Logistic Regression

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library(tidyverse)
library(dplyr)
library(corrgram)
library(DataExplorer)
library(ppcor)
library(caTools)
library(ggplot2)
library(corrplot)
library(data.table)
library(plotly)
library(modelr)
library(arm)
library(cowplot)

Logistic regression which is also known as the logit model, predicts the probability of an event occurring. It is used to model dichotomous outcome variables. Logistic regression implies that the possible outcomes are not numerical but rather categorical. Examples of such categories are: Yes / No or 1/0.

Logistic regression in R Programming is a classification algorithm used to find the probability of event success and event failure.

Logistic sample: model \leftarrow glm(Y \sim x, binomial(), data)

The *logit function* is shown below

$$logit(p) = log(\frac{p}{1-p})$$

To get values of x between 0 and 1, take the inverse.

$$logit^{-1}(a) = \frac{1}{1 + e^{-a}}$$

$$Deviance = -2 * log - likelihood = -2LL$$

$$AIC = -2LL + 2k$$

Using AIC, we can compare multiple models, but as we increase the number of predictors the AIC k penalty will increase.

Below is an example of how to implement the Logistic Regression.

The dataset used for this project can be downloaded at this link: https://www.kaggle.com/datasets/dileep070/heart-disease-prediction-using-logistic-regression?resource=download

The variables in the dataset are:

Male: Gender (1 = Male, 0 = Female) Age: Patient age Education: Education level (1 = some high school, 2 = high school/GED, 3 = some college, 4 = college) CurrentSmoker: 1 = patient is smoker CigsPerDay: Number of cigarettes patient smokes per day BPMeds: 1 = patient is on blood pressure medication PrevalentStroke: 1 = patient has previously had a stroke PrevalentHyp: 1 = patient has hypertension Diabetes: 1 = patient has diabetes Chol: total cholesterol (mg/dL) SysBP: systolic blood pressure (mmHg) DiaBP: diastolic blood pressure (mmHg) BMI: body mass index (weight / $height^2$) HeartRate: Heart rate (beats per minute) Glucose: blood glucose level (mg/dL) TenYearCHD: 1 = patient developed coronary heart disease within 10 years of exam

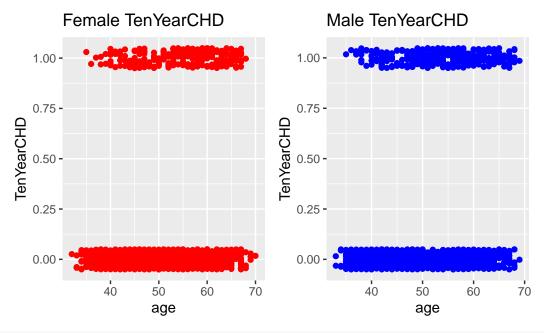
```
# Importing the dataset
data = read.csv('framingham.csv')
head(data)
     male age education currentSmoker cigsPerDay BPMeds prevalentStroke
##
## 1
         1
            39
                         4
                                                             0
                                         0
                                                     0
## 2
         0
                         2
                                         0
                                                     0
                                                             0
                                                                                0
            46
## 3
         1
            48
                         1
                                         1
                                                    20
                                                             0
                                                                                0
         0
            61
                         3
                                                    30
                                                             0
                                                                                0
## 4
                                         1
                         3
## 5
         0
            46
                                         1
                                                    23
                                                             0
                                                                                0
                         2
                                         0
                                                                                0
## 6
         0
            43
                                                     0
                                                             0
##
     prevalentHyp diabetes totChol sysBP diaBP
                                                       BMI heartRate glucose TenYearCHD
## 1
                  0
                            0
                                   195 106.0
                                                  70 26.97
                                                                    80
                                                                             77
                                                                                           0
## 2
                  0
                                                                             76
                            0
                                   250 121.0
                                                  81 28.73
                                                                    95
                                                                                           0
## 3
                  0
                            0
                                   245 127.5
                                                  80 25.34
                                                                    75
                                                                             70
                                                                                           0
                            0
                                                  95 28.58
                                                                    65
## 4
                  1
                                   225 150.0
                                                                            103
                                                                                           1
## 5
                  0
                            0
                                   285 130.0
                                                  84 23.10
                                                                    85
                                                                             85
                                                                                           0
## 6
                                                                                           0
                  1
                            0
                                   228 180.0
                                                 110 30.30
                                                                    77
                                                                             99
dim(data)
```

[1] 4238 16

summary(data)

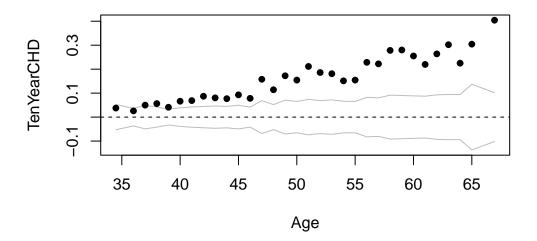
```
##
                                                         currentSmoker
         male
                                          education
                            age
##
    Min.
            :0.0000
                      Min.
                              :32.00
                                        Min.
                                               :1.000
                                                         Min.
                                                                 :0.0000
##
    1st Qu.:0.0000
                      1st Qu.:42.00
                                        1st Qu.:1.000
                                                         1st Qu.:0.0000
    Median :0.0000
                      Median :49.00
                                        Median :2.000
                                                         Median :0.0000
##
            :0.4292
                              :49.58
                                                :1.979
                                                                 :0.4941
##
    Mean
                      Mean
                                        Mean
                                                         Mean
##
    3rd Qu.:1.0000
                      3rd Qu.:56.00
                                        3rd Qu.:3.000
                                                         3rd Qu.:1.0000
            :1.0000
                                                                 :1.0000
##
    Max.
                      Max.
                              :70.00
                                        Max.
                                                :4.000
                                                         Max.
##
                                        NA's
                                                :105
                                          prevalentStroke
##
      cigsPerDay
                           BPMeds
                                                                prevalentHyp
##
                              :0.00000
                                                  :0.00000
            : 0.000
                      Min.
                                          Min.
                                                               Min.
                                                                       :0.0000
##
    1st Qu.: 0.000
                      1st Qu.:0.00000
                                          1st Qu.:0.000000
                                                               1st Qu.:0.0000
    Median : 0.000
                      Median :0.00000
                                          Median :0.000000
##
                                                               Median : 0.0000
##
    Mean
            : 9.003
                              :0.02963
                                                  :0.005899
                                                                      :0.3105
                      Mean
                                          Mean
                                                               Mean
##
    3rd Qu.:20.000
                      3rd Qu.:0.00000
                                          3rd Qu.:0.000000
                                                               3rd Qu.:1.0000
            :70.000
                              :1.00000
                                                  :1.000000
##
    Max.
                      Max.
                                          Max.
                                                                      :1.0000
                                                               Max.
##
    NA's
            :29
                      NA's
                              :53
##
                           totChol
                                             sysBP
                                                               diaBP
       diabetes
##
            :0.00000
                               :107.0
                                                                  : 48.00
    Min.
                       Min.
                                         Min.
                                                 : 83.5
                                                          Min.
##
    1st Qu.:0.00000
                        1st Qu.:206.0
                                         1st Qu.:117.0
                                                          1st Qu.: 75.00
##
    Median :0.00000
                       Median :234.0
                                         Median :128.0
                                                          Median: 82.00
##
    Mean
                                         Mean
                                                :132.4
                                                          Mean
                                                                 : 82.89
            :0.02572
                       Mean
                               :236.7
    3rd Qu.:0.00000
                        3rd Qu.:263.0
                                         3rd Qu.:144.0
                                                          3rd Qu.: 89.88
```

```
## Max. :1.00000 Max. :696.0 Max. :295.0 Max. :142.50
##
                     NA's :50
                                      glucose
##
        BMI
                     heartRate
                                                      TenYearCHD
          :15.54 Min. : 44.00
                                   Min. : 40.00 Min. :0.000
## Min.
                 1st Qu.: 68.00
## 1st Qu.:23.07
                                   1st Qu.: 71.00 1st Qu.:0.000
## Median :25.40 Median : 75.00
                                   Median: 78.00 Median: 0.000
## Mean :25.80 Mean : 75.88
                                   Mean : 81.97
                                                    Mean :0.152
                   3rd Qu.: 83.00
                                    3rd Qu.: 87.00
## 3rd Qu.:28.04
                                                    3rd Qu.:0.000
                                    Max. :394.00
## Max.
         :56.80
                   Max. :143.00
                                                    Max. :1.000
## NA's
         :19
                   NA's :1
                                    NA's
                                         :388
#checking for missing values
sum(is.na(data))
## [1] 645
#removes cases with missing data
data <- data %>% drop_na
#checking again for missing values
sum(is.na(data))
## [1] 0
# Sub-setting the data
male <- filter(data, male == 1)</pre>
dim(male)
## [1] 1622
             16
female <- filter(data, male == 0)</pre>
dim(female)
## [1] 2034
            16
# Visualizing Data
fcolor = "red"
mcolor = "blue"
female.plot \leftarrow ggplot(female, aes(x = age, y = TenYearCHD)) +
  geom_jitter(width = 0, height = 0.05, color = fcolor) +
 labs(title = "Female TenYearCHD")
male.plot \leftarrow ggplot(male, aes(x = age, y = TenYearCHD)) +
  geom_jitter(width = 0, height = 0.05, color = mcolor) +
  labs(title = "Male TenYearCHD")
plot_grid(female.plot, male.plot)
```



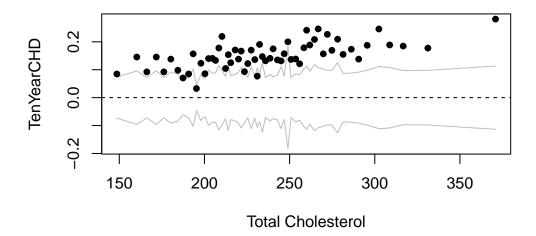
A quick plot of age against TenYearCHD binnedplot(data\$age, data\$TenYearCHD,xlab="Age",ylab="TenYearCHD",main="TenYearCHD vs Age")

TenYearCHD vs Age



binnedplot(data\$totChol, data\$TenYearCHD, xlab="Total Cholesterol",ylab="TenYearCHD",main="TenYearCHD v

TenYearCHD vs Cholesterol



Fitting the logistic regression model

```
# split the data into training and testing data:
set.seed(42)
split = sample.split(data, SplitRatio = 0.8)
train = subset(data, split == TRUE)
test = subset(data, split == FALSE)
row.names(train) <- NULL</pre>
row.names(test) <- NULL</pre>
# using the glm() command on the training data.
# summary to view the outcome
logit <- glm(TenYearCHD ~., family="binomial", data=train)</pre>
summary(logit)
##
## Call:
## glm(formula = TenYearCHD ~ ., family = "binomial", data = train)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    3Q
                                            Max
## -2.0767 -0.5770 -0.4204 -0.2858
                                         2.8426
##
## Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                   -7.944280
                                0.840272 -9.454 < 2e-16 ***
                    0.600154
                                0.128972
                                           4.653 3.27e-06 ***
## male
                    0.063844
                                0.007954
                                           8.027 1.00e-15 ***
## age
## education
                   -0.047638
                                0.059345
                                          -0.803
                                                  0.42213
## currentSmoker
                    0.063430
                                0.184888
                                           0.343
                                                  0.73154
## cigsPerDay
                    0.016502
                                0.007335
                                           2.250
                                                  0.02445 *
## BPMeds
                    0.416300
                                0.276493
                                           1.506 0.13216
```

```
## prevalentHyp
                    0.099443
                               0.165464
                                          0.601 0.54784
                                          0.390
## diabetes
                    0.145469
                               0.373150
                                                 0.69665
## totChol
                    0.002335
                               0.001320
                                                 0.07698
                                          1.768
## sysBP
                    0.014477
                               0.004448
                                          3.255
                                                 0.00113 **
                   -0.001067
## diaBP
                               0.007677
                                        -0.139
                                                 0.88950
## BMI
                                         -0.886
                   -0.014027
                               0.015824
                                                 0.37536
## heartRate
                   -0.005037
                               0.004997
                                         -1.008
                                                 0.31340
## glucose
                    0.008371
                               0.002667
                                          3.138 0.00170 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 2239.3 on 2741 degrees of freedom
## Residual deviance: 1988.8 on 2726 degrees of freedom
## AIC: 2020.8
##
## Number of Fisher Scoring iterations: 5
Making Prediction based on the model
subject_1 = data.frame(male = 1, age = 50, education = 2, currentSmoker = 1, cigsPerDay =
                                                                                            0, BPMeds =
predict(logit,subject_1,type='response')
##
            1
## 0.06859464
According to the model, the probability of this subject (smoker with diabetes) developing heart
```

0.316 0.75177

According to the model, the probability of this subject(smoker with diabetes) developing heart disease within 10 years is 68.6%.

```
subject_2 = data.frame(male = 1, age = 50, education = 2, currentSmoker = 0, cigsPerDay = 0, BPMeds =
predict(logit,subject_2,type='response')
```

```
## 1
## 0.05639219
```

prevalentStroke 0.179263

0.566743

According to the model, the probability of this subject(none smoker without diabetes) developing heart disease within 10 years is 56.39%.

It is important to note, that the probability of a subject developing heart disease within 10 years, varies for a smoker with diabetes and a none smoker without diabetes.

Other Predictions using classification is also possible. That discussion will be carried out in the python version of Logistic Regression.