.6 Training and Prediction Implementation

### Training Algorithm Implementation

The provided algorithm outlines the prediction process for the Linger Classifier implemented in Python. It begins by fitting a Nearest Neighbors model with a specified number of neighbors using the training data. Next, it computes the nearest neighbors for each sample in the input data and initializes an empty list to store the differences between the test samples and their corresponding neighbors. If the input data is sparse, it is converted to a dense array for compatibility. The algorithm then iterates through each test sample and its nearest neighbors to calculate the feature differences. After computing the differences, it proceeds to make predictions using the trained classifier. If weighted KNN is enabled, it calculates the weighted results based on the differences and distances to determine the item with the highest weighted sum as the prediction. Otherwise, it finds the most common item among the predictions. Finally, the predicted target values are aggregated and returned as the output of the algorithm.

#### Algorithm 17 Training Implementation Algorithm for Base Linger Classifier

**Input:** Dataset, X, label vector y, number of neighbors  $n\_neighbors\_1$ 

```
1: function FIT(X, y)
2:
       Increment n neighbors 1
3:
       neighbors \leftarrow \text{Fit scikit-learn's NearestNeighbors function to } X
4:
       Compute nearest neighbors for each sample in X
       distances, indices \leftarrow neighbors.kneighbors(X)
5:
       differences \ X \leftarrow []
6:
       differences\_y \leftarrow []
7:
8:
       if variant == 1 (LCV1) then
          Call\ addition\_of\_context\_func\_fit(X, y, indices, differences\_X, differences\_y)
9:
          differences\_X, differences\_y = addition\_of\_context\_func\_fit(X, y, indices, differences\_x)
10:
       else if variant == 2 \text{ (LCV2)} then
11:
          Call duplicate difference based on distance (differences X, differences y, distance
12:
          differences\_X, differences\_y = duplicate\_difference\_based\_on\_distance(differences\_x)
13:
       else if variant == 3 (LCV3) then
14:
15:
          Call add additional distance column(differences X, distances)
          differences X = add \ additional \ distance \ column(differences X, distances)
16:
       else
17:
18:
          for each sample i in nearest neighbors indices do
              base \leftarrow Index of base case
19:
              for each neighbor n of i do
20:
                 Append (X[base] - X[n]) to differences\_X
21:
                 Append (y[base] - y[n]) to differences y
22:
              end for
23:
          end for
24:
       end if
25:
26:
       Fit MLPClassifier with differences X and differences y
27:
       Set train X = X
       Set train_y = y
28:
29:
       return Fitted LingerClassifier
30: end function
```

#### Prediction Algorithm Implementation

The prediction algorithm for the Linger Classifier, implemented in Python, outlines the process of predicting target values for the input data. Initially, it fits a Nearest Neighbors model with a specified number of neighbors using the training data. Then, it computes the nearest neighbors for each sample in the input data and initializes an empty list to store the feature differences between the test samples and their corresponding neighbors. If the input data is sparse, it is converted to a dense array for compatibility. The algorithm iterates through each test sample and its NearestNeighbors to calculate the feature differences. After computing the differences, it proceeds to make predictions using the trained LingerClassifier. If weighted KNN is enabled, it calculates the weighted sum of target values for each neighbor based on the differences and distances, and selects the item with the highest weighted sum as the prediction. Otherwise, it finds the most common item among the predictions. Finally, the predicted target values are aggregated and returned as the output of the algorithm.

```
Algorithm 18 Prediction Algorithm for Linger Classifier
Input: Input data, X, number of neighbors n_neighbours_2
 1: function PREDICT(X)
       Fit Nearest Neighbors model with n neighbours 2 using train X
 2:
       Compute nearest neighbors for each sample in X
 3:
 4:
       Initialize empty list differences test X
       is sparse X \leftarrow \text{Check if } X \text{ is sparse}
 5:
       if is sparse X then
 6:
          Convert X to dense array
 7:
       end if
 8:
 9:
       for each sample test in X do
          for each nearest neighbor nn\_in\_training in indices[test] do
10:
                        (X[test,:] - train X[indices[test][nn in training],:])
11:
   differences test X
          end for
12:
       end for
13:
       if variant == 1 (LCV1) then
14:
          Call addition of context func pred(differences\ test\ X,X)
15:
          differences test X_{=}addition of context func pred(differences test X, X)
16:
       else if variant == 3 (LCV3) then
17:
          Call add additional distance column(differences\ test\ X, distances)
18:
          differences\_X = add\_additional\_distance\_column(differences\_test\_X, distances)
19:
       end if
20:
       predictions \leftarrow \text{Predict using LingerClassifier with } differences\_test\_X
21:
       Split predictions into batches of size n neighbours 2
22:
       Initialise y\_pred as an empty list
23:
       y pred = []
24:
       if Weighted KNN is enabled then
25:
26:
                     each
                                indexes.
                                                 differences,
                                                                       distance
                                                                                      in
   zip(indices, differences test X, distances) do
              Compute weights for each neighbor
27:
              weights = 1 \div (dist + 1e - 8)
28:
29:
              Compute weighted sum of target values,
30:
              weighted sum = []
              weighted_sum = [w \times (train_y[i] + d)] for i, d, w in zip(indexes, differences, weights)
31:
              Find the item with the highest weighted sum
32:
              max\_sum = max(weighted\_sum)
33:
              Append max sum to y pred
34:
          end for
35:
36:
       else
          for each indexes, differences in 6zip(indices, predictions) do
37:
              results = [train_{v}[i] + dfori, dinzip(indexes, differences)]
38:
```

Find the most common item in results

39:

#### 3.6.7 Evaluation

Evaluation metrics for the LingerClassifier include accuracy, precision, recall, F1-score, and confusion matrix analysis. These metrics provide insights into the model's performance and its ability to classify instances accurately.

# 3.6.8 Optimization

To enhance the performance of the LingerClassifier, several optimization strategies are considered:

- **Hyperparameter Tuning**: Utilize grid search or randomized search cross-validation to fine-tune the hyperparameters for optimal classifier performance.
- Feature Engineering: Experiment with different feature combinations and transformations to uncover informative patterns in the data and improve classifier accuracy.
- Regularization Techniques: Apply L1 and L2 regularization methods to the classifier to mitigate overfitting and enhance generalization ability.

These optimization strategies aim to maximize the predictive capability of the LingerClassifier model.

#### 3.6.9 Limitations and Future Work

The LingerClassifier shares similar limitations and avenues for future work as the regression model, including sensitivity to noise and interpretability challenges. Future work may focus on improving noise robustness and enhancing interpretability for complex classification tasks.

#### 3.6.10 Conclusion

The LingerClassifier offers a novel approach to classification tasks by integrating the learning from differences methodology. Its modular design and extensible architecture

make it well-suited for a wide range of classification problems, particularly those where interpretability and adaptability are paramount.

For more details on the LingerClassifier, and LingerRegressor variations, refer to Table 3.7.

# 3.7 Variations For LingerRegressor (LR) and LingerClassifier (LC)

# 3.7.1 Variation 1: Addition of Context Design and Implementation (LRV1, LCV1)

#### Objective

The objective of adding context is to incorporate the original attribute values of the source cases into the generated differences array. This ensures that the new datasets used for fitting and prediction contain both the original attribute values of the source cases and the differences between them and their nearest neighbors. This may aid in the learning process and improve the model. Its design is the same for both the LingerRegressor and LingerClassifier.

### Training Design

# Algorithm 19 Training Algorithm for Learning from Differences, with context included in LingerClassifier and LingerRegressor

- 1: Split the dataset D into training set  $D^{train}$  and test set  $D^{test}$  using an 80%-20% split.
- 2: Initialize  $\Delta D^{train}$  as an empty list.
- 3: for each case  $C_i = (X_i^{train}, y_i^{train}) \in D^{train}$  do
- 4: Retrieve n similar cases from  $D^{train}$  using nearest neighbors.
- 5: for each similar case  $(X_j^{train}, y_j^{train}) \in D^{train}$  do
- 6: Compute the differences, with concatenated context:  $\Delta D_{ij}^{train} = ((X_i^{train} X_j^{train}) : X_i^{train}, y_i^{train} y_j^{train}).$
- 7: Append  $\Delta D_{ij}^{train}$  to  $\Delta D^{train}$ .
- 8: end for
- 9: end for
- 10: Train the MLPClassifier or MLPRegressor neural network model using  $\Delta D^{train}$ .
- 11: **return** Trained neural network model TrainedNN().

#### **Prediction Design**

15: end for

# Algorithm 20 Prediction Algorithm for Variant 1, context included.

**Input:** Test dataset  $D^{test}$ , trained neural network model TrainedNN(), number of neighbors n

```
1: Initialize y^{pred} as an empty list.
2: for each case X_i^{test} in D^{test} do
        Retrieve n similar cases from D^{train} using nearest neighbors.
3:
        Initialize y_j^{pred} as an empty list.
4:
        for each similar case (X_i^{train}, y_i^{train}) in D^{train} do
5:
             Compute the differences: \Delta X_{ji}^{test} = ((X_j^{test} - X_i^{train}) : X_j^{test}).
6:
             Use the trained neural network to predict: Trained NN(\Delta X_{ji}^{test}) = \Delta X_{ji}^{pred}.
7:
             Adapt neighbor's y values: y_{ji}^{pred} = y_i^{train} + \Delta X_{ji}^{pred}.
8:
        end for
9:
        if Regression then
10:
             Average the adapted y values: y_j^{pred} = \frac{1}{n} \sum_{i=1}^n y_j^{pred}.
11:
        else if Classification then
12:
             Perform majority voting on y_j^{pred} to obtain y_j^{pred}.
13:
        end if
14:
```

16: Compare  $y_j^{pred}$  to  $y_j^{test}$  to evaluate accuracy.

#### Training Implementation

This algorithm is called during the Fit stage of both the LingerClassifier, and LingerRegressor.

# Algorithm 21 Context Addition Function for Base Linger Classifier

Input: Dataset X, label vector y, nearest neighbor indices indices, differences in X  $differences\_X$ , differences in y  $differences\_y$  Output: Updated differences in X  $differences\_X$ , updated differences in y  $differences\_y$ 

```
1: function addition\_of\_context\_func\_fit(X, y, indices, differences\_X,
   differences y)
       for i in indices do
2:
3:
           base \leftarrow i[0]
           neighbors \leftarrow i[1:]
 4:
           for n in neighbors do
5:
              base \ case \leftarrow X[base]
6:
              diff \leftarrow X[base] - X[n]
 7:
              combined list \leftarrow []
8:
              for pair in zip(diff, base_case) do
9:
                  for item in pair do
10:
                      Append item to combined list
11:
                  end for
12:
              end for
13:
              Append np.array(combined list) to differences X
14:
              Append y[base] - y[n] to differences y
15:
           end for
16:
       end for
17:
       return\ differences\_X,\ differences\_y
18:
19: end function
```

#### **Prediction Implementation**

This algorithm is called during the predict algorithm for both the LingerClassifier, and LingerRegressor.

Algorithm 22 Context Addition Function for Base Linger Classifier during Prediction Input: Differences in test data differences\_test\_X, input data X Output: Combined differences in test data combined differences test X

```
1: function addition of context func pred(differences\ test\ X,X)
2:
       combined differences test X \leftarrow []
3:
       duplicated test data \leftarrow [item \text{ for } item \text{ in } X \text{ for } in range(n \text{ neighbours } 2)]
       num \ items \leftarrow length \ of \ duplicated \ test \ data
 4:
       for item pos in range(num items) do
5:
           combined list \leftarrow []
6:
           for pair in zip(differences\ test\ X[item\ pos], duplicated\ test\ data[item\ pos])
 7:
   do
8:
              for item in pair do
9:
                  Append item to combined list
              end for
10:
           end for
11:
           Append np.array(combined list) to combined differences test X
12:
13:
       end for
       return combined differences test X
14:
15: end function
```

# 3.7.2 Variation 2: Duplication Based on Distance Design and Implementation (LRV2, LCV2)

#### Objective

A novel variation introduced in this study involves duplicating differences based on distance, aiming to amplify the influence of neighbors closely resembling the base case. This innovative approach represents a departure from conventional methods in the learning from differences paradigm. By magnifying the impact of differences that exhibit stronger correlation with the base case, this technique effectively mitigates the influence of outliers, leading to more robust model performance.

This novel approach is specifically integrated into the fitting process of both the LingerClassifier and LingerRegressor models. By emphasizing the significance of closely resembling neighbors, this technique enhances the model's ability to discern meaningful patterns in the data, thereby improving its predictive accuracy and generalization capabilities.

- 1. Normalize Distances: Normalize the distances from the base case to its nearest neighbors represented by  $Distances_{ij}$ . We apply a logarithmic transformation to the distances:  $Distances_{ij} = \log_e(Distances_{ij} + 1)$ , with the addition of 1 to prevent a logarithm of 0.
- 2. **Determine Maximum and Minimum Distances**: Determine the maximum distance MaxDistance and minimum distance MinDistance in  $Distances_{ij}$ .
- 3. Compress Distances: Compress the distances within  $Distances_{ij}$  to a range between 0 and 10 using the formula:

$$Distances_{ij} = \text{round}\left(10 - \frac{(Distances_{ij} - MinDistance)}{(MaxDistance - MinDistance) \times 10}\right)$$

4. **Duplicate Items**: Duplicate each item  $\Delta D_{ij}^{train}$  by the corresponding distance in  $Distances_{ij}$ . It's important to note that this duplication process can significantly increase the size of the dataset and, consequently, the training time overhead. The process of duplication is only used in the training process of the algorithm.

#### Training Design

Algorithm Duplication Based Distance in LingerClassifier on LingerRegressor

**Input:** Distances  $Distances_{ij}$ , Base dataset  $\Delta D^{train}$ 

- 1: Normalize Distances:
- 2: for each distance  $Distances_{ij}$  do
- $Distances_{ij} \leftarrow \log_e(Distances_{ij} + 1)$ ▶ Apply logarithmic transformation
- 4: end for
- 5: Determine Maximum and Minimum Distances:
- 6:  $MaxDistance \leftarrow \text{maximum value of } Distances_{ij}$
- 7:  $MinDistance \leftarrow minimum value of <math>Distances_{ij}$
- 8: Compress Distances:

9: **for** each distance 
$$Distances_{ij}$$
 **do**
10:  $Distances_{ij} \leftarrow \text{round} \left(10 - \frac{(Distances_{ij} - MinDistance)}{(MaxDistance - MinDistance) \times 10}\right)$ 

- 11: end for
- 12: Duplicate Items:
- 13: **for** each item  $\Delta D_{ij}^{train}$  in  $\Delta D^{train}$  **do**
- Duplicate  $\Delta D_{ij}^{train}$  by the corresponding distance in  $Distances_{ij}$
- 15: end for

#### Training Implementation

## Algorithm 24 Difference Duplication Based on Distance

```
duplicate difference based on distance(differences X,
 1: function
    differences y, distances)
       distances X \leftarrow []
2:
3:
       for d in distances do
           neighbors \leftarrow d[1:]
4:
           for n in neighbors do
5:
               append n to distances X
6:
 7:
           end for
       end for
8:
       distances \ array \leftarrow np.array(distances \ X)
9:
       log\_values \leftarrow np.log(distances\_array + 1)
10:
       min\ val \leftarrow np.min(log\ values)
11:
12:
       max \ val \leftarrow np.max(log \ values)
       if min \ val == max \ val then
13:
           scaled\ distances\ rounded \leftarrow np.ones\_like(log\_values).astype(int)
14:
       else
15:
           scaled \ distances \leftarrow 10 - ((log \ values - min \ val) / (max \ val - min \ val) \times 
16:
    10)
           scaled\_distances\_rounded \leftarrow np.round(scaled\_distances).astype(int)
17:
       end if
18:
       filtered data X \leftarrow []
19:
       filtered data y \leftarrow []
20:
21:
       for each item, count in zip(differences\_X, scaled\_distances\_rounded) do
           if count \neq 0 then
22:
               append item to filtered data X
23:
           end if
24:
       end for
25:
26:
       for each item, count in zip(differences_y, scaled_distances_rounded) do
           if count \neq 0 then
27:
               append item to filtered_data_y
28:
           end if
29:
       end for
30:
31:
       duplicated\ list\ X \leftarrow []
       duplicated\ list\ y \leftarrow []
32:
       for each item, count in zip(filtered\ data\ X, scaled\ distances\ rounded) do
33:
           for \leftarrow 1 to count do
34:
               append item to duplicated list X
35:
           end for
36:
                                              54
       end for
37:
       for each item, count in zip(filtered data y, scaled distances rounded) do
38:
```

# 3.7.3 Variation 3: Addition of Distance Column Design and Implementation (LRV3, LCV3)

#### Objective

Variation 3 introduces a novel approach by incorporating the distance between each base case and its nearest neighbor into both the training and prediction phases of the neural network. This innovative method aims to leverage the proximity information to enhance the learning process and predictive performance of the model.

By integrating distance information, the neural network gains insight into the spatial relationships between data points. This allows the model to potentially learn associations between differences and their corresponding distances, leading to improved accuracy and effectiveness in both training and prediction tasks.

The motivation behind this variation lies in its potential to provide the model with a deeper understanding of the underlying data structure. By considering distance as a factor in the learning process, the model can better capture nuanced patterns and relationships, resulting in more robust and reliable predictions.

#### Design for Training

In the fit phase, the distances between each base case  $D_i^{train}$  and its nearest neighbor in  $D^{train}$  are computed and stored in  $Distances_{ij}$ . To incorporate these distances into the training data, each distance in  $Distances_{ij}$  is concatenated with the corresponding difference  $\Delta D^{train}$ . This results in a new dataset where each difference is paired with its corresponding distance, ensuring a one-to-one ratio between distances and differences.

**Algorithm 25** Training Algorithm for Learning from Differences, with Distance Column **Input:** Dataset D, Neural network model, Number of neighbors n, Number of epochs E

```
1: Split D into training set D^{train} and test set D^{test} with an 80%-20% split
```

- 2: Initialize  $\Delta D^{train}$  and Distances as empty lists
- 3: for each case  $C_i = (X_i^{train}, y_i^{train}) \in D^{train}$  do
- 4: Retrieve n similar cases from  $D^{train}$  using nearest neighbors
- 5: **for** each similar case  $(X_i^{train}, y_i^{train}) \in D^{train}$  **do**
- 6: Compute the differences:  $\Delta D_{ij}^{train} = (X_i^{train} X_j^{train}, y_i^{train} y_j^{train})$
- 7: Compute the distance:  $Distances_{ij} = ||X_i^{train}, X_j^{train}||$  (Euclidean distance)
- 8: Concatenate  $Distances_{ij}$  as a new attribute to  $\Delta D_{ij}^{train}$
- 9: end for
- 10: end for
- 11: Train the MLPRegressor neural network model using  $\Delta D^{train}$  over E epochs
- 12: **return** Trained neural network model TrainedNN().

### Design for Predict

In the prediction phase, distances between each test case  $X_j^{test}$  and its nearest neighbors in  $D^{train}$  are stored in  $Distances_{ji}$ . These distances are concatenated with the corresponding differences  $\Delta X^{test}$ , ensuring a one-to-one ratio between distances and differences in the prediction dataset.

Algorithm 26 Prediction Algorithm for Learning from Differences with Additional Distance Column

**Input:** Test dataset  $D^{test}$ , Trained neural network model, Number of neighbors n, TrainedNN()

```
1: Initialize \Delta D^{train} and Distances as empty lists
2: for each case X_i^{test} \in D^{test} do
        Retrieve n similar cases from D^{train} using nearest neighbors
3:
        for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do
4:
             Compute the differences: \Delta X_{ij}^{test} = (X_j^{test} - X_i^{train})
5:
             Compute the distance: Distances_{ji} = ||X_j^{test}, X_i^{train}|| (Euclidean distance)
6:
             Add Distances_{ji} as a new attribute to \Delta X_{ji}^{test}
7:
             Use the trained neural network to predict: TrainedNN(\Delta X_{ji}^{test}) = \Delta X_{ji}^{pred}
8:
             Adapt neighbor's y values: y_{j}^{pred} = y_{i}^{train} + \Delta X_{ji}^{pred}
9:
        end for
10:
        if Regression then
11:
             Average the adapted y values: y_j^{pred} = \frac{1}{n} \sum_{i=1}^n y_j^{pred}
12:
        else if Classification then
13:
             Perform majority voting on y_j^{pred} to obtain y_j^{pred}
14:
```

end if

Compare  $y_j^{pred}$  to  $y_j^{test}$  to evaluate accuracy

15:

16:

17: end for

#### Implementation for Training, and Prediction

The same function is called during both predict and training.

## Algorithm 27 Add Additional Distance Column

**Input:** Differences dataset differences X, Distances of the nearest neighbors distances

- 1: **function** add additional distance column(differences X, distances)
- 2: Adds an additional column with distance values associated with each differences X during fitting.
- 3: Output: differences X with an additional column.
- 4: **for** i **in** range(len(distances)) **do**
- 5:  $diff\_res \leftarrow Convert \ distances[i] \ to \ numpy \ array$
- 6: Append  $diff\_res$  to  $differences\_X[i]$
- 7: end for
- 8: **return** differences X
- 9: end function

# 3.8 Acronym Guide

Table 3.7: Variations for LingerRegressor and LingerClassifier

Variation	Acronym
Addition of Context	LRV1, LCV1
Duplication Based on Distance	LRV2, LCV2
Addition of Distance Column	LRV3, LCV3

# 3.9 Learning From differences Implicitly

#### 3.9.1 Introduction and Motivation

This design segment aims to implement and extend the algorithms proposed by Ye et al. [18] for both classification and regression tasks. The primary objective is to develop a unified framework where a single set of algorithms can be employed for both classification and regression tasks, leveraging implicit learning from differences within case pairs.

As outlined in the literature review (see Section 2), the algorithms (Algorithm 9, Algorithm 10) proposed by Ye et al. were chosen as the basis for our model

implementation. Variant 5, as demonstrated in the paper, exhibited superior performance among the variants explored, prompting its adoption in our implementation.

Moreover, while the paper focuses on classification tasks, it overlooks the potential application of implicit difference learning within case pairs for regression tasks. Thus, our secondary motivation is to explore the adaptability of Variant 5 to regression models. We seek to investigate whether the framework outlined in Algorithm 9 and Algorithm 10 can be extended and optimized for regression tasks effectively.

By extending the application of Variant 5 to regression tasks, we aim to provide a comprehensive and versatile framework for both classification and regression tasks, harnessing the power of implicit learning from differences within case pairs.

# 3.10 Linger Implicit Classification Model:

LingerImplicitClassifier (LIC)

# 3.10.1 Objective

The objective of the Linger Implicit Classification Base Model (LingerImplicitClassifier) is to implement the learning from differences methodology seen in [18] for classification tasks. The primary goals include:

- Developing a versatile classification model that learns through implicit differences in case pairs.
- Ensuring compatibility with Scikit-learn for seamless integration and extensive hyperparameter testing.
- Providing interpretable predictions to facilitate user understanding, for a variety of tasks.
- Implementing enhancements to the learning from differences algorithm for improved classification performance through hyperparameter testing.
- Designing a modular and extensible codebase to support future variations and enhancements.

The LingerImplicitClassifier is tailored for classification problems where interpretability and adaptability are critical, Where explicit differences may not be easily calculable. It adds another layer of interpretability, as both the target case and retrieved case are visible within the case pair which the Neural Nets are trained on.

#### 3.10.2 Architecture

The LingerImplicitClassifier leverages a hybrid architecture incorporating K-nearest neighbors (KNN) and Scikit-learn's MLPClassifier to tackle classification tasks. In the training phase, KNN plays a pivotal role in computing nearest neighbors, thereby facilitating the creation of case pairs. During the prediction phase, KNN is again utilized to retrieve the most similar cases from each class.

The process of generating case pairs for predictions involves KNN's functionality to identify the nearest neighbors. These neighbors serve as crucial elements in forming case pairs, enabling the classifier to make informed predictions based on similarities observed within the dataset.

The integration of KNN with the MLPClassifier offers a comprehensive approach to classification tasks, combining the strengths of both algorithms. While KNN excels in identifying similarities and forming case pairs, the MLPClassifier contributes by providing a powerful neural network-based classification model capable of learning intricate patterns and relationships within the data.

By harnessing the complementary capabilities of KNN and the MLPClassifier, the LingerImplicitClassifier aims to achieve robust and accurate classification results across diverse datasets, making it a versatile tool for various machine learning applications.

## 3.10.3 Components

The key components of the LingerClassifier include:

- KNN Module: Computes nearest neighbors and extracts differences during training and prediction phases.
- MLPClassifier: Offers flexibility in activation functions, solvers, and hyperparameters for classification.

 Additional Features: Class to class pairs, random N selected neighbors, and N nearest neighbors.

#### 3.10.4 Parameterization

The model provides extensive parameterization options for fine-tuning KNN, MLPClassifier, and additional features. Hyperparameters for the classification model mirror those available in standard KNN and neural networks, with additional parameters specific to LingerClassifier.

## 3.10.5 Training and Prediction Design

The training and prediction algorithms for the LingerImplicitClassifier.

### Training Algorithm Design

```
Algorithm 28 Training Algorithm for LingerImplicitClassifier
Input: Dataset D, number of neighbors 1
  Split D into training set D^{train} and test set D^{test} with an 80%-20% split
  Create CasePairs() dictionary.
  Create AdaptNN(), a dictionary to store each Neural Network
  List of unique Classes UniqueClasses
  for each case C_i = (X_i^{train}, y_i^{train}) \in D^{train} do
      Retrieve 1 similar case from D^{train} using nearest neighbors.
     for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do
         CasePairs(y_{j}^{train}).append([X_{j}^{train}:X_{i}^{train},y_{i}^{train}])
      end for
  end for
  for each unique Class in UniqueClasses do
      Create a new Classification Neural Network, trained on Case Pairs
      AdaptNN(Class).fit(CasePairs(Class))
  end for
  return Trained neural network models dictionary AdaptNN().
```

#### Prediction Algorithm Design

During the prediction phase, various methods exist for retrieving neighbors within each class. These methods can be categorized into three variants:

- 1. Variant 1: (LICV1) Selecting N random items from each class.
- 2. Variant 2: (LICV2) Selecting the single nearest neighbor from each class.

Each variant may be suitable depending on the specific characteristics of the dataset and the objectives of the prediction task.

```
Algorithm 29 Prediction Algorithm for LingerImplicitClassifier
Input: Dataset D^{test}, Dictionary AdaptNN(), Set UniqueClasses, and Dictionary
CasePairs()
  Initialize an empty list y^{pred}
  for each case X_i^{test} \in D^{test} do
      Create an empty list preds
      for each unique class Class in UniqueClasses do
         if Base version: (LIC) then
            Retrieve N nearest neighbors from CasePairs(Class)
         else if variant 1: (LICV1) then
             Select N random items from CasePairs(Class)
         else if variant 2: (LICV2) then
             Select the single nearest neighbor from CasePairs(Class)
         end if
         for each selected case (X_i^{CasePair}, y_i^{CasePair})do
            for each (X_z^{train}, X_q^{train}) \in X_i^{CasePair} do
                preds.append(AdaptNN(Class).predict(X_z^{train}:X_i^{test}))
            end for
         end for
         Perform a majority vote on preds
         y_i^{pred} = MajorityVote(preds)
      end for
  end for
  return y^{pred}
```

# 3.10.6 Training and Prediction Implementation

#### Training Algorithm Implementation

The fit function of the LingerImplicitClassifier model trains the classifier using the provided training data X and target labels y. It begins by handling input data, converting sparse matrices to dense arrays if necessary. Next, it initializes structures to store trained adaptation neural networks and unique classes. The algorithm then computes the nearest neighbors for each sample in X, generates pairs of cases (consisting of base and retrieved cases), and organizes the data based on class labels. Finally, it trains adaptation neural networks for each class label using the generated case pairs and target labels. Overall, this process enables the LingerImplicitClassifier model to adapt to specific instances retrieved during inference, enhancing its performance on the task.

#### Algorithm 30 Fit Function for LingerImplicitClassifier

```
Input: Training data X, target labels y
 1: function FIT(X, y)
        is sparse X \leftarrow \text{Check if } X \text{ is sparse}
 2:
       is sparse y \leftarrow \text{Check if } y \text{ is sparse}
 3:
 4:
        if is\_sparse\_X then
           Convert X to dense array
 5:
        end if
 6:
       if is_sparse_y then
 7:
           Convert y to dense array
 8:
        end if
 9:
10:
        classes\_ \leftarrow Get unique classes from y
        adaptation \ networks \leftarrow \{\}
11:
        neighbours \leftarrow \text{Fit Nearest Neighbors with } X
12:
        distances, indices \leftarrow Compute nearest neighbors for each sample in X
13:
        Initialize case pairs X and case pairs y
14:
15:
        for each i in indices do
           base \leftarrow i[0]
16:
           neighbors \leftarrow i[1:]
17:
18:
           for each n in neighbors do
               case x \leftarrow [X[base], X[n]]
19:
               case y \leftarrow [y[base], y[n]]
20:
               Append case\_x to case\_pairs\_X
21:
22:
               Append case_y to case_pairs_y
           end for
23:
        end for
24:
        Initialize dictionaries: case_pairs_by_class, cases_without_concatenation,
25:
    case pairs y
        for each (source, target) in zip(case\ pairs\ X, case\ pairs\ y) do
26:
           Append source[0] to cases without concatenation[target[1]]
27:
           problem \ query \leftarrow Concatenate \ source[0] \ and \ source[1]
28:
           Append problem_query to case_pairs_by_class[target[1]]
29:
           Append target[0] to case pairs y[target[1]]
30:
31:
        end for
        for each class label, cases in case pairs by class do
32:
           Initialize MLPClassifier with parameters
33:
           Fit MLPClassifier with cases and case_pairs_y[class_label]
34:
           Store the fitted MLPClassifier in adaptation networks [class label]
35:
        end for
36:
37: end function
```

#### Prediction Algorithm Implementation

The predict function of the LingerImplicitClassifier model predicts class labels for the input samples. It creates nearest neighbor finders for each class, then iterates through the test samples to predict class labels. Depending on the chosen variant, it either selects nearest neighbors using (LICV1) or a single nearest neighbor using (LICV2). Finally, it performs majority voting to decide the final classification.

## Algorithm 31 Predict Function for LingerImplicitClassifier

```
Input: Test data X
 1: function PREDICT(X)
       predictions \leftarrow []
 2:
       is sparse X \leftarrow \text{Check if } X \text{ is sparse}
 3:
       if is\_sparse\_X then
 4:
           Convert X to dense array
 5:
       end if
 6:
       nbrs\_by\_class \leftarrow \text{Create nearest neighbor finders for each class}
 7:
 8:
       for each sample in X do
           if variant == 2 (LICV2) then
 9:
               class predictions
                                    \leftarrow Predict class labels for sample using 1
10:
    NearestNeighbor
           else
11:
12:
               class predictions
                                      \leftarrow Predict class labels for sample using N
    NearestNeighbors
13:
           end if
           majority \ prediction \leftarrow Perform \ majority \ voting \ on \ class \ predictions
14:
           Append majority prediction to predictions
15:
       end for
16:
       return predictions
17:
18: end function
```

# Algorithm 32 Helper: Create Nearest Neighbor Finders

```
1: function _CREATE_NBRS_BY_CLASS
       nbrs\_by\_class \leftarrow \{\}
2:
       {\bf for} \ {\bf each} \ class\_label \ {\bf in} \ classes\_ \ {\bf do}
3:
           n\_neighbors \leftarrow 1 \text{ if } variant == 2 \text{ (LICV2) else } n\_neighbours\_2
4:
           nbrs \leftarrow \texttt{NearestNeighbors}(n\_neighbors).fit(cases\_without\_concatenation[class\_label])
5:
           nbrs\_by\_class[class\_label] \leftarrow nbrs
6:
       end for
7:
       {\bf return}\ nbrs\_by\_class
8:
9: end function
```

#### Algorithm 33 Helper: Predict Class Labels

```
1: function predict class(sample, nbrs by class)
       class \ predictions \leftarrow \{class \ label : [] \ for \ class \ label in \ classes \ \}
2:
       for each class label, nbrs in nbrs by class.items() do
3:
           if variant == 1 (LICV1) then
 4:
              indices
                           \leftarrow Randomly
                                               select n neighbours 2
                                                                              indices
                                                                                         from
5:
   range(len(cases\ without\ concatenation[class\ label]))
6:
           else
 7:
              distances, indices \leftarrow nbrs.kneighbors([sample])
           end if
8:
9:
           nearest neighbors \leftarrow indices[0]
           for each neighbor\_index in nearest\_neighbors do
10:
              neighbor\_sample \leftarrow cases\_without\_concatenation[class\_label][neighbor\_index]
11:
              merged\ case\ pair \leftarrow Concatenate\ neighbor\ sample\ and\ sample
12:
              adapted\_prediction \leftarrow Predict with adaptation\_networks\_[class\_label]
13:
   using merged case pair
              Append adapted prediction[0] to class predictions[class label]
14:
           end for
15:
       end for
16:
17:
       {f return}\ class\_predictions
18: end function
```

#### **Algorithm 34** Helper: Perform Majority Voting

```
1: function majority vote(class predictions)
   2:
                              all\_predictions \leftarrow [prediction \text{ for predictions in } class\_predictions.values() \text{ for prediction in } prediction of the prediction of 
                             prediction \ counter \leftarrow Counter(all \ predictions)
   3:
                              most common predictions \leftarrow prediction counter.most common(1)
   4:
                              If the case occurs where there is no distinct most common.
   5:
                              if len(most\ common\ predictions) > 1 then
   6:
   7:
                                             majority \ prediction \leftarrow Randomly select from most \ common \ predictions
                              else
   8:
                                             majority prediction \leftarrow most common predictions
   9:
                              end if
10:
                              return majority_prediction
11:
12: end function
```

## 3.10.7 Optimization

To enhance the performance of the LingerImplicitClassifier, several optimization strategies are considered:

- **Hyperparameter Tuning**: Utilize grid search or randomized search cross-validation to fine-tune the hyperparameters for optimal classifier performance.
- Feature Engineering: Experiment with different feature combinations and transformations to uncover informative patterns in the data and improve classifier accuracy.
- **Regularization Techniques**: Apply Regularization techniques to improve accuracy, and reduce noise.

#### 3.10.8 Limitations and Future Work

The LingerImplicitClassifier including sensitivity to noise. Future work may focus on improving noise robustness and enhancing interpretability for complex classification tasks.

#### 3.10.9 Conclusion

The LingerImplicitClassifier offers a novel approach to classification tasks by integrating the learning from differences implicitly through case pairs. It performs well for a variety of classification tasks. That could benefit from a more interpretable learning methodology

# 3.11 Linger Implicit Regression Model:

LingerImplicitRegressor

# 3.11.1 Objective

The objective of the LingerImplicitRegressor is to pioneer a learning methodology seen in [18] tailored specifically for regression tasks, known as Learning from

Differences. The primary objectives encompass:

- Creation of a flexible regression model capable of learning implicitly from differences observed in pairs of cases.
- Adaptation of regression tasks into the Learning from Differences framework to unlock its potential.
- Seamless integration with Scikit-learn to ensure compatibility and enable extensive hyperparameter optimization.
- Provision of interpretable predictions crucial for user comprehension across a wide spectrum of regression scenarios.
- Continuous enhancement of the Learning from Differences algorithm through rigorous hyperparameter testing to achieve superior regression performance.
- Designing a modular and extensible codebase to accommodate future variations and improvements.

The LingerImplicitRegressor is designed to address regression challenges where explicit differences may be elusive, prioritizing interpretability and adaptability. It implements the classification methodology described in [18] but facilitates its use for regression tasks. This is a novel approach. It provides added transparency by exposing both the target case and the retrieved case within the case pair, facilitating a deeper understanding during model training.

#### 3.11.2 Architecture

The LingerImplicitRegressor utilizes a hybrid architecture integrating K-nearest neighbors (KNN) with Scikit-learn's MLPClassifier. In the training phase, KNN plays a pivotal role in computing nearest neighbors, thereby facilitating the creation of case pairs. During the prediction phase, KNN is again utilized to retrieve the most similar cases from each class.

The process of generating case pairs for predictions involves KNN's functionality to identify the nearest neighbors. These neighbors serve as crucial elements in forming case pairs, enabling the regressor to make informed predictions based on similarities observed within the dataset.

The integration of KNN with the MLPClassifier offers an interesting approach to regression tasks, combining the strengths of both algorithms. It places regression values within specified ranges, offering a new type of solution to classic regression issues. While KNN excels in identifying similarities and forming case pairs, the MLPClassifier contributes by providing a powerful neural network-based classification model capable of learning intricate patterns and relationships within the data. Classifying regression values.

By harnessing the complementary capabilities of KNN and the MLPClassifier, the LingerImplicitRegressor aims to achieve robust and accurate regression results across diverse datasets while using a classifier, making it a versatile tool for various machine learning applications. This new approach to regression tasks that allows for categorization of regression results. It processes a regression task and converts it to a classification task, this could be useful for problems where ranges of values are highly important. This would make certain regression tasks more interpretable.

### 3.11.3 Components

The key components of the LingerRegressor include:

- KNN Module: Computes nearest neighbors and extracts differences during training and prediction phases.
- MLPClassifier: Offers flexibility in activation functions, solvers, and hyperparameters for classification.
- Additional Features: Class to class pairs, random N selected neighbors, and N nearest neighbors.

#### 3.11.4 Parameterization

The model provides extensive parameterization options for fine-tuning KNN, MLPClassifier, and additional features. Hyperparameters for the classifier model mirror those available in standard KNN and neural networks, with additional parameters specific to LingerRegressor.

### 3.11.5 Training and Prediction Design

The training and prediction algorithms for the LingerImplicitRegressor.

### Training Algorithm Design

```
Algorithm 35 Training Algorithm for LingerImplicitRegressor
Input: Dataset D, number of neighbors 1, N Classes
  Split D into training set D^{train} and test set D^{test} with an 80%-20% split
  Create CasePairs() dictionary.
  Create AdaptNN(), a dictionary to store each Neural Network
  Convert training data y values into classes, using the algorithm 36
  D^{train}y,\,unique\_ranges,\,y_{\rm train}^{\rm max},\,y_{\rm train}^{\rm min}=RegToClassConverterFunction(D^{train},N)
  Convert test y values based on the train y value range. So that a new range is the
  same for both.
  D^{test}y, unique\_ranges, y_{\text{test}}^{\text{max}}, y_{\text{test}}^{\text{min}} = RegToClassConverterFunction(D^{train}, N, y_{\text{train}}^{\text{max}}, y_{\text{train}}^{\text{min}})
  List of unique Classes UniqueClasses
  for each case C_i = (X_i^{train}, y_i^{train}) \in D^{train} do
      Retrieve 1 similar case from D^{train} using nearest neighbors.
      for each similar case (X_i^{train}, y_i^{train}) \in D^{train} do
          CasePairs(y_i^{train}).append([X_i^{train}:X_i^{train},y_i^{train}])
      end for
  end for
  for each unique Class in UniqueClasses do
      Create a new Classification Neural Network, trained on Case Pairs
      AdaptNN(Class).fit(CasePairs(Class))
  end for
  return Trained neural network models dictionary AdaptNN().
```

#### Prediction Algorithm Design

In the prediction phase for regression, several methods exist for retrieving neighbors within each class. These methods can be categorized into three variants:

- 1. Variant 1: (LIRV1) Selecting N random items from each class.
- 2. Variant 2: (LIRV2) Selecting the single nearest neighbor from each class.

The prediction algorithm mirrors Algorithm 29. The key distinction lies in the preprocessing step, where continuous y values are converted into classes to enable accuracy testing.

### 3.11.6 Training and Prediction Implementation

Both the LingerImplicitClassifier and LingerImplicitRegressor share the same training and prediction implementations. This shared functionality is encapsulated in a base class, allowing for code reuse and maintenance. The algorithm 36 found in the 3.11.7 section is used during the data preprocessing stage in the same way as sklearn LabelEncoder. To convert the regression problem into a classification problem.

#### Training Implementation

The training algorithm for LingerImplicitRegressor is outlined in 3.10.6. The function 3.11.7 is called before training to convert y values into class labels. For both training and test datasets

#### Prediction Implementation

The prediction algorithm for LingerImplicitRegressor is outlined in 3.10.6.

# 3.11.7 Regression to Classification Converter Design and Implementation

(RTCC) This function serves to categorize continuous y target values for training, validation, and testing. It returns a human-readable range with their corresponding

numeric prediction. This ensures that the results are interpretable to humans at the end of the process. Central to its operation is the parameter equal division, which indicates whether samples should be equally distributed into N classes. This feature enables uniform representation across different segments of the target variable, promoting fairness and consistency in the categorization process.

#### Regression to Classification Converter Design

The "Regression to Classification Converter" algorithm (Algorithm 36) is designed to transform continuous regression target values into categorical classes. It takes as input a dataset D, the desired number of segments N, and optional parameters such as  $y_{\text{max}}$ ,  $y_{\text{min}}$ , and Equal division.

If Equal division is set, the algorithm divides the data into N segments based on nearly equal counts. Otherwise, it calculates the range for each segment based on the provided or inferred maximum and minimum values of y. It then iterates through each value in y, determining the corresponding category based on the segment ranges. The algorithm returns the transformed y values, along with the unique ranges, minimum and maximum values of y, providing a categorical representation suitable for classification tasks.

### Algorithm 36 Converter algorithm, regression to classification

```
Input: Dataset D, number of segments N, optional: y_{\text{max}}, y_{\text{min}}, Equal division
 1: (X, y) \in D
 2: Get the minimum and maximum values of the labels
 3: Ensure that the max and min are used from the test set so that y values are classified
    the same in both fit and predict.
 4: if Equal division then
        Divide the data into N segments based on nearly equal counts
 5:
        quantiles \leftarrow \text{np.linspace}(0, 1, N + 1)
 6:
 7:
        if unique ranges is None then
 8:
             unique ranges \leftarrow np.quantile(y, quantiles)
        end if
 9:
        categories \leftarrow \text{np.digitize}(y, unique \ ranges[:-1])
10:
        category \ counts \leftarrow Counter(categories)
11:
12:
        Return categories, unique_ranges, y_{\min}, y_{\max}
13: else
        if y_{\text{max}} and y_{\text{min}} are provided then
14:
             Leave y_{\text{max}} and y_{\text{min}} as is
15:
        else
16:
             y_{\text{max}} \leftarrow \text{MAX}(y)
17:
             y_{\min} \leftarrow \text{MIN}(y)
18:
        end if
19:
        Calculate the range for each segment for y values
20:
        segmentRange \leftarrow \frac{y_{max} - y_{min}}{N}
21:
22:
        Initialize an empty list: categories
        Initialize an empty dictionary: unique ranges
23:
        current index \leftarrow 0
24:
        for each value val in y do
25:
26:
             for i in range(N) do
                 if i < N-1 then
27:
                     if y_{\min} + i \times \text{segmentRange} \leq \text{val} < y_{\min} + (i+1) \times \text{segmentRange} then
28:
                         category \leftarrow (y_{\min} + i \times segmentRange) - (y_{\min} + (i + 1) \times i
29:
    segmentRange)
                         if category not in unique_ranges then
30:
                             unique \ ranges[category] \leftarrow current \ index
31:
                             current index \leftarrow current index + 1
32:
                         end if
33:
34:
                         Append unique ranges[category] to categories
                         break
35:
                     end if
36:
                 else
                                                    74
37:
                     if y_{\min} + i \times \text{segmentRange} \leq \text{val} \leq y_{\max} then
38:
```

 $category \leftarrow (y_{\min} + i \times \text{segmentRange}) - (y_{\max})$ 

39:

### Regression to Classification Converter Implementation

This function is encapsulated within a class called RegressionToClassificationConverter. The transform function carries out the conversion of regression values to classification values.

#### Algorithm 37 Transform function

```
1: function TRANSFORM(y, min\_val = None, max\_val = None, unique\_ranges =
   None
       Input:
2:
       y (list or array-like): The continuous target variable.
3:
       min val (float): Minimum value of the target variable.
 4:
       max val (float): Maximum value of the target variable.
5:
       unique ranges (array-like): Predefined unique ranges for segments.
 6:
       Output:
 7:
8:
       categories (list): A list of categories (segment indices) corresponding to each value
   in y.
       unique ranges (dict or array-like): Unique ranges for segments.
9:
       min val (float): Minimum value of the target variable.
10:
       max val (float): Maximum value of the target variable.
11:
       if min val is None and max val is None then
12:
13:
           min \ val \leftarrow \min(y)
14:
           max \ val \leftarrow \max(y)
       end if
15:
16:
       if equal division is None then
           segment \ range \leftarrow (max \ val - min \ val)/n \ segments
17:
           categories \leftarrow []
18:
           unique ranges \leftarrow \{\}
19:
20:
           current index \leftarrow 0
21:
           for val in y do
              for i in range(n\_segments) do
22:
23:
                  if i < n segments -1 then
                      if min\ val + i \times segment\ range \leq val < min\ val + (i + 1) \times i
24:
   segment range then
25:
                         category \leftarrow int(min \ val + i \times segment \ range)
                         int((min\ val + (i+1)) \times segment\_range)
26:
27:
                         if category not in unique ranges then
                             unique ranges[category] \leftarrow current index
28:
29:
                             current index \leftarrow current index + 1
                         end if
30:
                         categories.append(unique ranges[category])
31:
                         break
32:
                      end if
33:
                  else
34:
                      if min\ val + i \times segment\ range \leq val \leq max\ val then
35:
                         category \leftarrow int(min\_val + i \times segment\_range)
36:
                         int(max \ val)
37:
                         if category not in unique ranges then
38:
                             unique ranges[category] \leftarrow current index
39:
40:
                             current index \leftarrow current index + 1
41:
                         end if
                         categories.append(unique ranges[category])
42:
                         break
43:
                      end if
44:
                  end if
45:
              end for
46:
                                             76
47:
           end for
48:
           return categories, unique ranges, min val, max val
       else
49:
```

### 3.11.8 Optimization

To enhance the performance of the LingerImplicitRegressor, several optimization strategies are considered:

- **Hyperparameter Tuning**: Utilize grid search or randomized search cross-validation to fine-tune the hyperparameters for optimal model performance.
- Feature Engineering: Experiment with different feature combinations and transformations to uncover informative patterns in the data and improve regressor accuracy.
- Regularization Techniques: Apply regularization techniques to improve accuracy and reduce noise.

#### 3.11.9 Limitations and Future Work

One of the limitations of the LingerImplicitClassifier is its sensitivity to noise, particularly when labeling values based on the maximum and minimum. However, opting to evenly distribute samples into classes can mitigate this sensitivity. For future research, exploring alternative methods to bucket regression values based on diverse distributions could be an intriguing avenue.

#### 3.11.10 Conclusion

The LingerImplicitClassifier offers a novel approach to regression tasks by integrating the learning from differences implicitly through case pairs. It performs well for a variety of regression tasks, while utilizing a learning from differences classification model. The number of segments greatly affects the outcome of this model.

### 3.12 Learning from Differences For Images

#### 3.12.1 Introduction and Motivation

The introduction of the LingerImageClassifier and LingerImageRegressor represents a novel approach to image classification and regression tasks. Motivated by

the innovative methodology outlined in "Learning from Differences 2022," these tools are specifically designed to enhance interpretability and explainability in processing image data. The aim was to ensure these models not only integrate smoothly into the existing software framework but also support the customization of Keras convolutional neural networks. This strategy diverges from traditional methods, such as those employed by Scikit-learn's MLPClassifier and MLPRegressor, offering a fresh perspective on addressing image-centric challenges.

## 3.13 Linger Image Classification Model

LingerImageClassifier (LIMC)

### 3.13.1 Objective

The motivation behind the development of (LIMC) stems from the growing demand for more sophisticated image classification tools capable of handling the complexities and nuances of real-world data. Traditional models often fall short in terms of explainability, and transparency. (LIMC) aims to address these gaps by:

- Incorporating state-of-the-art convolutional neural network (CNN) designs that improve upon the limitations of existing models in capturing intricate patterns in image data.
- Utilizing a novel training methodology seen in [7] that enhances model learning from image differences, inspired by recent research findings.
- Aiming to demystify the black-box nature of deep neural networks by providing insights into the decision-making process, making the model more trustworthy and applicable in sensitive areas such as medical diagnosis and autonomous driving.

#### 3.13.2 Architecture

The LingerImageClassifier employs a sophisticated, modular architecture designed to leverage the nuances of image data, enhancing both predictive accuracy and interpretability. This architecture consists of three integral components:

• Custom Fit Method: Developed to integrate with the scikit-learn [?] ecosystem, this Fit method is central to the classifier's functionality. It generates

a unique dataset of image differences, effectively capturing variations between image pairs. This method not only emphasizes the importance of contrastive learning but also enriches the model's understanding of nuanced features within the data, such as changes in texture, lighting, and spatial relationships. The process involves computing the differential aspects of images, focusing on attributes that significantly influence the y label values, thereby enabling a more focused and effective learning strategy. It also guarantees that we know what it is precisely learning from, its visual difference to its neighbor.

- Convolutional Neural Network (CNN): At the heart of the classifier lies a customizable Convolutional Neural Network, tailored from Keras's comprehensive library. This CNN is specifically designed to process and predict the differences highlighted by the custom Fit method. The architecture features a combination of convolutional layers, activation functions, and pooling layers, strategically organized to maximize feature extraction and minimize information loss. Special attention is given to the network's depth, filter sizes, and the incorporation of advanced techniques such as batch normalization and dropout for regularization. This careful construction ensures optimal performance in discerning subtle differences in image data, thus significantly contributing to the precision of subsequent predictions.
- Custom Predict Method: Complementing the custom Fit method, the Predict function stands as a testament to the model's innovative approach to classification. This component takes the CNN's predictions on image differences and synthesizes them with the original data to formulate the final classification outcomes. The method employs an algorithm that accurately applies predicted differences to their corresponding instance, accounting for the model's understanding of contrastive features within the dataset. This not only enhances the model's accuracy but also its adaptability to various image classification scenarios, ensuring that the final predictions are both precise and contextually grounded.

Integration and Workflow: The synergy between these components forms the cornerstone of the LingerImageClassifier's architecture. Initially, the custom Fit method preprocesses the input images to create a differential dataset, which is then fed into the CNN for feature extraction and difference prediction. The custom Predict method subsequently interprets these predictions, applying them to derive the final classification results. This integrated workflow ensures a coherent and efficient processing pipeline, from initial data preparation to final outcome generation.

Innovations and Contributions: The architecture of the LingerImageClassifier

introduces several key innovations to the field of image classification. By focusing on image differences, the model uncovers deeper insights into the data, facilitating a more nuanced understanding and interpretation of the factors driving classification decisions. This approach not only improves model performance across diverse datasets but also enhances the explainability of its predictions, addressing a critical need within the domain of deep learning. Visually we could Identify exactly what the image is learning from based on the difference image generated.

### 3.13.3 Components

The key components of the LingerImageClassifier include:

• KNN Module: Computes nearest neighbors used to extract differences during training phase and prediction phase.

•

• Convolutional Neural Network (CNN): The heart of the classification process is a Convolutional Neural Network (CNN), meticulously designed to analyze and interpret the differences identified by the KNN module. This CNN is notable for its flexibility, allowing for the customization of activation functions, solvers, and an extensive range of hyperparameters to optimize classification performance. The adaptability of the CNN component ensures that the model can be fine-tuned to suit various datasets and classification challenges. It excels in processing the contrastive features extracted by the KNN module, effectively learning from these differences to make accurate predictions. The CNN's architecture, which can include layers specifically tailored to enhance feature extraction and reduce overfitting, such as dropout and batch normalization layers, is instrumental in capturing the complex patterns inherent in image data.

#### 3.13.4 Parameterization

The LingerImageClassifier is designed with flexibility and adaptability at its core, offering a comprehensive suite of parameters that can be fine-tuned to optimize performance across a wide range of image classification tasks. The use can vary the design of the (CNN) convolutional Neural Network, as well as vary the number of neighbors used in the fit and prediction methods.

### 3.13.5 Training and Prediction Design

#### Training Design

The Image Classification Training Algorithm outlines the steps involved in training a convolutional neural network (CNN) for image classification tasks using the differences between nearest neighbor images.

```
Algorithm 38 Image Classification Training Algorithm
```

function TrainImageClassifier(X, y)

**Input:** Dataset of images X, Target labels y

Output: Trained CNN model

Generate the image difference datasets.

 $differences\_X, differences\_y \leftarrow GenerateDifferences(X, y)$ 

Initialize (CNN) model.

Train CNN model using differences X and differences y

return Trained CNN model

end function

The 'GenerateDifferences' 39 algorithm encapsulates the process of computing differences between nearest neighbor images and their base image, preparing the data for training the k-nearest neighbors classifier. It iterates through each image in the training dataset, identifies its nearest neighbors, and calculates the absolute differences between their pixel values. These differences, along with the target value differences, are stored in lists for subsequent use in the training process.

### Algorithm 39 Generate Differences Algorithm

```
function GENERATEDIFFERENCES(X, y)
   Input: Training images X, Target values y
   Output: List of arrays representing differences differences_X, List of target dif-
ferences differences_u
   if Shape of X is More than 2-dimensional then
      Reshape X to 2-dimensional array
   else
      Keep X as it is
   end if
   Increment n neighbours 1 by 1
   Initialize empty list differences X
   Initialize empty list differences y
   Fit nearest neighbors to find indices of nearest neighbors
   Compute nearest neighbor indices for each image in X
   for each image I in X do
      Get nearest neighbors indices for I
      for each neighbor index N do
          Get neighbor image and target value
          Compute absolute difference between I and neighbor image
         Append difference to differences X
         Append target value difference to differences y
      end for
   end for
   {\bf return} \ differences\_X, \ differences\_y
end function
```

#### Prediction Design

This algorithm, named "Image Classification Prediction Algorithm," takes a dataset of images X and a trained convolutional neural network (CNN) model trainedCNN as input. It utilizes the trained CNN model to predict the differences between images in the dataset. The predicted differences are then processed further using the FinalPrediction algorithm (referenced as Algorithm 41) to compute the final predictions for the images. Finally, the algorithm returns the predicted target values  $y_p$  redictions.

#### Algorithm 40 Image Classification Prediction Algorithm

- 1: **function** PredictImageClassifier(X, trainedCNN)
- 2: **Input:** Dataset of images X, Trained CNN model trainedCNN
- 3: **Output:** Predictions
- 4: Use trained CNN on X to predict differences
- 5:  $difference pred \leftarrow trainedCNN(X)$
- 6: Compute final predictions using Algorithm:  $y\_predictions \leftarrow FinalPrediction(difference\_pred)$
- 7: **return** y\_predictions
- 8 end function

This algorithm, titled "FinalPrediction," takes input data X, a trained CNN model model, and the input shape  $input_shape$ . It computes the predicted target values  $y_pred$  based on the differences between the input data and the training images using the trained CNN model.

First, it fits nearest neighbors to the training data and then computes the absolute differences between each test image and its nearest neighbors from the training set. These differences are reshaped to match the input shape and used to make predictions using the trained CNN model.

Finally, it computes the predicted results for each nearest neighbor and determines the most common item among them to form the final prediction  $y_p red$ . If no items are found, it handles this case by appending "None" to  $y_p red$ .

#### Algorithm 41 Image Classification Prediction Algorithm

```
1: function FINALPREDICTIONCLASSIFICATION(X, model, input shape)
       Input: Input data X, Trained CNN model model, Input shape input shape
2:
3:
       Output: Predicted target values y pred
       Fit nearest neighbors to the training data
 4:
       Initialize empty list differences\_test\_X
5:
6:
       for test in range(length of X) do
                                                ▷ Compute differences between test and
   training images
          for nn in training in range (length of nearest neighbors) do
 7:
8:
              Compute difference between test and nearest neighbor:
                                                                         X[test]
9:
                diff
                                  absolute
                                              difference
                                                            between
                                                                                    and
   self.train \ X[indices[test][nn \ in \ training]]
              Append diff to differences\_test\_X
10:
          end for
11:
       end for
12:
       Reshape differences test X to match input shape
13:
       Make predictions using the trained CNN model:
                                                                      predictions
14:
   model.predict(differences\ test\ X)
       Initialize empty list y pred
15:
       for indexes, differences in zip(indices, predictions) do
16:
          Compute predicted results for each nearest neighbor:
17:
18:
            results \leftarrow [self.train \ y[i][0] + d \text{ for } i, d \text{ in } zip(indexes, differences)]
          Compute counts of each result: counts \leftarrow count of each value in results
19:
          Retrieve most common item: most common item \leftarrow most common value in
20:
   results
          if most common item exists then
21:
22:
              Append most\_common\_item to y\_pred
          else
23:
                                                           ▶ Handle cases with no items
24:
              Append None to y pred
          end if
25:
       end for
26:
       return y\_pred
27:
28: end function
```

### 3.13.6 Training and Prediction Implementation

### Training Implementation

7: end procedure

### Algorithm 42 Initialize LingerImageClassifier

```
1: Number of nearest neighbors for difference computation
2: Input: n\_neighbours\_1, n\_neighbours\_2
3: procedure InitializeClassifier(n\_neighbours\_1, n\_neighbours\_2)
4: self.n\_neighbours\_1 \leftarrow n\_neighbours\_1
5: self.n\_neighbours\_2 \leftarrow n\_neighbours\_2
6: return self
```

#### Algorithm 43 Generate Differences

```
1: procedure GENERATEDIFFERENCES(X, y, n\_neighbours)
      Input: X - dataset of images, y - target labels, n\_neighbours - number of
   neighbors
      Differences in images and labels
3:
      Output: differences_X, differences_y
4:
      Initialize differences\_X and differences\_y as empty lists
5:
      neigh \leftarrow Fit NearestNeighbors on X with n neighbours
6:
      for each image I in X do
7:
          Find n\_neighbours nearest neighbors for I
8:
          for each neighbor N do
9:
             Compute absolute difference between I and N
10:
             Append difference to differences_X
11:
12:
             Compute difference in target values and append to differences_y
          end for
13:
      end for
14:
      return differences_X, differences_y
15:
16: end procedure
```

### Algorithm 44 Train with LingerImageClassifier

- 1: procedure TRAIN LINGERIMAGECLASSIFIER $(X_{train}, y_{train}, X_{test})$
- 2: Load dataset into  $X_{train}, y_{train}, X_{test}, y_{test}$
- 3: Initialize LingerImageClassifier with  $n\_neighbours\_1$  and  $n\_neighbours\_2$
- 4:  $differences_X, differences_y \leftarrow \text{GenerateDifferences}(X_{train}, y_{train})$
- 5: Train CNN model on  $differences\_X, differences\_y$
- 6: end procedure

### **Prediction Implementation**

### Algorithm 45 Prediction Process with LingerImageClassifier

- 1: **procedure** PREDICT $(X_{test}, y_{test})$
- 2: For making predictions and evaluating performance
- 3: **Input:**  $X_{test}$  Test images,  $y_{test}$  True labels for evaluation
- 4: Predict target values for  $X_{test}$  using the PREDICT procedure.
- 5: Compute final predictions and compare against  $y_{test}$  to evaluate accuracy.
- 6: Calculate and report model performance metrics (e.g., accuracy, precision, recall).
- 7: **return** Model performance metrics.
- 8: end procedure

### Algorithm 46 Prediction Implementation with LingerImageClassifier

```
1: procedure PREDICT(X, model, input shape)
                                                             ▶ Pythonic steps for predicting
   target values using image differences.
       Input: X - Input data, model - Trained CNN, input shape - Shape for CNN
   input.
       Output: y\_pred - Predicted targets.
3:
       nbrs \leftarrow \text{NearestNeighbors}(n \ neighbors = self.n \ neighbours \ 2).\text{fit}(self.train \ X.\text{reshape}(ler))
 4:
       indices \leftarrow nbrs.kneighbors(X.reshape(len(X), -1), return \ distance = False)
5:
       differences test X
                                                            [np.abs(X[test].flatten()
   self.train \ X[indices[test][nn]].flatten()) for test in range(len(X)) for nn in
   range(len(indices[0]))]
       differences\_test\_X \leftarrow np.array(differences\_test\_X).reshape(-1, *input\_shape)
7:
       predictions \leftarrow model.predict(differences\_test\_X)
8:
       y pred \leftarrow []
9:
       for indexes, differences in zip(indices, predictions) do
10:
11:
           results \leftarrow [self.train\_y[i][0] + d \text{ for } i, d \text{ in } zip(indexes, differences)]
           counts \leftarrow Counter(results)
12:
           most\_common \leftarrow counts.most\_common(1)
13:
           if most common then
14:
              y pred.append(most common[0][0])
15:
           else
16:
              y\_pred.append(None)
17:
           end if
18:
       end for
19:
       return y\_pred
20:
21: end procedure
```

### 3.13.7 Optimization

To enhance the performance of the LingerImageClassifier, several optimization strategies are considered:

- **Hyperparameter Tuning**: Utilize grid search to test multiple values for the integrated knn for both fit and predict.
- Convolutional Network: Vary the structure of the convolutional neural network. To suit different datasets

#### 3.13.8 Limitations and Future Work

The main limitation with this model is its resource intensity, and testing with only one classification image dataset. In the future a GPU could be used to attain results faster

on a wide range of image datasets. The inclusion of the original image could be useful when training the Convolutional network.

### 3.14 Linger Image Regressor Model

LingerImageRegressor (LIMR)

### 3.14.1 Objective

The motivation behind the development of (LIMR) stems from the growing demand for more sophisticated image regression tools capable of image data and solving regression issues. Traditional models often fall short in terms of explainability, and transparency. (LIMR) aims to address these gaps by:

- Incorporating state-of-the-art convolutional neural network (CNN) designs that improve upon the limitations of existing models in capturing intricate patterns in image data.
- Utilizing a novel training methodology seen in [7] that enhances model learning from image differences, inspired by recent research findings.
- Aiming to demystify the black-box nature of deep neural networks by providing insights into the decision-making process, making the model more trustworthy and applicable in sensitive areas such as medical diagnosis and autonomous driving.

#### 3.14.2 Architecture

Its architecture is similar to the classifier, only that it uses a convolutional neural net to predict continuous values rather than classes. The method of applying the generated differences to the data during prediction varies slightly. The structure of the LingerImageClassifier, and LingerImageRegressor is identical, the functionality of thier predict methods vary. See section 3.13.2 for a more indepth analysis.

### 3.14.3 Components

The key component within the LingerImageRegressor are identical to those in the LingerImageClassifier. For more details see section 3.13.3.

#### 3.14.4 Parameterization

The LingerImageRegressor is designed with flexibility and adaptability at its core, offering a comprehensive suite of parameters that can be fine-tuned to optimize performance across a wide range of image classification tasks. The use can vary the design of the (CNN) convolutional Neural Network, as well as vary the number of neighbors used in the fit and prediction methods.

### 3.14.5 Training and Prediction Design

#### Training Design

The Image Regression Training Algorithm outlines the steps involved in training a convolutional neural network (CNN) for image regression tasks using the differences between nearest neighbor images. For regression, it uses the same algorithm ?? to generate the image differences datasets as LingerImageClassifier.

```
Algorithm 47 Image Regression Training Algorithm
```

function TrainImageRegressor(X, y)

**Input:** Dataset of images X, Target labels y

Output: Trained CNN model

Generate the image difference datasets.

 $differences \ X, differences \ y \leftarrow GenerateDifferences(X, y)$ 

Initialize (CNN) model.

Train CNN model using differences X and differences y

return Trained CNN model

end function

The predict method varies as it no longer takes a majority vote. To finalize its prediction but takes an average of nearest neighbors with their predicted differences added to them.

This algorithm outlines a method for image regression prediction using a Convolutional Neural Network (CNN). It involves fitting nearest neighbors to training data, calculating differences between test images and their nearest training images using, and using these differences as inputs to a pre-trained CNN model to predict target values. The algorithm computes predictions by averaging adjustments made to the nearest neighbors' target values based on the CNN's output 49, thereby producing a final prediction for each input image. This approach combines instance-based learning with

#### Algorithm 48 ImageRegression Prediction Algorithm

- 1: **function** PredictImageClassifier(X, trainedCNN)
- 2: **Input:** Dataset of images X, Trained CNN model trainedCNN
- 3: Output: Predictions
- 4: Use trained CNN on X to predict differences:  $difference\_pred \leftarrow trainedCNN(X)$
- 5: Compute final predictions using Algorithm:  $y\_predictions \leftarrow FinalPrediction(difference\ pred)$
- 6:  $\mathbf{return} \ y\_predictions$
- 7 end function

deep learning to enhance prediction accuracy for image-based regression tasks. The method of learning from differences is based on the algorithms in the paper [7],

### Algorithm 49 Image Regression Prediction Algorithm

- 1: **function** FinalPrediction(X, model,  $input\_shape$ )
- 2: **Input:** Input data X, Trained CNN model model, Input shape input shape
- 3: Output: Predicted target values y pred
- 4: Fit nearest neighbors to the training data
- 5: Initialize empty list differences test X
- 6: **for** test in range(length of X) **do**  $\triangleright$  Compute differences between test and training images
- 7: **for** nn in training in range(length of nearest neighbors) **do**
- 8: Compute difference between test and nearest neighbor:
- 9:  $diff \leftarrow absolute difference between X[test] and <math>train_X[indices[test][nn\_in\_training]]$
- 10: Append diff to differences test X
- 11: end for
- 12: end for
- 13: Reshape  $differences\_test\_X$  to match input shape
- 14: Make predictions using the trained CNN model:  $predictions \leftarrow model.predict(differences\ test\ X)$
- 15: Initialize empty list *y* pred
- 16: for indexes, differences in zip(indices, predictions) do
- 17: Compute predicted results for each nearest neighbor:
- 18:  $results \leftarrow [self.train\_y[i][0] + d \text{ for } i, d \text{ in } zip(indexes, differences)]$
- 19: Compute average of each result:  $average \leftarrow$  average of values in results
- 20: Append average to  $y\_pred$
- 21: end for
- 22: **return** y pred
- 23: end function

### 3.14.6 Training and Prediction Implementation

### Training Implementation

### Algorithm 50 Initialize LingerImageRegressor

```
1: Number of nearest neighbors for difference computation

2: Input: n\_neighbours\_1, n\_neighbours\_2

3: procedure InitializeRegressor(n\_neighbours\_1, n\_neighbours\_2)

4: self.n\_neighbours\_1 \leftarrow n\_neighbours\_1

5: self.n\_neighbours\_2 \leftarrow n\_neighbours\_2

6: return self
```

The same algorithm 43 is used to generate differences for the training process in the LingerImageRegressor as the LingerImplicitClassifier.

### Algorithm 51 Train with LingerImplicitRegressor

- 1: procedure Train LingerImageRegressor $(X_{train}, y_{train}, X_{test})$
- 2: Load dataset into  $X_{train}, y_{train}, X_{test}, y_{test}$
- 3: Initialize LingerImageRegressor with n neighbours 1 and n neighbours 2
- 4:  $differences_X, differences_y \leftarrow \text{GenerateDifferences}(X_{train}, y_{train})$
- 5: Train CNN model on  $differences\_X, differences\_y$
- 6: end procedure

7: end procedure

### **Prediction Implementation**

### Algorithm 52 Prediction Process with LingerImageRegressor

- 1: **procedure** PREDICT $(X_{test}, y_{test})$
- 2: For making predictions and evaluating performance
- 3: **Input:**  $X_{test}$  Test images,  $y_{test}$  True labels for evaluation
- 4: Predict target values for  $X_{test}$  using the PREDICT procedure.
- 5: Compute final predictions and compare against  $y_{test}$  to evaluate accuracy.
- 6: Calculate and report model performance metrics (e.g., accuracy, precision, recall).
- 7: **return** Model performance metrics.
- 8: end procedure

### Algorithm 53 Prediction with LingerImageRegressor

- 1: **procedure** PREDICT(X, model, dataset, input shape)
- 2: Predicts target values using a regression approach based on image differences.
- 3: **Input:** X Input data for prediction, model Trained regression model, dataset Dataset object containing training data,  $input\_shape$  Shape of input data expected by the model.
- 4: **Output:** *y* pred Predicted target values for the input data.
- 5: **if** len(X.shape) > 2 **then**
- 6:  $X \leftarrow X.reshape(len(X), -1)$  > Flatten the input if it's multi-dimensional.
- 7: end if
- 8: Train the NearestNeighbors function on our data.
- 9:  $nbrs \leftarrow \text{NearestNeighbors}(n\_neighbors = self.n\_neighbours\_2).\text{fit}(dataset.train\_X.reshape)$
- 10:  $indices \leftarrow nbrs.kneighbors(X, return\_distance = False)$   $\triangleright$  Identify nearest neighbors in the training set.
- 11: Prepare  $differences\_test\_X$  by computing absolute differences between X and its nearest neighbors in the training set.
- 12: Reshape differences\_test\_X to match input\_shape for compatibility with the model.
- 13:  $predictions \leftarrow model.predict(differences\_test\_X)$   $\triangleright$  Predict target values based on computed differences.
- 14: Initialize an empty list *y pred* to store final predictions.
- 15: **for** each *indexes*, *differences* pair in zipped *indices*, *predictions* **do**
- 16: Calculate the sum of the training target values and the predicted differences.
- 17: Compute the average result to obtain the regression prediction.
- 18: Append the average result to  $y\_pred$ .
- 19: end for
- 20:  $\mathbf{return} \ y\_pred$

▶ Return the list of predicted target values.

21: end procedure

### 3.14.7 Optimization

To enhance the performance of the LingerImageClassifier, several optimization strategies are considered:

- **Hyperparameter Tuning**: Utilize grid search to test multiple values for the integrated knn for both fit and predict.
- Convolutional Network: Vary the structure of the convolutional neural network. To suit different datasets

### 3.14.8 Limitations and Future Work

Similar to the LingerImageClassifier the LingerImplicitRegressor's main difficulty is in testing due to its high computational costs. A high end GPU would be useful to test it on multiple datasets. The inclusion of the original image could be useful when training the Convolutional network.

# Chapter 4

# **Experiments**

### 4.1 Research Objective

The overarching objective of this study is to investigate the efficacy of blended learning approaches in machine learning tasks, particularly focusing on regression and classification problems. Blended learning, which integrates the strengths of model-based and instance-based learning while mitigating their respective weaknesses, offers a promising avenue for enhancing the interpretability, reliability, and performance of machine learning systems.

Specifically, this research aims to achieve the following objectives:

- 1. Evaluate Blended Learning Methods: The first objective is to evaluate the performance of blended learning methodologies in contrast to traditional model-based and instance-based approaches across various regression and classification tasks. This assessment will encompass key metrics including accuracy, interpretability, computational efficiency, and robustness. By comparing the effectiveness of blended learning methods, we aim to determine their potential to enhance the overall performance of machine learning systems.
- 2. Investigate Model Interpretability: The second objective is to explore the interpretability of blended learning models compared to traditional black-box models, such as neural networks. Understanding the interpretability of these models is crucial for enhancing trust and usability in critical domains. By investigating how blended learning methods provide insights into model decisions, we aim to demonstrate their potential to address the interpretability challenges associated with traditional machine learning approaches.

- 3. Examine Efficiency and Scalability: The third objective is to investigate the computational efficiency and scalability of blended learning methods, particularly in scenarios with large datasets. This examination will involve analyzing the memory and computational overhead of blended learning models compared to traditional approaches. By assessing the efficiency and scalability of blended learning methods, we aim to identify their suitability for practical deployment in real-world applications.
- 4. Explore Novel Architectures: The fourth objective is to explore novel architectures and techniques for implementing blended learning, including ensemble models, case-based reasoning principles, and approaches that leverage differences between sets of features. By exploring innovative approaches, we aim to further enhance the performance and interpretability of blended learning methods, thereby advancing the state-of-the-art in machine learning.
- 5. Provide Insights for Practical Applications: The fifth objective is to provide insights and recommendations for the practical application of blended learning methods in real-world scenarios, with a particular focus on critical domains such as healthcare, finance, and decision support systems. By discussing the implications of the findings for stakeholders and suggesting best practices for deploying blended learning models effectively, we aim to facilitate the adoption of these methods in critical domains.
- 6. Develop Python Package for Seamless Integration: The final objective is to develop a Python package that seamlessly integrates with scikit-learn, allowing users to incorporate blended learning methods into their machine learning pipelines and workflows effortlessly. This package should provide compatibility with scikit-learn's APIs, enabling users to import it like any other scikit-learn package and use it seamlessly within their existing workflows. By developing such a package, we aim to enhance the accessibility and usability of blended learning methods for the broader machine learning community.

By addressing these objectives, this research seeks to advance our understanding of blended learning approaches and their potential to address the challenges faced by traditional model-based and instance-based methods. Ultimately, the goal is to contribute to the development of more interpretable, reliable, and efficient machine learning systems with broader applicability across various domains.

### 4.1.1 Data Collection and Preprocessing

All datasets used in this study were collected from the UCI Machine Learning Repository [1], a widely recognized and reliable source of machine learning datasets. These datasets cover various domains and have been extensively studied in the machine learning community.

#### Preprocessing For Labelled Datasets

The preprocessing procedure involves several steps to ensure the quality and suitability of the data for machine learning tasks. These steps are applied uniformly across all labeled datasets.

- 1. Column Naming: The columns of the dataset are assigned appropriate names for clarity and consistency throughout the analysis.
- 2. Handling Missing Values: Rows containing missing values in specified features are removed from the dataset. This ensures that the dataset used for training and testing is complete and does not contain any incomplete or unreliable data points.
- 3. **Index Resetting**: After removing rows with missing values, the index of the dataset is reset to maintain a continuous and consistent index structure.
- 4. **Data Splitting**: The dataset is split into two subsets: a development set and a test set. This splitting is performed using a train-test split ratio of 80 : 20 to ensure a sufficient amount of data for training while also reserving a portion for evaluating the model's performance.
- 5. **Development Set Copying**: A copy of the development set is created to preserve the original dataset for future reference or comparison.
- 6. Feature Transformation: Numeric features undergo feature scaling using the StandardScaler to ensure that they are on a similar scale, which aids in model convergence and performance. Nominal features are transformed using one-hot encoding to convert categorical variables into a numerical format suitable for machine learning algorithms.

These preprocessing steps collectively prepare the data for subsequent modeling and analysis, ensuring that it is clean, complete, and appropriately formatted for use in machine learning tasks.

### 4.2 Results and Analysis

### 4.2.1 Experiment 1: Glass Dataset Classification

#### Methodology

In Experiment 1, we conducted classification tasks on the Glass dataset using a two-step methodology. Initially, we trained a neural network (NN) classifier through grid search and cross-validation to determine the optimal hyperparameters. These hyperparameters were then applied to train a LingerClassifier (LC) and its variants for improved robustness, tested across five runs. For comparative analysis, we also evaluated the performance of K-Nearest Neighbors (KNN), weighted (KNN), and (NN) on the same dataset. The results section details the hyperparameters selected and the test accuracies achieved.

### Hyperparameter Optimization

For both the Neural Network and Linger Classifier, a comprehensive exploration of hyperparameters was conducted, as summarized in Table 4.1. This table delineates the varied hyperparameters scrutinized during the optimization phase, spanning hidden layer configurations, activation functions, regularization terms, and more, underscoring our meticulous approach to model tuning.

Table 4.1: Tested Hyperparameters for Neural Network and Linger Classifier

Hyperparameter	Values		
Neural Network			
Hidden Layer Sizes	(256, 128), (128, 64), (100,), (200, 100), (300, 200, 100)		
Activation	identity, logistic, tanh, relu		
Alpha	0.0001,0.001,0.01,0.1		
Max Iterations	1000, 1500		
Early Stopping	True		
Validation Fraction	0.1, 0.2, 0.3		
Learning Rate Init	0.001,0.01,0.1		
Solver	adam, sgd		
Beta 1	0.9, 0.95, 0.99		
Beta 2	0.999,0.995,0.9		
Linger Classifier			
Neighbors 1	2, 5, 7, 10, 13, 15, 17, 21		
Neighbors 2	2, 5, 7, 10, 13, 15, 17, 21		
Weighted KNN	False		
Additional Distance Column	True, False		
Duplicated on Distance	True, False		
Addition of Context	True, False		

### (LC) Results

Table 4.2: Best Parameters for Classifiers

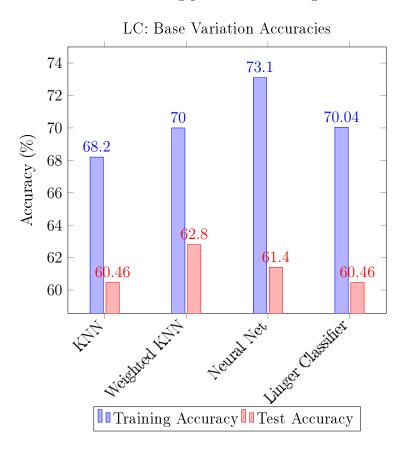
Classifier	Hyperparameter	Value		
Common Parameters for Neural Net and Linger Classifier				
Neural Net / Linger Classifier	activation	relu		
Neural Net / Linger Classifier	alpha	0.0001		
Neural Net / Linger Classifier	beta_1	0.9		
Neural Net / Linger Classifier	beta_2	0.995		
Neural Net / Linger Classifier	early_stopping	True		
Neural Net / Linger Classifier	hidden_layer_sizes	(300, 200, 100)		
Neural Net / Linger Classifier	learning_rate_init	0.01		
Neural Net / Linger Classifier	max_iter	1000		
Neural Net / Linger Classifier	solver	$\operatorname{adam}$		
Neural Net / Linger Classifier	${\it validation\_fraction}$	0.3		
KNN Classifier Specific				
KNN	n_neighbors	2		
Weighted KNN	$n\_neighbors$	7		
Linger Classifier Specific				
Linger Classifier	addition_of_context	False		
Linger Classifier	additional_distance_column	False		
Linger Classifier	$duplicated\_on\_distance$	False		
Linger Classifier	n_neighbors_1	2		
Linger Classifier	n_neighbors_2	5		
Linger Classifier	weighted_knn	False		

Table 4.3: Average Training and Test Accuracy Results

Classifier	Training Accuracy (%)	Test Accuracy (%)
KNN Classifier	68.2	60.46
Weighted KNN Classifier	70.0	62.8
Neural Net Classifier	73.1	61.4
Linger Classifier	70.04	60.46

### (LC) Analysis

The initial setup without any specific variation (LC) demonstrates that the Neural Net Classifier achieves the highest training accuracy but does not significantly outperform other models in test accuracy. This could suggest a tendency towards overfitting within the (NN) model. The LingerClassifier, even in its base form, shows competitive test accuracy, emphasizing its potential robustness. Interestingly, the addition of context and other specific features in the LingerClassifier's variations aims to address this balance between training performance and generalization to unseen data.



### (LCV1) Results

Table 4.4: Best Parameters for Classifiers (LCV1)  $\,$ 

Classifier	Hyperparameter	Value		
Common Parameters for Neural Net and Linger Classifier with Context (Variation 1)				
Neural Net / Linger Classifier	activation	relu		
Neural Net / Linger Classifier	alpha	0.1		
Neural Net / Linger Classifier	beta_1	0.9		
Neural Net / Linger Classifier	beta_2	0.999		
Neural Net / Linger Classifier	$early\_stopping$	True		
Neural Net / Linger Classifier	hidden_layer_sizes	(300, 200, 100)		
Neural Net / Linger Classifier	$learning\_rate\_init$	0.01		
Neural Net / Linger Classifier	$\max_{}$ iter	1500		
Neural Net / Linger Classifier	solver	adam		
Neural Net / Linger Classifier	${\rm validation\_fraction}$	0.3		
KNN Classifier Specific				
KNN	n_neighbors	2		
Weighted KNN Classifier Specific				
Weighted KNN	n_neighbors	7		
Linger Classifier with Context (Variation 1) Specific				
Linger Classifier	addition_of_context	True		
Linger Classifier	$additional\_results\_column$	False		
Linger Classifier	${\rm duplicated\_on\_distance}$	False		
Linger Classifier	$n\_neighbours\_1$	17		
Linger Classifier	$n\_neighbours\_2$	17		
Linger Classifier	weighted_knn	False		

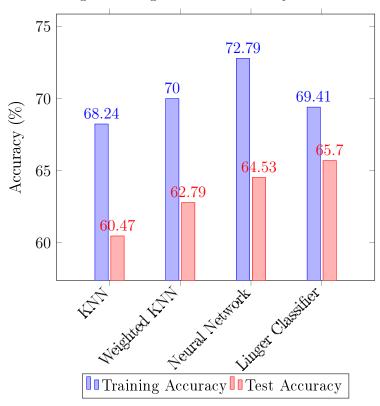
Table 4.5: Average Training and Test Accuracy Results for Classifiers (LCV1)

Classifier	Training Accuracy (%)	Test Accuracy (%)
KNN Classifier	68.24	60.47
Weighted KNN Classifier	70.00	62.79
Neural Network Classifier	72.79	64.53
Linger Classifier	69.41	65.70

#### (LCV1) Analysis

In LCV1, the inclusion of context, (setting  $addition_o f_context == \text{True}$ ) for the LingerClassifier led to a noticeable improvement in test accuracy for the Linger Classifier, outperforming the NN in test accuracy while maintaining competitive training accuracy. This improvement underscores the value of incorporating contextual information into the model, potentially enhancing its ability to generalize from training to test data.

LCV1: Average Training and Test Accuracy Results for Classifiers



# (LCV2) Results

Table 4.6: Best Parameters for Classifiers (LCV2)  $\,$ 

Classifier	Hyperparameter	Value
Common Parameters for Neuro	al Net and Linger Classifier, D	uplication using Distance (Variation 2)
Neural Net / Linger Classifier	activation	relu
Neural Net / Linger Classifier	alpha	0.1
Neural Net / Linger Classifier	beta_1	0.9
Neural Net / Linger Classifier	beta_2	0.995
Neural Net / Linger Classifier	$early\_stopping$	True
Neural Net / Linger Classifier	hidden_layer_sizes	(300, 200, 100)
Neural Net / Linger Classifier	learning_rate_init	0.01
Neural Net / Linger Classifier	$\max_{}$ iter	1000
Neural Net / Linger Classifier	solver	$\operatorname{adam}$
Neural Net / Linger Classifier	validation_fraction	0.3
KNN Classifier Specific		
KNN	$n\_neighbors$	2
Weighted KNN Classifier Speci	fic	
Weighted KNN	n_neighbors	7
Linger Classifier, Duplication using Distance (Variation 2) Specific		
Linger Classifier	addition_of_context	False
Linger Classifier	$additional\_distance\_column$	False
Linger Classifier	$duplicated\_on\_distance$	True
Linger Classifier	$n\_neighbours\_1$	21
Linger Classifier	$n\_neighbours\_2$	13
Linger Classifier	weighted_knn	False

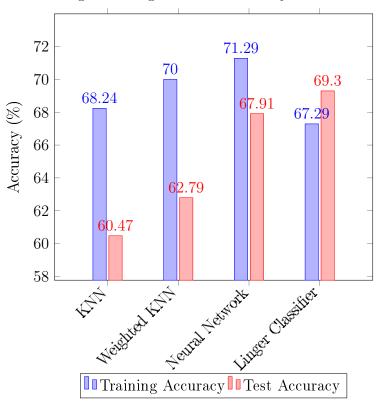
Table 4.7: Average Training and Test Accuracy Results for Classifiers (LCV2)

Classifier	Training Accuracy (%)	Test Accuracy (%)
KNN Classifier	68.24	60.47
Weighted KNN Classifier	70.00	62.79
Neural Network Classifier	71.29	67.91
Linger Classifier	67.29	69.30

#### (LCV2) Analysis

Variation 2, focusing on duplicating data based on distance  $(duplicated_on_distance == \text{True})$ , yielded the most significant test accuracy increase for the LingerClassifier, surpassing even the Neural Network. This strategy might have provided a more nuanced understanding of the dataset's structure, aiding the model in better capturing the underlying patterns. This result suggests that data duplication based on distance could be a powerful method for improving model performance, especially in classification tasks where spatial relationships within the data are informative.

LCV2: Average Training and Test Accuracy Results for Classifiers



# (LCV3) Results

Table 4.8: Best Parameters for Classifiers (LCV3)  $\,$ 

Classifier	Hyperparameter	Value
Common Parameters for Neuro	al Net and Linger Classifier, Ad	$dditional\ Distance\ Column\ (Variation\ 3$
Neural Net / Linger Classifier	activation	relu
Neural Net / Linger Classifier	alpha	0.001
Neural Net / Linger Classifier	beta_1	0.99
Neural Net / Linger Classifier	beta_2	0.999
Neural Net / Linger Classifier	early_stopping	True
Neural Net / Linger Classifier	hidden_layer_sizes	(300, 200, 100)
Neural Net / Linger Classifier	learning_rate_init	0.01
Neural Net / Linger Classifier	$\max_{}$ iter	1000
Neural Net / Linger Classifier	solver	$\operatorname{adam}$
Neural Net / Linger Classifier	$validation\_fraction$	0.3
KNN Classifier Specific		
KNN	n_neighbors	2
Weighted KNN Classifier Speci	fic	
Weighted KNN	n_neighbors	7
Linger Classifier with Additional Distance Column (Variation 3) Specific		
Linger Classifier	addition_of_context	False
Linger Classifier	$additional\_distance\_column$	True
Linger Classifier	$duplicated\_on\_distance$	False
Linger Classifier	$n\_neighbours\_1$	21
Linger Classifier	$n\_neighbours\_2$	13
Linger Classifier	$weighted\_knn$	False

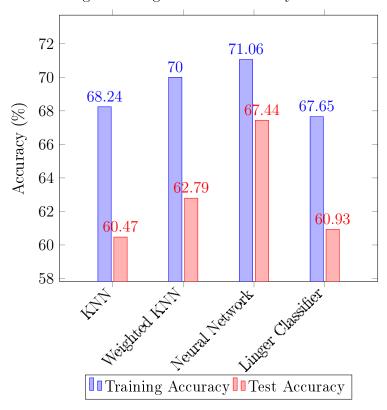
Table 4.9: Average Training and Test Accuracy Results for Classifiers (LCV3)

Classifier	Training Accuracy (%)	Test Accuracy (%)
KNN Classifier	68.24	60.47
Weighted KNN Classifier	70.00	62.79
Neural Network Classifier	71.06	67.44
Linger Classifier	67.65	60.93

#### (LCV3) Analysis

The third variation, which introduced an additional distance column  $(additional_distance_column == True)$ , did not lead to improvement in test accuracy for the LingerClassifier compared to LCV2 but maintained a competitive edge against the base NN model. This indicates that while adding distance-based features can be beneficial, there may be diminishing returns to complexity, or specific dataset characteristics may not fully leverage this type of information.

LCV3: Average Training and Test Accuracy Results for Classifiers



(LIC)

(LICV1)

(LICV2)

#### **Concluding Remarks**

## 4.2.2 Experiment 2: Abalone Dataset Regression

#### Methodology

In Experiment 2, we explored regression tasks on the Abalone dataset with a two-step approach. Initially, a neural network (NN) regressor was trained using grid search and cross-validation to identify optimal hyperparameter combinations. These selected hyperparameters were then applied to train a LingerRegressor (LR) and its variants, targeting improved robustness, with their performance evaluated across four runs. Additionally, to benchmark the LingerRegressor's performance, K-Nearest Neighbors (KNN), weighted KNN, and NN models were similarly assessed on the dataset. The results section will detail the hyperparameters and performance metrics obtained from Experiment 2.

## Tested Hyperparameters

Table 4.10: Tested Hyperparameters for Neural Network and Linger Regressor

Hyperparameter	Values	
Neural Network		
Hidden Layer Sizes	(256, 128), (128, 64), (200, 100), (300, 200, 100)	
Activation	relu	
Alpha	0.0001, 0.001, 0.01, 0.1	
Max Iterations	2000	
Early Stopping	True	
Validation Fraction	0.1	
Learning Rate Init	0.001, 0.01, 0.1	
Solver	adam, sgd	
Beta 1	0.9, 0.95, 0.99	
Beta 2	0.999, 0.995, 0.9	
Linger Regressor		
N Neighbours 1	2, 5, 7, 10, 13, 15, 17, 21	
N Neighbours 2	2, 5, 7, 10, 13, 15, 17, 21	
Weighted KNN	False	
Additional Distance Column	True, False	
Duplicated on Distance	True, False	
Addition of Context	True, False	

## (LR) Results

Table 4.11: Best Parameters for Regressors (LR)

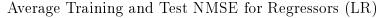
Regressor	Hyperparameter	Value
Common Parameters for Neuro	al Net Regressor and Linger Re	gressor
Neural Net / Linger Regressor	Activation	$\operatorname{relu}$
Neural Net / Linger Regressor	Alpha	0.01
Neural Net / Linger Regressor	Beta 1	0.95
Neural Net / Linger Regressor	Beta 2	0.9
Neural Net / Linger Regressor	Early Stopping	True
Neural Net / Linger Regressor	Hidden Layer Sizes	(200, 100)
Neural Net / Linger Regressor	Learning Rate Init	0.01
Neural Net / Linger Regressor	Max Iter	2000
Neural Net / Linger Regressor	Solver	$\operatorname{sgd}$
Neural Net / Linger Regressor	Validation Fraction	0.1
KNN Regressor Specific		
KNN Regressor	n_neighbors	17
Weighted KNN Regressor Speci	fic	
Weighted KNN Regressor	n_neighbors	21
Linger Regressor Specific		
Linger Regressor	Addition of Context	False
Linger Regressor	Additional Distance Column	False
Linger Regressor	Duplicated on Distance	False
Linger Regressor	n_Neighbours_1	5
Linger Regressor	$n_Neighbours_2$	21
Linger Regressor	Weighted KNN	False

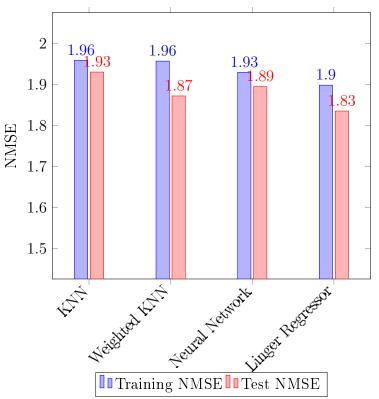
Table 4.12: Average Training and Test Negative Mean Squared Error Results (NMSE) for Regressors (LR)  $\,$ 

Regressor	Average Training NMSE	Average Test NMSE
KNN Regressor	-1.95857	-1.92999
Weighted KNN Regressor	-1.9567	-1.8717
Neural Net Regressor	-1.92956	-1.89454
Linger Regressor	-1.89797	-1.83486

#### (LR) Analysis

In an examination of the LingerRegressor's performance across five iterations, it became evident that this model, even in its unvaried form, consistently outshined its counterparts during both the training and testing phases. This superior performance underscores the efficacy of its unique "learning from differences" approach, adeptly uncovering and leveraging the dataset's underlying patterns. Notably, while extensive hyperparameter optimization was applied to the Neural Network models, the LingerRegressor has yet to undergo a similar level of fine-tuning due to resource limitiations. This observation hints at the untapped potential of the LingerRegressor, suggesting that with targeted hyperparameter adjustments and the exploration of variations, there could be a significant opportunity to further enhance its performance.





# (LRV1) Results

Table 4.13: Best Parameters for Regressors (LRV1)

Regressor	Hyperparameter	Value
Common Parameters for Neura	ul Net Regressor and Linger Re	gressor
Neural Net / Linger Regressor	Activation	relu
Neural Net / Linger Regressor	Alpha	0.1
Neural Net / Linger Regressor	Beta 1	0.99
Neural Net / Linger Regressor	Beta 2	0.9
Neural Net / Linger Regressor	Early Stopping	True
Neural Net / Linger Regressor	Hidden Layer Sizes	(300, 200, 100)
Neural Net / Linger Regressor	Learning Rate Init	0.01
Neural Net / Linger Regressor	Max Iter	2000
Neural Net / Linger Regressor	Solver	$\operatorname{sgd}$
Neural Net / Linger Regressor	Validation Fraction	0.1
KNN Regressor Specific		
KNN Regressor	$n_{neighbors}$	17
Weighted KNN Regressor Specia	fic	
Weighted KNN Regressor	n_neighbors	21
Linger Regressor Specific		
Linger Regressor	Addition of Context	True
Linger Regressor	Additional Distance Column	False
Linger Regressor	Duplicated on Distance	False
Linger Regressor	n_neighbours_1	2
Linger Regressor	$n_{\text{neighbours}} 2$	21
Linger Regressor	Weighted KNN	False

Table 4.14: Average Training and Test Negative Mean Squared Error Results for Regressors (LRV1)  $\,$ 

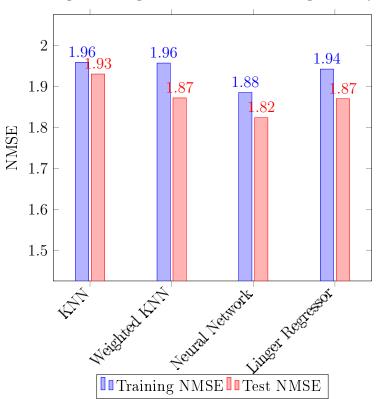
Regressor	Average Training NMSE	Average Test NMSE
KNN Regressor	-1.9586	-1.9300
Weighted KNN Regressor	-1.9567	-1.8717
Neural Net Regressor	-1.8848	-1.8234
Linger Regressor	-1.9420	-1.8697

#### (LRV1) Analysis

The exploration of the LingerRegressor in its variation one (LRV1) configuration, incorporating the addition of context as a new parameter, has yielded intriguing insights. This variation maintained the LingerRegressor's competitive edge, particularly in the testing phase, where it achieved a lower Negative Mean Squared Error (NMSE) compared to its baseline and even outperformed the Neural Net Regressors training results. The selected hyperparameters for LRV1—emphasizing a higher alpha and a shift in beta values—suggest an optimized balance between model complexity and regularization, contributing to its enhanced performance. Remarkably, the Linger Regressor's capacity to integrate context into its predictive process appears not especially benefit its ability to generalize, as evidenced by its test (NMSE) scores, as they are very similar and slightly worse than the base version.

This phase of experimentation underscores the substantial impact that tailored hyperparameter adjustments and strategic feature incorporation can have on model performance. Despite the Neural Net Regressor undergoing extensive hyperparameter optimization, the Linger Regressor, with its focused enhancements in LRV1, demonstrates that thoughtful model refinement alter performance gains. The results from LRV1 not only reaffirm the LingerRegressor's potential in leveraging complex patterns within the data but also spotlight the promising avenue that lies in further exploring and fine-tuning this model's capabilities.

## Average Training and Test NMSE for Regressors (LR)



## (LRV2) Results

(LRV3)

(LIR)

Table 4.15: Updated Best Parameters for Regressors (LRV1)

Regressor	Hyperparameter	Value
Common Parameters for Neural Net Regre	essor and Linger Impl	licit Regressor
Basic Neural Network / Linger Regressor	Activation	$\operatorname{relu}$
Basic Neural Network / Linger Regressor	Alpha	0.01
Basic Neural Network / Linger Regressor	Beta 1	0.9
Basic Neural Network / Linger Regressor	Beta 2	0.9
Basic Neural Network / Linger Regressor	Early Stopping	True
Basic Neural Network / Linger Regressor	Hidden Layer Sizes	(128, 64)
Basic Neural Network / Linger Regressor	Learning Rate Init	0.01
Basic Neural Network / Linger Regressor	Max Iter	2000
Basic Neural Network / Linger Regressor	Solver	$\operatorname{sgd}$
Basic Neural Network / Linger Regressor	Validation Fraction	0.1
KNN Regressor Specific		
KNN Regressor	$n\_neighbors$	21
Weighted KNN Regressor Specific		
Weighted KNN Regressor	n_neighbors	21
Linger Regressor Specific		
Linger Regressor	$n\_segments$	3
Linger Regressor	equal_division	True
Linger Regressor	n_neighbors_1	21
Linger Regressor	$n\_neighbors\_2$	13
Linger Regressor	Random Pairs	False
Linger Regressor	Single Pair	False

(LIRV1)

(LIRV2)

### 4.2.3 Experiment 3: Raisin Dataset Classification

#### Methodology

In Experiment 3, we conducted classification tasks on the Raisin dataset from [3], specifically the dataset [5] using a two-step methodology. Initially, we trained a neural network (NN) classifier through grid search and cross-validation to determine the optimal hyperparameters. These hyperparameters were then applied to train a LingerClassifier (LC) and its variants for improved robustness, tested across five runs. For comparative analysis, we also evaluated the performance of K-Nearest Neighbors (KNN), weighted (KNN), and (NN) on the same dataset. The sections below detail the hyperparameters selected and the test accuracies achieved.

# Tested Hyperparameters

Table 4.16: Tested Hyperparameters for Neural Network and Linger Regressor

Hyperparameter	Values
Neural Network	
Hidden Layer Sizes	(256, 128), (128, 64), (200, 100), (300, 200, 100), (400, 300, 200, 100)
Activation	identity, logistic, tanh, relu
Alpha	0.0001, 0.001, 0.01, 0.1
Max Iterations	1500, 2000
Early Stopping	True
Validation Fraction	0.1, 0.2, 0.3
Learning Rate Init	0.001, 0.01, 0.1
Solver	adam, sgd
Beta 1	0.9, 0.95, 0.99
Beta 2	0.999, 0.995, 0.9
	Linger Regressor
N Neighbours 1	2, 5, 7, 10, 13, 15, 17, 21
N Neighbours 2	2, 5, 7, 10, 13, 15, 17, 21
Weighted KNN	False
Additional Distance Column	True, False
Duplicated on Distance	True, False
Addition of Context	True, False

# (LC) Results

Table 4.17: Best Parameters for Classifiers (LC)

Classifier	Hyperparameter	Value		
Common Parameters for Neural Net Classifier and Linger Classifier				
Neural Net / Linger Classifier	Activation	identity		
Neural Net / Linger Classifier	Alpha	0.1		
Neural Net / Linger Classifier	Beta 1	0.95		
Neural Net / Linger Classifier	Beta 2	0.999		
Neural Net / Linger Classifier	Early Stopping	True		
Neural Net / Linger Classifier	Hidden Layer Sizes	(200, 100)		
Neural Net / Linger Classifier	Learning Rate Init	0.01		
Neural Net / Linger Classifier	Max Iter	2000		
Neural Net / Linger Classifier	Solver	$\operatorname{adam}$		
Neural Net / Linger Classifier	Validation Fraction	0.2		
KNN Classifier Specific				
KNN Classifier	n_neighbors	13		
Weighted KNN Classifier Specific				
Weighted KNN Classifier	n_neighbors	13		
Linger Classifier Specific				
Linger Classifier	Addition of Context	False		
Linger Classifier	Additional Distance Column	False		
Linger Classifier	Duplicated on Distance	False		
Linger Classifier	n_neighbors_1	5		
Linger Classifier	$n_{neighbors}_{2}$	13		
Linger Classifier	Weighted KNN	False		

Table 4.18: Average Training and Test Accuracy Results for Classifiers (LC)

Classifier	Average Training Accuracy (%)	Average Test Accuracy (%)
KNN Classifier	91.718	91
Weighted KNN Classifier	91.218	91
Neural Net Classifier	94.098	91
Linger Classifier	91.655	90.5

## (LC) Analysis

## (LCV1) Results

This was only run twice as there were constraints on resources during testing that resulted in less robust trials.

Table 4.19: Best Parameters for Classifiers (LCV1)  $\,$ 

Classifier	Hyperparameter	Value		
Common Parameters for Neural Net Classifier and Linger Classifier				
Neural Net / Linger Classifier	Activation	identity		
Neural Net / Linger Classifier	Alpha	0.1		
Neural Net / Linger Classifier	Beta 1	0.95		
Neural Net / Linger Classifier	Beta 2	0.999 (0.9 for Linger Classifier)		
Neural Net / Linger Classifier	Early Stopping	True		
Neural Net / Linger Classifier	Hidden Layer Sizes	(200, 100)		
Neural Net / Linger Classifier	Learning Rate Init	0.01		
Neural Net / Linger Classifier	Max Iter	2000		
Neural Net / Linger Classifier	Solver	adam		
Neural Net / Linger Classifier	Validation Fraction	0.2 (0.3 for Linger Classifier)		
KNN Classifier Specific				
KNN Classifier	$n\_neighbors$	13		
Weighted KNN Classifier Specific				
Weighted KNN Classifier	n_neighbors	13		
Linger Classifier Specific				
Linger Classifier	Addition of Context	True		
Linger Classifier	Additional Distance Column	False		
Linger Classifier	Duplicated on Distance	False		
Linger Classifier	$n_neighbors_1$	15		
Linger Classifier	$n\_neighbors\_2$	21		
Linger Classifier	Weighted KNN	False		

Table 4.20: Average Training and Test Accuracy Results for Classifiers (LCV1)

Classifier	Average Training Accuracy (%)	Average Test Accuracy (%)
KNN Classifier	91.718	91
Weighted KNN Classifier	91.218	91
Neural Net Classifier	94.139	90
Linger Classifier	91.843	90.168

(LCV2)

(LCV3)

(LIC)

(LICV1)

(LICV2)

# 4.3 Discussion

Summarize the key findings from the experiments and discuss their implications. Compare the performance of different models and datasets, and highlight any insights gained from the analysis.

# Chapter 5

Conclusions and Future Work

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