

2.5

I) $\frac{P \wedge (P \rightarrow Q) \rightarrow Q}{t_4 T_2 ? t_5 F_3 F \not\in F_1}$

II) $\frac{\neg Q \wedge (P \rightarrow Q) \rightarrow \neg P}{t_4 F_5 t_3 ? t_6 F_7 F F_1 t_2}$

III) $\frac{P \vee \neg P}{F_1 F F_2 ?}$

IV) $\frac{\neg(P \wedge \neg P)}{F t_2 t_1 t_3 ?}$

V) $\frac{(\neg P \rightarrow P) \rightarrow P}{F_4 ? t_2 F_3 F F_1}$

VI) $\frac{(P \rightarrow Q) \wedge (\neg P \rightarrow Q) \rightarrow Q}{F_7 t_3 F_6 t_2 F_8 ? t_4 F_5 F F_1}$

VII) $\frac{\neg(P \wedge Q) \leftrightarrow (\neg P \vee \neg Q)}{1 \begin{array}{c} t_1 ? F_3 +_8 F F_4 t_6 F_2 F_5 t_7 \\ \hline F_1 \end{array} 2 \begin{array}{c} t_2 t_3 t_4 F F_7 t_6 t_2 t_8 ? \end{array}}$

$$\text{VIII) } \neg(P \vee Q) \leftrightarrow (\neg P \wedge \neg Q)$$

\neg	$t_1 F_1 F_3 F_5$	F	$t_2 F_6 \underline{F_2} F_8 ?$
2	$\underline{F_1} ? t_3 F_8$	F	$t_4 F_6 \underline{t_2} + t_5 F_7$

IX)

$$\frac{P \wedge \neg P \rightarrow Q}{t_3 t_2 t_4 ? \vdash F_1}$$

(2.6)

I)

$$\begin{array}{c|cc} P & P \wedge P \\ \hline F & F_1 F \bar{F}_2 \\ + & t_1 + t_2 \end{array}$$

→ Contingency

II

Not receiving $\neg P$ evidence	P Q R		$((P \rightarrow Q) \rightarrow R) \leftrightarrow (P \rightarrow (Q \rightarrow R))$	
	1.1	1.2	$t_9 t_{10} \underline{F_2} F_3 + F_7 \underline{F_2} + 8 F_6 F_5$	$F_8 ? \underline{t_1} F_7 F \underline{t_3} F_2 + 6 F_4 F_5$
2.1 2.2	$t_1 + F$		$t_9 t_{10} \underline{F_2} F_3 + F_7 \underline{F_2} + 8 F_6 F_5$	$F_8 ? \underline{t_1} F_7 F \underline{t_3} F_2 + 6 F_4 F_5$
2.2 2.1			$t_9 t_{10} ? \underline{F_1} F_3 F$	$\underline{t_6} \underline{t_2} F_8 \underline{t_7} F_5$

→ Contingency

III) (I won't do a Partial Because it'll need to
do a lot of assumptions)

$P \ Q \ R$	$(P \leftrightarrow (Q \rightarrow R)) \leftrightarrow ((R \rightarrow Q) \leftrightarrow R)$							
T T T		T	T				T	T
T T F		F	F				T	F
T F T		F	F				F	F
T F F		T	T				F	T
F T T		F	F				F	F
F F T		T	F				F	T
F F F		T	F				T	T
P F F		F	T				T	F

→ tautology

IV

$P \ Q$	$\neg(P \rightarrow Q) \leftrightarrow (P \wedge \neg Q)$								
1.1 + F	<u>t₁</u>	<u>t₅</u>	<u>F₃</u>	<u>F₄</u>	+ T	+ t ₆	<u>t₂</u>	<u>t₇</u>	<u>F₈</u>
1.2									
2.1	<u>t₇</u>	<u>t₅</u>	<u>F₃</u>	<u>F₄</u>	F	+ t ₆	<u>F₂</u>	<u>F₇</u>	?
2.2	<u>F₁</u>	?	<u>t₃</u>	<u>F₂</u>	F	+ t ₄	<u>t₂</u>	<u>t₅</u>	<u>F₆</u>

→ tautology

2.2

III) $| \phi \vee \psi |_A = F$ iff $|\phi|_A = F$ and $|\psi|_A = F$

IV) $|\phi \rightarrow \psi |_A = F$ iff $|\phi|_A = T$ and $|\psi|_A = F$.

V) $|\phi \leftrightarrow \psi |_A = F$ iff $|\phi|_A \neq |\psi|_A$

2.8

According to definition 2.9 $I \models \phi$ iff there is no L_1 -structure in which all sentences ~~other than~~ true in I are true and ϕ is false.

According to definition 2.11 a set of sentences is consistent iff there is an L_1 -structure under which all sentences in the structure are true.

It's so, if a set is inconsistent there is no L_1 -structure under which all sentences ^{in that set} are true.

If the set containing all sentences $\vdash I$ and $\neg \phi$ is inconsistent then there is no counterexample as in definition 2.10. therefore, the argument must be valid.