Testing

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Modeling Robinson's SheafCanon Sheaf:

For specifics and citations, reference https://arxiv.org/abs/1603.01446

Robinson, Michael. "Sheaves Are the Canonical Data Structure for Sensor Integration." Information Fusion, vol. 36, Elsevier B.V, 2017, pp. 208–24, https://doi.org/10.1016/j.inffus.2016.12.002.

```
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.1 --
## v ggplot2 3.3.5
                    v purrr
                              0.3.4
## v tibble 3.1.6
                    v dplyr
                              1.0.8
## v tidyr
           1.2.0
                    v stringr 1.4.0
## v readr
           2.1.2
                    v forcats 0.5.1
## -- Conflicts -----
                            ## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
Table1 <- read.csv("Assignment2.csv") # Copied Table 1, page 218.
Table1
##
         Sensor Key entity
                              Case1
                                       Case2
                                                Case3
                                                      Units
## 1
     Flight plan
                             70.662
                U1
                                      70.663
                                               70.612
                                                          W
## 2
     Flight plan
                 U1
                             42.829
                                      42.752
                                               42.834
                                                          N
                        у
## 3
     Flight plan
                 U1
                        z 11178.000 11299.000 11237.000
                                                          m
## 4
            ATC
                 U2
                        х
                             70.587
                                      70.657
                                               70.617
                                                          W
## 5
                 U2
            ATC
                             42.741
                                      42.773
                                               42.834
                                                          N
                        У
```

```
## 6
               ATC
                    U2
                             z 11346.000 11346.000 11236.000
## 7
               ATC
                    U2
                           v_x
                                 -495.000
                                           -495.000
                                                      -419.000 \text{ km/h W}
               ATC
                                                        310.000 km/h N
## 8
                    U2
                                  164.000
                                             164.000
                           v_y
## 9
             RDF 1
                    U3 Theta1
                                   77.100
                                              77.200
                                                         77.200 true N
## 10
             RDF 1
                    UЗ
                                    0.943
                                               0.930
                                                          0.985
                             t
                                                                      h
## 11
             RDF 2
                    U4 Theta2
                                   61.300
                                              63.200
                                                         63.300 true N
## 12
             RDF 2
                    U4
                                    0.890
                                                          1.050
                                               0.974
                             t
                                                                      h
## 13
               Sat
                    U5
                             S
                                       NA
                                                  NA
                                                             NA
                    U5
                                              64.630
                                                         62.742
                                                                      W
## 14
               Sat
                                   64.599
                           s_x
## 15
               Sat U5
                                   44.243
                                              44.287
                                                         44.550
                                                                      N
                           s_y
```

```
## 16
            Field
                                 70.649
                                            70.668
                                                       70.626
                            х
## 17
            Field
                                            42.809
                                                       42.814
                                                                   N
                                  42.753
## 18
            Field
                           z 11220.000 11431.000 11239.000
            Field
                     Х
                                         -495.000
                                                     -419.000 \, km/h \, W
## 19
                          v_x -495.000
## 20
            Field
                     Х
                                 164.000
                                           164.000
                                                      311.000 km/h N
                          v_y
            Field
                                   0.928
                                             1.050
                                                        1.020
## 21
```

```
#Should these be global variables?

r_1x <- -73.662574

r_1y <- 42.733838

r_2x <- -77.0897

r_2y <- 38.935
```

What should be done with variables outside of the assignment table that we need? Constraints for functions not in any assignment table...

Restriction Functions:

Page 214: s_x , s_y are coordinates of an object detected in the satellite image, r_1x , r_1y are coordinates of teh first RDF sensor and r_2x , r_2y are coordinates of the second RDF sensor.

$$A(x, y, z, v_x, v_y, t) = \left(tan^{-1} \frac{x + v_x t - r_{1x}}{y + v_y t - r_{1y}}, t\right)$$

```
A <- function(stalk) {
   r_1x <- -73.662574
   r_1y <- 42.733838

stalk %>%
   mutate(Theta1=atan2(x + v_x*t - r_1x, y + v_y*t - r_1y)) %>%
   select(Theta1, t)
}
```

$$B(x, y, z, v_x, v_y, t) = \left(tan^{-1} \frac{x + v_x t - r_{2x}}{y + v_y t - r_{2y}}, t\right)$$

```
B <- function(stalk) {
   r_2x <- -77.0897
   r_2y <- 38.935

   stalk %>%
      mutate(Theta2=atan2(x + v_x*t - r_2x, y + v_y*t - r_2y))
}
```

$$C(s_x, s_y) = tan^{-1} \frac{s_x - r_{1x}}{s_y - r_{1y}}$$

```
C <- function(stalk) {
   r_1x <- -73.662574
   r_1y <- 42.733838

   stalk %>%
      mutate(Theta1=atan2(s_x - r_1x, s_y - r_1y)) %>%
      select(c(Theta1))
}
```

$$D(s_x, s_y) = tan^{-1} \frac{s_x - r_{2x}}{s_y - r_{2y}}$$

```
D <- function(stalk){
   r_2x <- -77.0897
   r_2y <- 38.935

stalk %>%
   mutate(Theta2=atan2(s_x - r_2x, s_y - r_2y)) %>%
   select(c(Theta2))
}
```

$$E(x, y, z, v_x, v_y, t) = (x + v_x t, y + v_y t)$$

```
E <- function(stalk) {
    # s = expected location, where coordinates = y + displacement and x+ displacement from the equation,
    stalk %>%
        mutate(s_x = c(x + v_x*t), s_y = c(y + v_y*t)) %>%
        select(c(s_x, s_y))
}
```

Check Example 15:

```
pr1xpr2 <- function(stalk){
    stalk %>%
        select(c(x, y, z, v_x, v_y))
}
```

```
#pr1 for u2 -> u1
U2_pr1 <- function(stalk){
    stalk %>%
    select(c(x, y, z))
}

#pr1 for u3 -> v1, this shouldnt work yet bc we havent figured out theta storage.
U3_pr1 <- function(stalk){
    stalk %>%
        select(c(Theta1))
}
```

```
#pr2 for u3 -> v3
U34_pr2 <- function(stalk){</pre>
  stalk %>%
      select(c(t))
}
\#pr1 for u4 \rightarrow v2, again shiuldnt work yet.
U4_pr1 <- function(stalk){</pre>
stalk %>%
      select(c(Theta2))
}
#Problems: ID function should Select its own column?
ID <- function(stalk){</pre>
  stalk
IDU1 <- function(stalk){</pre>
  stalk %>%
    select(U1)
}
IDU2 <- function(stalk){</pre>
  stalk %>%
    select(U2)
IDU3 <- function(stalk){</pre>
  stalk %>%
    select(U3)
}
IDU4 <- function(stalk){</pre>
  stalk %>%
    select(U4)
}
IDU5 <- function(stalk){</pre>
  stalk %>%
    select(U5)
\#V1 = THETA1, V2=THETA2, V3=T
IDV1 <- function(stalk){</pre>
  stalk %>%
      select(c(Theta1))
```

IDV2 <- function(stalk){</pre>

select(c(Theta2))

stalk %>%

```
IDV3 <- function(stalk){
   stalk %>%
      select(c(t))
}
```

Table representation of Figure 6 (b), page 214:

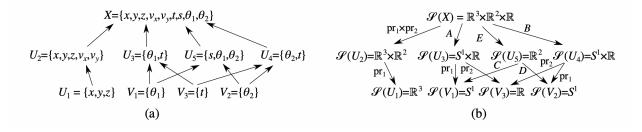


Figure 1: Figure 6

```
select(entity, Case1, Key) %>%
pivot_wider(names_from = entity, values_from = Case1) %>%
right_join(SixB, by = c(Key = "SSource")) %>%
nest(stalkinput = 2:12) %>%
mutate(stalkoutput = map2(.x= DMap, .y = stalkinput, .f = exec)) -> FinSheaf
FinSheaf
```

```
## # A tibble: 20 x 5
##
                                                                                                                                      stalkoutput
                                     SDest DMap
                                                                              stalkinput
##
                   <chr> <chr< <li><chr> <chr> <chr< <li><chr< <l><chr< </t>>
                                                                                                                                       t>
           1 U1
                                     U1
                                                        <fn>
                                                                              <tibble [1 x 11]> <tibble [1 x 11]>
##
           2 U2
                                                                             <tibble [1 x 11]> <tibble [1 x 3]>
##
                                     U1
                                                        <fn>
                                                                           <tibble [1 x 11]> <tibble [1 x 11]>
## 3 U2
                                     U2
                                                       <fn>
## 4 U3
                                     V1
                                                        <fn>
                                                                            <tibble [1 x 11]> <tibble [1 x 1]>
                                                                            <tibble [1 x 11]> <tibble [1 x 1]>
## 5 U3
                                     VЗ
                                                        <fn>
## 6 U3
                                    UЗ
                                                       <fn>
                                                                           <tibble [1 x 11]> <tibble [1 x 11]>
                                                       <fn> <tibble [1 x 11]> <tibble [1 x 1]>
## 7 U4
                                     V3
                                                 <fn> <tibble [1 x 11]> <tibble [1 x 1]>
## 8 U4
                                     V2
## 9 U4
                                     U4
                                                       <fn>
                                                                            <tibble [1 x 11]> <tibble [1 x 11]>
## 10 U5
                                     V1
                                                       <fn>
                                                                            <tibble [1 x 11]> <tibble [1 x 1]>
## 11 U5
                                     ٧2
                                                        <fn>
                                                                             <tibble [1 x 11]> <tibble [1 x 1]>
```

```
## 12 U5
             U5
                    \leq fn >
                            <tibble [1 x 11]> <tibble [1 x 11]>
## 13 X
             U2
                    \leq fn >
                            <tibble [1 x 11]> <tibble [1 x 5]>
## 14 X
             UЗ
                    \leq fn >
                            <tibble [1 x 11]> <tibble [1 x 2]>
                            <tibble [1 x 11]> <tibble [1 x 2]>
## 15 X
             U5
                    \leq fn >
## 16 X
             U4
                    \leq fn >
                            <tibble [1 x 11]> <tibble [1 x 11]>
                            <tibble [1 x 11]> <tibble [1 x 11]>
## 17 X
             X
                    \leq fn >
## 18 V1
                            <tibble [1 x 11]> <tibble [1 x 11]>
             V1
                    \leq fn >
                            <tibble [1 x 11]> <tibble [1 x 11]>
## 19 V2
             ٧2
                    \leq fn >
## 20 V3
             VЗ
                    <fn>
                            <tibble [1 x 11]> <tibble [1 x 11]>
```

Consistency Radius: radius =ish sd/var of stalkoutputs/ diameter of stalkoutputs. Coord. comp Unnest. pivot wider, aggregate along all of the columns. Put the STD together, remember units are diff chi square, normvar. Idealy have user suoply agregation function.

process below should be a specific function, so to optimize consistency radius. bestconsistency radius fin like lm taking consistency radius function.

```
#FinSheaf %>%
# group_by(SDest) %>%
# summarise(rad = ) # have pre-consistency radii , ungroup and aggreate all rads to get consistencey r
# ends with: for each stalk you have a radius, then agregate them, max, sum of squares.
```

Testing:

```
#Option 1:
Table1 %>%
  select(entity, Case1, Key)%>%
  pivot_wider(names_from = entity, values_from = Case1) %>%
 mutate(sourcekey = Key)
## # A tibble: 6 x 13
                                       v_y Theta1
                                                        t Theta2
                                                                          s_x
               х
                                 v_x
                                                                      S
                                                                                 s_y
                      У
                            z
     <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
                                                    <dbl>
                                             <dbl>
                                                           <dbl> <dbl>
                                                                        <dbl> <dbl>
## 1 U1
            70.7
                   42.8 11178
                                  NA
                                        NA
                                             NA
                                                   NA
                                                            NA
                                                                     NA
                                                                         NA
                                                                                NA
## 2 U2
            70.6
                   42.7 11346
                                -495
                                       164
                                             NA
                                                   NA
                                                            NA
                                                                     NA
                                                                         NA
                                                                                NA
## 3 U3
            NA
                   NA
                           NA
                                  NA
                                        NA
                                             77.1 0.943
                                                            NA
                                                                     NA
                                                                         NA
                                                                                NA
## 4 U4
                           NA
                                  NA
                                        NA
                                                    0.89
                                                                         NA
            NA
                   NA
                                             NA
                                                            61.3
                                                                     NA
                                                                                NA
## 5 U5
            NA
                   NA
                           NA
                                  NA
                                        NA
                                             NA
                                                   NA
                                                            NA
                                                                     NA
                                                                         64.6
                                                                                44.2
            70.6 42.8 11220
                               -495
                                       164
                                             NA
                                                    0.928
                                                            NA
                                                                     NA
                                                                         NA
                                                                                NA
## # ... with 1 more variable: sourcekey <chr>
#Option 3:
Table1 %>%
  select(entity, Case1, Key)%>%
 nest_by(Key)%>%
  unnest_wider(data)
## # A tibble: 6 x 3
     Key
                 entity
                              Case1
     <chr> <list<chr>> <list<dbl>>
## 1 U1
                                 [3]
                    [3]
```

```
## 2 U2
                   [5]
                                [5]
## 3 U3
                                [2]
                   [2]
## 4 U4
                   [2]
                                [2]
## 5 U5
                   [3]
                                [3]
## 6 X
                                [6]
                   [6]
#Option 7: Lets look at this first:
Table1 %>%
 mutate(label = str_c(Sensor, ".", entity))%>%
  select(label, Case1, Key)%>%
 pivot_wider(names_from = label, values_from = Case1)
## # A tibble: 6 x 22
           'Flight plan.x' 'Flight plan.y' 'Flight plan.z' ATC.x ATC.y ATC.z
     Key
                                                      <dbl> <dbl> <dbl> <dbl> <
##
     <chr>
                     <dbl>
                                      <dbl>
## 1 U1
                      70.7
                                       42.8
                                                      11178 NA
                                                                   NA
## 2 U2
                      NA
                                       NA
                                                         NA 70.6 42.7 11346
## 3 U3
                      NA
                                       NA
                                                         NA NA
                                                                   NA
                                                                           NA
## 4 U4
                      NA
                                       NA
                                                         NA NA
                                                                   NA
                                                                            NA
## 5 U5
                      NA
                                       NA
                                                         NA NA
                                                                   NA
                                                                           NA
## 6 X
                      NA
                                       NA
                                                         NA NA
                                                                   NA
                                                                           NA
## # ... with 15 more variables: ATC.v_x <dbl>, ATC.v_y <dbl>,
      'RDF 1.Theta1' <dbl>, 'RDF 1.t' <dbl>, 'RDF 2.Theta2' <dbl>,
## #
       'RDF 2.t' <dbl>, Sat.s <dbl>, Sat.s_x <dbl>, Sat.s_y <dbl>, Field.x <dbl>,
      Field.y <dbl>, Field.z <dbl>, Field.v_x <dbl>, Field.v_y <dbl>,
```

#

Field.t <dbl>